EE2025 (July-Nov 2019) - Tutorial 1 : Transmission Lines

July 2019

Note : All transmission lines can be assumed to be lossless, unless mentioned otherwise.

1. Sinusoidally varying voltage and current can be in general represented as $Ve^{j\omega t}$ and $Ie^{(j\omega t+\phi)}$, where V and I are the phasors representing the voltage and current respectively. Find an expression for the average power (over a cycle) in terms of these phasors.

2. The length of a microstrip trace line connecting two components on a chip is 50 cm. A sinusoidal signal of frequency 1 GHz is supplied to the trace at one end. Assuming the velocity of propagation of the signal is 2×10^8 m/sec and there are no reflections,
   (a) Calculate the time taken by the signal to reach the other end of the trace.
   (b) What is the phase difference between the signal at the two ends of the trace ?

3. Using the concepts of electrostatics, find the capacitance per unit length, C of
   (a) parallel wire line, with each wire of radius a and separated by a distance $2d$, where $a << 2d$.
   (b) coaxial cable of inner radius a and outer radius b.

4. You are required to buy a cable from an electronics shop to connect your dish antenna to your set top box and your set top box to your TV.
   (a) Write the name of the cable you would buy.
   (b) Upto what length do you think you can use this cable, in the lumped circuit model and why ?

5. A transmission line with characteristic impedance Z_0 = 50 - j5 Ω and propagation constant γ = 0.2 + j2.5 /m is connected to a load impedance of 100 + j50 Ω. Find
   (a) Reflection coefficient of the line at the load end.
   (b) Reflection coefficient of the line $5m$ from the load.

6. A 300 Ω transmission line is connected to a circuit with an input impedance of 75+j35 Ω. Show that the impedance along the line will lie between Z_0/ρ and $Z_0\rho$, where ρ is the VSWR. Find
   (a) ρ
   (b) Maximum impedance seen on the line
   (c) Minimum impedance seen on the line

7. An RG-59U coaxial cable has a loss of 10 dB per 100 ft of length. A 10 V - 3 A signal is generated using a function generator and connected to one end of the 50 ft long cable. On the other side, the cable is impedance matched to a set top box unit. Find the power delivered to the load.

8. According to the maximum power transfer theorem, maximum time averaged power is transferred from a source with internal impedance Z_g to a load, Z_L when $Z_g = Z_L^*$. A 50 MHz generator with an internal impedance (Z_g) of 50 Ω is connected to an impedance 50−j25 Ω. How would you ensure maximum power transfer in this case using a transmission line of characteristic impedance 100 Ω, and what should be the minimum length of the transmission line element ?

9. On a 50 Ω BNC cable line, the reflection co-efficient is measured at the load end to be $0.7\angle 30°$. If the propagation constant of the line is $20\angle 89°\ /m$, find the impedance seen on the transmission line at a distance of 4 m from the load. (Note : BNC is a very popular type of coaxial cable used for frequencies even up to 4 GHz)

10. Calculate the average power dissipated by each resistor in the circuit shown in Fig. 1.

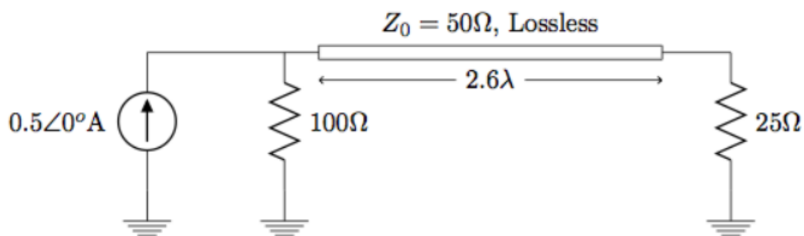

Figure 1: Problem 9

11. Given the system in (Fig. 2) is operating with $\lambda = 100cm$ and $Z_0 = 300\Omega$. If $d_1 = 10cm$, $d = 25cm$, and the system is matched to 300 Ω, find Z_L?

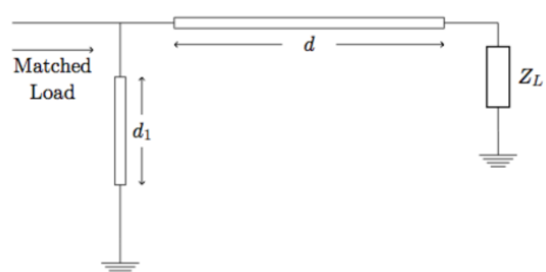

Figure 2:

12. The two-wire lines shown in Fig. 3 are all lossless and have $Z_0 = 200\Omega$. Find the possible values of d and d_1 to provide a matched load if $\lambda = 100cm$. (Note that the un-shaded and shaded conductor are both parts of the same transmission line, for example they can be the inner and outer conductor of a coaxial cable.)

13. Approximate distributed circuit models of (lossless) a lossless transmission operating in high frequency modes is shown in Fig. 4. Note that L has units $H \cdot m$, C has units $F \cdot m$, L_0 has units H/m and C_0 has units F/m. Obtain expressions for the propagation constant β and the characteristic impedance Z_0 of the line for both circuits at frequency ω.

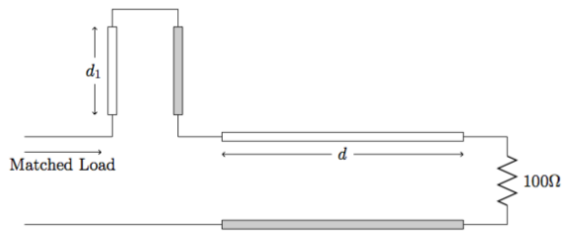

Figure 3:

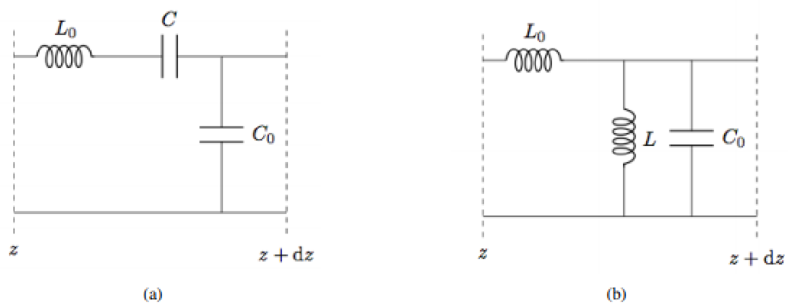

Figure 4:

14. For the transmission line represented in Fig. 5, calculate the potential developed across the 80Ω resistor for (a) $f = 60Hz$, (b) $f = 1MHz$, (c) Repeat part (a) with length $10^7 m$ instead of $80m$.

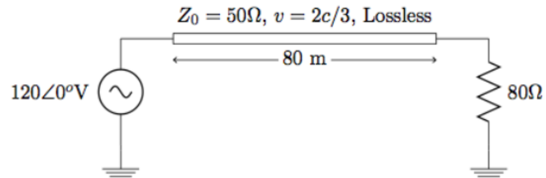

Figure 5: