Lec 23

Can you conclude "handling in a test ently & causes" a student to have cidifferent
Mean test slove" (statement 16)? NO.
You cannot conclude this, This conceptual
jump is not cationally justified, Byt is
it a good question? YES.

We indeed with to know company wonds to know if it's drug "company wonds to know if it's drug "company wonds to know if offering you a compon "causes a part, of sale to increase, the Federal Resprice wants to know if lowering interestrates "causes a part, of inflation to decrease, et e. Most scientific questions are worded this way. So we need a way to answer them.

Scenario 12. A factory has a betch of wire on a spool. They cut no short pieces and no long pieces. They are interested to proving that the electrical revistances

Yell, 11, 11, 11, 11, 11 independent of you I received

and they run a wald test, Lety say they resistances by w the short and long writes to different 2a)

But... can you conclude that.
"a different wire length "causes" a different
resistence " (statement 2b)?

Likely 25 is true. What's He difference b/W 16 and 26?

The distinguishing difference is the "treatment variable." (the categories)

difference between the two populations

which is full time ve cedical exam

time in scenario 1 and short vs long

leagth in Scenario 2) is "continuated"

(confused, obfuscaded, hidden) in

Scenario 1 but not scenario 2. The

cofond has is due to other variables being

different in the two population. In scenario 1...

Student IQ, amount of time studied, etc. These

cofounding variables inflyence both the cause

(treatment variable) and the effect (the response, the test score). If there is no confounding variable, the b statement is justified.

Some Vocabilary, In this class, we will consider treatment variables consisting of two categories (AKA two "arms") called the treatment (T) and the control (C). T is usually the situation whose effect on the phenomenon $\vec{y} = [y_1, ..., y_n]^T (AKA "response"; "end point" or "outcome") you wish to muestisate$ and C is usually the "business as usual case". In a clinical trial the T is usually the "pill" and the C is usually the "placebo" Let the treatment variable be denoted w= [w1,-, un] where w1=1 means the it subject got I and wi= 0 means the it subject got Confis the number of subjects that got T and ne is the number of subjects that got C and n=n+nc is the total simple size.

FYI: more than 2 arms or non categorical treatment variables are also important but

we j'ust don't have time ...

The Rubin Causal Model/Potential Outcomes
Framework: every subject is has a potential outcome for C, yo, i. Before the subject is "assigned" (given, allocated) to Tor C, both are observable. But after they are assigned only one is observable. Every subject has a unit-level causal treatment effect, yt, -yo, i which is not measureable since only one of the two quantities can be measured. This is called "The fundamental problem of causal inference."

How do we learn anything?

We make assumptions. Let's assume a constant, additive treatment effect theatur

YT, e = Yc, + 0

We reed an estimator. So first define YT as
the DGP that produces "YT, i's and YC as
the DGP that produced YC, is both one Postably
not Identically distributed but we will assume

onse;

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nd

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independence (look up SVTVA online for a related concept) I know that;

0= E[4] - E[4c] = 7+ - Vc

= - 2 YT: - - E & YC, i \$ i: W(2) } {c: V(2)}

Can't we use the "Plane estimate" aboute?

No. Why?

Just as we said before. The subjects in

T are not necessarily the "same" as subjects

"In C. There may be a confounding variable.

Assume one confounder and denote its

value for subject i as x; (e.s. let x; be the

number of hours studied in Scenario 1). Assume

the confounder is linear in the response:

Yce = BX: +e:

beta is scaling paramete (another unknown charactery but a nuisance parameter) and e: is a random component you don't understand (AKA "error" or "noise"). Patting these two

equations together we get: YT = O + Bx + e: Our naive estimate under these assumptions is: Tr-yi= + EBXi+ei to the EBXi+ei

{ist. Vi=1} oave? =(0+BX-[W]+E-[W])-(BX(W)+E,W) = 0+ \$ (x, -x)[v]-(e,-e)[v] If you assume the ei's are the result of a sum of a bunch of random stuff and Assumo there's no diffrence b/w the DGP is In the T and C groups, then the CLT says: 豆丁-豆心N(0, 5元(十十元))=ショマーモーモーマロ = B[Y- 70] = O+B(X--X0)[ii] Is this estimator browed? Yes! It's brosed by

7-7-7-0+B(x--xc)+(e,-ec)

for asstonment

In scenario I... or's the Gasual effect of handling in the exam early (negative).... but XT-XZ is the average study time in the band in exam early group Minus the average study time in the hand in-exam on-thre group and XT > XC they studied more! So it's positive! that more positive man or is negative. ET-EC is a missance and close to 0.

The reason the estimate is biased is due to "selection bias" which is bias in the wis. Students who studied more are more likely give themselves the T-assignment Chand in exam early).

How to fix it? You can we "linear regression to isolate and remove the effect of the confounder X or "matching" (we don't disting these). But it there's a confounder you didn't think of ... you're hosed.

To a most certainly get around this, You can't merely be an observer of the situation (Scenario 1 is called an 11 observational study"), you need to be able to assign T/E's (AKA manipulate) to the values war on Wn . Sometimes this is unethical. This ability to manipulate is called an "experimental study" ridied The gold standard to estimate casuality 15 He "randomized experiment" (Fisher, 1925) nutrance meaning wis ove ficked randomly. There are many ways to do this assignment ("experimental design") If T/C cores from s due a 50-50 coin Pipp Pt's called the more "Bernoulli trial" I nork on designs that hower the MSE of the estimator O. The design where n==n==1/2 and all 19/18/18/19 Such assignments are equally likely, P(W) = /(1)
is called the completely randomized design". You can Show: EN [EE [7- Po]]= @ an w's

this is the essential reason why we use randomized experiments. You're never doing more than one experiment, W/2 / ..., who so how is this any distroit?: 7- 70=0+B(XT-XC)[w]+(ET-E)[getting this really close to 0 185 what It work on Ragelner