$$U_{\alpha} = e^{iq\alpha}$$