```
library(mvtnorm)
library(micEcon)
# calculate mle of binomial distribution -
calculate_binom_mle <- function(sample) {</pre>
 # calculate negative log likelihood
 nll <- function(data, n, p) {</pre>
  -sum(dbinom(x=data, size=n, prob=p, log=TRUE))
 }
 mle = optim(par = c(p = 0.5), n = 10, fn = nll, data = sample, method = "BFGS")
 return(mle)
}
# calculate MLE of multivariate distribution
calculate_multivariate_mle <- function(sample) {</pre>
 # calculate negative log likelihood
 nll <- function(par, data) {
  mu = c(par[1], par[2])
  #print(mu)
  sigma = matrix(c(par[3], par[4], par[5], par[6]), 2, 2)
  sigma[lower.tri(sigma)] = t(sigma)[lower.tri(sigma)]
  #print(sigma)
  -sum(dmvnorm(x = data, mu, sigma, log = TRUE))
 mle = optim(par = c(mu = c(2,2), sigma = matrix(c(2,2,2,2), 2, 2)), fn = nll, data = sample, method =
"SANN")
 return(mle)
}
```

calculate mle of multinomial distribution -

```
calculate_multinom_mle <- function(sample) {</pre>
 # calculate negative log likelihood
 nll <- function(parameters, data) {</pre>
  p = parameters
  # cat("p",p)
  #-sum(dmultinom(x=data[,1], size=NULL, prob=p, log=TRUE))
  -sum(apply(X = data,MARGIN = 2,FUN = dmultinom,size =1, prob = p, log = TRUE))
 }
 len = nrow(sample)
 mle = optim(par <- rep(1/len,len), fn = nll, data = sample, method = "L-BFGS-B",
        lower = rep(0.000000001,len),upper = rep(1,len))
 return(mle)
}
# calculate mle of geometric
calculate_geometric_mle <- function(sample) {</pre>
 nll <- function(parameters, data) {</pre>
  prob = parameters[1]
  -sum(dgeom(x=data, prob=prob, log=TRUE))
 }
 mle = optim(par = c(prob=0.4), fn=nll, data=sample,
        control = list(parscale = c(prob=0.4)))
 return(mle)
}
# calculate mle of poisson
calculate_poisson_mle <- function(sample) {</pre>
```

```
nll <- function(parameters, data) {</pre>
  lambda = parameters[1]
  -sum(dpois(x = data, lambda = lambda, log=TRUE))
 }
 mle = optim(par = c(lambda=8), fn = nll, data = sample,
        control = list(parscale = c(lambda = 8)))
 return(mle)
}
# calculate one step of poisson
onestep_pois <- function(sample, m, reptn = 100)</pre>
{
 #mean of sample poisson distribution
 x_mean <- mean(sample)</pre>
 for(i in 1:reptn)
  #log-likelihood of PDF of poisson
  lglik <- expression(log((exp(-m)*(m^(sample)))/factorial(sample))))</pre>
  #First partial derivative of log-likelihood wrt mu
  f_derv <- D(lglik, "m")
  frst_derv <- eval(f_derv)</pre>
  #Second partial derivative of log-likelihood wrt mu
  s_derv <- D(f_derv, "m")</pre>
  sec_derv <- eval(s_derv)</pre>
  sdbt <- sum(frst_derv)</pre>
  sdbtt <- sum(sec_derv)</pre>
  #sequence that converges to MLE
```

```
theta <- m
  theta.hat <- theta - (sdbt / sdbtt)
  m <- theta.hat
 }
 return(m)
}
# calculate mle of exponential -
calculate_exp_mle <- function(sample) {</pre>
 nll <- function(parameters, data) {</pre>
  lambda = parameters[1]
  -sum(dexp(x = data, rate = lambda, log=TRUE))
 }
 mle = optim(par = c(lambda=8), fn = nll, data = sample,
        control = list(parscale = c(lambda = 8)))
 return(mle)
}
# calculate mle of beta -
calculate_beta_mle <- function(sample) {</pre>
 nll <- function(parameters, data) {</pre>
  alpha = parameters[1]
  beta = parameters[2]
  -sum(dbeta(x = data, shape1 = alpha, shape2 = beta, log=TRUE))
 }
 mle = optim(par = c(alpha = 1, beta = 10), fn = nll, data = sample,
        control=list(parscale = c(alpha = 1, beta = 10)))
 return(mle)
```

```
# calculate mle of uniform distribution
calculate_uniform_mle <- function(sample) {</pre>
 nll <- function(parameters, data) {</pre>
  min = parameters[1]
  max = parameters[2]
  -sum(dunif(x = data, min = min, max = max, log=TRUE))
 }
 mle = optim(par = c(min = -10, max = 10), fn = nll, data = sample,
        control=list(parscale = c(min = -10, max = 10)))
 return(mle)
}
# calculate mle of normal distribution
calculate_normal_mle <- function (sample) {</pre>
 # calculate negative log likelihood
 nll <- function(parameters, data) {</pre>
  mu = parameters[1]
  sigma = parameters[2]
  -sum(dnorm(x = data, mean = mu, sd = sigma, log = TRUE))
 }
 mle = optim(par = c(mu=0.2, sigma = 1.5), fn = nll, data = sample,
        control = list(parscale = c(mu = 0.2, sigma = 1.5)))
 return(mle)
}
```

}

```
main <- function (sample_vec,dist_type)</pre>
{
 if(dist_type == "uniform" || dist_type == "Uniform" || dist_type == "UNIFORM")
 {
  uniform_sample = runif(10, -10, 10)
  uniform_mle = calculate_uniform_mle(uniform_sample)
  cat("\n\ndistribution type is ",dist_type)
  cat("\n\nsample is\n",sample,"\n")
  cat("MLE is given Below\n")
  print(uniform_mle$par)
}
 else if(dist_type == "beta" || dist_type == "Beta" || dist_type == "BETA")
 {
  sample = rbeta(10,1,10)
  cat(sample)
  sample_mle = calculate_beta_mle(sample)
  cat("\n\ndistribution type is ",dist_type)
  cat("\n\nsample is\n",sample,"\n")
  cat("MLE is given Below\n")
  print(sample_mle$par)
}
 else if(dist_type == "normal" || dist_type == "Normal" || dist_type == "NORMAL")
  sample = rnorm(10)
  normal_mle = calculate_normal_mle(sample)
  cat("\n\ndistribution type is ",dist_type)
```

```
cat("\n\nsample is\n",sample,"\n")
 cat("MLE is given Below\n")
 print(normal_mle$par)
}
else if(dist_type=="poisson"||dist_type=="Poisson"||dist_type=="POISSON")
{
 sample = rpois(10, 8)
 poisson_mle = calculate_poisson_mle(sample)
 cat("\n\ndistribution type is ",dist_type)
 cat("\n\nsample is\n",sample,"\n")
 cat("MLE is given Below\n")
 print(poisson_mle$par)
 posison_os = onestep_pois(sample, 8, 100)
 cat("The approximated MLE value using one-step is",posison_os,"\n")
}
else if(dist_type=="geometric"||dist_type=="Geometric"||dist_type=="GEOMETRIC")
{
 sample = rgeom(10, 0.4)
 cat("\n\ndistribution type is ",dist_type)
 cat("\n\nsample is\n",sample,"\n")
 cat("MLE is given Below\n")
 geom_mle = calculate_geometric_mle(sample)
 print(geom_mle$par)
}
else if(dist_type=="binomial"||dist_type=="Binomial"||dist_type=="BINOMIAL")
 sample = rbinom(4,10,0.5)
 cat("\n\ndistribution type is ",dist_type)
```

```
cat("\n\nsample is\n",sample,"\n")
  cat("MLE is given Below\n")
  binom_mle = calculate_binom_mle(sample)
  print(binom_mle$par)
}
else if(dist_type=="exponential"||dist_type=="Exponential"||dist_type=="EXPONENTIAL")
{
  sample = rexp(5)
  cat("\n\ndistribution type is ",dist_type)
  cat("\n\nsample is\n",sample,"\n")
  cat("MLE is given Below\n")
  sample_mle = calculate_exp_mle(sample)
  print(sample_mle$par)
}
else if(dist_type=="multinomial"||dist_type=="Multinomial"||dist_type=="MULTINOMIAL")
{
  sample = rmultinom(5,1,rep(1/10,10))
  cat("\n\ndistribution type is ",dist_type)
  cat("\n\nsample is\n",sample,"\n")
  cat("MLE is given Below\n")
  sample_mle = calculate_multinom_mle(sample)
  print(sample_mle$par)
}
else if(dist_type =="Multivariate Normal"||dist_type=="multivariate
normal"||dist_type=="MULTIVARIATE NORMAL")
{
  sigma <- matrix(c(3,2,2,8), 2, 2)
  mu <- c(7,10)
  sample <- rmvnorm(10, mean = mu, sigma = sigma)</pre>
```

```
cat("\n\ndistribution type is ",dist_type)
cat("\n\nsample is")
print(sample)
cat("MLE is given Below\n")
sample_mle = calculate_multivariate_mle(sample)
print(sample_mle$par)
}
main(c(),'poisson')
```