

Indian Institute of Technology Madras  
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**Tutorial-6**

1. Consider a plane boundary between two media of permeability  $\mu_1$  and  $\mu_2$ , as shown in Figure 1. Find the relation between the angles  $\theta_1$  and  $\theta_2$ . Assume that the media are linear with  $\vec{B}$  and  $\vec{H}$  in the same direction.

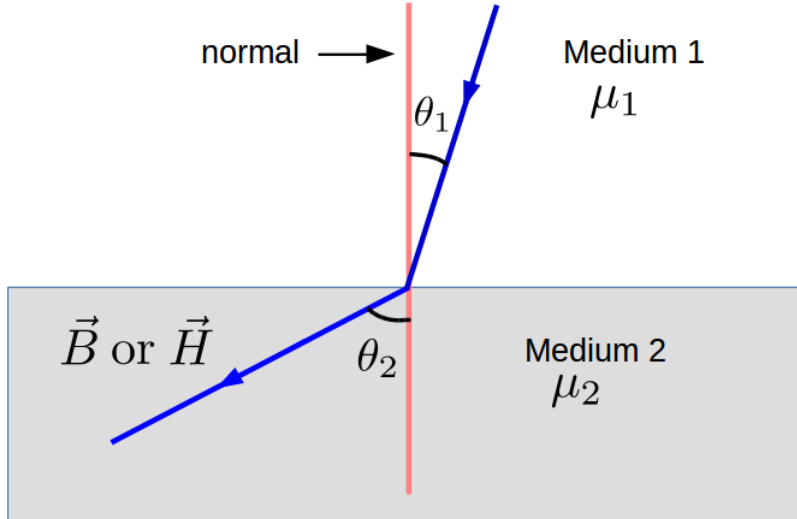


Figure 1

2. A sphere of a linear magnetic material of susceptibility  $\chi_m$  is placed in an otherwise uniform magnetic field  $\vec{B}_0$ . Determine the new field inside the sphere.

3. A long straight wire of radius  $a$  is made of a homogeneous, linear magnetic material with a susceptibility  $\chi_m$ . A uniformly distributed current  $I$  flows down the wire. Determine

- (a) the magnetic field at a distance  $s$  from the axis of the wire and
- (b) the net bound current flowing in the wire.

4. An infinitely long straight wire located along the  $z$ -axis carries a steady current  $I$  in the positive  $z$ -direction. A copper rod is located on the  $y$ -axis, such that its ends are at  $y = a$  and  $y = b$ . The rod moves with a constant velocity  $\vec{v} = v_0 \hat{e}_z$ . Find the emf induced in the rod.

5. A long circular cylinder of radius  $a$  carries

- (a) a uniform magnetisation  $\mathbf{M}$  parallel to its axis. Find the magnetic field due to  $\mathbf{M}$  inside and outside the cylinder.
- (b) a magnetisation  $\mathbf{M} = \frac{M_0 s^2}{a^2} \hat{\phi}$  where  $M_0 > 0$  is a constant,  $s$  is the distance from the axis, and  $\hat{\phi}$  is the usual azimuthal unit vector.

Find  $\mathbf{J}_b, \mathbf{K}_b$  and the magnetic field  $\mathbf{B}$  due to  $\mathbf{M}$  inside and outside the cylinder.