## EE2001-Tutorial 2

## Date: 30th January 2018

## **Gate-Level Minimization and Some Combinational Logic**

- 1) Simplify the following Boolean functions, using Karnaugh maps:
- (a)  $F(x, y, z) = \Sigma(2, 3, 6, 7)$
- (b)  $F(A, B, C, D) = \Sigma(4, 6, 7, 15)$
- (c)  $F(A, B, C, D) = \Sigma(3, 7, 11, 13, 14, 15)$
- (d)  $F(w, x, y, z) = \Sigma(2, 3, 12, 13, 14, 15)$
- (e)  $F(w, x, y, z) = \Sigma(11, 12, 13, 14, 15)$
- (f)  $F(w, x, y, z) = \Sigma(8, 10, 12, 13, 14)$
- 2) Simplify the following Boolean expressions, using four variable K-maps:
- (a) w'z + xz + x'y + wx'z
- (b) AD' + B'C'D + BCD' + BC'D
- (c) AB'C + B'C'D' + BCD + ACD' + A'B'C + A'BC'D
- (d) wxy + xz + wx'z + w'x
- 3) Find the minterms of the following Boolean expressions:
- (a) xy + yz + xy'z
- (b) C'D + ABC' + ABD' + A'B'D
- (c) wyz + w'x' + wxz'
- (d) A'B + A'CD + B'CD + BC'D'
- 4) Find all the prime implicants for the following Boolean functions, and determine which are essential:
- (a)  $F(w, x, y, z) = \Sigma (0, 2, 4, 5, 6, 7, 8, 10, 13, 15)$
- (b)  $F(A, B, C, D) = \Sigma (0, 2, 3, 5, 7, 8, 10, 11, 14, 15)$
- (c)  $F(A, B, C, D) = \Sigma (2, 3, 4, 5, 6, 7, 9, 11, 12, 13)$
- (d)  $F(w, x, y, z) = \Sigma (1, 3, 6, 7, 8, 9, 12, 13, 14, 15)$
- (e)  $F(A, B, C, D) = \Sigma (0, 1, 2, 5, 7, 8, 9, 10, 13, 15)$
- (f)  $F(w, x, y, z) = \Sigma (0, 1, 2, 5, 7, 8, 10, 15)$
- 5) (i) Convert the following Boolean function from a sum-of-products form to a simplified product-of-sums form.

$$F(w, x, y, z) = \Sigma (0, 1, 2, 5, 8, 10, 13)$$

- (ii) Simplify the following expressions to (1) sum-of-products and (2) products-of-sums:
- (a) x'z' + y'z' + yz' + xy
- (b) ACD' + C'D + AB' + ABCD
- (c) (A + B + D')(A' + B' + C')(A' + B' + C)(B' + C + D')
- (d) BCD' + ABC' + ACD

- 6) Simplify the following Boolean function F, together with the don't-care conditions d, and then express the simplified function in sum-of-products form:
- (a)  $F(x, y, z) = \Sigma (0, 1, 4, 5, 6), d(x, y, z) = \Sigma (2, 3, 7)$
- (b)  $F(A,B,C,D) = \Sigma$  (0, 6, 8, 13, 14),  $d(A,B,C,D) = \Sigma$  (2,4,10)
- (c)  $F(A,B,C,D) = \Sigma$  (5, 6, 7, 12, 14, 15),  $d(A,B,C,D) = \Sigma$  (3, 9,11)
- (d)  $F(A,B,C,D) = \Sigma$  (4, 12, 7, 2, 10),  $d(A,B,C,D) = \Sigma$  (0, 6, 8)
- 7) (i) With the use of maps, find the simplest sum-of-products form of the function F = fg, where f = abc' + c'd + a'cd' + b'cd' and g = (a + b + c' + d')(b' + c' + d)(a' + c + d')
- (ii) Implement  $F(A, B, C, D) = \Sigma (0, 4, 8, 9, 10, 11, 12, 14)$  using the two-level forms of logic
- (a) NAND-AND, (b) AND-NOR, (c) OR-NAND and (d) NOR-OR
- 8(i) Design a combinational circuit with three inputs and one output.
- (a) The output is 1 when the binary value of the inputs is less than 3. The output is 0 otherwise.
- (b) The output is 1 when the binary value of the inputs is an even number.
- (ii) A majority circuit is a combinational circuit whose output is equal to 1 if the input variables have more 1's than 0's. The output is 0 otherwise. Design a 3-input majority circuit by finding the circuit's truth table, Boolean equation, and a logic diagram.
- 9(i) Design a combinational circuit that converts a four-bit Gray code to a bit four binary number. Implement the circuit with exclusive-OR gates.
- (ii) Design a four-bit combinational circuit 2's complementer. (The output generates the 2's complement of the input binary number.) Show that the circuit can be constructed with exclusive-OR gates. Can you predict what the output functions are for a five-bit 2's complementer?
- 10) (i) Design a half-subtractor circuit with inputs x and y and outputs  $D_{iff}$  and  $B_{out}$ . The circuit subtracts the bits x y and places the difference in  $D_{iff}$  and the borrow in  $B_{out}$ .
- (ii) Design a full-subtractor circuit with three inputs x, y,  $B_{in}$  and two outputs  $D_{iff}$  and  $B_{out}$ . The circuit subtracts  $x-y-B_{in}$ , where  $B_{in}$  is the input borrow,  $B_{out}$  is the output borrow, and  $D_{iff}$  is the difference.