# SymPy Cheatsheet (http://sympy.org)

## **Basics**

Sympy help: help(function)

Declare symbol: x = Symbol('x')

Substitution: expr.subs(old, new)

Numerical evaluation: expr.evalf()

Expanding: expr.expand()

Common denominator: ratsimp(expr)

Simplify expression: simplify(expr)

#### Constants

# $\pi$ : pi e: E $\infty$ : oo i: I

# Numbers types

 $\begin{array}{ll} \operatorname{Integers} (\mathbb{Z}) \colon & \operatorname{Integer}(\mathtt{x}) \\ \operatorname{Rationals} (\mathbb{Q}) \colon & \operatorname{Rational}(\mathtt{p}, \ \mathtt{q}) \\ \operatorname{Reals} (\mathbb{R}) \colon & \operatorname{Float}(\mathtt{x}) \end{array}$ 

## Basic functions

Trigonometric: sin cos tan cot Cyclometric: asin acos atan acot Hyperbolic: sinh cosh tanh coth Area hyperbolic: asinh acosh atanh acoth Exponential: exp(x)Square root: sqrt(x) Logarithm ( $\log_b a$ ): log(a, b) Natural logarithm: log(a) Gamma  $(\Gamma(x))$ : gamma(x) Absolute value: abs(x)

# Calculus

```
\lim f(x):
                                              limit(f, x, a)
\lim f(x):
                                  limit(f, x, a, dir='-')
\lim f(x):
                                  limit(f, x, a, dir='+')
x \rightarrow a_+
\frac{\frac{d}{dx}}{\frac{\partial}{\partial x}}f(x):
                                                    diff(f, x)
                                                    diff(f, x)
\int f(x) dx:
                                             integrate(f, x)
\int_a^b f(x) dx:
                                  integrate(f, (x, a, b))
Taylor series (at a, deg n)
                                          f.series(x, a, n)
```

#### **Equations**

Equation f(x) = 0: solve(f, x) System of equations: solve([f, g], [x, y]) Differential equation: dsolve(equation, f(x))

## Geometry

Points: a = Point(xcoord, ycoord)
Lines: l = Line(pointA, pointB)
Circles: c = Circle(center, radius)
Triangles: t = Triangle(a, b, c)
Area: object.area
Intersection: intersection(a, b)
Checking tangency: c.is\_tangent(1)

#### Plotting

Plot: Plot(f, [a, b]) Zoom: +/-: R/F or PgUp/PgDn or Numpad +/-Rotate X,Y axis: Arrow Keys or WASD Rotate Z axis: Q and E or Numpad 7 and 9 View XY: View XZ: F2 F3 View YZ: View Perspective: F4 Axes Visibility: F5 Axes Colors: F6 Screenshot: F8 Exit plot: ESC

## Discrete math

Factorial (n!): factorial(n)
Binomial coefficient  $\binom{n}{k}$ : binomial(n, k)
Sum  $(\sum_{n=a}^{b} expr)$ : summation(expr, (n, a, b))
Product  $(\prod_{n=a}^{b} expr)$ : product(expr, (n, a, b))

# Linear algebra

# Printing

Python print: print latex()
Pretty print: print python()
Pretty print: pprint()

# Examples

Find 100 digits of  $\pi^e$ :

```
(pi**E).n(100)

Expand (x + y)^2(x - y)(x^2 + y):

((x + y)**2 * (x - y) * (x**2 + y)).expand()

Simplify \frac{1}{x} + \frac{x \sin x - 1}{x^2 - 1}:

simplify((1/x) + (x * sin(x) - 1)/(x**2 - 1))
```

Check if line passing through points (0,1) and (1,1) is tangent to circle with center at (5,5) and radius 3: Circle(Point(5,5), 3).is\_tangent(Line(Point(0,1), Point(1,1)))

Find roots of  $x^4 - 4x^3 + 2x^2 - x = 0$ : solve(x\*\*4 - 4\*x\*\*3 + 2\*x\*\*2 - x, x)

Solve the equations system: x + y = 4, xy = 3: solve([x + y - 4, x\*y - 3], [x, y])

Calculate limit of the sequence  $\sqrt[n]{n}$ : limit(n\*\*(1/n), n, oo)

Calculate left-sided limit of the function  $\frac{|x|}{x}$  in 0: limit(abs(x)/x, x, 0, dir='-')

Calculate the sum  $\sum_{n=0}^{100} n^2$ : summation(n\*\*2, (n, 0, 100))

Calculate the sum  $\sum_{n=0}^{\infty} \frac{1}{n^2}$ : summation(1/n\*\*2, (n, 0, oo))

Calculate the integral  $\int \cos^3 x \, dx$ : integrate( $\cos(x)**3$ , x)

Calculate the integral  $\int_1^\infty \frac{dx}{x^2}$ : integrate(1/x\*\*2, (x, 1, oo))

Find 10 terms of series expansion of  $\frac{1}{1-2x}$  at 0: (1/(1-2\*x)).series(x, 0, 10)

Solve the differential equation f''(x) + 9f(x) = 1: dsolve(f(x).diff(x, x) + 9\*f(x) - 1, f(x))