

Math 341 / 641

Fall 2025 (4 credits)

Course Syllabus

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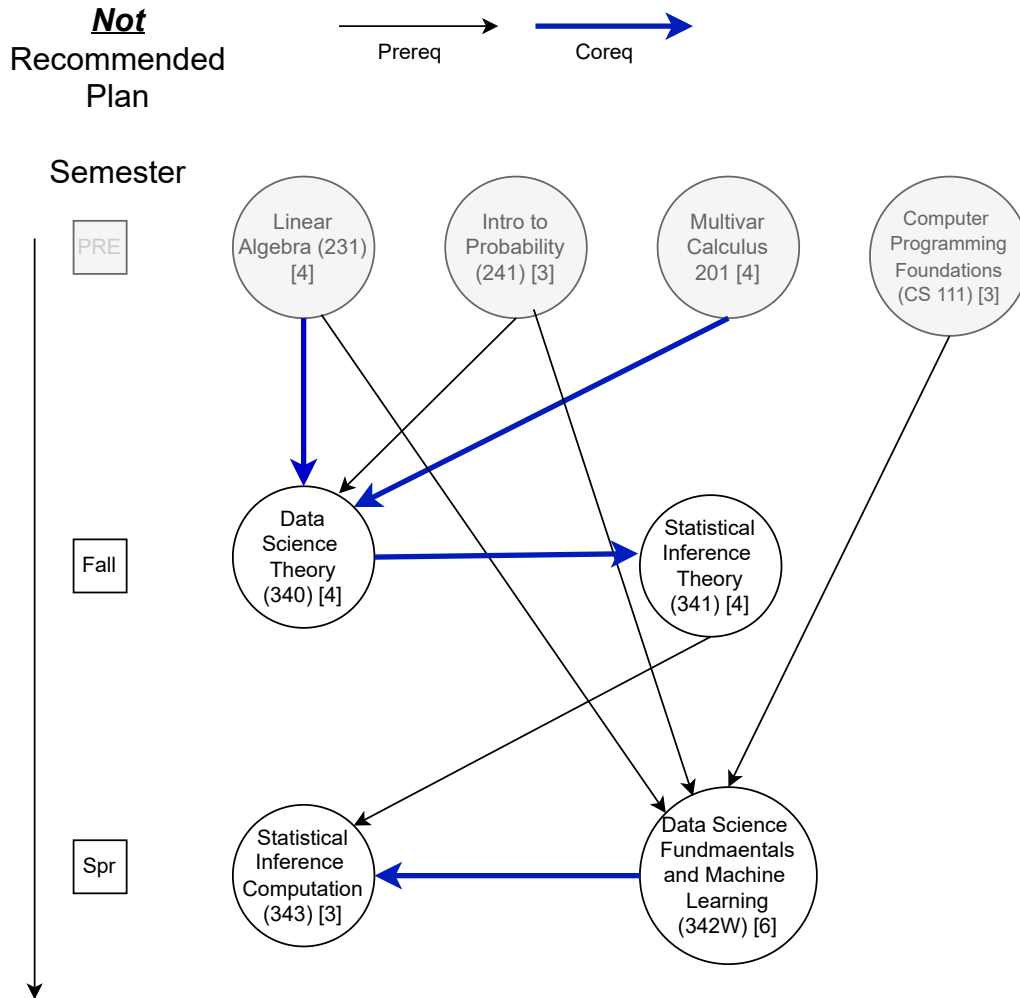
Course Homepage	https://github.com/kapelner/QC_Math_341_Fall_2025
Discord Channel	https://discord.com/channels/1407494938773553273/
Contact	kapelner@qc.cuny.edu
Office	604 Kiely Hall
Lecture Time / Loc	Mon and Wed 6:45 – 8:35PM / KY 258
Instructor Office Hours / Loc	see course homepage
TA(s) / Office Hours Time / Loc	Bryan Nevarez / see course homepage

Course Overview

MATH 341 / 641. Statistical Theory for Data Science. 4 hr.; 4 cr. Coreq.: MATH 340 or 640. Sampling, point estimation via method of moments and maximum likelihood, loss and risk, bias-variance decomposition, frequentist confidence intervals, frequentist hypothesis testing, the p-value, type I/II errors, power, Neyman-Pearson Lemma, the model selection problem, Bayesian inference, prior distribution specification, conjugacy, Bayesian point estimation, credible regions, posterior predictive distribution, Beta-Binomial and Normal-Inverse-Gamma model, consistency, Cramer-Rao lower bound, delta method. Not open to students who are taking or who have received credit for MATH 341. Students cannot receive credit for both: MATH 341 and 641. Fall, Spring

This class proceeds in *lockstep* with its corequisite, Math 340 / 640. What we use in the 340 lecture is timed to be used in the 341 lecture afterwards. This means that if you took 340 in a previous year, you need to make an effort to review the notes lecture-by-lecture to refresh the concepts!

This class is part of the four 34x series which constitute the data science core. There is an order that the four classes need to be taken. Below are three plans, the first is over two semesters and hence it is not *not recommended* as it will be a *very* heavy workload. The second is over four semesters and it is the recommended plan as I believe it will allow students to absorb the material more effectively.

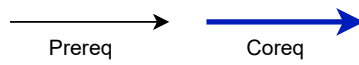


Examining the above, we note that MATH 340 can be taken as a standalone course as a higher-level math elective. It can be thought of as advanced probability following MATH 241. This course is also recommended for students who are considering an actuarial career as this course provides great practice for Exam P.

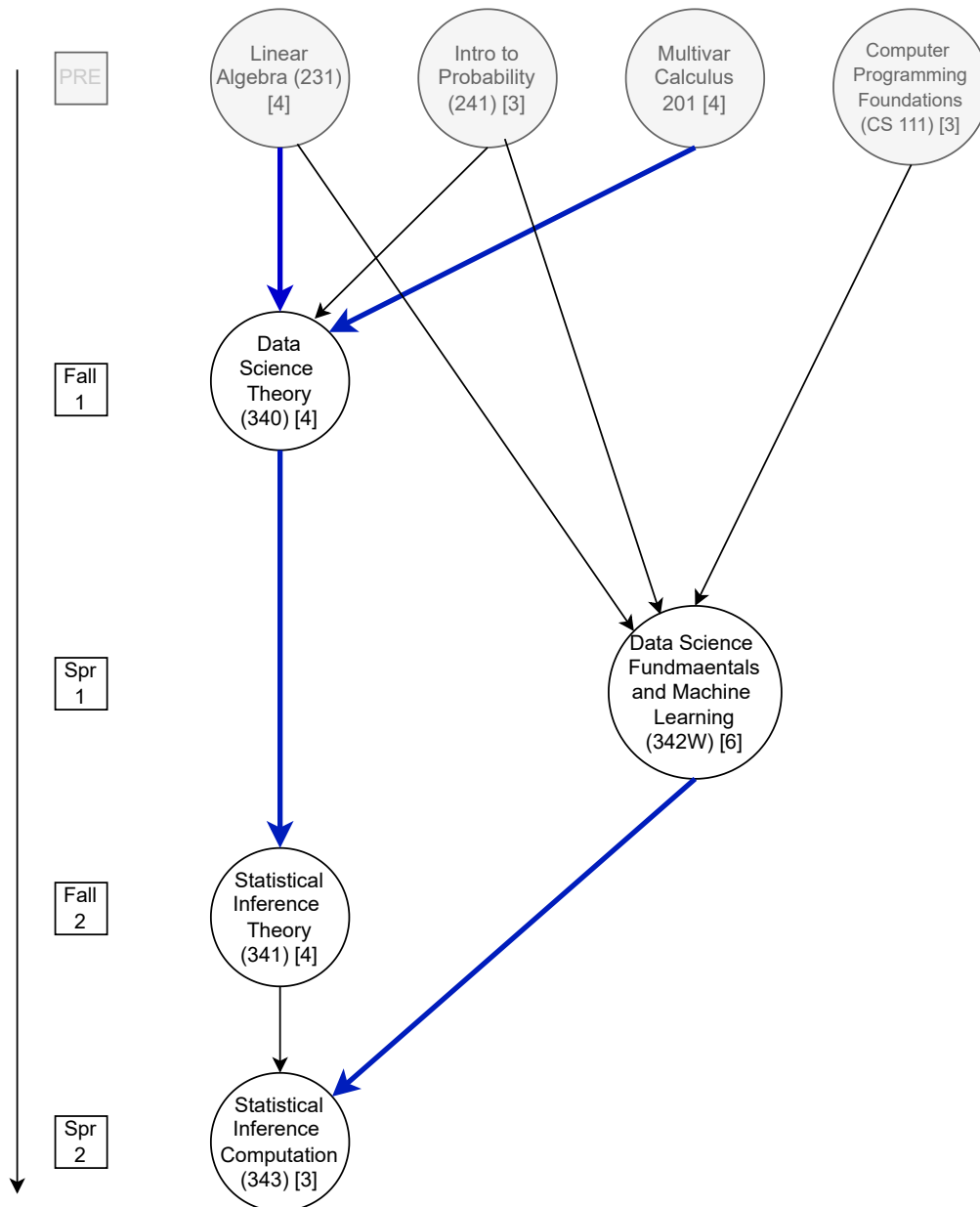
There is also a third way (not pictured) which is Spring year 1: MATH 342W, Fall year 2: Math 340 and Math 341, Spring year 2: Math 343 which is a middle path with a very difficult Fall semester.

Examining the above, we note that MATH 341 and 343 form a series of two statistics courses: the first, theoretical with traditional topics and the second, computational with modern topics. Both heavily rely on the theoretical topics taught in MATH 340.

Recommended Plan



Semester



Tentative Day-by-Day Schedule

Lectures and their topics with rough time estimates per topic are below:

- Day 1 [20min] Surveys, populations, sampling, sample size n , representativeness, SRS; [30min] definition of parameter, parameter space, inference, statistic, the three goals of statistical inference: point estimation, theory testing and confidence set construction; [20min] Sampling with/without replacement, iid assumption, equivalence of populations and data generating processes (DGPs) [55min] estimators, point estimation metrics: biasedness and unbiasedness, loss functions (absolute, squared error, others), risk function, mean squared error (MSE), bias-variance decomposition of MSE, maximum risk for iid Bernoulli model;
- Day 2 [15min] Comparison of bad estimator with sample average [60min] Introduction to hypothesis testing, the intellectual honesty of assuming the null hypothesis H_0 , the theory you wish to prove H_a , right, left and two-sided tests of single parameters, test statistics, null distributions, retainment and rejection regions, the two test outcomes, statistical significance [15min] the Binomial exact test of one proportion in the iid Bernoulli DGP [15min] size, level, Type I and II errors, 2×2 confusion table of testing errors, scientific convention of α
- Day 3 [10min] Facts about normal distributions [30min] Motivation of exact Z tests for one sample with known variance [5min] equivalence of size and level [15min] Fisher's p-value and calculations under normal sampling distributions; [25min] Definition of power, assuming a true sampling distribution to compute the probability of Type II errors and power [15min] Power function and its inputs [10min] Power convention in study design
- Day 4 [20min] θ_0 in one-sided, one-sample tests and a discussion about what “retain” vs “accept” means in the context of scientific theories [10min] Rigorous definition of p-value based on examination of 1-sided tests [15min] the exact two-sample z-test under different variances and shared variance [10min] review of moments, definition of sample moments; [20min] the system of equations yielding the method of moments (MM) estimators [10min] MME for the expectation, MME for the variance [20min] MME for the two parameters in the iid Binomial DGP, nonsensical MME values
- Day 5 [5min] Definition of asymptotically normal estimator [20min] the approximate one-proportion z-test based on the CLT [10min] introduction of the likelihood and its equivalence to the JMF/JDF [15min] definition of argmax in a precalculus context, proof of its invariance under strictly increasing functions [10min] the concept of an maximum likelihood estimator (MLE) and log likelihood's role in finding MLE's [10min] MLE for the iid Bernoulli DGP [10min] MLE for the iid normal DGP's mean and MLE for the iid normal DGP's variance [10min] boundary solution for the MLE of a normal with unknown right-hand side boundary and comparison with the MM
- Day 6 [5min] the nonexistence of a minimum MSE estimator [5min] definition of uniformly minimum variance unbiased estimators (UMVUEs) [5min] definition of the Cramer-Rao Lower Bound (CRLB) [35min] proof of the CRLB, definition of the score function, expectation of the score function is zero, both definitions of Fisher Information, inverse Fisher Information; [10min] proof that the sample average is the UMVUE for the iid Bernoulli DGP

[10min] proof that the sample average is the UMVUE for the iid normal DGP [10min] definition of interval estimators, confidence interval (CI) estimator, CI estimates

- Day 7 [20min] derivation of the CI estimator using test inversions [10min] the three unsatisfying interpretations of CI estimates [15min] CI estimator for 1-proportion [20min] definition of clinical or practical significance and the eventual rejection (statistical significance) of every H_0 with high n [20min] Review of Type I/II errors [20min] multiple hypothesis tests, family-wise error rates (FWER), weak control of FWER
- Day 8 [5min] Boole's Inequality [10min] Bonferroni's Correction [10min] Sidak-Dunn correction [30min] Simes procedure [20min] False discovery rate (FDR) vs. FWER [5min] Simes procedure for FDR (Benjamini-Hochberg) [10min] Empirical CDF [20min] Glivenko-Cantelli theorem and the one-sample Kolmogorov-Smirnov test, Kolmogorov distribution and its critical values
- Day 9 [Midterm I Review](#)
- Day 10 [Midterm I](#)
- Day 11 [20min] two-sample Kolmogorov-Smirnov test [40min] two-proportion z-test using CMT+Slutsky theorems [15min] shared average estimator via WLLN [40min] one-proportion CI using CMT+Slutsky theorems
- Day 12 [20min] two-proportion CI using CMT+Slutsky theorems [20min] non-parametric Wald Z test for one sample [20min] non-parametric Wald Z test for two samples [10min] unbiasedness of the sample variance estimator, Bessel's correction [10min] statement of the core MLE theorem (asymptotic normality and variance as a function of the Fisher Information) [20min] proof of the core MLE theorem
- Day 13 [40min] using the core MLE theorem to construct one-sample tests and one-sample CIs [30min] Example of the core MLE theorem to test the Gumbel parameter [40min] The score test, its proof of its asymptotic normality
- Day 14 [15min] non-closed form MLE for the logistic distribution's mean parameter [40min] example of the score test testing the logistic distribution's mean parameter [10min] likelihood ratio (LR) definition [20min] proof of asymptotic distribution of the scaled log LR using CMT+Slutsky theorems, LR test [5min] iid Bernoulli likelihood ratio statistic [5min] visualizing the Wald, Score and LR tests [30min] Neyman-Pearson Lemma
- Day 15 [10min] Reparameterization of the Bernoulli parameter as odds against [30] Delta method and proof of its asymptotic normality [15min] example of inference for log mean [15min] Student's t-test for one sample, critical t values, one-sample confidence intervals [20min] two sample t-tests for equal variances, two-sample confidence intervals [25min] Welch-Satterthwaite approximate 2-sample t-test for unequal variances and confidence interval
- Day 16 [10min] Equivalent of Z and chi-squared tests, equivalence of T and F tests [20min] F-test for homogeneity of variances in two iid normal samples [30min] Chi-squared test for goodness-of-fit / multinomial parameter [30min] Chi-squared test of independence [20min] Chi-squared test of homogeneity

- Day 17 [15min] DGP as a “model” [30min] Model selection problem, AIC, AICc selection [35min] Problems with frequentism [30min] Introduction to Bayesian inference
- Day 18 [30min] Bayesian inference for the bernoulli with a finite set of possible parameters [10min] Laplace’s principle of indifference [10min] Maximum a posteriori (MAP) point estimation as the MLE under Laplace [10min] joint data-parameter distribution visualization [10min] principle of indifference on the entire parameter space as the standard uniform [30min] posterior distribution is beta [5min] MAP estimator for beta posterior [10min] proof that minimum mean squared error estimate is the posterior expectation
- Day 19 [Midterm II Review](#)
- Day 20 [Midterm II](#)
- Day 21 [5min] proof that minimum mean absolute error estimate is the posterior median for continuous posteriors [10min] 2-sided credible regions (CRs) as a solution to the confidence set inference question [10min] CRs for the beta posterior with the qbeta function [20min] one-sided hypothesis tests and the definition of the Bayesian p-value [10min] one-sided hypothesis tests for the beta posterior with the pbeta function [10min] two-sided hypotheses tests a choice of the margin of equivalence [10min] two sided hypothesis tests for the beta posterior [5min] two sided hypothesis testing using CRs [10min] general beta prior [5min] conjugacy [5min] pseudodata interpretation of prior hyperparameters
- Day 22 [10min] MMSE as a shrinkage estimator [10min] equivalence of the binomial DGP with the iid bernoulli DGP [20min] definition of the posterior predictive distribution [10min] derivation of the betabinomial posterior predictive distribution in the beta-binomial model [10min] betabinomial model where only one observation is required [30min] reparameterization of the binomial parameter in log-odds and demonstration that principle of indifference is not invariant
- Day 23 [30min] binomial vs betabinomial model for birth data, AIC calculation [10min] betaprime conjugacy for binomial model with log odds parameterization [10min] motivation of Jeffrey’s procedure to create priors [10min] proof that Jeffrey’s procedure works as specified [20min] Jeffrey’s prior for the binomial DGP [10min] motivation of Haldane’s prior, Haldane’s prior for the binomial DGP [10min] discussion of subjective priors [10min] case study of inferring career batting averages using an empirical prior
- Day 24 [20min] proof that gamma is conjugate for iid poisson DGP with pseudodata interpretation [10min] Laplace prior for iid poisson DGP [5min] Haldane prior for iid poisson DGP [20min] Jeffrey’s prior for iid poisson DGP [10min] MMSE, MMAE MAP estimator for gamma posteriors [15min] CR’s and hypothesis tests for gamma posteriors [10min] posterior predictive distribution as an extended negative binomial distribution for iid poisson DGP with gamma prior [10min] MMSE as a shrinkage estimator for iid poisson DGP with gamma prior [10min] iid normal DGP with variance known proof that prior is normal
- Day 25 [5min] MMSE, MMAE MAP estimator for normal posteriors [5min] MMSE as a shrinkage estimator [5min] CRs and hypothesis tests for normal posteriors [5min] Laplace and prior for iid normal DGP with variance known [5min] reparameterization of hyperparameters to

reveal pseudodata interpretation [5min] Haldane prior for iid normal DGP with variance known [10min] Jeffrey's prior for iid normal DGP with variance known [5min] posterior predictive distribution is normal for next observation [10min] iid normal DGP with mean known proof that prior is inverse gamma [5min] derivation of inverse gamma's mode [5min] MAP, MMSE and MMAE for inverse gamma posterior [5min] MMSE as a shrinkage estimator [5min] pseudodata interpretation of prior hyperparameters [5min] the problem with Laplace's prior for the iid normal DGP with mean known [5min] Haldane's prior for the iid normal DGP with mean known [10min] Jeffrey's prior for the iid normal DGP with mean known [5min] CR's and hypothesis tests for inverse gamma posteriors [20min] deriving the posterior predictive distribution for next observation as the location-scale Student's T distribution

Day 26 [20min] iid normal DGP proof that normalinversegamma is conjugate [5min] point estimation for multidimensional posteriors [5min] CRs and hypothesis testing for normalinversegamma as too complicated to pursue [5min] Jeffrey's and Haldane's standard prior for the iid normal DGP [10min] marginal posterior of the mean parameter as the location-scale Student's T distribution [10min] marginal posterior of the variance parameter as an inverse gamma [30min] posterior predictive distribution for next observation as the location-scale Student's T distribution

Day 27 [15min] posterior predictive intervals for all models studied [10min] sampling from the normalinversegamma posterior in two ways [30min] Gibbs sampling, sampling from the normalinversegamma posterior via Gibbs sampling [10min] burning Gibbs chains [10min] thinning Gibbs chains [10min] demo of Gibbs sampler for the normalinversegamma model [10min] iid Poisson time-change model [10min] demo of Gibbs sampler for the Poisson time-change model

Day 28 [Final Review](#)

This is more of a typical mathematics theory course than the rest of the data science series. But we will still attempt to keep our eye on developing ideas and concepts for helping to make decisions in the real world. Thus we may make limited use of computation using the R statistical language.

Corequisites

MATH 340 or an intermediate probability class that covers similar topics. Critical is coverage of the Central Limit Theorem, convergence in probability, Slutsky's theorem, Cochran's theorem.

Course Materials

Textbooks: For the first 2/3 of the class, we will be doing classical or "Frequentist Inference". Here, I will be referencing Larry Wasserman's *All of Statistics: A concise course in statistical inference* which can be purchased on Amazon and Casella and Berger's *Statistical Inference* which can be purchased on Amazon. There is no excuse not to have these books. They are *required*. However, I will not usually be teaching "from the book" — most of the material

in the class comes from the lecture notes. The textbooks are a way to get “another take” on the material and they will only cover about only half of the material done in class. For the other half, you will have to make use of other resources. I also recommend Rice’s *Mathematical Statistics and Data Analysis*, 3rd edition which can be purchased on Amazon as well but I will not reference it during class. When the class transitions to the last third, we will switch to “Bayesian Inference”. A good introductory book is *Introduction to Bayesian Statistics* by William M. Bolstad First Edition. It can be purchased used on Amazon. This is *recommended*. The Bayesian Bible is *Bayesian Data Analysis* by Andrew Gelman et al. which can be purchased on Amazon as well. This latter book is very dense and we will only scratch the surface of its topics in this class. Note that these books constitute a means to get “another take” on the material. However, most of the material in the class comes from the lecture notes.

Popular Books: For the first Frequentist section of the class, I recommend *The Lady Tasting Tea* by David Salsburg which can be purchased on Amazon. For the Bayesian section of the class, I recommend *The Theory that Would not Die: How Bayes’ Rule Cracked the Enigma Code, Hunted Down Russian Submarines, and Emerged Triumphant from Two Centuries of Controversy* by Sharon B. McGrayne which can be purchased on Amazon.

Computer Software: During lectures, there will be demos using R which is a free, open source statistical programming language and console. You can download it from: <http://cran.mirrors.hoobly.com/>. I do not expect you to do *any* programming. If R will be part of the homework, I will give you the code to run and expect you to interpret the results based on concepts explained during the course.

Calculator: You can use a TI-84, 85, 89 or any calculator which you wish. I strongly suggest you use Wolfram Alpha and its smartphone app.

The 641 Section

You are the students taking this course as part of a masters degree in mathematics. Thus, there will be extra homework problems for you and you will be graded on a separate curve.

Discord Coupled with Github as a Learning Management System

Each assignment and exam will have its own channel. You can feel free to discuss things with your fellow students there. If you are asking me a question, you must do so in the **#discussions** channel for a general questions or the assignment-specific channel (e.g. **#hw03**) so other students can see the question and benefit from the answer. Do **not** open “issues” on github! If you pm me for help with a class assignment, I will not answer and just ask you to move it to the appropriate public channel. Do not be afraid to ask questions. There are many people who will have your same question!

Discord is to be used professionally so **no posting about random stuff!**

Announcements

Course announcements will be made via discord in the **#general** channel (not on email). I am known to send a few discord messages per week on important issues.

I can't stress the following enough: **if you are not on discord, you will miss all class announcements!!!** Discord notifies you when there are messages.

Class Meetings

There are 28 scheduled meetings. Of these, 23 will be lectures, 2 will be midterm exams which are in class and 3 will be review periods during the meeting before the exams (see lecture schedule section above). The exam schedule is given on page 11. The last class of the semester *may* be rescheduled to be a review period that is conveniently before the final. We will discuss later in the semester.

Reschedule of One Class Meeting

Due to the Jewish holidays, I cannot be here to teach on one day (see course homepage).

Homework

There will be 6–9 theory homework assignments. Homeworks will be assigned and placed on the course homepage and will usually be due a week later. Homework will be **graded** out of 100 with extra credit getting scores possibly > 100 . I (or the TA if one exists) will be doing the grading and will either grade an *arbitrary subset of the assignment* which is determined after the homework is handed in or *will grade based on completeness*.

You will send by email your finished homework as a PDF to me (kapelner@gmail.com). To generate this PDF file that you push to your repository, **you must do one of two things:**

- **Print out the homework and handwrite your answers in the allotted space for each question. Then scan your homework as a PDF. There are a ton of good photo \Rightarrow PDF apps for both iPhone and droid.**
- **Open the PDF on your device and use a PDF editing program to electronically handwrite your answers and save the PDF.**

I will NOT accept homework that is not atop the original rendered homework PDF file. Remember to write your name. There are no regrades during this pandemic semester. Homework must be at maximum 5MB.

You are highly recommended to work with each other and help each other. You must, however, submit your own solutions, *with your own write-up* and in *your own words*. There can be no collaboration on the actual *writing*. Failure to comply will result in severe penalties. The university honor code is something I take seriously and I send people to the Dean every semester for violations.

Philosophy of Homework

Homework is the *most* important part of this course.¹ Success in Statistics and Mathematics courses comes from experience in working with and thinking about the concepts. It's kind of like weightlifting; you have to lift weights to build muscles. My job as an instructor is to provide assistance through your zone of proximal development. With me, you can grow more than you can alone. To this effect, homework problems are color coded **green** for easy, **yellow** for harder, **red** for challenging and **purple** for extra credit. You need to know how to do all the greens by yourself. If you've been to class and took notes, they are a joke. Yellows and reds: feel free to work with others. Only do extra credits if you have already finished the assignment. The "[Optional]" problems are for extra practice — highly recommended for exam study.

Time Spent on Homework

This is a four credit course. Thus, the amount of work outside of the 4 hours in-class time per week is 8–10 hours per the QC bulletin. I will aim for 9 hours of homework per week on average. This will be time well-spent. I guarantee that by doing the homework well, you will study and understand the concepts in the lectures and you won't have all that much to do when the exams roll around.

Late Assignment Policy

Late homework will be penalized 10 points per business day (Monday–Friday save holidays) for a maximum of five days. *Do not ask for extensions*; just hand in the homework late. After five days, **you can hand it in whenever you want** until *the last scheduled class meeting according to the official academic calendar*. As far as I know, this is one of the most lenient and flexible homework policies in college. I realize things come up. Do not abuse this policy; you will fall far, far behind.

L^AT_EX Homework Bonus Points

Part of good mathematics is its beautiful presentation. Thus, **there will be a 1–5 point bonus** added to your theory homework grade for typing up your homework using the L^AT_EX typesetting system based on the elegance of your presentation. The bonus is arbitrarily determined by me.

I recommend using overleaf to write up your homeworks (make sure you upload both the hw#.tex and the preamble.tex file). This has the advantage of (a) not having to install anything on your computer and thus not having to maintain your L^AT_EX installation (b) allowing easy collaboration with others (c) always having a backup of your work since it's always on the cloud. If you insist to have L^AT_EX running on your computer, you can download it for Windows here and for MAC here. For editing and producing PDF's, I recommend T_EXworks which can be downloaded here. Please use the L^AT_EX code provided on the course homepage for each homework assignment.

If you are handing in homework this way, read the comments in the code; there are two lines to comment out and you should replace my name with yours and write your section. The easiest way to use overleaf is to copy the raw text from hwxx.tex and preamble.tex into

¹In one student's observation, I give a "mind-blowing homework" every week.

two new overleaf tex files with the same name. If you are asked to make drawings, you can take a picture of your handwritten drawing and insert them as figures or leave space using the “\vspace” command and draw them in after printing or attach them stapled.

Since this is extra credit, do not ask me for help in setting up your computer with L^AT_EX in class or in office hours. Also, **never share your L^AT_EX code with other students** — it is cheating and if you are found I will take it seriously.

Homework Extra Credit

There will be many extra credit questions sprinkled throughout the homeworks. They will be worth a variable number of points arbitrarily assigned based on my perceived difficulty of the exercise. Very high homework scores are not unheard of. They are a good boost to your grade; I once had a student go from a B to an A- based on these bonuses.

Examinations

Examinations are solely based on homeworks (which are rooted in the lectures)! If you can do all the green and yellow problems on the homeworks, the exams should not present any challenge. I will *never* give you exam problems on concepts which you have not seen at home on one of the weekly homework assignments. There will be three exams and the schedule is below.

Exam Schedule

- Midterm examination I will be on [see course homepage] with the first review session on the class meeting prior
- Midterm examination II will be on [see course homepage] with a review on the class meeting prior.
- The final examination will be on [see course homepage] with a review on the final class meeting.

Exam Policies and Materials

I allow you to bring any calculator you wish but it cannot be your phone. The only other items allowed are pencil and eraser. I do not recommend using pen but it is allowed. **Food is not allowed** during exams **but beverages are allowed**.

I also allow “cheat sheets” on examinations. For midterm I, you are allowed to bring *one* 8.5” × 11” sheet of paper (front and back). **Two sheets single sided are not allowed**. Midterm II, you are allowed to bring *one* 8.5” × 11” cheat sheet. For the final, you are allowed to bring *three* 8.5” × 11” cheat sheets. **Six sheets single sided are not allowed**. On these sheet(s) of paper you can write anything you would like which you believe will help you on the exam. I will be handing back the cheat sheets so you can reuse your midterm cheat sheets for the final if you wish.

Cheating on Exams

If I catch you cheating, you can either take a zero on the exam, or you can roll the dice before the University Honor Council who may choose to suspend you.

Missing Exams

There are no make-up exams. If you miss the exam, you get a zero. If you are sick, I need documentation of your visit to a hospital or doctor. Expect me to call the doctor or hospital to verify the legitimacy of your note.

Accommodations for Students with Disabilities

Candidates with disabilities needing academic accommodation should: 1) register with and provide documentation to the Special Services Office, Frese Hall, Room 111; 2) bring a letter indicating the need for accommodation and what type. This should be done during the first week of class. For more information about services available to Queens College candidates, contact: Special Service Office; Frese Hall, Room 111; 718-997-5870 (Monday – Thursday 8:00 a.m. to 5:00 p.m. & Friday 8:00 a.m. to 4 p.m.).

Class Participation

This portion of your grade is assessed based on your level of interaction during the course lectures e.g. asking / answering questions. Participation on discord counts towards this total.

Grading and Grading Policy

Your course grade will be calculated based on the percentages as follows:

Homework	20%
Midterm Examination I	20%
Midterm Examination II	20%
Final Examination	35%
Class participation	5%

The semester is split into three periods :

- (a) From the beginning until midterm I. Midterm I covers material during this time.
- (b) From midterm I to midterm II. Midterm II covers material in this period only.
- (c) From midterm II until the final. The final is cumulative and covers all course material.

Each of the periods is assessed evenly. Thus, each period must count the same towards your grade. Since there is 75% of the grade allotted to exams, there is 25% allotted to each period. Thus, the final is upweighted towards the material covered in the third period. In summary,

the final will have 5/35 points $\approx 14\%$ for the first period's material, 5/35 points $\approx 14\%$ for the second period's material and 25/35 points $\approx 71\%$ for the last period's material. A good strategy for the final is to just study the material after Midterm II and minimal studying for the previous material.

The Grade Distribution

As this is a small and advanced class; thus, the class curve will be quite generous. Last year, it was approximately 40% A's and 40% B's. If you do your homework and demonstrate understanding on the exams, you should expect to be rewarded with an A or a B. C's are for those who can only demonstrate basic understanding. F's are rare, but occur.

Checking your grade and class standing

You can always check your grades in real-time using <https://qc.gradesly.com>. You will enter in your QC ID number (or CUNYfirst email address). I will provide you with your password by email the first week of class.

Auditing

Auditors are welcome. They are encouraged to do all course assignments. I will even grade them. Note that the university does not allow auditors to take examinations.