## DEPARTMENT OF PHYSICS INDIAN INSTITUTE OF TECHNOLOGY, MADRAS

## PH1020 Physics II

## Tutorial 1 (22.1.2018)

- 1. Consider an infinite uniformly-charged plate occuping the xoy plane, carrying a surface charge density  $\sigma$ , with a circular hole of radius a centered at the origin. Find the force on a charge Q lying on the z-axis. If the charge is negative, (i.e., Q < 0), discuss the force on it when released at a distance x close to the origin (i.e., z << a).
- 2. Determine the electric field at the center of a sphere of radius R that carries a charge on its surface with charge density  $\sigma = \vec{k} \cdot \vec{r}$ , where  $\vec{k}$  is a constant vector.
- 3. A fixed charge +q at a point O is surrounded by a continuous distribution of charge whose density ρ(< 0) is a function only of the distance r from O. The total negative charge exceeds q in magnitude. A point charge +q', with a mass m, is free to move on a line passing through O. (a) Obtain the condition for +q' to be in equilibrium at a distance r<sub>0</sub> from O. (b) If q' is released at a point very close to r<sub>0</sub>, find the force acting on it.
- 4. Evaluate the electrostatic energy W of a charge distribution in the form of a uniform charge density within a sphere of radius a and total charge Q. Express the answer in terms of  $\epsilon_0$ , a, and Q.
- 5. Verify if  $\vec{E} = \frac{a}{\rho^2} [\hat{e}_{\rho}(1 + \cos \phi) + \hat{e}_{\phi} \sin \phi]$  can be a electric field and if so find the volume charge density that creates it. Note:  $(\rho, \phi, z)$  represent the cylindrical polar co-ordinates.
- 6. A hemisphere of radius R has a uniformly distributed surface charge with total charge Q. Find the potential at any position along the z axis due to the entire hemisphere of surface charge?