STyLuS*: A Temporal Logic Optimal Control Synthesis Tool for Large-Scale Multi-Robot Systems

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I. SETTING UP STYLUS*

A. Dependencies

STyLuS has been tested on Windows 7 and on macOS HighSierra on MATLab R2016b. To use STyLuS, the ltl2ba toolbox needs to be installed that is available online on http://www.lsv.fr/~gastin/ltl2ba/. Once the executable file is generated, it should be placed in the folder functions. Executable files generated on Windows 7 (ltl2baWin7) and macOS HighSierra (ltl2ba) are already included there. The user is encouraged to generate new executable files to avoid any inconsistencies. The ltl2ba toolbox is used in the function create_buchi to translate LTL formulas into Non-deterministic Bucchi automata (NBA). Note that the current MATLAB folder should be .../functions/ (i.e., where the executable file is located), otherwise create_buchi will not be able to generate a NBA.

B. Inputs

The user-specified inputs to STyLuS are determined in the function DefineInputs.m:

• a weighted Transition System (TS) modeling robot mobility; see also Figs. 1-2. STyLuS has currently been implemented assuming that all robots have the same model, i.e., the same TS. A TS is represented by a structure T. The user needs to define the (i) number of TS states (numStates) and the TS state-space defined as T.Q = [1 : numStates)], (ii) the physical locations of the TS states, i.e., the x (vector T.x with dimensions numStates \times 1) and y (vector T.y with dimensions numStates \times 1) coordinate of each state, and (iii) the adjacency matrix of the TS (T.adj which is a numStates \times numStates matrix) where the entry T.adj(i,j) is 0 if a direct transition from state i to state i is infeasible/possible and 1 otherwise. By default, STyLuS generates these three inputs randomly. If a user-specified TS is needed, the command T=createFTS (numOfStates, degree/2) should be commented out. The field T.Dist is a numStates xnumStates capturing the cost for each TS transition that will be generated automatically. T.Dist is defined so that it captures the Euclidean distance from the TS state i to the TS state i if it holds T.adj(i,j) = 1; for all other transitions for which T.adj(i,j) = 0, it holds that T.Dist(i,j) = Inf. The user can comment out the command T.Dist = DistanceMatrixA(T) and assign manually new weights to each transition.

Fig. 1. A weighted Transition System as an input to STyLuS*.

Fig. 2. Structure of a weighted Transition System as an input to STyLuS*.

- number N of robots and their initial state x0; see also Fig. 3. x0 is an N \times 1 vector where the *i*-th entry captures the initial state of robot *i* and has to be an integer within the interval [1, numStates].
- an LTL mission captured in the string phi; see also Fig. 4. To define the LTL formula phi, the following notation is used: G, F, U, X stand for the 'always', 'eventually', 'until', and 'next' operator, and &, |,! stand for the logical 'and', 'or', and 'not' operators. The number of atomic predicates p that appear in phi needs to be defined as well (see Np). For instance, consider the LTL task

$$phi = F(p1) \& G(!p2)$$
 (1)

Fig. 3. Initialization of a team of N robots.

which requires that eventually p1 to be satisfied and that p2 should never be satisfied. The definition of where the predicates (e.g., p1 and p2) in phi are satisfied is captured by the cell array AP; see also Fig. 5. Let pk denote the k-th predicate which is captured by AP(k,:). Specifically, AP(k,r) is an empty cell if robot r does not play any role in satisfying pk and a non-empty cell array otherwise. If it is a non-empty cell, then AP(k,r) is defined as $AP(k,r) = \{[\text{state } 1, \text{state } 2, \dots, \text{state } m]\}$ collecting all states that if at least one of them is visited by robot r then AP(k,r) is true. Note that this definition allows more than one robot to contribute to satisfaction of pk. For instance, if pk is defined to be true if robots either robot r1 or robot r2, or robot r3 are in state r4, then r5 is defined as follows $AP(k,r) = \{m\}$ 4, $AP(k,r) = \{m\}$ 5. Otherwise, if $AP(k,r) = \{m\}$ 6, it means that all three robots have to be in state r6 so that r7 is true.

Fig. 4. An LTL formula as an input to STyLuS*.

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AP(1,4)
               = \{[720,340]\}; %robot 4 has to be in either region 720 or 340 (boolean formula: b_1^1)
AP(1,3)
               = \{[110,330]\}; %robot 3 has to be in either region 110 or 330 (boolean formula: b_2^1)
AP(1,1)
               = \{[110,980]\}; %robot 1 has to be in either region 110 or 980 (boolean formula: b_3^1)
AP(1,2)
               = \{210\};
                               %robot 2 has to be in region 210 (boolean formula: b_4^1) ...
AP(1,5)
              = \{172\};
               = \{10\};
AP(1,6)
AP(1,7)
               = \{107\};
AP(1,8)
               = {501};
AP(1,9)
               = \{104\};
AP(1,10)
               = \{71\};
AP(1.11)
               = \{ [900. 800] \}:
AP(1,12)
               = \{11\};
```

Fig. 5. Determining when p1 is satisfied within STyLuS*.

• Termination criterion (Termination); see also Fig. 6. The user needs to define if STyLuS should terminate once the first feasible solution is found (Termination.MaxIter=0) or after a maximum number of iterations (Termination.MaxIter=1). In the later case, the user needs to determine the maximum number of iterations for the construction of the prefix (Termination.nMaxPre) and suffix (Termination.nMaxSuf) plan.

Fig. 6. Determining the termination criterion of STyLuS*.

• a parameter $w \in [0,1]$ required to determine the cost of a prefix suffix plan; see also Fig. 7. In particular the cost of a prefix-suffix plan is (1-w)J(prefix) + wJ(suffix), where the cost of the prefix and suffix (i.e., J(prefix), J(suffix) is determined by T.Dist.

Fig. 7. Determining the cost-related parameter w within STyLuS*.

C. Outputs

The output of STyLuS is generated by the function MainSTyLuS star and includes the following:

- the best found prefix-suffix plan (BestPrefix, BestSuffix). The prefix part is defined as an array with dimensions $H \times N$ where H captures the number or waypoints that the multi robot system has to take. To get the full prefix path, type in the command window BestPrefix. To get k-th waypoint of robot j, type in the command window BestPrefix (k, j). The same holds for the corresponding suffix part BestSuffix.
- a cell array containing all the detected prefix parts (ListOfPrefix) including the best one. To get the m-th prefix part, type in the command window: ListOfPrefixm . To get k-th waypoint of robot j type in the m-th prefix part, type in the command window ListOfPrefixm(k, j) . The same holds for the cell array containing all the detected suffix parts (ListOfSuffix)
- a vector (wrongPre) containing the indices of the detected prefix parts that did not pass sanity checks (e.g., a prefix path has to respect the transition rule of the TS). If any prefix part does not pass the sanity check a warning message will appear on the command window and the index to these prefix parts will be included in this vector. A corresponding vector for the suffix parts is also returned (wrongSuf).

D. Execution

To execute STyLuS*, type $STyLuS_star$ in the MATLab command window. The output of $STyLuS^*$ for a case study with N=100 robots where each robot is modeled as TS with 1000 states and collaborative LTL formula corresponding to an NBA with 21 states is shown in Fig. 8. This is the default input case study for $STyLuS^*$.

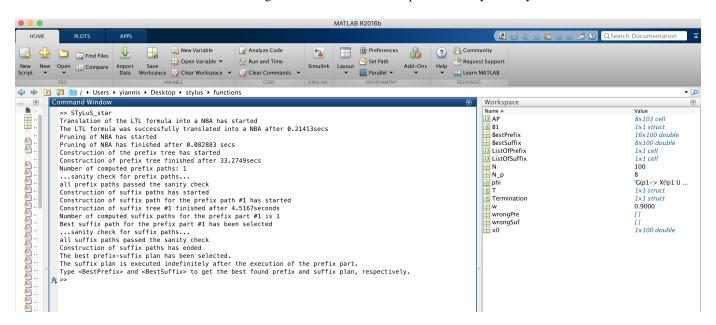


Fig. 8. Output of STyLuS* for a case study with (i) N = 100 robots, (ii) TS with 1000 states, and (iii) an LTL formula corresponding to an NBA with 21 states

II. EXAMPLE: SETTING UP A SINGLE-AGENT REACHABILITY AVOIDANCE TASK

In this section, we discuss how STyLuS* can be configured to set up a simple single-agent reachability avoidance task. Here, we consider a randomly generated transition system with 1000 states as discussed in the previous section. Also, we assume that the initial state of the robot is $10 \in [1,1000]$. Thus, we define N=1, and $\times 0 = 10$; see also Fig. 9.

The robot mission requires the robot to eventually reach either the state/region 720 or 340 and always avoid the regions 191, 20, 1000, 500, 600. This mission can be defined as an LTL formula that has the same structure as in (1). This mission is given as an input to STyLuS* as shown in Fig. 10 where p1 and p2 are defined as in Fig. 11.

%%	Team of robots	
Ν	= 1; % number of robots	
×0	= 10; % initial states of robots with	nin their TS
%		

Fig. 9. Initializing the single-robot system.

Fig. 10. Specifying a reachability-avoidance task as an LTL formula as an input to STyLuS*.

To run STyLuS* for this case study, open STyLuS_star.m (type open STyLuS_star.m), replace DefineInputs() with DefineInputs4ReachabilityAvoidance(), save the changes, and then type in the command window STyLuS_star. The output of STyLuS* for this case study is shown in Fig. 12.

Fig. 11. Defining variables p1 and p2 for the reachability-avoidance task (1).

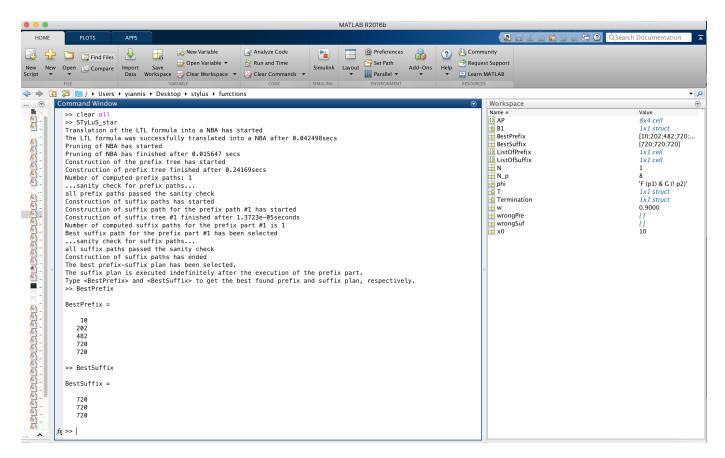


Fig. 12. Output of $STyLuS^*$ for a case study with (i) N=1 robots, (ii) TS with 1000 states, and (iii) an LTL formula corresponding to the task (1).