

EE1101 Signals and Systems – Tutorial 9

April 16, 2018

- Find the Laplace transforms and the associated ROC for the following signals

- $e^{-2t} \cos(3t)u(t)$
- $f(t) = \sin(t)$, $0 \leq t \leq 1$ and $f(t) = 0$, elsewhere
- $(e^{-4t} + e^{-5t} \sin t)u(t)$
- $e^{-2t}u(t-1)$
- $e^{-2(t-1)}u(t-1)$
- $e^{2t}u(-t) + e^{3t}u(-t)$
- $te^{-2|t|}$

- Find the inverse Laplace transform of

- $\frac{1}{s(s+1)}$, $\text{Re}\{s\} > 0$
- $\frac{1}{s(s+1)}$, $\text{Re}\{s\} < -1$
- $\frac{1}{s(s+1)}$, $-1 < \text{Re}\{s\} < 0$
- $\frac{s+1}{(s+1)^2 + 9}$, $\text{Re}\{s\} < -1$
- $\frac{s+1}{s^2 + 5s + 6}$, $-3 < \text{Re}\{s\} < -2$

- Use the properties of Laplace transform and find the inverse Laplace transform of

- $e^{-s} \frac{10s^2}{(s+1)(s+3)}$, $\text{Re}\{s\} > -1$
- $\frac{d}{ds} \left(e^{-2s} \frac{1}{(s+2)^2} \right)$, $\text{Re}\{s\} > -2$

- The Laplace transform of a function $e(t)$ is $E(s) = \frac{s+1}{(s+1)^2 + 4}$, $\text{Re}\{s\} > -1$. Without explicitly finding $e(t)$, evaluate

- $\int_{-\infty}^{\infty} e(t)dt$
- $\int_{-\infty}^{\infty} te(t)dt$

- For each of the four signals $x(t)$ given below: (1) Find the Laplace transform $X(s)$ and its ROC, (2) determine if $\{s|s = j\omega, \omega \in R\} \subset \text{ROC}$ and calculate the inverse Fourier transform if possible.

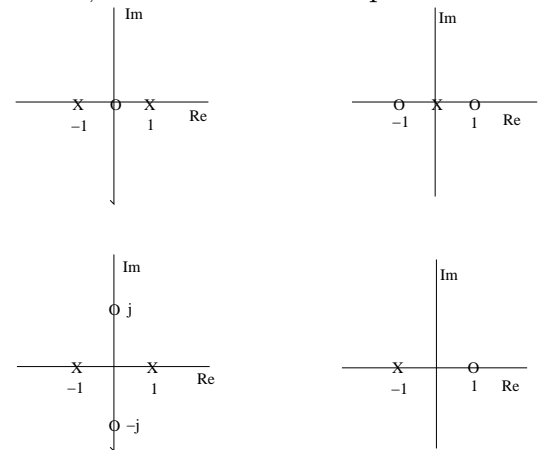
- $x(t) = u(t-2)$
- $x(t) = u(t) - u(t-3)$
- $x(t) = e^{3t}u(t)$
- $x(t) = te^{-t}u(t)$
- $x(t) = \sin t \cdot u(t)$

- Consider a signal $y(t)$ which is related to two signals $x_1(t)$ and $x_2(t)$ by

$$y(t) = x_1(t-2) * x_2(-t+3)$$

where $x_1(t) = e^{-2t}u(t)$ and $x_2(t) = e^{-3t}u(t)$. Use the properties of Laplace transform to determine the Laplace transform of $y(t)$

- Show that if $x(t)$ is an even function of time, then $X(s) = X(-s)$.
 - Determine which, if any, of the pole-zero plots in the following figure could correspond to an even function of time. For those that could, indicate the required ROC.



- Let $x(t)$ be a sampled signal specified as

$$x(t) = \sum_{n=0}^{\infty} e^{-nT} \delta(t - nT)$$

where $T > 0$

- Determine $X(s)$ and the ROC
- Sketch the pole zero plot for $X(s)$