## **Input and Output for Assignment 4**

## (final output on page 11 and 12)

```
Input:
```

```
Initial means are
```

```
a b c d e
1 -9.4204480 1.672011 0.5089758 1.919512 -1.2325192
2 -0.7937296 -8.406403 1.3410895 -7.408800 1.0881077
3 2.9175982 2.718769 4.4998348 6.377856 -0.4397304
```

iteration no is 1

cluster1

mean1

a b c d e -9.4204480 1.6720109 0.5089758 1.9195125 -1.2325192

cov1

a b c d e a 5.985680 -2.089963 -1.5818739 -0.6721620 -1.2599845 b -2.089963 7.305001 -1.4128364 -1.9661746 -1.6846534 c -1.581874 -1.412836 5.7619557 -1.4918565 -0.9824421 d -0.672162 -1.966175 -1.4918565 5.0982408 -0.8905932 e -1.259985 -1.684653 -0.9824421 -0.8905932 5.0434275

## cluster2

mean2

a b c d e
-0.7940714 -8.4063790 1.3429678 -7.4077954 1.0883341
cov2 a b c d e
a 18.40006 11.86390 13.05764 10.18516 12.57426
b 11.86390 18.64869 13.30232 10.51993 13.29332
c 13.05764 13.30232 19.15432 12.25455 15.19714
d 10.18516 10.51993 12.25455 17.05884 12.44665
e 12.57426 13.29332 15.19714 12.44665 21.04011

## cluster3

cov3

mean3
 a b c d e
2.9183410 2.7198585 4.4981140 6.3781482 -0.4401291
cov3 a b c d e
a 8.749969 -3.954609 4.804421 -6.609096 9.91628
b -3.954609 11.048413 -5.783369 9.426482 -11.69843
c 4.804421 -5.783369 9.933372 -8.911018 11.96886
d -6.609096 9.426482 -8.911018 18.858745 -18.76723

```
e 9.916280 -11.698432 11.968864 -18.767229 30.12665
probs are
0.3363229 0.3453234 0.3183537
current log likelihood is
[1] -95098.71
previous log likelihood is
[1] 0.1
iteration no is 2
cluster1
mean1
                         d
-9.4205060 1.6720724 0.5089308 1.9195034 -1.2324936
cov1
                          d
                   С
                                е
a 5.9858831 -2.090019 -1.5820851 -0.6721671 -1.2599166
b -2.0900186 7.304879 -1.4127506 -1.9661996 -1.6845217
c -1.5820851 -1.412751 5.7620046 -1.4919348 -0.9823376
d -0.6721671 -1.966200 -1.4919348 5.0981603 -0.8904070
e -1.2599166 -1.684522 -0.9823376 -0.8904070 5.0429855
cluster2
mean2
                         d
           b
                  С
-0.1831928 -7.7277414 1.9469064 -6.6807636 1.6196682
               b
                          d
                    С
a 22.10993 15.62496 16.26908 14.18844 15.63820
b 15.62496 22.54165 16.71423 14.52362 16.56081
c 16.26908 16.71423 22.64098 16.17123 18.27582
d 14.18844 14.52362 16.17123 21.55906 15.99915
e 15.63820 16.56081 18.27582 15.99915 23.71488
cluster3
cov3
mean3
          b
                С
                       d
                             е
2.536827 3.104285 4.061753 7.005323 -1.320706
                b
                       С
                             d
a 6.503355 -3.585795 3.115404 -5.368328 6.814663
b -3.585795 9.982440 -5.190547 8.518503 -10.629332
c 3.115404 -5.190547 7.476592 -7.796976 8.261310
d -5.368328 8.518503 -7.796976 16.643502 -16.369918
e 6.814663 -10.629332 8.261310 -16.369918 24.058562
probs are
```

```
current log likelihood is
[1] -98994.16
previous log likelihood is
[1] -95098.71
iteration no is 3
cluster1
mean1
                  С
                         d
-9.4205261 1.6720925 0.5089545 1.9195567 -1.2325717
cov1
           b
                 С
                        d
                               е
a 5.985577 -2.089884 -1.582008 -0.6719820 -1.2600897
b -2.089884 7.304713 -1.412763 -1.9662602 -1.6843796
c -1.582008 -1.412763 5.762066 -1.4918616 -0.9825120
d -0.671982 -1.966260 -1.491862 5.0982172 -0.8905837
e -1.260090 -1.684380 -0.982512 -0.8905837 5.0432891
cluster2
mean2
                         d
           h
                  С
                                е
0.1713816 -7.3707978 2.3142853 -6.3079899 1.9871336
        а
              b
                   С
                          d
                               е
a 23.38398 16.87246 17.44728 15.41086 17.06273
b 16.87246 23.69436 17.74265 15.72950 17.90369
c 17.44728 17.74265 23.87780 17.28962 19.50689
d 15.41086 15.72950 17.28962 22.81109 17.13565
e 17.06273 17.90369 19.50689 17.13565 25.08275
cluster3
cov3
mean3
          b
                С
                       d
                             e
2.241167 3.550116 3.690686 7.688975 -2.156220
                b
                             d
         а
                      С
a 5.115679 -2.635674 1.946899 -3.439285 4.031911
b -2.635674 7.780693 -3.640833 5.713763 -7.587262
c 1.946899 -3.640833 5.815178 -5.385393 5.033825
d -3.439285 5.713763 -5.385393 12.078489 -10.983038
e 4.031911 -7.587262 5.033825 -10.983038 16.959273
probs are
0.336315 0.4022754 0.2614096
```

current log likelihood is

0.3363134 0.3782597 0.2854268

```
[1] -102065.2
previous log likelihood is
[1] -98994.16
iteration no is 4
cluster1
mean1
           b
                  С
                         d
     а
-9.4205468 1.6721053 0.5089535 1.9195673 -1.2325795
     а
           b
                         d
                  C
                                е
a 5.985468 -2.089837 -1.5820123 -0.6719210 -1.2601217
b -2.089837 7.304680 -1.4127629 -1.9662887 -1.6843492
c -1.582012 -1.412763 5.7620839 -1.4918656 -0.9825199
d -0.671921 -1.966289 -1.4918656 5.0982051 -0.8905796
e -1.260122 -1.684349 -0.9825199 -0.8905796 5.0432869
cluster2
mean2
           b
                  С
                         d
0.3989927 -7.1541384 2.5596857 -6.0691634 2.2295424
               b
                          d
         а
                     C
                                е
a 23.86436 17.29754 18.04054 15.94369 17.69096
b 17.29754 23.96099 18.15606 16.23392 18.37468
c 18.04054 18.15606 24.43122 17.79777 20.08580
d 15.94369 16.23392 17.79777 23.34730 17.60735
e 17.69096 18.37468 20.08580 17.60735 25.66664
cluster3
cov3
mean3
          b
                 С
                       d
                             е
1.999576 3.972345 3.367925 8.297107 -2.875985
                             d
          а
                 b
                       С
                                    е
a 4.1211054 -1.361649 0.8286628 -1.444612 1.594368
b -1.3616486 5.369867 -1.8281432 2.354499 -3.730085
c 0.8286628 -1.828143 4.3635565 -2.734051 1.884284
d -1.4446120 2.354499 -2.7340513 7.154235 -5.138261
e 1.5943680 -3.730085 1.8842836 -5.138261 10.027699
probs are
0.3363136 0.4200294 0.243657
current log likelihood is
```

[1] -103525.2

```
previous log likelihood is
[1] -102065.2
iteration no is 5
cluster1
mean1
           b
                         d
                  С
-9.4205614 1.6721135 0.5089522 1.9195750 -1.2325835
cov1
            b
                   С
                         d
                                е
a 5.9854005 -2.089810 -1.5820199 -0.6718787 -1.2601406
b -2.0898101 7.304665 -1.4127620 -1.9663079 -1.6843348
c -1.5820199 -1.412762 5.7620975 -1.4918674 -0.9825253
d -0.6718787 -1.966308 -1.4918674 5.0981947 -0.8905765
e -1.2601406 -1.684335 -0.9825253 -0.8905765 5.0432897
cluster2
mean2
           b
                         d
     а
                  С
0.5245994 -6.9859114 2.7050324 -5.8587533 2.3437311
                          d
        а
               b
                    С
                                е
a 23.79001 17.47044 18.12586 16.28817 17.65223
b 17.47044 24.26299 18.40016 16.88909 18.41653
c 18.12586 18.40016 24.49630 18.18729 19.99505
d 16.28817 16.88909 18.18729 24.19872 17.82646
e 17.65223 18.41653 19.99505 17.82646 25.47693
cluster3
cov3
mean3
                       d
          b
                С
                             е
1.854169 4.285466 3.140671 8.714164 -3.379047
                                d
                  h
          а
                        С
a 3.7041524 -0.61204445 0.1824500 -0.34234120 0.2578649
b -0.6120444 3.63132854 -0.6072887 0.04016705 -0.9524094
c 0.1824500 -0.60728871 3.4197673 -1.00483583 -0.1067574
d -0.3423412  0.04016705 -1.0048358  4.06741954 -1.4610259
e 0.2578649 -0.95240937 -0.1067574 -1.46102590 5.5590027
probs are
0.3363126 0.4330677 0.2306197
current log likelihood is
[1] -106541.4
```

previous log likelihood is

```
[1] -103525.2
iteration no is 6
cluster1
mean1
           b
                         d
                  С
-9.4206026 1.6721418 0.5089468 1.9195965 -1.2325987
cov1
            b
                          d
                   С
                                 е
a 5.9852325 -2.089735 -1.5820495 -0.6717643 -1.2601971
b -2.0897349 7.304589 -1.4127507 -1.9663613 -1.6842671
c -1.5820495 -1.412751 5.7621396 -1.4918724 -0.9825463
d -0.6717643 -1.966361 -1.4918724 5.0981697 -0.8905686
e -1.2601971 -1.684267 -0.9825463 -0.8905686 5.0432795
cluster2
mean2
           b
                  С
                         d
0.5563972 -6.9214197 2.7480024 -5.7803718 2.3705892
        а
               b
                    С
                          d
a 23.68541 17.52607 18.10571 16.39182 17.57374
b 17.52607 24.49692 18.52509 17.26322 18.42610
c 18.10571 18.52509 24.48093 18.35713 19.91484
d 16.39182 17.26322 18.35713 24.63268 17.89127
e 17.57374 18.42610 19.91484 17.89127 25.33418
cluster3
cov3
mean3
                       d
    а
                 С
                             е
1.817054 4.367419 3.065671 8.829752 -3.535710
cov3
           а
                  b
                         С
                                d
a 3.66617362 -0.4682693 0.01372052 -0.1061356 -0.06013146
b -0.46826927 3.2661360 -0.29652880 -0.4992564 -0.26276222
c 0.01372052 -0.2965288 3.12287620 -0.5234561 -0.74078621
d -0.10613557 -0.4992564 -0.52345613 3.3555327 -0.50813998
e -0.06013146 -0.2627622 -0.74078621 -0.5081400 4.25026832
probs are
0.3363096 0.4372175 0.2264729
current log likelihood is
[1] -109207.3
previous log likelihood is
[1] -106541.4
iteration no is 7
```

```
cluster1
```

cluster1

```
mean1
    а
          b
                С
                       d
-9.420640 1.672166 0.508942 1.919616 -1.232611
cov1
            b
                          d
a 5.9850857 -2.089672 -1.5820781 -0.6716606 -1.2602451
b -2.0896722 7.304532 -1.4127416 -1.9664090 -1.6842136
c -1.5820781 -1.412742 5.7621779 -1.4918758 -0.9825643
d -0.6716606 -1.966409 -1.4918758 5.0981456 -0.8905615
e -1.2602451 -1.684214 -0.9825643 -0.8905615 5.0432749
cluster2
mean2
          b
                 С
                       d
0.556480 -6.921087 2.748154 -5.780003 2.370692
               b
                          d
a 23.68501 17.52615 18.10554 16.39203 17.57343
b 17.52615 24.49863 18.52561 17.26547 18.42620
c 18.10554 18.52561 24.48067 18.35783 19.91455
d 16.39203 17.26547 18.35783 24.63501 17.89156
e 17.57343 18.42620 19.91455 17.89156 25.33356
cluster3
cov3
mean3
          b
                 С
                       d
                             е
    а
1.816915 4.367623 3.065379 8.830111 -3.536339
                  b
                                d
                         С
a 3.66613293 -0.4679031 0.01312731 -0.1054236 -0.06140707
b -0.46790311 3.2657056 -0.29570474 -0.5003787 -0.26093841
c 0.01312731 -0.2957047 3.12183291 -0.5219747 -0.74351283
d -0.10542364 -0.5003787 -0.52197468 3.3538682 -0.50491422
e -0.06140707 -0.2609384 -0.74351283 -0.5049142 4.24477078
probs are
0.3363068 0.4372359 0.2264573
current log likelihood is
[1] -109216
previous log likelihood is
[1] -109207.3
iteration no is 8
```

```
d
-9.4206401 1.6721661 0.5089419 1.9196165 -1.2326116
cov1
                          d
a 5.9850839 -2.089671 -1.5820784 -0.6716593 -1.2602457
b -2.0896714 7.304532 -1.4127415 -1.9664095 -1.6842130
c -1.5820784 -1.412742 5.7621783 -1.4918759 -0.9825645
d -0.6716593 -1.966410 -1.4918759 5.0981453 -0.8905614
e -1.2602457 -1.684213 -0.9825645 -0.8905614 5.0432748
cluster2
mean2
                         d
           b
                  C
                                е
0.5564796 -6.9210863 2.7481543 -5.7800026 2.3706915
             b
                    С
                          d
a 23.68501 17.52614 18.10554 16.39203 17.57343
b 17.52614 24.49863 18.52561 17.26548 18.42620
c 18.10554 18.52561 24.48067 18.35783 19.91455
d 16.39203 17.26548 18.35783 24.63501 17.89156
e 17.57343 18.42620 19.91455 17.89156 25.33356
cluster3
cov3
mean3
                       d
          h
                             e
                 C
1.816915 4.367623 3.065379 8.830111 -3.536339
                               d
a 3.66613292 -0.4679031 0.0131273 -0.1054236 -0.06140713
b -0.46790308 3.2657056 -0.2957047 -0.5003788 -0.26093835
c 0.01312730 -0.2957047 3.1218329 -0.5219746 -0.74351290
d -0.10542359 -0.5003788 -0.5219746 3.3538682 -0.50491411
e -0.06140713 -0.2609383 -0.7435129 -0.5049141 4.24477062
probs are
0.3363068 0.4372359 0.2264573
current log likelihood is
[1] -109216
previous log likelihood is
[1] -109216
iteration no is 9
cluster1
mean1
           b
                         d
     а
                  С
                                е
```

mean1

```
cov1
      а
            b
                   С
                          d
                                 е
a 5.9850839 -2.089671 -1.5820784 -0.6716593 -1.2602457
b -2.0896714 7.304532 -1.4127415 -1.9664095 -1.6842130
c -1.5820784 -1.412742 5.7621783 -1.4918759 -0.9825645
d -0.6716593 -1.966410 -1.4918759 5.0981453 -0.8905614
e -1.2602457 -1.684213 -0.9825645 -0.8905614 5.0432748
cluster2
mean2
           b
                  C
                         d
0.5564796 -6.9210863 2.7481543 -5.7800026 2.3706915
               b
                    С
                          d
a 23.68501 17.52614 18.10554 16.39203 17.57343
b 17.52614 24.49863 18.52561 17.26548 18.42620
c 18.10554 18.52561 24.48067 18.35783 19.91455
d 16.39203 17.26548 18.35783 24.63501 17.89156
e 17.57343 18.42620 19.91455 17.89156 25.33356
cluster3
cov3
mean3
          b
                 С
                       d
                             e
1.816915 4.367623 3.065379 8.830111 -3.536339
                  b
                               d
           а
                         С
a 3.66613292 -0.4679031 0.0131273 -0.1054236 -0.06140713
b -0.46790308 3.2657056 -0.2957047 -0.5003788 -0.26093835
c 0.01312730 -0.2957047 3.1218329 -0.5219746 -0.74351290
d -0.10542359 -0.5003788 -0.5219746 3.3538682 -0.50491411
e -0.06140713 -0.2609383 -0.7435129 -0.5049141 4.24477062
probs are
0.3363068 0.4372359 0.2264573
current log likelihood is
[1] -109216
previous log likelihood is
[1] -109216
iteration no is 10
cluster1
mean1
                         d
-9.4206401 1.6721661 0.5089419 1.9196165 -1.2326116
cov1
```

-9.4206401 1.6721661 0.5089419 1.9196165 -1.2326116

```
b
                   С
                          d
                                 е
a 5.9850839 -2.089671 -1.5820784 -0.6716593 -1.2602457
b -2.0896714 7.304532 -1.4127415 -1.9664095 -1.6842130
c -1.5820784 -1.412742 5.7621783 -1.4918759 -0.9825645
d -0.6716593 -1.966410 -1.4918759 5.0981453 -0.8905614
e -1.2602457 -1.684213 -0.9825645 -0.8905614 5.0432748
cluster2
mean2
           b
                  С
                         d
0.5564796 -6.9210863 2.7481543 -5.7800026 2.3706915
        а
               b
                    С
                          d
                                е
a 23.68501 17.52614 18.10554 16.39203 17.57343
b 17.52614 24.49863 18.52561 17.26548 18.42620
c 18.10554 18.52561 24.48067 18.35783 19.91455
d 16.39203 17.26548 18.35783 24.63501 17.89156
e 17.57343 18.42620 19.91455 17.89156 25.33356
cluster3
cov3
mean3
          b
                 С
                       d
                             е
1.816915 4.367623 3.065379 8.830111 -3.536339
                  b
                               d
           а
                         С
a 3.66613292 -0.4679031 0.0131273 -0.1054236 -0.06140713
b -0.46790308 3.2657056 -0.2957047 -0.5003788 -0.26093835
c 0.01312730 -0.2957047 3.1218329 -0.5219746 -0.74351290
d -0.10542359 -0.5003788 -0.5219746 3.3538682 -0.50491411
e -0.06140713 -0.2609383 -0.7435129 -0.5049141 4.24477062
probs are
0.3363068 0.4372359 0.2264573
current log likelihood is
[1] -109216
previous log likelihood is
[1] -109216
total elements in respective clusters are
[1] 150
[1] 195
[1] 101
Final mean for cluster 1
                         d
                                е
-9.4206401 1.6721661 0.5089419 1.9196165 -1.2326116
```

```
0.5564796 -6.9210863 2.7481543 -5.7800026 2.3706915
Final mean for cluster 3
          b
                С
1.816915 4.367623 3.065379 8.830111 -3.536339
Final covariance for cluster 1
                                        b
                                                             е
a 5.9850839 -2.089671 -1.5820784 -0.6716593 -1.2602457
b -2.0896714 7.304532 -1.4127415 -1.9664095 -1.6842130
c -1.5820784 -1.412742 5.7621783 -1.4918759 -0.9825645
d -0.6716593 -1.966410 -1.4918759 5.0981453 -0.8905614
e -1.2602457 -1.684213 -0.9825645 -0.8905614 5.0432748
Final covariance for cluster 2
                                                  d
                                      b
                                 а
                                                        e
a 23.68501 17.52614 18.10554 16.39203 17.57343
b 17.52614 24.49863 18.52561 17.26548 18.42620
c 18.10554 18.52561 24.48067 18.35783 19.91455
d 16.39203 17.26548 18.35783 24.63501 17.89156
e 17.57343 18.42620 19.91455 17.89156 25.33356
Final covariance for cluster 3
                                                              е
a 3.66613292 -0.4679031 0.0131273 -0.1054236 -0.06140713
b -0.46790308 3.2657056 -0.2957047 -0.5003788 -0.26093835
c 0.01312730 -0.2957047 3.1218329 -0.5219746 -0.74351290
d -0.10542359 -0.5003788 -0.5219746 3.3538682 -0.50491411
e -0.06140713 -0.2609383 -0.7435129 -0.5049141 4.24477062
```

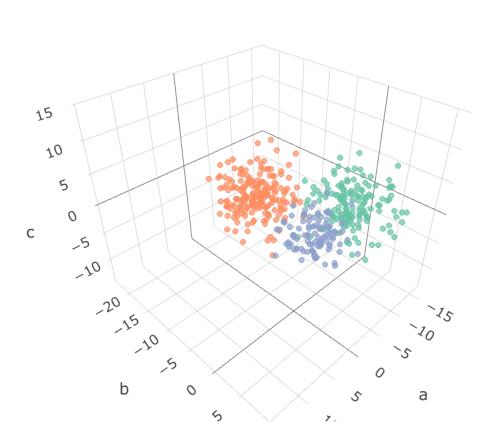
Final mean for cluster 2 b

а

C

d

3D Plot



Cluster1 Cluster2 Cluster3