

An exploded view diagram of the HTC Vive VR headset components. The parts are arranged in a disassembled state, showing the front and rear faceplates, the main body with internal components like the camera and sensors, the head strap, and various smaller parts like the lens, foam padding, and screws. The HTC logo is visible on the head strap.

EE 267 Virtual Reality

stanford.edu/class/ee267/

WARNING

- this class will be dense!
- will learn how to use nonlinear optimization (Levenberg-Marquardt algorithm) for pose estimation
- why ???
 - more accurate than homography method
 - can dial in lens distortion estimation, and estimation of intrinsic parameters (beyond this lecture, see lecture notes)
 - LM is very common in 3D computer vision → camera-based tracking

Overview

The diagram illustrates the overview of a system. A camera on the left captures a scene, projecting rays onto a plane. This plane contains a vector $b = \begin{bmatrix} x_1^n \\ y_1^n \\ \vdots \\ x_4^n \\ y_4^n \end{bmatrix}$. The plane is connected to a 3D volume, which is further connected to a vector $p = \begin{bmatrix} \theta_x \\ \theta_y \\ \theta_z \\ t_x \\ t_y \\ t_z \end{bmatrix}$. The 3D volume is also connected to a vector $\begin{bmatrix} x_i \\ y_i \\ 0 \end{bmatrix}$.

- $$\underset{\{p\}}{\text{minimize}} \left\| b - \underset{\substack{\uparrow \\ \text{image formation}}}{f(g(p))} \right\|_2^2$$

- minimize reprojection error
- pose p is 6-element vector with 3 Euler angles and translation of VRduino w.r.t. base station

Overview

- review: gradients, Jacobian matrix, chain rule, iterative optimization
- nonlinear optimization: Gauss-Newton, Levenberg-Marquardt
- pose estimation using LM
- pose estimation with VRduino using nonlinear optimization

Review

Review: Gradients

- gradient of a function that depends on multiple variables:

$$\frac{\partial}{\partial x} f(x) = \left(\frac{\partial f}{\partial x_1}, \frac{\partial f}{\partial x_2}, \dots, \frac{\partial f}{\partial x_n} \right)$$

$$f : \Re^n \rightarrow \Re$$

Review: The Jacobian Matrix

- gradient of a vector-valued function that depends on multiple variables:

$$\frac{\partial}{\partial x} f(x) = J_f = \begin{pmatrix} \frac{\partial f_1}{\partial x_1} & \dots & \frac{\partial f_1}{\partial x_n} \\ \vdots & \ddots & \vdots \\ \frac{\partial f_m}{\partial x_1} & \dots & \frac{\partial f_m}{\partial x_n} \end{pmatrix}$$

$$f : \Re^n \rightarrow \Re^m, \quad J_f \in \Re^{m \times n}$$

Review: The Chain Rule

- here's how you've probably been using it so far:

$$\frac{\partial}{\partial x} f(g(x)) = \frac{\partial f}{\partial g} \cdot \frac{\partial g}{\partial x}$$

- this rule applies when $f : \mathfrak{K} \rightarrow \mathfrak{K}$
 $g : \mathfrak{K} \rightarrow \mathfrak{K}$

Review: The Chain Rule

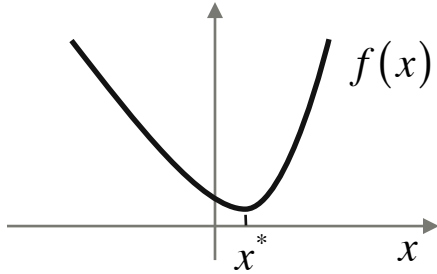
- here's how it is applied in general:

$$\frac{\partial}{\partial x} f(g(x)) = J_f \cdot J_g = \begin{pmatrix} \frac{\partial f_1}{\partial g_1} & \dots & \frac{\partial f_1}{\partial g_o} \\ \vdots & \ddots & \vdots \\ \frac{\partial f_m}{\partial g_1} & \dots & \frac{\partial f_m}{\partial g_o} \end{pmatrix} \cdot \begin{pmatrix} \frac{\partial g_1}{\partial x_1} & \dots & \frac{\partial g_1}{\partial x_n} \\ \vdots & \ddots & \vdots \\ \frac{\partial g_o}{\partial x_1} & \dots & \frac{\partial g_o}{\partial x_n} \end{pmatrix}$$

$$f : \mathfrak{R}^o \rightarrow \mathfrak{R}^m, \quad g : \mathfrak{R}^n \rightarrow \mathfrak{R}^o, \quad J_f \in \mathfrak{R}^{m \times o}, \quad J_g \in \mathfrak{R}^{o \times n}$$

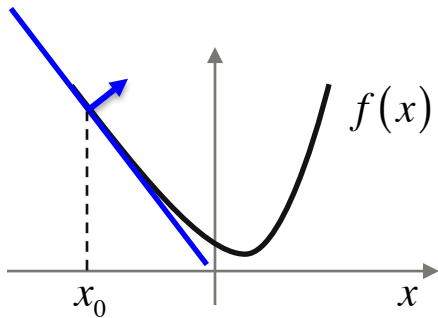
Review: Minimizing a Function

- goal: find point x^* that minimizes a nonlinear function $f(x)$



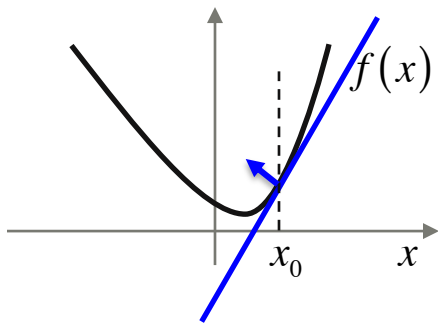
Review: What is a Gradient?

- gradient of f at some point x_0 is the slope at that point



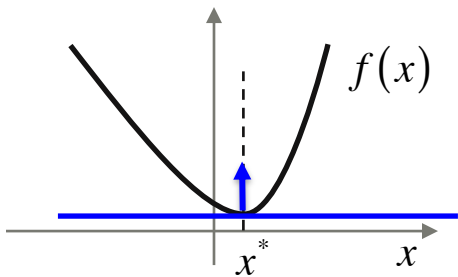
Review: What is a Gradient?

- gradient of f at some point x_0 is the slope at that point



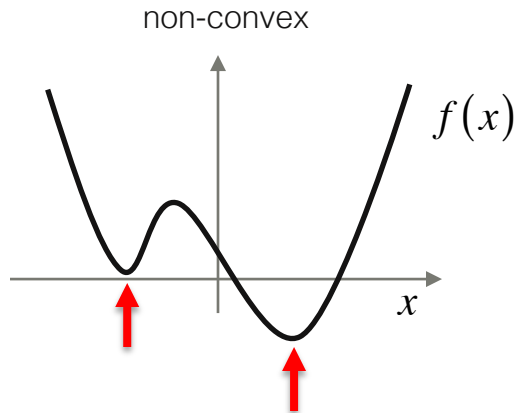
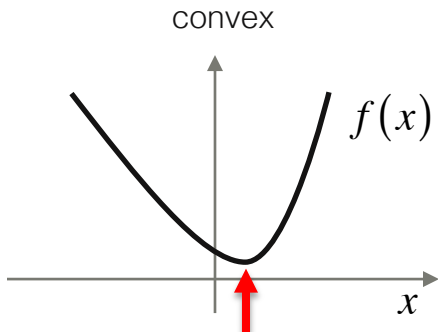
Review: What is a Gradient?

- extremum is where gradient is 0! (sometimes have to check 2nd derivative to see if it's a minimum and not a maximum or saddle point)



Review: Optimization

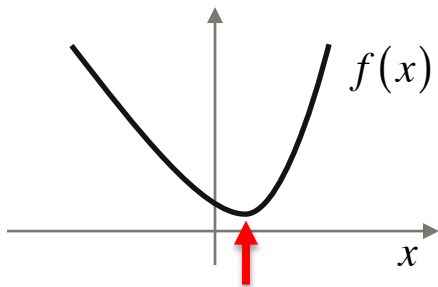
- extremum is where gradient is 0! (sometimes have to check 2nd derivative to see if it's a minimum and not a maximum or saddle point)



- convex optimization: there is only a single *global* minimum
- non-convex optimization: multiple *local* minima

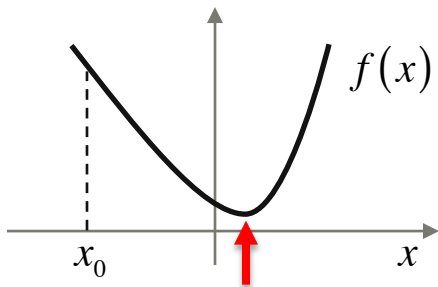
Review: Optimization

- how to find where gradient is 0?



Review: Optimization

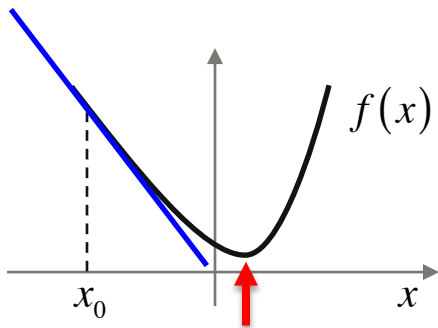
- how to find where gradient is 0?



1. start with some initial guess x_0 , e.g. a random value

Review: Optimization

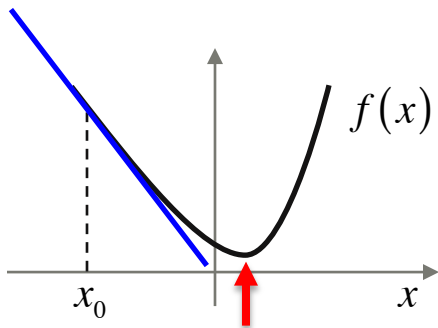
- how to find where gradient is 0?



1. start with some initial guess x_0 , e.g. a random value
2. update guess by linearizing function and minimizing that

Review: Optimization

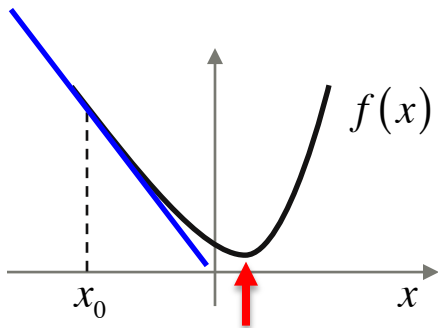
- how to linearize a function? \rightarrow using Taylor expansion!



$$f(x_0 + \Delta x) \approx f(x_0) + J_f \Delta x + \varepsilon$$

Review: Optimization

- find minimum of linear function approximation

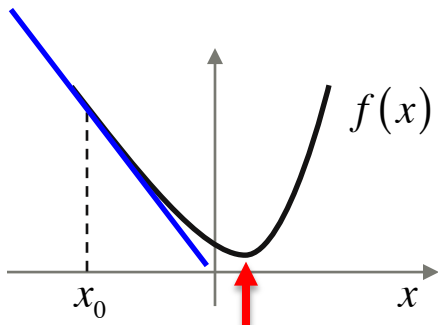


$$f(x_0 + \Delta x) \approx f(x_0) + J_f \Delta x + \varepsilon$$

$$\begin{aligned} \underset{\Delta x}{\text{minimize}} \quad & \|b - f(x_0 + \Delta x)\|_2^2 \\ & \approx \|b - (f(x_0) + J_f \Delta x)\|_2^2 \end{aligned}$$

Review: Optimization

- find minimum of linear function approximation (gradient=0)



$$f(x_0 + \Delta x) \approx f(x_0) + J_f \Delta x + \varepsilon$$

$$\begin{aligned} \underset{\Delta x}{\text{minimize}} \quad & \|b - f(x_0 + \Delta x)\|_2^2 \\ & \approx \|b - (f(x_0) + J_f \Delta x)\|_2^2 \end{aligned}$$

equate gradient to zero:

$$0 = J_f^T J_f \Delta x - J_f^T (b - f(x))$$

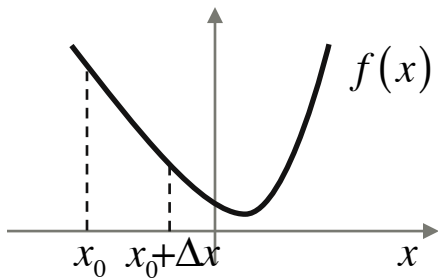


$$\Delta x = (J_f^T J_f)^{-1} J_f^T (b - f(x))$$

normal equations

Review: Optimization

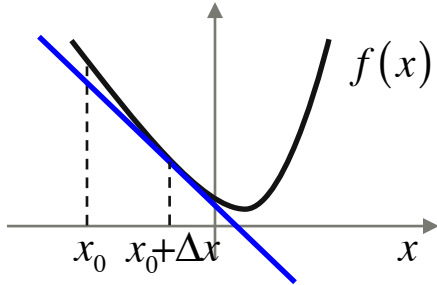
- take step and repeat procedure



$$\Delta x = \left(J_f^T J_f \right)^{-1} J_f^T (b - f(x))$$

Review: Optimization

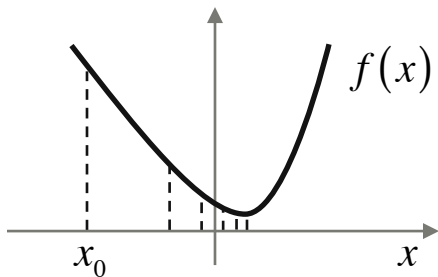
- take step and repeat procedure, will get there eventually



$$\Delta x = \left(J_f^T J_f \right)^{-1} J_f^T (b - f(x))$$

Review: Optimization – Gauss-Newton

- results in an iterative algorithm

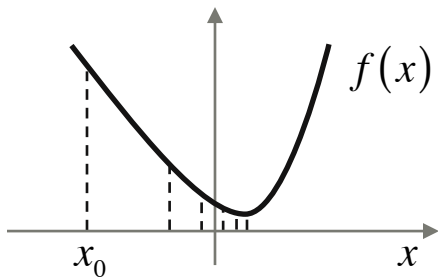


$$x_{k+1} = x_k + \Delta x$$

$$\Delta x = \left(J_f^T J_f \right)^{-1} J_f^T (b - f(x))$$

Review: Optimization – Gauss-Newton

- results in an iterative algorithm

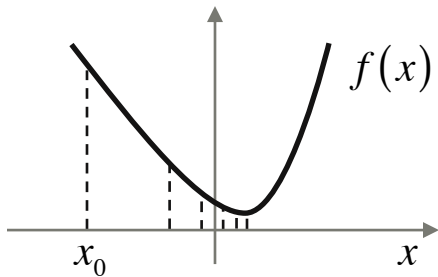


```
1. x = rand() // initialize x0
2. for k=1 to max_iter
3.   f = eval_objective(x)
4.   J = eval_jacobian(x)
5.   x = x + inv(J'*J)*J'*(b-f) // update x
```

$$\Delta x = \left(J_f^T J_f \right)^{-1} J_f^T (b - f(x))$$

Review: Optimization – Gauss-Newton

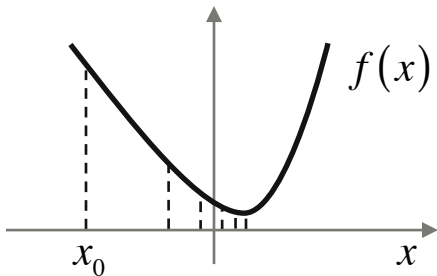
- matrix $J^T J$ can be ill-conditioned (i.e. not invertible)



$$\Delta x = \left(J_f^T J_f \right)^{-1} J_f^T (b - f(x))$$

Review: Optimization – Levenberg

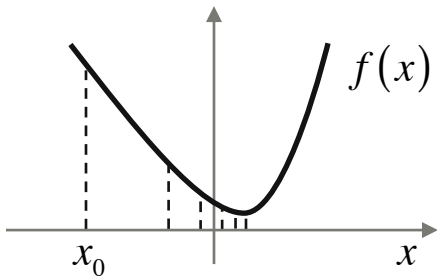
- matrix $J^T J$ can be ill-conditioned (i.e. not invertible)
- add a diagonal matrix to make invertible – acts as damping



$$\Delta x = \left(J_f^T J_f + \lambda I \right)^{-1} J_f^T (b - f(x))$$

Review: Optimization – Levenberg-Marquardt

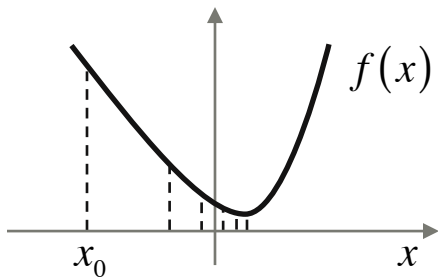
- matrix $J^T J$ can be ill-conditioned (i.e. not invertible)
- better: use $J^T J$ instead of I as damping. This is LM!



$$\Delta x = \left(J_f^T J_f + \lambda \operatorname{diag} \left(J_f^T J_f \right) \right)^{-1} J_f^T (b - f(x))$$

Review: Optimization – Levenberg-Marquardt

- matrix $J^T J$ can be ill-conditioned (i.e. not invertible)
- better: use $J^T J$ instead of $/$ as damping. This is LM!



```
1. x = rand() // initialize x0
2. for k=1 to max_iter
3.   f = eval_objective(x)
4.   J = eval_jacobian(x)
5.   x = x + inv(J' * J + lambda * diag(J' * J)) * J' * (b - f)
```

$$\Delta x = \left(J_f^T J_f + \lambda \text{diag}(J_f^T J_f) \right)^{-1} J_f^T (b - f(x))$$

Pose Estimation via Levenberg-Marquardt

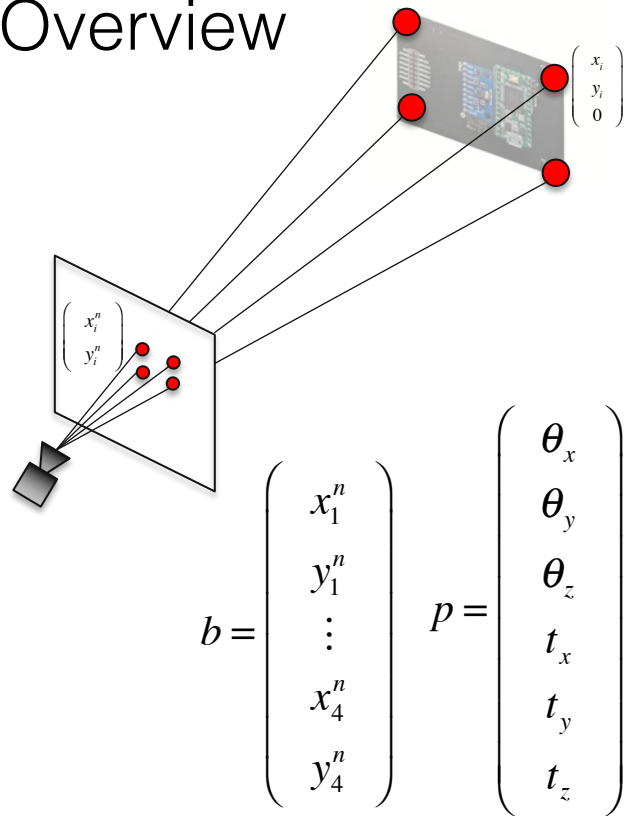
Pose Estimation - Overview

- goal: estimate pose via nonlinear least squares optimization

$$\underset{\{p\}}{\text{minimize}} \left\| b - f(g(p)) \right\|_2^2$$

↑
image formation

- minimize reprojection error
- pose p is 6-element vector with 3 Euler angles and translation of VRduino w.r.t. base station



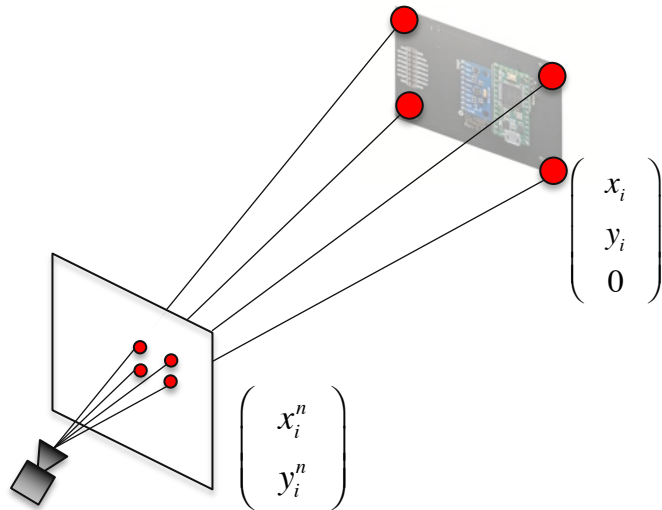
Pose Estimation - Objective Function

- goal: estimate pose via nonlinear least squares optimization

$$\underset{\{p\}}{\text{minimize}} \left\| b - f(g(p)) \right\|_2^2$$

↑
image formation

- objective function is sum of squares of reprojection error



$$\left\| b - f(g(p)) \right\|_2^2 = \left(x_1^n - f_1(g(p)) \right)^2 + \left(y_1^n - f_2(g(p)) \right)^2 + \dots + \left(x_4^n - f_7(g(p)) \right)^2 + \left(y_4^n - f_8(g(p)) \right)^2$$

Image Formation

1. transform 3D point into view space:

$$\begin{pmatrix} x_i^c \\ y_i^c \\ w_i^c \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \cdot \begin{pmatrix} r_{11} & r_{12} & t_x \\ r_{21} & r_{22} & t_y \\ r_{31} & r_{32} & t_z \end{pmatrix} \cdot \begin{pmatrix} x_i \\ y_i \\ 1 \end{pmatrix}$$
$$= \begin{pmatrix} h_1 & h_2 & h_3 \\ h_4 & h_5 & h_6 \\ h_7 & h_8 & h_9 \end{pmatrix} \cdot \begin{pmatrix} x_i \\ y_i \\ 1 \end{pmatrix}$$

2. perspective divide:

$$\begin{pmatrix} x_i^n \\ y_i^n \end{pmatrix} = \begin{pmatrix} \frac{x_i^c}{w_i^c} \\ \frac{y_i^c}{w_i^c} \end{pmatrix}$$

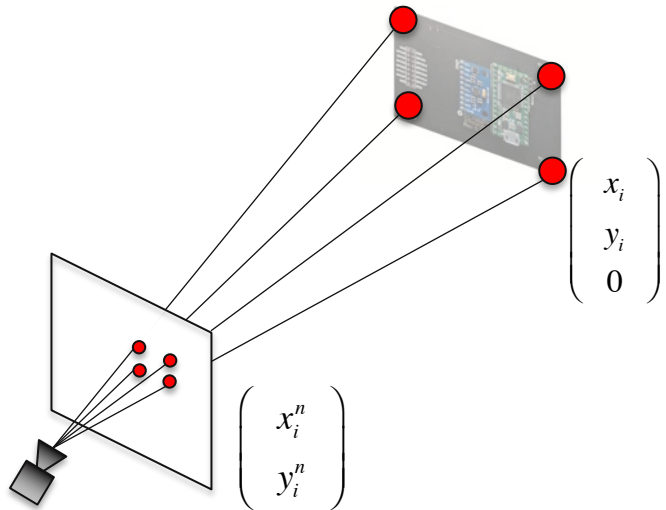


Image Formation: $g(p)$ and $f(h)$

- split up image formation into two functions

$$f(h) = f(g(p))$$

$$g : \mathfrak{R}^6 \rightarrow \mathfrak{R}^9, \quad f : \mathfrak{R}^9 \rightarrow \mathfrak{R}^8$$

Image Formation: $f(h)$

- $f(h)$ uses elements of homography matrix h to compute projected 2D coordinates as

$$f(h) = \begin{pmatrix} f_1(h) \\ f_2(h) \\ \vdots \\ f_7(h) \\ f_8(h) \end{pmatrix} = \begin{pmatrix} x_1^n \\ y_1^n \\ \vdots \\ x_4^n \\ y_4^n \end{pmatrix} = \begin{pmatrix} \frac{h_1x_1 + h_2y_1 + h_3}{h_7x_1 + h_8y_1 + h_9} \\ \frac{h_4x_1 + h_5y_1 + h_6}{h_7x_1 + h_8y_1 + h_9} \\ \vdots \\ \frac{h_1x_4 + h_2y_4 + h_3}{h_7x_4 + h_8y_4 + h_9} \\ \frac{h_4x_4 + h_5y_4 + h_6}{h_7x_4 + h_8y_4 + h_9} \end{pmatrix}$$

Jacobian Matrix of $f(h)$

$$f_1(h) = \frac{h_1 x_1 + h_2 y_1 + h_3}{h_7 x_1 + h_8 y_1 + h_9}$$

$$J_f = \begin{pmatrix} \frac{\partial f_1}{\partial h_1} & \dots & \frac{\partial f_1}{\partial h_9} \\ \vdots & \ddots & \vdots \\ \frac{\partial f_8}{\partial h_1} & \dots & \frac{\partial f_8}{\partial h_9} \end{pmatrix}$$

- first row of Jacobian matrix



$$\frac{\partial f_1}{\partial h_1} = \frac{x_1}{h_7 x_1 + h_8 y_1 + h_9}$$

$$\frac{\partial f_1}{\partial h_2} = \frac{y_1}{h_7 x_1 + h_8 y_1 + h_9}$$

$$\frac{\partial f_1}{\partial h_3} = \frac{1}{h_7 x_1 + h_8 y_1 + h_9}$$

$$\frac{\partial f_1}{\partial h_4} = 0, \quad \frac{\partial f_1}{\partial h_5} = 0, \quad \frac{\partial f_1}{\partial h_6} = 0$$

$$\frac{\partial f_1}{\partial h_7} = - \left(\frac{h_1 x_1 + h_2 y_1 + h_3}{(h_7 x_1 + h_8 y_1 + h_9)^2} \right) x_1$$

$$\frac{\partial f_1}{\partial h_8} = - \left(\frac{h_1 x_1 + h_2 y_1 + h_3}{(h_7 x_1 + h_8 y_1 + h_9)^2} \right) y_1$$

$$\frac{\partial f_1}{\partial h_9} = - \frac{h_1 x_1 + h_2 y_1 + h_3}{(h_7 x_1 + h_8 y_1 + h_9)^2}$$

Jacobian Matrix of $f(h)$

$$J_f = \begin{pmatrix} \frac{\partial f_1}{\partial h_1} & \dots & \frac{\partial f_1}{\partial h_9} \\ \vdots & \ddots & \vdots \\ \frac{\partial f_8}{\partial h_1} & \dots & \frac{\partial f_8}{\partial h_9} \end{pmatrix}$$

- the remaining rows of the Jacobian can be derived with a similar pattern
- see ***course notes*** for a detailed derivation of the elements of this Jacobian matrix

Image Formation: $g(p)$

- $g(p)$ uses 6 pose parameters to compute elements of homography matrix h as

$$g(p) = \begin{pmatrix} g_1(p) \\ \vdots \\ g_9(p) \end{pmatrix} = \begin{pmatrix} h_1 \\ \vdots \\ h_9 \end{pmatrix}$$

definition of homography matrix:

$$\begin{pmatrix} h_1 & h_2 & h_3 \\ h_4 & h_5 & h_6 \\ h_7 & h_8 & h_9 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \cdot \begin{pmatrix} r_{11} & r_{12} & t_x \\ r_{21} & r_{22} & t_y \\ r_{31} & r_{32} & t_z \end{pmatrix}$$

rotation matrix from Euler angles:

$$R = R_z(\theta_z) \cdot R_x(\theta_x) \cdot R_y(\theta_y)$$
$$\begin{pmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{pmatrix} = \begin{pmatrix} \cos(\theta_z) & -\sin(\theta_z) & 0 \\ \sin(\theta_z) & \cos(\theta_z) & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos(\theta_x) & -\sin(\theta_x) \\ 0 & \sin(\theta_x) & \cos(\theta_x) \end{pmatrix} \begin{pmatrix} \cos(\theta_y) & 0 & \sin(\theta_y) \\ 0 & 1 & 0 \\ -\sin(\theta_y) & 0 & \cos(\theta_y) \end{pmatrix}$$

Image Formation: $g(p)$

- write as

$$h_1 = g_1(p) = \cos(\theta_y)\cos(\theta_z) - \sin(\theta_x)\sin(\theta_y)\sin(\theta_z)$$

$$h_2 = g_2(p) = -\cos(\theta_x)\sin(\theta_z)$$

$$h_3 = g_3(p) = t_x$$

$$h_4 = g_4(p) = \cos(\theta_y)\sin(\theta_z) + \sin(\theta_x)\sin(\theta_y)\cos(\theta_z)$$

$$h_5 = g_5(p) = \cos(\theta_x)\cos(\theta_z)$$

$$h_6 = g_6(p) = t_y$$

$$h_7 = g_7(p) = \cos(\theta_x)\sin(\theta_y)$$

$$h_8 = g_8(p) = -\sin(\theta_x)$$

$$h_9 = g_9(p) = -t_z$$

Jacobian Matrix of $g(p)$

$$p = (p_1, p_2, p_3, p_4, p_5, p_6) = (\theta_x, \theta_y, \theta_z, t_x, t_y, t_z)$$

$$J_g = \begin{pmatrix} \frac{\partial g_1}{\partial p_1} & \dots & \frac{\partial g_1}{\partial p_6} \\ \vdots & \ddots & \vdots \\ \frac{\partial g_9}{\partial p_1} & \dots & \frac{\partial g_9}{\partial p_6} \end{pmatrix}$$

$$h_1 = g_1(p) = \cos(\theta_y)\cos(\theta_z) - \sin(\theta_x)\sin(\theta_y)\sin(\theta_z)$$

$$h_2 = g_2(p) = -\cos(\theta_x)\sin(\theta_z)$$

$$h_3 = g_3(p) = t_x$$

$$h_4 = g_4(p) = \cos(\theta_y)\sin(\theta_z) + \sin(\theta_x)\sin(\theta_y)\cos(\theta_z)$$

$$h_5 = g_5(p) = \cos(\theta_x)\cos(\theta_z)$$

$$h_6 = g_6(p) = t_y$$

$$h_7 = g_7(p) = \cos(\theta_x)\sin(\theta_y)$$

$$h_8 = g_8(p) = -\sin(\theta_x)$$

$$h_9 = g_9(p) = -t_z$$

Jacobian Matrix of $g(p)$

$$p = (p_1, p_2, p_3, p_4, p_5, p_6) = (\theta_x, \theta_y, \theta_z, t_x, t_y, t_z)$$

$$J_g = \begin{pmatrix} \frac{\partial g_1}{\partial p_1} & \dots & \frac{\partial g_1}{\partial p_6} \\ \vdots & \ddots & \vdots \\ \frac{\partial g_9}{\partial p_1} & \dots & \frac{\partial g_9}{\partial p_6} \end{pmatrix}$$

$$h_1 = g_1(p) = \cos(\theta_y)\cos(\theta_z) - \sin(\theta_x)\sin(\theta_y)\sin(\theta_z)$$

- first row of Jacobian matrix



$$\frac{\partial g_1}{\partial p_1} = -\cos(\theta_x)\sin(\theta_y)\sin(\theta_z)$$

$$\frac{\partial g_1}{\partial p_2} = -\sin(\theta_y)\cos(\theta_z) - \sin(\theta_x)\cos(\theta_y)\sin(\theta_z)$$

$$\frac{\partial g_1}{\partial p_3} = -\cos(\theta_y)\sin(\theta_z) - \sin(\theta_x)\sin(\theta_y)\cos(\theta_z)$$

$$\frac{\partial g_1}{\partial p_4} = 0, \quad \frac{\partial g_1}{\partial p_5} = 0, \quad \frac{\partial g_1}{\partial p_6} = 0$$

Jacobian Matrix of $g(p)$

$$J_g = \begin{pmatrix} \frac{\partial g_1}{\partial p_1} & \dots & \frac{\partial g_1}{\partial p_6} \\ \vdots & \ddots & \vdots \\ \frac{\partial g_9}{\partial p_1} & \dots & \frac{\partial g_9}{\partial p_6} \end{pmatrix}$$

- the remaining rows of the Jacobian can be derived with a similar pattern
- see ***course notes*** for a detailed derivation of the elements of this Jacobian matrix

Jacobian Matrices of f and g

- to get the Jacobian of $f(g(p))$, compute the two Jacobian matrices and multiply them

$$J = J_f \cdot J_g = \begin{pmatrix} \frac{\partial f_1}{\partial h_1} & \dots & \frac{\partial f_1}{\partial h_9} \\ \vdots & \ddots & \vdots \\ \frac{\partial f_8}{\partial h_1} & \dots & \frac{\partial f_8}{\partial h_9} \end{pmatrix} \cdot \begin{pmatrix} \frac{\partial g_1}{\partial p_1} & \dots & \frac{\partial g_1}{\partial p_6} \\ \vdots & \ddots & \vdots \\ \frac{\partial g_9}{\partial p_1} & \dots & \frac{\partial g_9}{\partial p_6} \end{pmatrix}$$

Pose Tracking with LM

- LM then iteratively updates pose as


$$p^{(k+1)} = p^{(k)} + \left(J^T J + \lambda \operatorname{diag}(J^T J) \right)^{-1} J^T \left(b - f(g(p^{(k)})) \right)$$

- pseudo-code
 - 1. `p = ... // initialize p0`
 - 2. `for k=1 to max_iter`
 - 3. `f = eval_objective(p)`
 - 4. `J = get_jacobian(p)`
 - 5. `p = p + inv(J'*J+lambda*diag(J'*J))*J'*(b-f)`


Pose Tracking with LM

1. `value = function eval_objective(p)`

2. `for i=1:4`

3. `value(2*(i-1)) = ...` 

$$\frac{h_1 x_i + h_2 y_i + h_3}{h_7 x_i + h_8 y_i + h_9}$$

4. `value(2*(i-1)+1) = ...` 

$$\frac{h_4 x_i + h_5 y_i + h_6}{h_7 x_i + h_8 y_i + h_9}$$

$$\frac{h_4 x_i + h_5 y_i + h_6}{h_7 x_i + h_8 y_i + h_9}$$


Pose Tracking with LM


1. `J = function get_jacobian(p)`

2. `Jf = get_jacobian_f(g(p))`

3. `Jg = get_jacobian_g(p)`

4. `J = Jf*Jg`


$$J_f = \begin{pmatrix} \frac{\partial f_1}{\partial h_1} & \dots & \frac{\partial f_1}{\partial h_9} \\ \vdots & \ddots & \vdots \\ \frac{\partial f_8}{\partial h_1} & \dots & \frac{\partial f_8}{\partial h_9} \end{pmatrix}$$

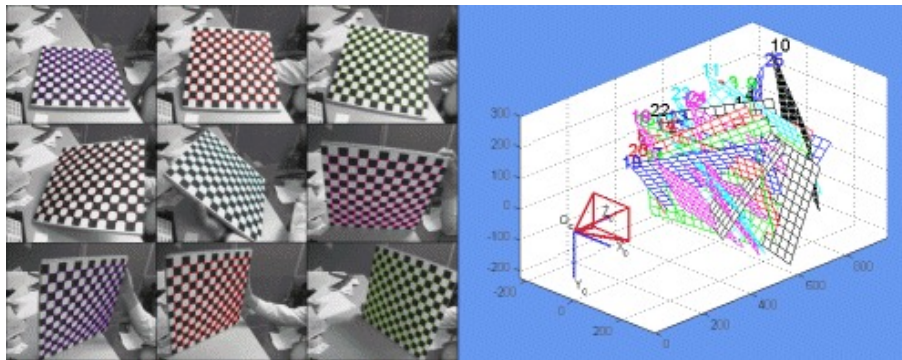

$$J_g = \begin{pmatrix} \frac{\partial g_1}{\partial p_1} & \dots & \frac{\partial g_1}{\partial p_6} \\ \vdots & \ddots & \vdots \\ \frac{\partial g_9}{\partial p_1} & \dots & \frac{\partial g_9}{\partial p_6} \end{pmatrix}$$

Pose Tracking with LM on VRduino

- some more hints for implementation:
 - let Arduino Matrix library compute matrix-matrix multiplications and also matrix inverses for you!
 - run homography method and use that to initialize p for LM
 - use something like 5-25 iterations of LM per frame for real-time performance
 - user-defined parameter λ
 - good luck!

Outlook: Camera Calibration

- camera calibration is one of the most fundamental problems in computer vision and imaging
- task: estimate intrinsic (lens distortion, focal length, principle point) & extrinsic (translation, rotation) camera parameters given images of planar checkerboards
- uses similar procedure as discussed today



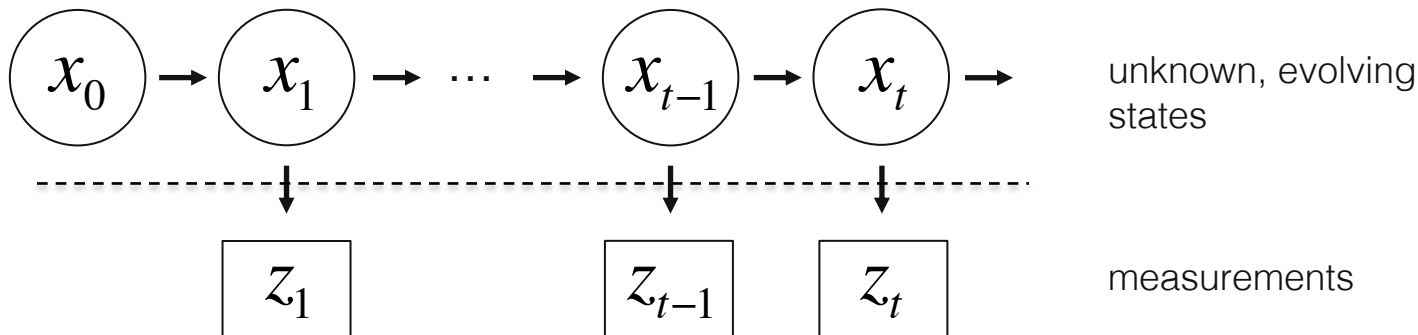
Outlook: Sensor Fusion with Extended Kalman Filter

- also desirable: estimate bias of each of all IMU sensors
- also desirable: joint pose estimation from all IMU + photodiode measurements
- can do all of that with an Extended Kalman Filter - slightly too advanced for this class, but you can find a lot of literature in the robotic vision community

Outlook: Sensor Fusion with Extended Kalman Filter

- Extended Kalman filter: can be interpreted as a Bayesian framework for sensor fusion
- Hidden Markov Model (HMM)

known initial
state



Must read: course notes on tracking!