Supplement to the paper 'Positive Unlabeled Classification Methods with Logistic Regression Revisited: An Evaluation of Optimization Techniques.'

Kacper Paczutkowski and Konrad Furmańczyk

Institute of Information Technology, Warsaw University of Life Sciences, Warsaw, Poland

1 Supplementary figures and tables

The following metrics of our study are presented: the area under the curve (AUC), precision, recall, precision, and F1 score. These metrics are the averages of the values obtained from the metrics in a subset of tests after 100 repetitions. The average values of all metrics considered are given in Fig.1- Fig.4. The method that obtained the best result for particular values of the parameter c is marked with a specific symbol in the figures. Figure 5 demonstrates the executing time of the considered optimization algorithms.

In Tables 1-12, all our numerical results are given depending on the optimization method used and the label parameter c. In addition, the values of the naive method are provided for comparison. The average values from 100 repetitions and the standard deviation are given in parentheses. The best results for particular values of the parameter c are in bold in the tables.

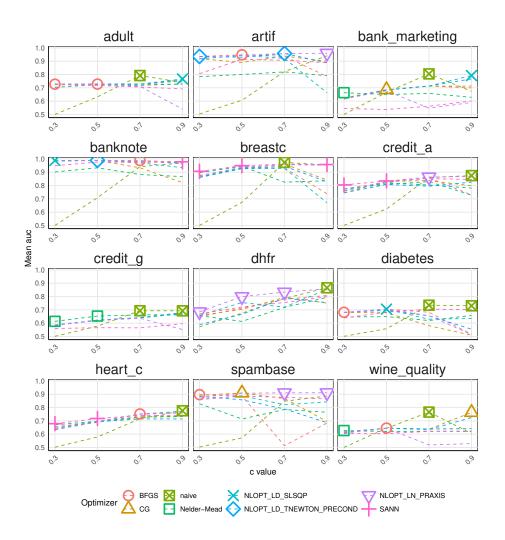


Fig. 1. Mean AUC for each optimizer

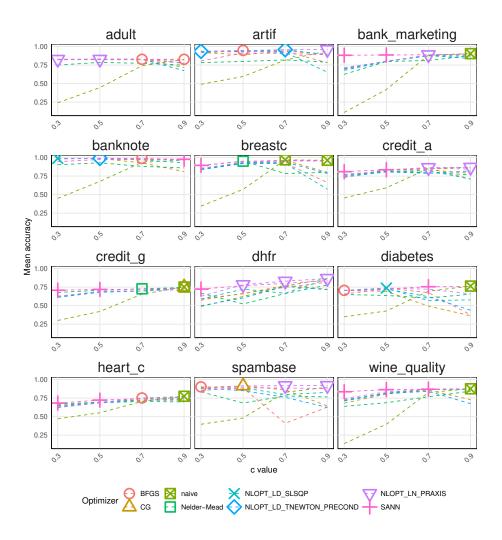


Fig. 2. Mean Accuracy for each optimizer

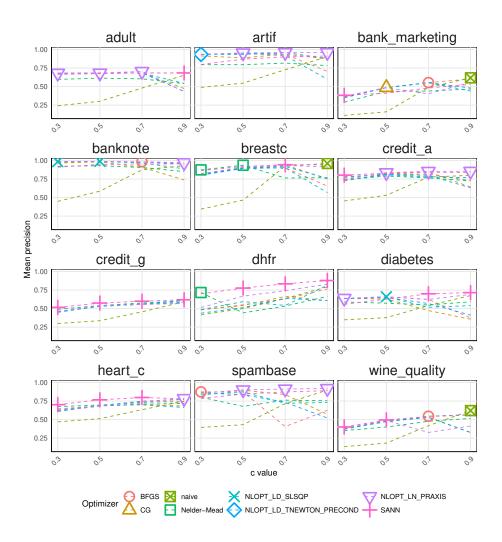


Fig. 3. Mean Precision for each optimizer

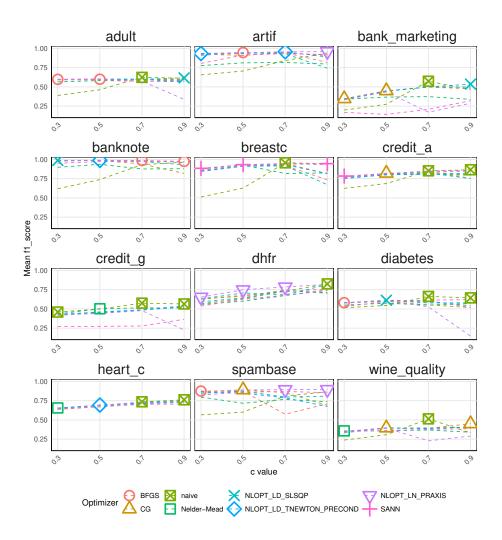
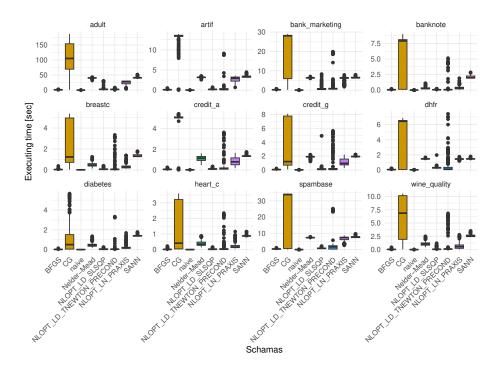


Fig. 4. Mean F1 Score for each optimizer



 ${\bf Fig.\,5.}$ Executing time for each optimizer

Table 1. Summary Statistics for dset = adult

optims	c mean	accuracy	mean pi	recision	mean	recall	mean	f1 score	mean	auc
BFGS BFGS BFGS CG	0.3 0.827 0.5 0.828 0.7 0.828 0.9 0.828 0.3 0.827	(0.004) (0.004) (0.004)	0.682 (0.683 ((0.015) (0.015) (0.013) (0.012)	0.535 0.533 0.532	(0.017) (0.015) (0.013)	0.599 0.599 0.598	(0.014) (0.011) (0.011) (0.010) (0.014)	0.728 0.727 0.727	(0.007) (0.007) (0.006)
CG CG CG NLOPT-LD-SLSQP NLOPT-LD-SLSQP	0.5 0.828 0.7 0.828 0.9 0.717 0.3 0.827 0.5 0.828	(0.004) (0.054) (0.005)	0.683 (0 0.474 (0 0.680 ().013)).084) (0.016)	0.533 0.847 0.535	(0.015) (0.131) (0.024)	0.599 0.592 0.598	(0.011) (0.011) (0.018) (0.014) (0.011)	$\begin{array}{c} 0.727 \\ 0.761 \\ \textbf{0.727} \end{array}$	(0.007) (0.017) (0.010)
NLOPT-LD-SLSQP NLOPT-LD-SLSQP NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND	0.5 0.828	(0.026) (0.044) (0.004)	0.542 (0 0.676 (0 0.682 (0.067) 0.043) (0.015)	0.745 0.539 0.535	(0.102) (0.052) (0.017)	0.617 0.596 0.599	(0.011) (0.016) (0.021) (0.011) (0.011)	0.767 0.726 0.728	(0.021) (0.016) (0.007)
NLOPT-LD-TNEWTON-PRECOND NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS	0.9 0.675 0.3 0.827 0.5 0.828 0.7 0.827 0.9 0.772	(0.005) (0.004) (0.005)		(0.016) (0.015) (0.017)	0.534 0.534 0.487	(0.018) (0.032)	0.598 0.599 0.575	(0.014) (0.011) (0.020)	0.727	(0.009) (0.007) (0.013)
Nelder-Mead Nelder-Mead Nelder-Mead Nelder-Mead SANN	0.3 0.750 0.5 0.786 0.7 0.774 0.9 0.750 0.3 0.823	(0.086) (0.111) (0.066)	0.597 (0 0.614 (0 0.604 (0 0.540 (0 0.666 (0).106)).120)).113)	0.602 0.613 0.689	(0.156) (0.171) (0.212)	0.582 0.576 0.566	(0.058) (0.030) (0.037) (0.022) (0.018)	0.704 0.724 0.719 0.729 0.724	(0.023) (0.035) (0.031)
SANN SANN SANN naive naive	0.5 0.823 0.7 0.821 0.9 0.817 0.3 0.241 0.5 0.445	(0.018) (0.023) (0.004)	0.674 (0 0.685 (0 0.684 (0.241 (0 0.302 (0	0.042) (0.017) 0.004)	0.484 0.449 1.000	(0.137)	0.571 0.588 0.388		0.718 0.706 0.692 0.500 0.632	(0.058) (0.075)
naive naive	$\begin{array}{c} 0.7 \ 0.741 \\ 0.9 \ 0.825 \end{array}$		0.480 (0 0.654 (0			(0.011) (0.013)			0.792 0.740	

Table 2. Summary Statistics for dset = artif

optims	c me	ean accurac	y mean pre	cision mean	recall 1	mean f1 score	mean auc
BFGS BFGS BFGS CG	0.5 0. 5 0.5 0.7 0.9 0.7			93) 0.987	(0.027) ((0.019) ((0.014) (0.936 (0.016) 0.948 (0.013) 0.937 (0.097) 0.785 (0.083) 0.920 (0.087)
CG CG CG NLOPT-LD-SLSQP NLOPT-LD-SLSQP	0.7 0.9 0.9 0.8 0.3 0.9	889 (0.154) 939 (0.085) 896 (0.105) 918 (0.048) 943 (0.046)	0.888 (0.1 0.938 (0.0 0.871 (0.1 0.934 (0.0 0.950 (0.0	092) 0.957 (41) 0.965 (27) 0.896	(0.019) ((0.021) ((0.105) (0.910 (0.099) 0.944 (0.057) 0.908 (0.082) 0.910 (0.063) 0.943 (0.031)	0.890 (0.151) 0.939 (0.086) 0.900 (0.098) 0.917 (0.049) 0.943 (0.047)
NLOPT-LD-SLSQP NLOPT-LD-SLSQP NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND	0.9 0.6 0.3 0. 9 0.5 0.9	929 (0.096)	0.935 (0.0	.10) 0.996 025) 0.934 098) 0.942	(0.011) (0.025) (0.030) (0.934 (0.063)	0.921 (0.113) 0.663 (0.096) 0.936 (0.016) 0.930 (0.089) 0.958 (0.012)
NLOPT-LD-TNEWTON-PRECOND NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS	0.3 0.9 0.5 0.9 0.7 0. 9	920 (0.029) 946 (0.015) 958 (0.011		0.902	(0.050) ((0.031) ((0.018) (0.889 (0.071) 0.916 (0.033) 0.943 (0.016) 0.957 (0.012) 0.959 (0.013)	0.889 (0.074) 0.920 (0.030) 0.945 (0.015) 0.958 (0.011) 0.960 (0.012)
Nelder-Mead Nelder-Mead Nelder-Mead Nelder-Mead SANN	0.5 0.7 0.7 0.8 0.9 0.7	783 (0.074) 799 (0.109) 820 (0.058) 790 (0.085) 807 (0.138)	0.796 (0.0 0.795 (0.1 0.817 (0.0 0.783 (0.0 0.798 (0.1	.18) 0.854 067) 0.825 094) 0.827	(0.084) ((0.077) ((0.068) (0.777 (0.068) 0.813 (0.065) 0.817 (0.051) 0.798 (0.050) 0.805 (0.227)	0.784 (0.069) 0.800 (0.105) 0.820 (0.058) 0.791 (0.081) 0.806 (0.143)
SANN SANN SANN naive naive	0.7 0.9 0.9 0.8 0.3 0.4	913 (0.018) 907 (0.101) 890 (0.125) 490 (0.022) 596 (0.029)	0.870 (0.0 0.901 (0.0 0.912 (0.0 0.488 (0.0 0.547 (0.0	0.909 024) 0.858 022) 1.000	(0.231) ((0.288) ((0.000) (0.915 (0.018) 0.933 (0.014) 0.921 (0.097) 0.656 (0.020) 0.707 (0.022)	0.914 (0.018) 0.907 (0.104) 0.889 (0.131) 0.503 (0.004) 0.607 (0.021)
naive naive		817 (0.022) 940 (0.011)	0.727 (0.0 0.903 (0.0			0.842 (0.020) 0.940 (0.012)	0.822 (0.019) 0.941 (0.011)

Table 3. Summary Statistics for dset = bank-marketing

optims	С 1	mean	accuracy	mean	precision	mean	recall	mean	f1 score	mean	auc
BFGS BFGS BFGS BFGS CG	0.5 (0.7 (0.9 (0.805 0.879 0.904	(0.321) (0.235) (0.114) (0.014) (0.320)	$\begin{array}{c} 0.486 \\ 0.554 \\ 0.602 \end{array}$	(0.152) (0.162) (0.104) (0.075) (0.153)	$\begin{array}{c} 0.529 \\ 0.501 \\ 0.437 \end{array}$	(0.309) (0.230) (0.154) (0.082) (0.294)	0.444 0.500 0.499	(0.110) (0.114) (0.072) (0.050) 6 (0.110)	$\begin{array}{c} 0.684 \\ 0.714 \\ 0.699 \end{array}$	(0.085) (0.081) (0.058) (0.035) (0.086)
CG CG CG NLOPT-LD-SLSQP NLOPT-LD-SLSQP	0.7 (0.9 (0.3 (0.873 0.876 0.702		$\begin{array}{c} 0.550 \\ 0.482 \\ 0.363 \end{array}$	(0.164) (0.112) (0.075) (0.153) (0.162)	$\begin{array}{c} 0.506 \\ 0.503 \\ 0.507 \end{array}$	(0.224) (0.162) (0.144) (0.305) (0.229)	0.497 0.476 0.336	(0.114) (0.076) (0.065) (0.108) (0.115)	$\begin{array}{c} 0.712 \\ 0.713 \\ 0.617 \end{array}$	(0.082) (0.058) (0.055) (0.085) (0.083)
NLOPT-LD-SLSQP NLOPT-LD-SLSQP NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND	0.9 (0.3 (0.5 (0.872 0.679 0.799	(0.243)	$\begin{array}{c} 0.481 \\ 0.348 \\ 0.485 \end{array}$	(0.105) (0.101) (0.156) (0.165) (0.105)	0.689 0.538 0.534	(0.179) (0.307) (0.229)	0.536 0.337 0.445	(0.072) 6 (0.061) (0.113) (0.113) (0.072)	0.792 0.617 0.683	(0.058) (0.069) (0.088) (0.081) (0.058)
NLOPT-LD-TNEWTON-PRECOND NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS	0.3 (0.5 (0.7 (0.716 0.799 0.889	(0.310) (0.244) (0.012)	$\begin{array}{c} 0.370 \\ 0.484 \\ 0.402 \end{array}$	(0.117) (0.157) (0.166) (0.213) (0.170)	$\begin{array}{c} 0.489 \\ 0.522 \\ 0.107 \end{array}$	(0.198) (0.305) (0.243) (0.113) (0.122)	0.333 0.435 0.171	(0.067) (0.109) (0.119) (0.141) (0.145)	$\begin{array}{c} 0.617 \\ 0.678 \\ 0.547 \end{array}$	(0.066) (0.085) (0.085) (0.054) (0.058)
Nelder-Mead Nelder-Mead Nelder-Mead Nelder-Mead SANN	0.5 (0.7 (0.9 (0.798 0.812 0.878	(0.203) (0.181) (0.029)	$\begin{array}{c} 0.435 \\ 0.440 \\ 0.466 \end{array}$	(0.152) (0.154) (0.140) (0.096) (0.122)	$\begin{array}{c} 0.458 \\ 0.461 \\ 0.309 \end{array}$	(0.271) (0.271) (0.266) (0.171) (0.060)	0.367 0.373 0.338	(0.095) (0.095) (0.093) (0.098) (0.076)	$\begin{array}{c} 0.650 \\ 0.658 \\ 0.629 \end{array}$	(0.078) (0.068) (0.075) (0.065) (0.027)
SANN SANN SANN naive naive	0.7 (0.9 (0.3 (0.889 0.894 0.111	(0.011)	$\begin{array}{c} 0.481 \\ 0.531 \\ 0.111 \end{array}$	(0.154) (0.151) (0.134) (0.009) (0.020)	$0.141 \\ 0.225 \\ 1.000$	(0.074) (0.099) (0.115) (0.001) (0.016)	0.209 0.320 0.199		$\begin{array}{c} 0.561 \\ 0.601 \\ 0.500 \end{array}$	(0.033) (0.045) (0.053) (0.001) (0.035)
naive naive					(0.044) (0.069)				(0.037) (0.045)		(0.026) (0.023)

Table 4. Summary Statistics for dset = banknote

optims	c mea	n accuracy	mean precision	mean recall	mean f1 score	mean auc
BFGS BFGS BFGS BFGS	0.5 0.98 0.7 0.9 8		0.977 (0.018) 0.982 (0.014) 0.984 (0.012) 0.965 (0.061)	0.992 (0.010) 0.991 (0.009) 0.988 (0.013) 0.986 (0.019)	0.984 (0.010) 0.986 (0.008) 0.986 (0.007) 0.974 (0.038)	0.986 (0.008) 0.988 (0.006) 0.988 (0.006) 0.976 (0.037)
CG	0.3 0.98	2 (0.009)	0.966 (0.020)	0.996 (0.006)	0.981 (0.010)	0.984 (0.008)
CG CG CG NLOPT-LD-SLSQP NLOPT-LD-SLSQP	0.7 0.92 0.9 0.81 0.3 0.9 8		0.983 (0.013) 0.908 (0.158) 0.738 (0.120) 0.985 (0.017) 0.989 (0.014)			0.988 (0.006) 0.933 (0.126) 0.822 (0.081) 0.988 (0.008) 0.989 (0.007)
NLOPT-LD-SLSQP NLOPT-LD-SLSQP NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND	0.9 0.92 0.3 0.98 0.5 0.9 8	39 (0.00 7)	0.967 (0.105) 0.889 (0.126) 0.983 (0.018) 0.988 (0.014) 0.979 (0.075)	0.985 (0.015) 0.989 (0.012) 0.983 (0.046) 0.988 (0.012) 0.986 (0.013)	0.972 (0.066) 0.931 (0.071) 0.982 (0.028) 0.988 (0.008) 0.981 (0.047)	0.970 (0.076) 0.934 (0.068) 0.985 (0.024) 0.989 (0.007) 0.981 (0.051)
NLOPT-LD-TNEWTON-PRECOND NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS	0.3 0.98 0.5 0.98 0.7 0.97	6 (0.056) 5 (0.015) 8 (0.007) 6 (0.073) 5 (0.044)	0.956 (0.083) 0.984 (0.016) 0.988 (0.014) 0.981 (0.078) 0.971 (0.060)	0.979 (0.029) 0.982 (0.029) 0.986 (0.013) 0.978 (0.039) 0.978 (0.035)	0.966 (0.054) 0.983 (0.018) 0.987 (0.008) 0.977 (0.057) 0.974 (0.045)	0.968 (0.052) 0.984 (0.016) 0.988 (0.007) 0.977 (0.062) 0.976 (0.042)
Nelder-Mead Nelder-Mead Nelder-Mead Nelder-Mead SANN	0.5 0.93 0.7 0.88 0.9 0.86	3 (0.127) 0 (0.134) 1 (0.154) 0 (0.175) 4 (0.086)	0.921 (0.127) 0.930 (0.139) 0.906 (0.154) 0.851 (0.180) 0.910 (0.076)	0.901 (0.135) 0.959 (0.048) 0.887 (0.161) 0.941 (0.066) 0.988 (0.100)	0.898 (0.111) 0.937 (0.095) 0.876 (0.141) 0.879 (0.120) 0.950 (0.051)	0.902 (0.121) 0.933 (0.119) 0.883 (0.142) 0.867 (0.160) 0.949 (0.080)
SANN SANN SANN naive naive	0.7 0.97 0.9 0.97 0.3 0.44	4 (0.010) 2 (0.043) 6 (0.010) 9 (0.029) 9 (0.067)	0.947 (0.021) 0.953 (0.018) 0.954 (0.020) 0.449 (0.029) 0.586 (0.056)	0.998 (0.004) 0.986 (0.100) 0.995 (0.008) 1.000 (0.000) 1.000 (0.000)		0.976 (0.009) 0.973 (0.048) 0.978 (0.009) 0.500 (0.001) 0.708 (0.060)
naive naive		6 (0.016) 7 (0.009)	0.874 (0.032) 0.931 (0.020)	1.000 (0.000) 1.000 (0.000)		0.942 (0.014) 0.970 (0.008)

Table 5. Summary Statistics for dset = breastc

optims	сn	nean	accuracy	mean	precision	mean	recall	mean	f1 score	mean a	uc
BFGS BFGS BFGS CG	$0.5\ 0$ $0.7\ 0$ $0.9\ 0$	0.925 0.924 0.664	(0.227) (0.137) (0.152) (0.312) (0.208)	$\begin{array}{c} 0.898 \\ 0.903 \\ 0.655 \end{array}$	(0.216) (0.137) (0.155) (0.307) (0.201)	$\begin{array}{c} 0.950 \\ 0.957 \\ 0.973 \end{array}$	(0.048) (0.038) (0.035) (0.036) (0.047)	$0.915 \\ 0.919 \\ 0.735$	(0.154) (0.098) (0.113) (0.222) (0.142)	0.862 (0.931 (0.932 (0.738 (0.876 (0.101) 0.112) 0.231)
CG CG CG NLOPT-LD-SLSQP NLOPT-LD-SLSQP	$0.7\ 0$ $0.9\ 0$ $0.3\ 0$	0.963 0.801 0.836	(0.136) (0.017) (0.226) (0.224) (0.146)	$\begin{array}{c} 0.940 \\ 0.752 \\ 0.802 \end{array}$	(0.137) (0.038) (0.258) (0.217) (0.146)	$\begin{array}{c} 0.954 \\ 0.969 \\ 0.945 \end{array}$	(0.037) (0.035) (0.036) (0.047) (0.039)	$\begin{array}{c} 0.946 \\ 0.816 \\ 0.844 \end{array}$	(0.098) (0.024) (0.179) (0.153) (0.104)	0.932 (0 0.961 (0 0.842 (0 0.860 (0 0.926 (0	0.019) 0.165) 0.169)
NLOPT-LD-SLSQP NLOPT-LD-SLSQP NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND	$0.9\ 0$ $0.3\ 0$ $0.5\ 0$	0.572 0.842 0.924	(0.136)	$\begin{array}{c} 0.568 \\ 0.808 \\ 0.898 \end{array}$	(0.159) (0.299) (0.210) (0.138) (0.122)	0.981 0.941 0.949	(0.035) (0.034) (0.050) (0.039) (0.034)	$0.671 \\ 0.848 \\ 0.914$	(0.117) (0.217) (0.149) (0.098) (0.089)	0.930 (0.671 (0.864 (0.930 (0.945 (0.	0.224) 0.165) 0.101)
NLOPT-LD-TNEWTON-PRECOND NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS	$0.3\ 0$ $0.5\ 0$ $0.7\ 0$	0.854 0.935 0.956	(0.269) (0.208) (0.107) (0.068) (0.026)	$\begin{array}{c} 0.824 \\ 0.908 \\ 0.933 \end{array}$	(0.273) (0.201) (0.111) (0.073) (0.063)	$\begin{array}{c} 0.936 \\ 0.945 \\ 0.954 \end{array}$	(0.037) (0.052) (0.042) (0.033) (0.035)	0.856 0.921 0.941	(0.195) (0.141) (0.079) (0.054) (0.034)	0.828 (0.872 (0.938 (0.956 (0.953 (0.	0.157) 0.080) 0.051)
Nelder-Mead Nelder-Mead Nelder-Mead Nelder-Mead SANN	0.5 0 0.7 0 0.9 0).951).785).801	(0.274)	0.937 0.765 0.770	(0.250)	$\begin{array}{c} 0.922 \\ 0.960 \\ 0.961 \end{array}$		0.928 0.817 0.825	(0.117) (0.033) (0.191) (0.176) (0.151)	0.897 (0.944 (0.825 (0.836 (0.907	0.027) 0.204) 0.189)
SANN SANN SANN naive naive	$0.7\ 0$ $0.9\ 0$ $0.3\ 0$	0.963 0.959 0.345	(0.074) (0.015) (0.067) (0.035) (0.162)	0.944 0.942 0.345	(0.089) 4 (0.035) (0.070) (0.035) (0.114)	0.951 0.953 1.000	(0.036) (0.032) (0.033) (0.000) (0.000)	0.947 0.945 0.512	(0.052) (0.039)	0.960 (0.017) (0.049) 0.000)
naive naive			(0.014) (0.016)		(0.035) (0.024)		(0.015) (0.040)				

Table 6. Summary Statistics for dset = credit-a

optims	с	mean	accuracy	mean	precision	mean	recall	mean	f1 score	mean auc
BFGS BFGS BFGS CG	$0.5 \\ 0.7 \\ 0.9$	0.821 0.858 0.710	(0.123) (0.095) (0.056) (0.110) (0.160)	$0.820 \\ 0.847 \\ 0.643$	(0.137) (0.109) (0.074) (0.126) (0.167)	$\begin{array}{c} 0.822 \\ 0.851 \\ 0.942 \end{array}$	(0.118) (0.083) (0.055) (0.054) (0.118)	0.811 0.845 0.754	(0.079) (0.062) (0.045) (0.073) (0.090)	0.775 (0.105) 0.822 (0.083) 0.858 (0.050) 0.729 (0.096) 0.744 (0.136)
CG CG CG NLOPT-LD-SLSQP NLOPT-LD-SLSQP	$0.7 \\ 0.9 \\ 0.3$	0.833 0.788 0.773	(0.084) (0.102) (0.095) (0.112) (0.110)	0.816 0.731 0.782	(0.094) (0.114) (0.125) (0.130) (0.127)	$\begin{array}{c} 0.867 \\ 0.912 \\ 0.778 \end{array}$	(0.077) (0.061) (0.056) (0.125) (0.095)	0.832 0.802 0.762	(0.058) (0.065) (0.068) (0.074) (0.069)	0.832 (0.075) 0.837 (0.091) 0.798 (0.085) 0.775 (0.098) 0.809 (0.095)
NLOPT-LD-SLSQP NLOPT-LD-SLSQP NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND	$0.9 \\ 0.3 \\ 0.5$	0.709 0.738 0.806	(0.115)	0.632 0.738 0.808	(0.120) (0.103) (0.158) (0.126) (0.164)	0.947 0.814 0.822	(0.072) (0.049) (0.131) (0.089) (0.076)	0.751 0.750 0.802	(0.060) (0.057) (0.085) (0.069) (0.093)	0.829 (0.075) 0.727 (0.080) 0.745 (0.128) 0.808 (0.102) 0.795 (0.140)
NLOPT-LD-TNEWTON-PRECOND NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS	$0.3 \\ 0.5 \\ 0.7$	0.751 0.833 0.86 5	(0.137) (0.066) (0.031)	0.748 0.836 0.85 5	(0.104) (0.150) 5 (0.083) 5 (0.053) 6 (0.047)	$\begin{array}{c} 0.812 \\ 0.808 \\ 0.848 \end{array}$	(0.053)	0.757 0.816 0.849	(0.051) (0.081) (0.051) (0.037) (0.033)	0.826 (0.061) 0.757 (0.119) 0.832 (0.058) 0.864 (0.030) 0.868 (0.029)
Nelder-Mead Nelder-Mead Nelder-Mead Nelder-Mead SANN	$0.5 \\ 0.7 \\ 0.9$	0.816 0.795 0.769	(0.136) (0.109) (0.142) (0.145) (0.067)	0.791 0.766 0.725	(0.148) (0.118) (0.141) (0.145) (0.113)	$\begin{array}{c} 0.867 \\ 0.889 \\ 0.912 \end{array}$	(0.119) (0.074) (0.068) (0.064) (0.175)	0.817 0.810 0.795	(0.082) (0.069) (0.087) (0.089) 4 (0.107)	0.763 (0.119) 0.820 (0.099) 0.804 (0.123) 0.781 (0.129) 0.804 (0.077)
SANN SANN SANN naive naive	0.7 0.9 0.3 0.5	0.854 0.846 0.455 0.592	(0.059) (0.038) (0.074) (0.039) (0.077) (0.028)	$\begin{array}{c} 0.843 \\ 0.837 \\ 0.455 \\ 0.532 \end{array}$	(0.070) (0.045) (0.048) (0.039) (0.060) (0.047)	0.833 0.825 1.000 0.977	(0.136) (0.099) (0.178) (0.002) (0.024)	0.841 0.846 0.624 0.686	(0.048)	0.835 (0.062) 0.852 (0.044) 0.846 (0.076) 0.500 (0.002) 0.623 (0.070) 0.860 (0.026)
naive naive			(0.028) (0.028)		(0.047) (0.045)		,		,	0.860 (0.026) 0.875 (0.026)

Table 7. Summary Statistics for dset = credit-g

optims	c n	nean	accuracy	mean	precision	mean	recall	mean f1 score	mean auc
BFGS BFGS BFGS BFGS CG	$0.5 \ 0.7 \ 0.9 \ 0.9 \ 0$	0.686 0.700 0.748	(0.152) (0.116) (0.110) (0.030) (0.156)	$\begin{array}{c} 0.529 \\ 0.560 \\ 0.607 \end{array}$	(0.109) (0.109) (0.115) (0.084) (0.112)	$0.455 \\ 0.499 \\ 0.478$	(0.277) (0.223) (0.213) (0.104) (0.278)	0.423 (0.086) 0.448 (0.102) 0.487 (0.091) 0.526 (0.065) 0.424 (0.088)	0.587 (0.057) 0.620 (0.059) 0.641 (0.052) 0.671 (0.039) 0.585 (0.057)
CG CG CG NLOPT-LD-SLSQP NLOPT-LD-SLSQP	$0.70 \\ 0.90 \\ 0.30$	0.697 0.751 0.621	(0.115) (0.114) (0.028) (0.157) (0.116)	$\begin{array}{c} 0.562 \\ 0.613 \\ 0.457 \end{array}$		$0.505 \\ 0.474 \\ 0.493$	(0.219) (0.215) (0.099) (0.291) (0.223)	0.452 (0.096) 0.489 (0.086) 0.527 (0.065) 0.416 (0.095) 0.449 (0.100)	0.622 (0.057) 0.641 (0.051) 0.672 (0.039) 0.583 (0.058) 0.620 (0.058)
NLOPT-LD-SLSQP NLOPT-LD-SLSQP NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND	$0.9 \ 0.3 \ 0.5 \ 0.5 \ 0$	0.751 0.612 0.681	(0.128)	$\begin{array}{c} 0.612 \\ 0.450 \\ 0.534 \end{array}$	(0.081) (0.108) (0.113)	$\begin{array}{c} 0.472 \\ 0.519 \\ 0.481 \end{array}$	(0.218) (0.097) (0.288) (0.229) (0.216)	0.486 (0.091) 0.525 (0.065) 0.426 (0.088) 0.461 (0.091) 0.487 (0.088)	0.640 (0.052) 0.671 (0.039) 0.584 (0.058) 0.623 (0.059) 0.641 (0.051)
NLOPT-LD-TNEWTON-PRECOND NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS	$0.3 \ 0.5 \ 0.7 \ 0.7 \ 0$	0.623 0.692 0.698	(0.033) (0.158) (0.111) (0.111) (0.032)	$\begin{array}{c} 0.462 \\ 0.540 \\ 0.555 \end{array}$	(0.108) (0.110) (0.113)	0.498 0.437 0.489	(0.133) (0.285) (0.222) (0.220) (0.156)	0.539 (0.064) 0.422 (0.089) 0.441 (0.106) 0.478 (0.099) 0.227 (0.159)	0.680 (0.040) 0.586 (0.056) 0.619 (0.059) 0.637 (0.055) 0.552 (0.057)
Nelder-Mead Nelder-Mead Nelder-Mead Nelder-Mead SANN	0.5 0 0.7 0 0.9 0	0.708 0.727 0.744	(0.057) (0.040)	$\begin{array}{c} 0.541 \\ 0.576 \\ 0.605 \end{array}$	(0.093) (0.090)	0.516 0.502 0.459	(0.223) (0.175) (0.161) (0.111) (0.134)	0.434 (0.113) 0.502 (0.077) 0.514 (0.074) 0.511 (0.065) 0.271 (0.135)	0.614 (0.054) 0.653 (0.042) 0.662 (0.040) 0.662 (0.038) 0.560 (0.047)
SANN SANN SANN naive naive	$0.70 \\ 0.90 \\ 0.30$	0.720 0.733 0.299	(0.035) (0.033) (0.032) (0.030) (0.051)	0.600 0.619 0.299		0.181 0.258 1.000 0.966	(0.138) (0.143) (0.000) (0.029)	0.273 (0.146) 0.278 (0.152) 0.365 (0.144) 0.459 (0.036) 0.498 (0.040)	0.578 (0.031)
naive naive			(0.036) (0.026)		(0.049) (0.071)				0.693 (0.029) 0.693 (0.030)

Table 8. Summary Statistics for dset = dhfr

-											
optims	с	mean	accuracy	mean	precision	mean	recall	mean	f1 score	mean	auc
BFGS	0.3	0.574	(0.137)	0.483	(0.111)	0.932	(0.068)	0.626	(0.090)	0.648	(0.098)
BFGS	0.5	0.666	(0.124)	0.552	(0.113)	0.909	(0.084)	0.677	(0.083)	0.713	(0.095)
BFGS	0.7	0.747	(0.087)	0.630	(0.123)	0.896	(0.120)	0.725	(0.084)	0.780	(0.066)
BFGS	0.9	0.815	(0.082)	0.765	(0.129)	0.787	(0.145)	0.759	(0.095)	0.808	(0.074)
CG	0.3	0.591	(0.114)	0.486	(0.092)	0.918	(0.078)	0.629	(0.080)	0.657	(0.083)
CG	0.5	0.660	(0.114)	0.541	(0.097)	0.890	(0.083)	0.666	(0.077)	0.704	(0.088)
CG	0.7	0.772	(0.103)	0.665	(0.121)	0.869	(0.075)	0.745	(0.086)	0.793	(0.077)
CG	0.9	0.721	(0.092)	0.608	(0.133)	0.866	(0.091)	0.702	(0.079)	0.751	(0.071)
NLOPT-LD-SLSQP	0.3	0.589	(0.117)	0.486	(0.097)	0.926	(0.073)	0.630	(0.083)	0.659	(0.085)
NLOPT-LD-SLSQP	0.5	0.722	(0.091)	0.594	(0.097)	0.890	(0.078)	0.707	(0.079)	0.755	(0.077)
NLOPT-LD-SLSQP	0.7	0.667	(0.105)	0.543	(0.098)	0.940	(0.051)	0.682	(0.074)	0.721	(0.081)
NLOPT-LD-SLSQP	0.9	0.860	(0.067)	0.813	(0.112)	0.831	(0.096)	0.815	(0.086)	0.854	(0.063)
NLOPT-LD-TNEWTON-PRECOND	0.3	0.498	(0.139)	0.438	(0.101)	0.951	(0.073)	0.591	(0.082)	0.589	(0.101)
NLOPT-LD-TNEWTON-PRECOND	0.5	0.604	(0.153)	0.513	(0.128)	0.919	(0.091)	0.644	(0.094)	0.666	(0.111)
NLOPT-LD-TNEWTON-PRECOND	0.7	0.759	(0.086)	0.640	(0.111)	0.893	(0.081)	0.736	(0.077)	0.787	(0.065)
NLOPT-LD-TNEWTON-PRECOND	0.9	0.715	(0.120)	0.607	(0.141)	0.907	(0.096)	0.711	(0.086)	0.754	(0.088)
NLOPT-LN-PRAXIS					(0.100)	0.919	(0.067)				(0.095)
NLOPT-LN-PRAXIS	0.5	0.783	(0.066)	0.668	(0.095)	0.865	(0.076)	0.749	(0.068)	0.799	(0.059)
NLOPT-LN-PRAXIS			(0.052)			0.844	(0.079)				(0.050)
NLOPT-LN-PRAXIS	0.9	0.867	(0.041)	0.829	(0.077)	0.821	(0.095)	0.819	(0.055)	0.859	(0.046)
Nelder-Mead	0.3	0.667	(0.152)	0.717	(0.235)	0.595	(0.278)	0.558	(0.125)	0.656	(0.091)
Nelder-Mead	0.5	0.523	(0.090)		(0.074)		(0.043)	0.602	(0.067)	0.613	(0.060)
Nelder-Mead			(0.084)	0.535	(0.093)	0.931	(0.056)	0.674	(0.075)	0.718	(0.063)
Nelder-Mead			(0.069)		(0.107)		(0.088)		(0.075)		(0.061)
SANN	0.3	0.723	(0.088)	0.699	(0.207)	0.453	(0.263)	0.536	(0.210)	0.670	(0.113)
SANN			(0.093)		(0.179)			0.626	(0.207)		(0.123)
SANN	0.7	0.800	(0.091)		(0.141)			0.678	(0.218)	0.755	(0.128)
SANN	0.9	0.837	(0.091)	0.879	(0.129)	0.646	(0.250)	0.747	(0.186)	0.799	(0.118)
naive	0.3	0.488	(0.064)	0.416	(0.061)		(0.062)		(0.062)		(0.049)
naive	0.5	0.623	(0.072)	0.500	(0.078)	0.876	(0.075)	0.633	(0.070)	0.675	(0.060)
naive	0.7	0.764	(0.057)	0.637	(0.087)	0.870	(0.071)	0.731	(0.068)	0.785	(0.052)
naive	0.9	0.865	(0.040)	0.793	(0.078)	0.868	(0.072)	0.825	(0.053)	0.866	(0.041)

Table 9. Summary Statistics for dset = diabetes

optims	c mea	n accuracy	mean p	recision	mean recall	mean	f1 score	mean auc
BFGS BFGS BFGS CG	0.5 0.73 0.7 0.63 0.9 0.33	06 (0.107) 66 (0.074) 75 (0.175) 76 (0.113) 95 (0.107)	0.635 (0 0.659 (0 0.625 (0 0.374 (0 0.636 (0).105)).170)).115)	0.599 (0.192 0.608 (0.150 0.680 (0.187 0.967 (0.122 0.595 (0.197) 0.612) 0.607) 0.520	,	0.682 (0.067) 0.705 (0.054) 0.682 (0.091) 0.516 (0.057) 0.680 (0.068)
CG CG CG NLOPT-LD-SLSQP NLOPT-LD-SLSQP	0.7 0.49 0.9 0.36 0.3 0.70	3 (0.145) 4 (0.203) 4 (0.069) 4 (0.107) 37 (0.074)	0.630 (0 0.473 (0 0.357 (0 0.636 (0 0.659 (0	0.185) 0.059) 0.133)	0.640 (0.190 0.849 (0.211 0.988 (0.08 0.592 (0.200 0.608 (0.150	0.552 80) 0.518 0.575	(0.071) (0.079) (0.046) (0.089) (0.068)	0.678 (0.084) 0.581 (0.107) 0.509 (0.025) 0.679 (0.069) 0.705 (0.053)
NLOPT-LD-SLSQP NLOPT-LD-SLSQP NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND	0.9 0.57 0.3 0.70 0.5 0.72	4 (0.101)	0.518 (0 0.540 (0 0.635 (0 0.650 (0 0.569 (0).196)).131)).116)	0.812 (0.212 0.782 (0.204 0.596 (0.194 0.616 (0.164 0.757 (0.208	0.581 0.579 0.608	(0.074) (0.091) (0.082) (0.067) (0.080)	0.630 (0.091) 0.635 (0.116) 0.681 (0.067) 0.696 (0.067) 0.655 (0.098)
NLOPT-LD-TNEWTON-PRECOND NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS	0.3 0.70 0.5 0.7 0.7 0.72	5 (0.106)		(0.130) (0.106) (0.206)	0.933 (0.158 0.591 (0.202 0.608 (0.150 0.430 (0.294 0.035 (0.084) 0.575) 0.612) 0.527	(0.061) (0.089) (0.068) (0.217) (0.138)	0.555 (0.077) 0.679 (0.068) 0.705 (0.054) 0.656 (0.108) 0.514 (0.035)
Nelder-Mead Nelder-Mead Nelder-Mead Nelder-Mead SANN	0.5 0.63 0.7 0.60 0.9 0.65	0 (0.150) 7 (0.170) 03 (0.182) 05 (0.153) 07 (0.124)	0.590 (0 0.573 (0 0.549 (0 0.591 (0 0.559 (0	0.160) 0.164) 0.158)	0.632 (0.255 0.687 (0.224 0.692 (0.262 0.658 (0.226 0.576 (0.299	0.574 0.550 0.572	(0.100) (0.079) (0.081) (0.078) (0.151)	0.647 (0.080) 0.649 (0.092) 0.620 (0.094) 0.658 (0.080) 0.638 (0.091)
SANN SANN SANN naive naive	0.7 0.7 0.9 0.75 0.3 0.34	55 (0.066) 55 (0.050) 8 (0.049) 9 (0.041) 9 (0.058)		(0.123) (0.082) 0.040) 0.048)	0.541 (0.245 0.538 (0.191 0.514 (0.175 1.000 (0.00 0.986 (0.01	0.615 0.620 02) 0.515 (6) 0.544	(0.050)	0.683 (0.083) 0.705 (0.073) 0.702 (0.073) 0.501 (0.003) 0.558 (0.031)
naive naive		5 (0.043) 64 (0.036)	0.540 (0 0.676 (0					0.735 (0.033) 0.730 (0.040)

Table 10. Summary Statistics for dset = heart-c

optims	c me	ean ac	curacy	mean	precision	mean	recall	mean	f1 score	mean auc
BFGS BFGS BFGS GG	0.3 0.6 0.5 0.6 0.7 0. 0.9 0.3	686 (0. 752 (0. 755 (0.	.112) 0.063) .066)	0.684 0.745 0.741	(0.122) (0.134) (0.101) (0.115) (0.134)	$\begin{array}{c} 0.752 \\ 0.742 \\ 0.776 \end{array}$	(0.202) (0.172) (0.128) (0.116) (0.208)	$0.690 \\ 0.732 \\ 0.745$	(0.098) (0.082) (0.075) (0.067) (0.093)	0.656 (0.091) 0.692 (0.096) 0.752 (0.060) 0.759 (0.057) 0.636 (0.101)
CG CG CG NLOPT-LD-SLSQP NLOPT-LD-SLSQP	0.5 0.6 0.7 0.3 0.9 0.3 0.3 0.6 0.5 0.6	720 (0. 721 (0. 542 (0.	.097) .074) .100)	0.711 0.682 0.629	(0.120)	0.776 0.833 0.718	(0.169) (0.154) (0.122) (0.212) (0.175)	$\begin{array}{c} 0.720 \\ 0.734 \\ 0.642 \end{array}$	(0.078) (0.079) (0.068) (0.101) (0.085)	0.690 (0.098) 0.727 (0.080) 0.732 (0.061) 0.645 (0.093) 0.694 (0.092)
NLOPT-LD-SLSQP NLOPT-LD-SLSQP NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND	$0.5 \ 0.6$	770 (0. 622 (0. 688 (0.	.064) .116) .114)	0.772 0.610 0.688	(0.105) (0.130) (0.135)	$0.750 \\ 0.773 \\ 0.755$	(0.131) (0.105) (0.206) (0.166) (0.155)	0.751 0.651 0.694	(0.076) (0.068) (0.090) (0.075) (0.081)	0.751 (0.060) 0.772 (0.057) 0.632 (0.101) 0.693 (0.097) 0.714 (0.094)
NLOPT-LD-TNEWTON-PRECOND NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS	0.9 0.6 0.3 0.6 0.5 0.6 0.7 0.7 0.9 0.7	626 (0. 687 (0. 749 (0.	.112) .111) .066)	0.623 0.684 0.743	(0.133)	0.731 0.749 0.740	(0.173) (0.131)	0.638 0.689 0.729	(0.075) (0.097) (0.085) (0.079) (0.076)	0.714 (0.080) 0.634 (0.097) 0.692 (0.096) 0.749 (0.062) 0.761 (0.055)
Nelder-Mead Nelder-Mead Nelder-Mead Nelder-Mead SANN	0.3 0.6 0.5 0.6 0.7 0.3 0.9 0.3	696 (0. 726 (0. 731 (0.	.095) .087) .086)	0.697 0.728 0.717	(0.133) (0.131)	0.733 0.747 0.783	(0.205) (0.189) (0.162) (0.139) (0.243)	$0.686 \\ 0.715 \\ 0.730$	(0.093) (0.094) (0.082) (0.070) (0.123)	0.670 (0.085) 0.697 (0.088) 0.730 (0.078) 0.734 (0.078) 0.679 (0.087)
SANN SANN SANN naive naive	0.5 0. 0.7 0.7 0.9 0.7 0.3 0.4 0.5 0.8	743 (0 746 (0 471 (0	.075) .081) .061)	0.798 0.781 0.469	(0.115) (0.109) (0.126) (0.061) (0.071)	$0.631 \\ 0.630 \\ 1.000$		$\begin{array}{c} 0.703 \\ 0.707 \\ 0.637 \end{array}$		0.718 (0.067) 0.740 (0.069) 0.741 (0.081) 0.502 (0.009) 0.579 (0.046)
naive naive	0.7 0.7 0.9 0.	,	.055) 0.048)		(0.076) (0.083)					0.716 (0.051) 0.776 (0.049)

Table 11. Summary Statistics for dset = spambase

-											
optims	c	mean	accuracy	mean	precision	mean	recall	mean	f1 score	mean	auc
BFGS	0.3	0.901	(0.013)	0.874	(0.026)	0.876	(0.028)	0.875	(0.018)	0.897	(0.014)
BFGS	0.5	0.886	(0.120)	0.872	(0.122)	0.889	(0.034)	0.873	(0.078)	0.887	(0.093)
BFGS	0.7	0.410	(0.075)	0.407	(0.075)	0.998	(0.017)	0.574	(0.048)	0.513	(0.058)
BFGS	0.9	0.627	(0.261)	0.625	(0.263)	0.945	(0.064)	0.711	(0.165)	0.684	(0.204)
CG	0.3	0.894	(0.054)	0.860	(0.057)	0.883	(0.030)	0.870	(0.037)	0.892	(0.042)
CG	0.5	0.915	(0.010)	0.897	(0.019)	0.886	(0.020)	0.891	(0.013)	0.910	(0.011)
CG	0.7	0.860	(0.140)	0.838	(0.164)	0.903	(0.043)	0.855	(0.099)	0.868	(0.109)
CG	0.9	0.644	(0.157)	0.571	(0.150)	0.933	(0.075)	0.690	(0.090)	0.695	(0.117)
NLOPT-LD-SLSQP	0.3	0.856	(0.147)	0.834	(0.143)	0.884	(0.045)	0.846	(0.092)	0.861	(0.114)
NLOPT-LD-SLSQP	0.5	0.889	(0.111)	0.876	(0.118)	0.886	(0.034)	0.874	(0.074)	0.889	(0.085)
NLOPT-LD-SLSQP	0.7	0.798	(0.125)	0.721	(0.161)	0.928	(0.045)	0.797	(0.090)	0.821	(0.095)
NLOPT-LD-SLSQP	0.9	0.828	(0.043)	0.731	(0.076)	0.912	(0.023)	0.808	(0.038)	0.842	(0.032)
NLOPT-LD-TNEWTON-PRECOND	0.3	0.885	(0.089)	0.859	(0.088)	0.880	(0.034)	0.865	(0.057)	0.885	(0.069)
NLOPT-LD-TNEWTON-PRECOND	0.5	0.850	(0.171)	0.837	(0.170)	0.897	(0.044)	0.850	(0.108)	0.858	(0.135)
NLOPT-LD-TNEWTON-PRECOND	0.7	0.761	(0.211)	0.734	(0.227)	0.921	(0.058)	0.787	(0.139)	0.789	(0.164)
NLOPT-LD-TNEWTON-PRECOND	0.9	0.625	(0.082)	0.523	(0.085)	0.971	(0.026)	0.675	(0.053)	0.686	(0.062)
NLOPT-LN-PRAXIS	0.3	0.878	(0.099)	0.854	(0.097)	0.874	(0.039)	0.858	(0.061)	0.877	(0.078)
NLOPT-LN-PRAXIS	0.5	0.914	(0.010)	0.901	(0.019)	0.878	(0.020)	0.889	(0.013)	0.908	(0.011)
NLOPT-LN-PRAXIS					(0.016)						(0.011)
NLOPT-LN-PRAXIS	0.9	0.920	(0.008)	0.920	(0.014)	0.872	(0.018)	0.895	(0.012)	0.911	(0.010)
Nelder-Mead	0.3	0.834	(0.080)	0.803	(0.084)	0.803	(0.062)	0.797	(0.050)	0.829	(0.062)
Nelder-Mead	0.5	0.684	(0.223)	0.678	(0.220)	0.856	(0.118)	0.717	(0.120)	0.714	(0.166)
Nelder-Mead	0.7	0.779	(0.169)	0.762	(0.169)	0.819	(0.094)	0.768	(0.096)	0.785	(0.127)
Nelder-Mead			(0.148)	0.755	(0.151)		(0.110)	0.737	(0.077)	0.765	(0.108)
SANN	0.3	0.855	(0.037)	0.784	(0.054)	0.884	(0.094)	0.824	(0.087)	0.860	(0.043)
SANN	0.5	0.888	(0.013)	0.845	(0.032)	0.878	(0.028)	0.860	(0.015)	0.886	(0.012)
SANN	0.7	0.886	(0.058)	0.873	(0.022)	0.833	(0.172)	0.870	(0.013)	0.877	(0.078)
SANN	0.9	0.879	(0.078)	0.891	(0.054)	0.799	(0.186)	0.854	(0.093)	0.865	(0.092)
naive	0.3	0.397	(0.013)	0.395	(0.013)		0.001)			0.503	(0.003)
naive	0.5	0.482	(0.023)	0.431	(0.017)	0.996	6(0.003)	0.602	(0.016)	0.572	(0.017)
naive	0.7	0.828	(0.019)	0.716	(0.030)	0.938	(0.015)	0.811	(0.018)	0.847	(0.015)
naive	0.9	0.898	(0.010)	0.899	(0.016)	0.835	(0.022)	0.865	(0.014)	0.887	(0.012)

Table 12. Summary Statistics for dset = wine-quality

optims	c mean	accuracy	mean precision	mean recall	mean f1 score	mean auc
BFGS BFGS BFGS BFGS CG	0.3 0.726 0.5 0.812 0.7 0.869 0.9 0.874 0.3 0.682	(0.177) (0.024) (0.018)	0.387 (0.151) 0.472 (0.127) 0.546 (0.107) 0.566 (0.101) 0.371 (0.159)	0.469 (0.287) 0.417 (0.214) 0.324 (0.097) 0.322 (0.070) 0.508 (0.301)	0.350 (0.112) 0.395 (0.090) 0.395 (0.072) 0.405 (0.071) 0.344 (0.108)	0.618 (0.080) 0.645 (0.065) 0.639 (0.039) 0.641 (0.034) 0.610 (0.081)
CG CG CG NLOPT-LD-SLSQP NLOPT-LD-SLSQP	0.5 0.805 0.7 0.858 0.9 0.729 0.3 0.719 0.5 0.819	(0.191) (0.082) (0.077) (0.277)	0.472 (0.131) 0.534 (0.116) 0.328 (0.078) 0.371 (0.154) 0.474 (0.123)	0.424 (0.219) 0.335 (0.131)	0.396 (0.088) 0.391 (0.072)	, ,
NLOPT-LD-SLSQP NLOPT-LD-SLSQP NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND NLOPT-LD-TNEWTON-PRECOND	0.7 0.869 0.9 0.874 0.3 0.711 0.5 0.812	(0.024) (0.018) (0.283) (0.179)	0.545 (0.107) 0.566 (0.101) 0.381 (0.155) 0.476 (0.129) 0.529 (0.131)	0.323 (0.097) 0.322 (0.070) 0.482 (0.288) 0.415 (0.213) 0.350 (0.165)	0.394 (0.072) 0.405 (0.071) 0.349 (0.111) 0.395 (0.088) 0.387 (0.079)	0.639 (0.038) 0.641 (0.034) 0.615 (0.079) 0.645 (0.065) 0.634 (0.045)
NLOPT-LD-TNEWTON-PRECOND NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS NLOPT-LN-PRAXIS	0.9 0.675 0.3 0.742 0.5 0.836 0.7 0.865 0.9 0.867	(0.257) (0.133) (0.019)	0.325 (0.123) 0.384 (0.150) 0.488 (0.110) 0.327 (0.357) 0.414 (0.322)	0.791 (0.254) 0.435 (0.283) 0.381 (0.184) 0.045 (0.114) 0.066 (0.129)	0.408 (0.105) 0.338 (0.119) 0.393 (0.088) 0.228 (0.187) 0.290 (0.174)	0.725 (0.090) 0.613 (0.078) 0.644 (0.059) 0.519 (0.050) 0.529 (0.058)
Nelder-Mead Nelder-Mead Nelder-Mead Nelder-Mead SANN	0.3 0.638 0.5 0.688 0.7 0.768 0.9 0.844 0.3 0.836	(0.295) (0.245) (0.116)	0.352 (0.162) 0.400 (0.174) 0.478 (0.170) 0.517 (0.143) 0.401 (0.157)	0.611 (0.310) 0.527 (0.305) 0.423 (0.268) 0.311 (0.208) 0.287 (0.236)	0.358 (0.111) 0.359 (0.104) 0.369 (0.092) 0.340 (0.114) 0.350 (0.125)	0.627 (0.090) 0.619 (0.077) 0.622 (0.064) 0.620 (0.066) 0.604 (0.081)
SANN SANN SANN naive naive		(0.019) (0.076) (0.019)	0.496 (0.162) 0.543 (0.144) 0.560 (0.114) 0.135 (0.018) 0.183 (0.029)	0.247 (0.184) 0.279 (0.129) 0.291 (0.125) 1.000 (0.002) 0.982 (0.023)	\ /	0.604 (0.076) 0.621 (0.057) 0.624 (0.049) 0.500 (0.002) 0.644 (0.043)
naive naive	0.7 0.826 0.9 0.876		0.418 (0.068) 0.622 (0.115)	0.683 (0.082) 0.234 (0.079)		0.766 (0.037) 0.606 (0.037)