

**DEPARTMENT OF PHYSICS  
INDIAN INSTITUTE OF TECHNOLOGY, MADRAS**

**PH1020 Physics II**

Problem Sheet 10

To be discussed on: (25.4.2018)

---

1. Calculate the total energy density of radiation in a blackbody at the following temperatures: (a) 300 K and (b) 2000 K. For each temperature calculate the wavelength at which the energy density is maximum.
2. Consider a particle bound in the region  $x > 0$ . If its wavefunction in one dimension is given by  $\Psi = e^{-x}(1 - e^{-x})$ , then what is the probability to find the particle to the right of  $x = a$  and the expectation value  $\langle x \rangle$ ?
3. A particle, moving in one dimension, has a ground state wavefunction (not normalized and do not normalize) given by  $\Psi_0(x) = e^{-\frac{\alpha^4 x^4}{4}}$  (where  $\alpha$  is a real constant) belonging to the energy eigenvalue  $E_0 = \frac{\hbar^2 \alpha^2}{m}$ . Determine the potential in which the particle moves.
4. Consider a particle of mass  $m$ , in one dimension, confined between to infinitely hard walls at  $x = -a$  and  $x = a$ . If the wavefunction of the particle is given by

$$\psi(x) = \frac{1}{\sqrt{2}} \cos\left(\frac{3\pi x}{2a}\right) + \frac{1}{\sqrt{2}} \sin\left(\frac{\pi x}{a}\right)$$

then, what is the probability to find the particle to the right of  $x=0$  and the expectation value of the energy of the particle?