Due date: 2025/10/9

Physical Constants: $g = 9.80 \text{ m/s}^2$ (gravitational acceleration)

Kinematics

1. The vector position of a particle varies in time according to the expression $\vec{r} = 3.00t\hat{i} - 6.00t^3\hat{j}$, where \vec{r} is in meters and t is in seconds. (a) Find an expression for the velocity of the particle as a function of time. (b) Determine the acceleration of the particle as a function of time. (c) Calculate the particle's position and velocity at t = 1.00 s.

$$α;$$
 $(t) = 3.00t ξ - 6.00t ∫$
 $γ(t) = V(t)$
 $V(t) = 3.00 ξ - 18.00t ∫$
 m/s
 $h. V(t) = α(t) = 0 ξ + (-3b.00t ∫)$
 $m/s2$
 $π(1) = 3.00 ξ - 6.00 ∫$
 $m/s2$
 $V(1) = 3.00 ξ - 18.00 ∫$
 $m/s2$

2. A test rocket starting from rest at point A is launched by accelerating it along a 200.0 m incline at 1.90 m/s² (Fig. 2.1). The incline rises at 35.0° above the horizontal, and at the instant the leaves it, the engines turn off and the rocket is subject to gravity only (ignore air resistance). Find (a) the maximum height above the ground that the rocket reaches, and (b) the rocket's greatest horizontal range beyond point A.

$$V = 2 \times 1.9 \times 200 = 760$$

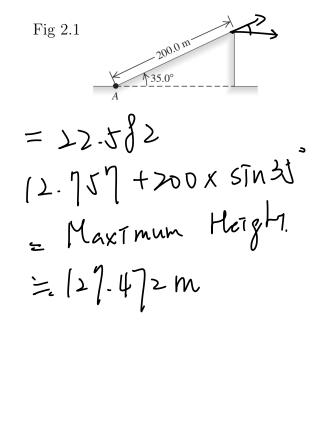
$$V = 760 = 5790$$

$$V = 100535° = 5790 \times 0.819$$

$$V = 100535° = 15.812$$

$$0 = (5.812)^{2} - 19 \times h$$

$$9.8 \times 2h = 150.03 = 12.757$$



b. 200 cos(32°) = 163.830 I. 算Vy從15.82つの新時間も D = Vy + (-9)t, $t_1 = \frac{13.812}{9.8} = 1.613$ Assume Vy 為落地 正算以從可認地的時間也 将的能直 Vy = 48.985 $V_{y}^{T} = 0 + \lambda x 9 \cdot \beta x H$ 47.985=0+9.812 Vy=19.6 x 127.472 141.603+ 163.830 t= 5-100 = >15 433 $t_1 + t_2 = b \cdot 13$ Vx =. 22.582 Vxt=/51.603

Dynamics

3. A constant force $F_1 = 72.0$ N is applied to a 6.00-kg block, which contacts a 12.0-kg block. They accelerate together on a horizontal frictionless surface. (a) How large is their common acceleration? (b) What is the magnitude of the force on the 6.0-kg block due to the contact with the 12.0-kg block? (c) What is the magnitude of the net force on the 6.0-kg block?

4. A small car with mass 0.800 kg travels at constant speed on the inside of a track that is a vertical circle with radius 5.00 m (Fig. 4.1). If the normal force exerted by the track on the car when it is at the top of the track (point B) is 6.00 N, what is the normal force on the car when it is at the bottom of the track (point A)?

$$N_{B}+m_{S} = \frac{mv^{2}}{R}$$

$$N_{A}-m_{S} = \frac{mv^{2}}{R}$$

$$N_{A}-m_{S} = \frac{mv^{2}}{R}$$

$$= 6+15\cdot68$$

$$N_{A}=N_{B}+m_{S}$$

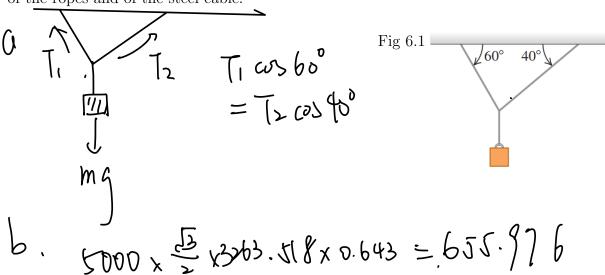
$$= 81\cdot68$$

5. A 2.2-kg fish is being pulled out of the water, in such a way that the tension in the fishing line is 3.0 times its weight. Draw the forces acting on the fish (free body diagram) and find the acceleration of the fish (magnitude and direction).

Tension (32)
$$\Sigma F = m \tilde{\alpha}$$

 $\Delta V = 19.6$
Weight

6. Two ropes are connected to a steel cable that supports a hanging weight (Fig. 6.1). (a) Draw a free-body diagram showing all of the forces acting at the knot that connects the two ropes to the steel cable. Based on your diagram, which of the two ropes will have the greater tension? (b) If the maximum tension either rope can sustain without breaking is 5000 N, determine the maximum value of the hanging weight that these ropes can safely support. Ignore the weight of the ropes and of the steel cable.



7. Block B, with mass 5.00 kg, rests on block A, with mass 8.00 kg, which in turn is on a horizontal tabletop (Fig. 7.1). There is no friction between block A and the tabletop, but the coefficient of static friction between blocks A and B is 0.750. A light string attached to block A passes over a frictionless, massless pulley, and block C is suspended from the other end of the string. What is the largest mass that block C can have so that blocks A and B still slide

The system is released from rest?

$$\int S Mox = MN = 0.75 \times Mb \times 9$$

$$= \frac{3}{4} \times 5 \times 9 \cdot 1 = 36.75$$

$$= (MA+Mb) \Omega$$

$$ME \Omega = MSNG (Fig. 7.1$$

$$MC = -7.35$$

$$MC = -7.3$$

8. (*) An object of mass m is dropped from rest in air. The drag force acting on it is proportional to the square of its speed, $f_d = cv^2$ where c is the a positive drag coefficient. (a) Write down the equation of motion for the object. (b) Derive the expression of the terminal velocity v_t . (c) Solve for the velocity v(t) as a function of time. (d) If the object is a human body of 60.0 kg and c = 0.430. Determine how long it takes for the object to reach 90% of its terminal velocity. (Hint: use hyperbolic function $tanh x = \frac{e^x - e^{-x}}{e^x + e^{-x}} = \frac{e^{2x} - 1}{e^{2x} + 1}$)

a.
$$\overline{z} = m \frac{dv}{dt} = m \frac{dv}{dt} = m \frac{dv}{dt} - Cv^{2}$$

b. $Vt = \sqrt{mg}$

C. $T - \frac{2}{3}$
 $Vt^{2} = \frac{mg}{dt} = m \frac{dv}{dt} - Cv^{2}$
 $Vt^{2} = \frac{mg}{dt} = \frac{ve^{2}}{m} - \frac{g}{vt^{2}}$
 $Vt^{2} = \frac{mg}{dt} - Cv^{2}$
 $Vt^{2} = \frac{mg}{dt} - Cv^{2}$

9. A 1400-kg car initially has a velocity of 33.3 m/s due south. It brakes to a stop over a 180 m distance. (a) What is the magnitude of the car's acceleration, in m/s^2 ? (b) What average net force magnitude was necessary to stop the car? (c) Assuming the tires do not skid, what coefficient of static friction between tires and pavement is needed?

9.
$$\int_{33.5}^{33.5}$$
 $\int_{33.5}^{33.5}$ $\int_{33.5$

$$\frac{dv}{dt} = \hat{g} - \frac{cv}{m} = g - \frac{gv}{vt} = g(1 - \frac{vt}{vt})$$

$$\frac{dv}{1 - (vt)} = g dt \qquad \int_{0}^{v} \frac{dv}{1 - (vt)} = g \int_{0}^{t} dt = gt$$

$$\int_{0}^{v} \frac{dv}{1 - (vt)} = \frac{g}{vt} \int_{0}^{t} \frac{dv}{1 - (vt)} = \frac{g}{vt} \int_{0}^{t} dv = gt$$

$$\int_{0}^{v} \frac{dv}{1 - (vt)} = \frac{g}{vt} \int_{0}^{t} \frac{dv}{1 - (vt)} dv$$

10. A box of mass M sits on an incline elevated an angle θ above the horizontal. The mass is held in place by a spring (of spring constant k) as shown. Assume that the coefficient of static friction between the box and the incline is μ . (a) Find the maximum amount that the spring can be **stretched** if the mass is to remain stationary on the incline. (b) Find the maximum amount that the spring can be **compressed** if the mass is to remain stationary on the incline.

ABSULE F = - KX 分=伸長重 D. Mg cost=N

Mgsint+F=fs

H Mg cosb= N Mg sin b= kx+ts F=fs-Masing Mg sind= KX+ Mg and M FS=M MgcDD kn=149 (Sinb-cosbu) F=Mg(Mcosb-sinb) X= Mg (SIND-MCODB)

11. A wedge with mass M rests on a frictionless, horizontal tabletop. A block with mass m is placed on the wedge, and a horizontal force \vec{F} is applied to the wedge (Fig. 11.1). (a) What must the magnitude of \vec{F} be if the block is to remain at a constant height above the tabletop? (b) If there is friction between mass M and m (the coefficient of static friction μ), what is the

System condition that the block is to remain at a constant height. I= (M+m)X Fig 11.1 ma sīn D Block: Brune T= ma Coot = mg sinb (block remain M) at a constant hy a=qtanb F= (Mtm)gtanb height) Case]: Present the block moving downward f3+mannab = mg sinb 1's=UN=Mmq cosb+Mmamin sin b

M mg cosb + Umamin STN & + Mamin cosb = mgs in &

Mmanin STn& + Manin cosb= mg sin & - My and (Union (Um STr. 10 + Mcood) = My STrib - May cosb Mnin = STNB - Mcosb

M sTrb+ cosb (ase 1): Present the block mouting upward Manax cosb = masinb - 1s $\int_{S} = manax cosb - masinb$ Js=MN=Mmg cost + MManax str & anaxusb-gsinb=Mgcoso+Manassinb $(1000 - 1510) = Ms \cos 0 + 9 stub$ Array = Leas b + SIND

Max = Coop - using J

12. A small rocket with mass 0.0 kg is moving in free fall toward the earth. Air resistance can be neglected. When the rocket is 80.0 m above the surface of the earth, it is moving downward with a speed of 30.0 m/s. At that instant the rocket engines start to fire and produce a constant upward force F on the rocket. Assume the change in the rocket's mass is negligible. What is the value of F if the rocket's speed becomes zero just as it reaches the surface of the earth, for a soft landing?

$$F \cdot dx_{(2)}(8) = F \times 8 + 1$$

$$= -80$$

$$= -80 \times (18)(0)^{2} - \frac{1}{8}(18)(18)^{2} = -9000 (T)$$

$$= -70 \times 9.8 \times 80 = -18680$$

$$= -900 + (180) = -90f.T (W)$$

13. (*) A spring with a uniform mass density ρ has a spring constant k. When the spring is placed horizontally on a table without being stretched, its length is L. What is its length when it is hung vertically and stretched by the gravitational force? Note that when the spring is hung vertically, its mass density is no longer uniform, because the upper part is stretched more than the lower part.

Work and Energy

14. A soccer ball with mass 0.420 kg is initially moving with speed 2.00 m/s. A soccer player kicks the ball, exerting a constant force of magnitude 40.0 N in the same direction as the ball's motion. Over what distance must the player's foot be in contact with the ball to increase the ball's speed to 6.00 m/s?

$$\begin{array}{l}
\Omega = \frac{40}{0.42} = 95.4 \text{ M/s}^{2} \\
V = V_{0}^{2} + 2aS \\
S = \frac{V_{0}^{2}}{2} = 0.16 \text{ M}
\end{array}$$

15. A force in the +x-direction with magnitude F(x) = 18.0 N - (0.530 N/m) x is applied to a 6.00 kg box that is sitting on the horizontal, frictionless surface of a frozen lake. F(x) is the only horizontal force on the box. If the box is initially at rest at x=0, what is its speed after it has traveled 14.0 m?

it has traveled 14.0 m?

$$W = \int_{0}^{14} \left(18 - 0.55 \right) d\chi$$

$$W = -\frac{0.55}{3} \chi + (8 \chi) 0$$

$$= -\frac{0.55}{3} \chi + (8 \chi) 0$$

$$= -\frac{0.53}{3} \chi + (8 \chi) 0$$

16. It is 5.0km from your home to the physics lab. As part of your physical fitness program, you could run that distance at $\sqrt{0}$ km/h (which uses up energy at the rate of 700 W), or you could walk it leisurely at 3.0 km/h (which uses energy at 290 W). Which choice would burn up more energy, and how much energy (in joules) would it burn? Why does the more intense