

H_0 : Green Aliens (Null) do not exist
 H_a : Green aliens do exist

α low (skeptical)

α high (bullable)

H_0 : Green aliens does not exist

H_a : Green aliens don't exist

α low (dogmatic)

α high

* Uber fires drivers if more than 5% riders complain. After 1000 rides Uber makes a decision.

$H_0: P \leq 0.05$ Assume driver is good

(good)

retain driver

retention or rejection

$H_a: P > 0.05$

(bad)

Fire driver

before

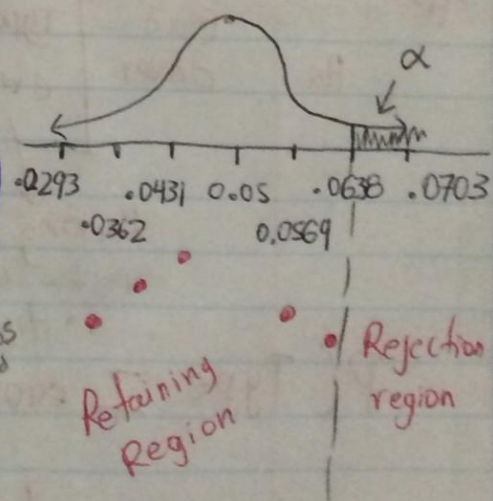
$H_0: p = 0.05$

$H_a: p \neq 0.05$

$$\hat{p} \sim N\left(0.05, \left(\sqrt{\frac{0.05 \times 0.95}{1000}}\right)^2\right)$$

$$= N(0.05, 0.00069^2)$$

$$\hat{p} \sim N(0.05, 0.00069^2)$$



$$\alpha = 5\%$$

$$\Rightarrow Z_{\alpha}$$

↑
Not $Z_{\frac{\alpha}{2}}$ cause not proportioning α to both sides

$Z_{2.5\%}$ is 2

5% for $Z_{\frac{\alpha}{2}}$
2.5% for Z_{α}

$$\text{Retaining region} = (-\infty, p + Z_{\alpha} \sqrt{\frac{p(1-p)}{n}}]$$

Percent to Z , Z to Percent.

$$= (-\infty, .0638]$$

$$\hat{p} = \frac{71}{1000} = 0.071 \notin \text{Retainment Region}$$

\Rightarrow Refer H_0

\Rightarrow Bad driver

\Rightarrow Fire

		Return H_0 Keep him (Reject H_0)	
True	H_0 Good driver	✓	Type I error
	H_a Bad driver	Type II error	✓

Firing a good driver
• Low cost

Keeping a bad driver
Cost - More complains -
• High cost

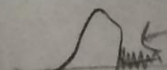
$$P(\text{Type I error}) = \alpha$$

* make α higher, Type II goes down
or * make n bigger

One-tailed

One-Proportion hypothesis Test

(Right Tail) when testing for $>$ than



One-tailed

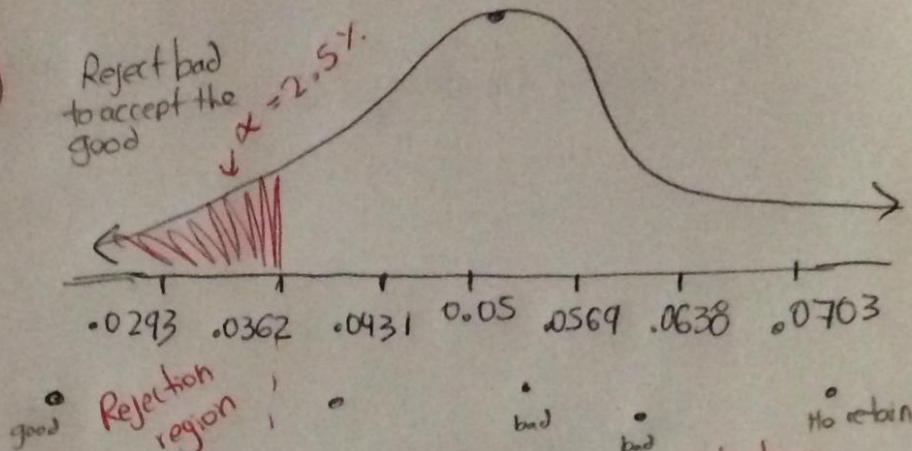
One-proportion Hypothesis Test (left tail)

Assume guy is bad, Prove you're good

$$H_0: p \geq 0.05 \quad (\text{bad})$$

$$H_a: p < 0.05 \quad (\text{good})$$

$$\alpha = 2.5\% \Rightarrow z_\alpha$$



$$\text{Retainment Region} = \left[p - z_\alpha \sqrt{\frac{p(1-p)}{n}}, \infty \right)$$

$$= [0.0362, \infty)$$

• at some point can't say he's bad anymore.

• Pick at certain point where I'm not comfortable anymore to say he's bad.

$$\hat{p} = \frac{71}{1000} = 0.071 \in \text{Retainment Region}$$

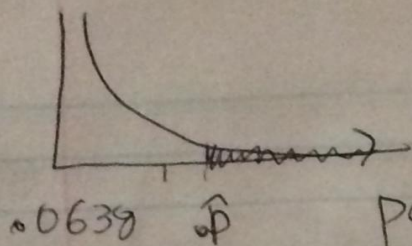
\Rightarrow No evidence to Support He's good

\Rightarrow Fire

		Decision	
		Retain	reject
True	H_0 Bad	Fire ✓	Keep Type I error \rightarrow Keeping a bad driver
	H_a Good	Type II error \rightarrow Firing a good driver	✓

$$P(\text{Type I driver}) = \alpha$$

Lowering α lower region



Prob of Seeing your data
or "more extreme" given the null hypothesis is true.

$$p_{\text{rob}} := P(\hat{p} > \hat{p} \mid H_0 \text{ is true})$$

$$= P(\hat{p} > .071 \mid p = .05)$$

$$= P\left(\frac{\hat{p} - .05}{.0069} > \frac{.071 - .05}{.0069}\right)$$

$$= P(Z > 3.04) = 0.0018$$

Significance level
0.1%

$< \alpha \Rightarrow \text{reject}$