

Problem 1

$$CPI = \frac{\sum_{i=1}^n (CPI_i \times I_i)}{I_c}$$

I_c is the instruction count of the program

CPI_i and I_i are the average cycles per instruction and instruction count for the respective type of instruction.

Using the formula, CPI for the program turns out to be **1.55**

$$MIPS = \frac{f}{CPI \times 10^6}$$

Given that $f = 40\text{MHz}$, MIPS is calculated to be **25.806**

Execution time = (Total no. of instruction cycles) / (Cycles executed per second) = **0.0038 sec**

Execution time can also be calculated using the formula **$T = I_c \times CPI \times t$**

Problem 2:

Machine A

$$CPI = \left(\frac{8}{18}\right) \times 1 + \left(\frac{4}{18}\right) \times 3 + \left(\frac{2}{18}\right) \times 4 + \left(\frac{4}{18}\right) \times 3 = 2.22$$

$$MIPS = \frac{f}{CPI \times 10^6} = \frac{200 \times 10^6}{2.22 \times 10^6} = 90$$

$$\text{Execution time} = \frac{(18 \times 10^6) \times 2.22}{200 \times 10^6} = 0.2 \text{ secs}$$

Machine B

$$CPI = \left(\frac{10}{24}\right) \times 1 + \left(\frac{8}{24}\right) \times 2 + \left(\frac{2}{24}\right) \times 4 + \left(\frac{4}{24}\right) \times 3 = 1.92$$

$$MIPS = \frac{f}{CPI \times 10^6} = \frac{200 \times 10^6}{1.92 \times 10^6} = 104$$

$$\text{Execution time} = \frac{(24 \times 10^6) \times 1.92}{200 \times 10^6} = 0.23 \text{ secs}$$

(b) Although machine B has higher MIPS than machine A, it requires a longer CPU time to execute the same set of benchmark programs. This is partially due to the fact that the machine B has more number of instructions for the same (benchmark) program.

Problem 3

$$\text{Average CPI} = (1 \times 0.6) + (2 \times 0.18) + (4 \times 0.12) + (8 \times 0.1) = \mathbf{2.24}$$

$$\text{MIPS} = (400 \times 10^6) / (2.24 \times 10^6) = \mathbf{178}$$

Problem 4

$$\text{Speedup} = \frac{1}{(1-f) + \frac{f}{N}}$$

Note that f is not the processor speed here. It is the fraction of instructions that can be processed parallelly.

Total single core processor cycles required = 5280000

Total single core processor cycles required after including coordination and synchronization instructions = 5755000

$$f = 5755000 / 5280000 = 0.9175$$

Theoretical speedup is calculated to be **5.07**