

$$i) \pi^+ + p : |1, +1\rangle | \frac{1}{2}, +\frac{1}{2} \rangle$$

$$\text{so } \frac{1}{2} \leq I_s^{\text{tot}} \leq \frac{3}{2}, \quad I_{ss}^{\text{tot}} = \frac{3}{2}$$

$$\therefore \text{only option for } I_s^{\text{tot}} = \frac{3}{2}$$

$$\therefore \pi^+ + p = | \frac{3}{2}, \frac{3}{2} \rangle$$

$$ii) \pi^+ + n : |1, -1\rangle | \frac{1}{2}, -\frac{1}{2} \rangle$$

$$\text{so } \frac{1}{2} \leq I_s^{\text{tot}} \leq \frac{3}{2}, \quad I_{ss}^{\text{tot}} = -\frac{3}{2}$$

$$\therefore \text{only option for } I_s^{\text{tot}} = \frac{3}{2}$$

$$\therefore \pi^+ + n = | \frac{3}{2}, -\frac{3}{2} \rangle$$

$$iii) \pi^0 + p : |1, 0\rangle | \frac{1}{2}, +\frac{1}{2} \rangle$$

$$\text{so } \frac{1}{2} \leq I_s^{\text{tot}} \leq \frac{3}{2}, \quad I_{ss}^{\text{tot}} = +\frac{1}{2}$$

$$\text{so } I_s^{\text{tot}} \text{ can be } \frac{1}{2} \text{ or } \frac{3}{2}$$

so we need to consult Clebsch-Gordan table or used the expression given

$$\therefore \pi^0 + p = \sqrt{\frac{2}{3}} | \frac{3}{2}, \frac{1}{2} \rangle - \sqrt{\frac{1}{3}} | \frac{1}{2}, \frac{1}{2} \rangle$$

Similarly as (iii) consulting expressions given

$$iv) \pi^- + p : |1, -1\rangle | \frac{1}{2}, \frac{1}{2} \rangle = \sqrt{\frac{1}{3}} | \frac{3}{2}, -\frac{1}{2} \rangle - \sqrt{\frac{2}{3}} | \frac{1}{2}, -\frac{1}{2} \rangle$$

$$v) \pi^+ + n : |1, +1\rangle | \frac{1}{2}, -\frac{1}{2} \rangle = \sqrt{\frac{1}{3}} | \frac{3}{2}, +\frac{1}{2} \rangle + \sqrt{\frac{2}{3}} | \frac{1}{2}, +\frac{1}{2} \rangle$$

$$vi) \pi^0 + n : |1, 0\rangle | \frac{1}{2}, -\frac{1}{2} \rangle = \sqrt{\frac{2}{3}} | \frac{3}{2}, -\frac{1}{2} \rangle + \sqrt{\frac{1}{3}} | \frac{1}{2}, -\frac{1}{2} \rangle$$