fo(d) = S fold (x) fold (d-x) I d-x & Supp[Y] dx

x & Supp[X]

-d = x x x & (d, 0) $= \int_{x \in (0,\infty)} e^{-x} e^{\frac{x-d}{4} \cdot (0,\infty)} dx = e^{d} \int_{x \in (0,\infty)} e^{-2x} \frac{1}{4} x \cdot (0,\infty) dx$ dzo => d= ldl, d<0 => d=- ldl-Laplace(0, 1) i.e. "standard Laplace" or "double-exponential" $X \sim \text{Laplace}(0, 1), Y = \mu + \sigma X \sim \text{Laplace}(\mu, \sigma) := \int_{\sqrt{0}} 0 = \frac{1}{Z_G} e^{-\frac{|y-A|}{G}}$ Laplace published this distribution in 1774 calling it the "first law of errors". Imagine you measure a quantity v but your measuring device has random error ϵ so $M=v+\epsilon$ where ϵ is a v. It makes sense that $E[\epsilon]=0=>E[M]=v$, further $Med[\epsilon]=0$ (i.e. 50% of the time $\epsilon>0$ and 50% of the time $\epsilon<0$) and $f(\epsilon)=f(-\epsilon)$. What distributions have these properties?

The problem with the above is small errors should be more likely than large errors. Thus, another consideration is $f'(\epsilon) < 0$ for $\epsilon > 0$ and $f'(\epsilon) > 0$ for $\epsilon < 0$. Thus, another consideration is $f'(\epsilon) < 0$ for $\epsilon > 0$ Then he reasoned if $f''(\epsilon) = f'(\epsilon) = > f(\epsilon) = ce^{-d|\epsilon|}$ when you solve this simple differential equation. Solving this for c,d to make it a valid PDF, you get c = 1/2, d = 1. (should be d = 1/2. This is only one

this simple differential equation. Solving this for c,d to make it a valid PDF, you get
$$c = 1/2$$
, $d = 1$. (should be $d = 1/2$. This is only one such valid solution). $c = d$ is full solution se
$$\frac{1}{2} \left(\sum_{i=1}^{k} x^{\frac{1}{k}} \right) = e^{-x} \int_{-\infty}^{\infty} x^{\frac{1}{k}} dx = e^{-x} \int_{-\infty}^{\infty} x^{$$

Weibull is a generalization of the exponential making a more

= | kx(xt) k-1 e-4 = 1/k t k-1 d4 $F(y) = \int_{t=0}^{t=y} k \lambda (\lambda t)^{k-1} e^{-(k \cdot \delta)^{k}} dt$ let u= (\lambdat)^k = \lambda^k t^k \Rightarrow \frac{du}{dt} = \lambda^k k t^{k-1} \Rightarrow dt = \frac{1}{\lambda^k k t^{k-1}} du, t = 0 \Rightarrow u = 0, t = y \Rightarrow 0 $= \left[-e^{-\kappa} \right]_{0}^{(\lambda y)^{K}} = \left[-e^{-(\lambda y)^{K}} \right] \Rightarrow S(y) = e^{-(\lambda y)^{K}}$

Let's consider the conditional probability $w = P(Y \ge y + c \mid Y \ge c), c > 0$ P(Y=y+L,Y=c) P(YZC) P(Y = y + c) k is called the "Weibull modulus". P(=20) $k = 1 \Rightarrow w = e^{\lambda(c - y + 9)} = e^{-\lambda y} = E \times \rho(\lambda)$ e-(1(4+0))k This is the "memorylessness property" of the exponential rv. The geometric also has this property due to the unc iid Bernoullis.

Order Statistics (p160). Let χ_1,\ldots,χ_n be continuous rv's then sort them from smallest to largest and denote them χ_0,\ldots,χ_n which are called the order statistics of the original set of rv's. X(1) = min & X, ,..., X, b $X(\kappa) = k^{+1}$ largest X(m) = MAX { X , ..., X , }

 $\mathbb{R}^{-1} = X_{(1)} - X_{(1)}$ which is called the "range" The goal is to find the distribution (PDF and CDF) of all order statistics given the distribution of the original collection.