

SeawavePy – Sea Surface Simulation

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Surface Module Description

Sea surface elevations can be calculated as the sum of the harmonics with deterministic amplitudes and random phases

$$\xi(\vec{r}, t) = \sum_{n=1}^N \sum_{m=1}^M A_n \cdot F_{nm} \cos(\omega_n t + \vec{\kappa}_{nm} \vec{r} + \psi_{nm}), \quad (1)$$
$$A_n(\kappa_n) = \frac{1}{2\pi} \sqrt{\int_{\Delta\kappa_n} S_\xi(\kappa) d\kappa},$$
$$F_{nm}(\kappa_n, \varphi_m) = \sqrt{\int_{\Delta\varphi_m} \Phi_\xi(\kappa_n, \varphi) d\varphi},$$

where $A_{nm}(\kappa)$ – wave amplitude calculated from one-dimensional wave spectrum $S_\xi(\kappa)$, \vec{r} – radius measured from zero sea level, ψ – random phases, Φ – azimuthal wave distribution.

Knowing the elevations, we can calculate the slopes of the surface

$$\begin{aligned} \sigma_x(\vec{r}, t) &= \frac{\partial \xi}{\partial x} \\ \sigma_y(\vec{r}, t) &= \frac{\partial \xi}{\partial y} \\ \sigma_z(\vec{r}, t) &= \frac{\partial \xi}{\partial z} = 1 \end{aligned} \quad (2)$$

The function **wind** in module **core.surface** calculates equations (1), (2) on the GPU and returns an array of the NetCDF format with fields:

- **elevations** – elevations of surface with dimensions (x, y, t)
- **slopes** – slopes of surface with dimensions $(3, x, y, t)$
- **velocities** – orbital velocities of surface with dimensions $(3, x, y, t)$
- **spectrum** – Two dimensional wave spectrum

Tilt-modulation

The equation (2) is the normal vector at a point on the surface

$$\vec{n} = \frac{\vec{i} \cdot \sigma_x + \vec{j} \sigma_y + \vec{k} \cdot 1}{\sqrt{\sigma_x^2 + \sigma_y^2 + 1}}$$

$$\vec{u} = (x, y, \xi)$$

Then we can calculate tilt-modulation effect

$$\sigma_{tilt}(x, y, t) = \begin{cases} \vec{n}\vec{u}, & \text{if } \vec{n}\vec{u} > 0 \\ 0, & \text{if } \vec{n}\vec{u} \leq 0 \end{cases}$$

These equations are a complete replacement for equations (3-6) from the article "Research of X-band Radar Sea Clutter Image Simulation Model"