

#### Past MATHCOUNTS Contest Questions

Note: MATHCOUNTS is a national middle-school contest; these are the MATHCOUNTS questions most appropriate for 4th and 5th grade students.

The questions are separated by the level of contest: school, then chapter, then state.

Feel free to skip questions, or raise your hand to ask for hints!

#### School-level Questions, 2024

Sprint 2	What is the tens digit of this sum? $+56,789$
-	Dora drinks a 12-ounce can of cola. Erika drinks half of a 20-ounce bottle of cola. unces of cola does Dora drink than Erika?
Sprint 4 one million?	What is the result when one hundred twenty-eight thousand is subtracted from
on Monday and 6	On Monday at 8 p.m., the temperature measured $-17$ degrees. Between 8 p.m. a.m. on Tuesday, the temperature increased 23 derees. On Tuesday, between 6 a.m. and rature decreased 5 degrees. What was the temperature on Tuesday at 3 p.m.?
<del>-</del>	The table shows all five lunch options on Friday at a middle school and the sthat ordered each. Based on this, what percent of the lunch orders on Friday were for

LUNCH	ORDERS
Pizza	132
Nuggets	112
Burger	88
Spaghetti	44
Salad	24

Sprint 9 \_\_\_\_\_ What is the 40th positive odd integer?

**Sprint 10** \_\_\_\_\_ What is the value of the expression  $1 + \frac{2}{1 - \frac{2}{3}}$ , in simplest form?

Sprint 12 \_\_\_\_\_ For each rock-paper-scissors match, paper beats rock, rock beats scissors, scissors beat paper and two identical items result in a tie. Based on this table, which summarizes the

results of Kalyani and Mark's last 200 matches, how many matches did Kalyani win?

		KALYANI		
		Rock	Paper	Scissors
×	Rock	30	24	20
MARK	Paper	26	21	21
Scissors		20	20	18

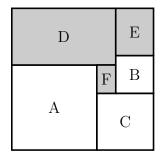
Sprint 14 \_\_\_\_\_ Maria was born on January 1, 2000. Her mother was born on January 1, 1975, and her father was born on January 1, 1970. In what year was the sum of their ages 100?

**Sprint 15** \_\_\_\_\_ A bicycle that originally cost \$200 is on sale for \$140. By what percent was the price reduced?

**Sprint 16** \_\_\_\_\_\_ Jay's dog outgrew his rectangular pen that measured 10 feet by 14 feet. To make it larger, he increased each side length by the same amount, which increased the pen's area by 81 square feet. What is the greater side length of the larger pen?

**Sprint 19** \_\_\_\_\_ Kendra surveyed 100 people who own a dog or a cat, or both. Of those surveyed, 15 own both a dog and a cat, and the number of people who own a dog is four times the number of people who own a cat. How many people surveyed own a cat?

Sprint 22 \_\_\_\_\_ The square labeled A has area 81 units<sup>2</sup>. The square labeled B has area 16 units<sup>2</sup>. The square labeled C has area 36 units<sup>2</sup>. These three squares along with the shaded, non-overlapping rectangles labeled D, E and F are arranged to form a large square as shown. What is the area of rectangle D?





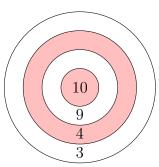
Sprint 26	If two standard, fair 6-sided dice are rolled, what is the probability that the
product of the two	numbers rolled is a perfect square? Express your answer as a common fraction.
Target 3	Penelope and George go trick-or-treating together. Penelope gets 152 pieces of
candy, and George	gets 124 pieces of candy. Penelope eats 5 pieces of candy every day, and George eats 4 $$
pieces of candy ever	ry day. After how many days will George have the same amount of candy as
Penelope?	
Target 7	Alan, Ben and Craig, who have three distinct ages, are among five children
running a race. Ass	suming there are no ties, in how many different orders can the five children finish the
race with Alan, Ber	n and Craig in order from oldest to youngest?
Team 2	How many ways are there to arrange the four integers 1, 2, 3 and 4 in a row so
that no two adjacer	nt numbers have a sum of 5?
Team 4	In the $5 \times 5$ grid shown, each row and each column is to contain the integers 1
through 5 exactly o	once with one integer per cell. The sum of the two integers in each (thickly) outlined
pair of cells is 5. W	That is the product of the integers in the four corner cells that are shaded?

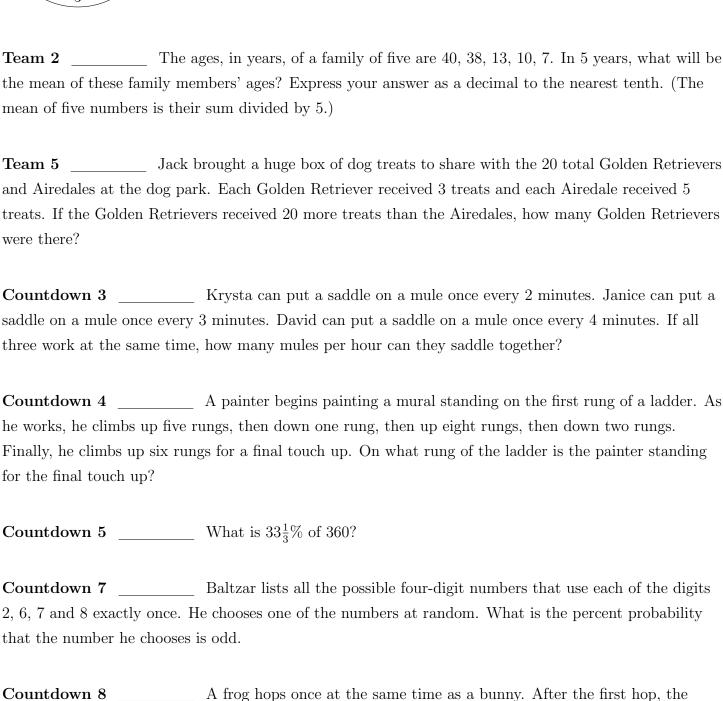
	2	
1		
		1
		3



### ${\bf Chapter-level~Questions,~2024}$

Sprint 5 _	What is the perimeter of a square whose area is 9cm <sup>2</sup> ?
Sprint 8 _	Vinnie is ordering a 2-topping pizza, and the table shows the three choices of
meat and fiv	ve choices of vegetable toppings offered. How many different combinations of one meat
topping and	one vegetable topping are there?
Meats	Vegetables
Pepperoni	Olives Spinach
Sausage	Onions Tomatoes
Bacon	Peppers
Sprint 10	Mr. Juarez can type 84 words per minute. How many words can Mr. Juarez
	inutes and 30 seconds?
v <b>-</b>	
Sprint 15	The area of a rectangle is 24cm <sup>2</sup> . If the length of the rectangle is 1.5 times its
	is the rectangle's perimeter?
Sprint 16	The product of two integers is 36. What is the greatest difference the two
numbers cou	
Target 1	There are 130 members of the Kelly family attending the family reunion cookou
	Each picnic table at the park seats eight people. What is the minimum number of picnic
_	ed when the entire family sits down to eat together?
Target 2	Yang arranges one $4\times4$ -inch square tile and five $2\times2$ -inch square tiles to form
_	uare. With no overlapping tiles and no space between adjacent tiles, what is the area of the
large square	?
Team 1 _	Four concentric circles form the dart board shown with regions worth 3, 4, 9 and
10 points. A	assuming every dart hits the board in one of these regions, what is the least number of darts
needed to so	core exactly 45 points?







bunny hops once every 5 seconds while the frog hops once every 8 seconds. How many seconds will pass before they hop at the same time again?

Countdown 12	What is the value of the product $0.75 \times 88$ ?
green olives. If the recipe v	A recipe for bacalao navideño calls for 1 kg of bacalao and one-half cup of were increased to use 2.5 kg of bacalao, how many cups of green olives would answer as a mixed number.
	For every egg laid by Mary the marine iguana, Seema the sea snake lays 6 eggs than Mary. How many eggs do they have all together?
	Fiona is 30 years old, and her daughter is one-third Fiona's age. In how aughter be half as old as Fiona?
	A dinner special consists of exactly one appetizer, one entree and one ppetizers, ten entrees, and three desserts from which to choose, how many there?
Countdown 21	An integer is 120 less than its cube. What is the value of this
monkey has one of four powent to the Make-a-Monke	At the Make-a-Monkey store, it costs \$29.99 to make a monkey. Each ssible types of fur, one of four accessories, and one of three sound effects. Bob by Store and decided to make one of every possible type of monkey. To the money did Bob spend at the Make-a-Monkey Store?
Countdown 34	How many diagonals does a regular octagon have?
Countdown 42inclusive (i.e., including bo	How many days are there from January 2, 2024 to December 25, 2024, oth those days)?



Countdown 50	What is the sum of the first 20 odd positive integers?		
the sum of the numbers	Dove rolls two fair, standard six-sided dice. What is the probability that she rolled is a prime number? Express your answer as a common fraction. (DMK: on type, "Somebody rolls two dice; what's the probability of?")		
gems consisting of three	How many different circular necklaces are there with six equally spaced identical red rubies and three identical blue sapphires? Two necklaces are the ed or flipped to create the other.		
the gumballs and found	Sylvie received a giant bag of 300 gumballs on her birthday. She sorted 120 were pink, 15 were white, 45 were blue, and 30 were green. The remaining at percent of the gumballs were red?		
of these three prime nur	The sum of three consecutive prime numbers is 59. What is the greatest nbers? (DMK: lots of questions involve prime numbers; it can be useful to up to 20 or 30, at least.)		
glasses. The first and se	There are three shelves in the kitchen cabinet. They hold a total of 40 cond shelves hold a total of 33 glasses. The second and third shelves hold a total of glasses does the second shelf hold?		
v	A bag contains 2 each of red, green, blue, yellow and white marbles. Fred les without replacement. What is the probability that Fred's two marbles are the ir answer as a common fraction.		
	Each of 10 tanks contains at least one fish. Each tank contains a different or two tanks that contain the same number of fish. What is the smallest total nks could contain?		
	The edges of a cube are tripled in length to produce a new, larger cube.  surface area of the larger cube to the surface area of the smaller cube?		



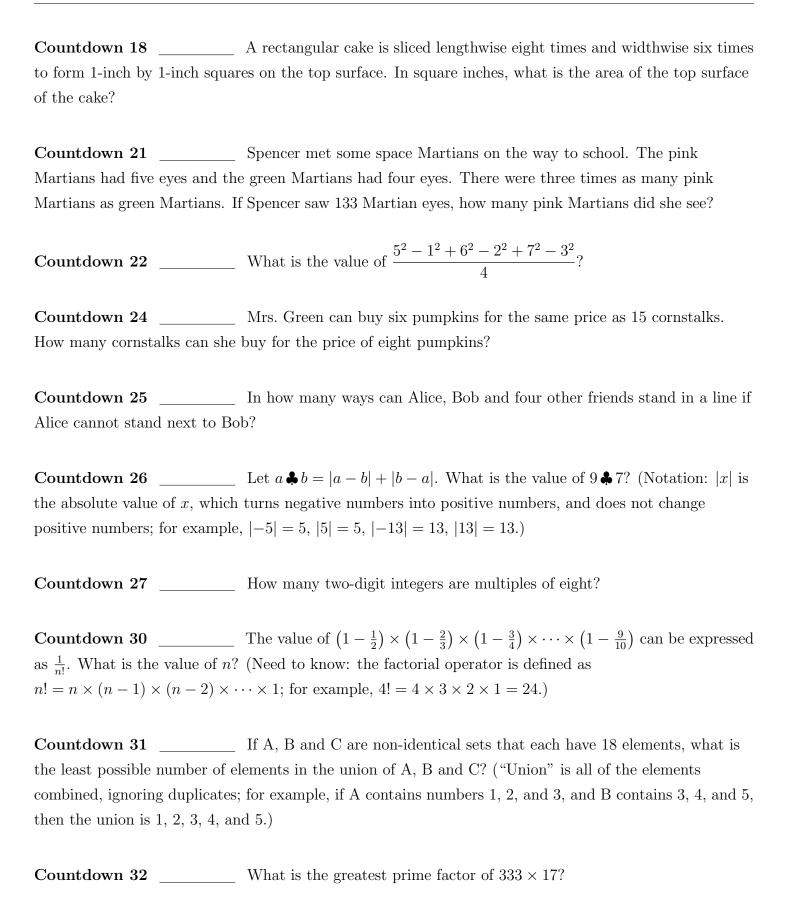
#### ${\bf State\text{-}level\ Questions,\ 2024}$

Sprint 1	If ten more than twice a number equals 48, what is that number?
Sprint 2	If 10 eggs cost \$0.75, how much will 32 eggs cost?
Sprint 3	The arithmetic mean of 3, $-4$ , 2, 0, 8 and $x$ is 2. What is the value of $x$ ?
Sprint 418. What is the value of	Suppose $y$ is a two-digit multiple of both 4 and 6. The product the digits of $y$ is of $y$ ?
word spelled correctly.	Emily spelled each word on a 20-word spelling test. She earned 5 points for each Three points were subtracted for each word spelled incorrectly. Emily earned a words did Emily spell incorrectly?
token is 25 grams, the	Carter has several tokens, each worth 25, 10 or 5 cents. The weight of a 25-cent weight of a 10-cent token is 10 grams, and the weight of a 5-cent token is 5 grams of all of Carter's tokens is 435 grams, what is the total value of his tokens?
and $3/4$ cup of sugar. I	A recipe calls for one 32-ounce jar of pickles, one packet of powdered drink mix, f the recipe amounts are increased proportionally so that 12 cups of sugar are sof pickles will be used?
integers is 5. What is t	The mean of three positive integers $a$ , $b$ , and $c$ is 10, and the median of these he greatest possible value for $c$ ? (Need to know: mean of three numbers is their an is the "middle" number, what's left after you remove the largest and smallest
	Robyn can travel from Lincoln to Omaha in 4 different ways and from Omaha erent ways. How many different round trips can Robyn make from Lincoln to Desigh Omaha in both directions?

	A glass jar holding identical cotton balls weighs 16 ounces. When the number of class jar is tripled, the total weight of the glass jar is 24 ounces. How many ounces s jar weigh?
people rode the bus	A group of 84 people attended the zoo field trip. For the trip to the zoo, 63 and the remaining people were in cars with 3 people in each car. On the return trip, d 4 people each, and the remaining people rode the bus. How many people rode the ip?
mushrooms popped Thursday, 135 new 1	On Monday, 5 mushrooms popped up in Sean's yard. On Tuesday, 15 new up, for a total of 20 mushrooms. On Wednesday, 45 new mushrooms popped up. On mushrooms popped up. If this pattern continues with the number of new mushrooms total, how many mushrooms will be in Sean's yard at the end of the day on
	Aditya writes down some of his favorite numbers. Every number on his list is a no two numbers on his list share any digits in common. What is the greatest possible Aditya's list?
for points. The only	_ In the exciting new game of Hyperfootball, two teams compete against each other ways to score points are by getting a touchdown, a smackdown or a shutdown worth respectively. What is the greatest integer score that a team cannot have during a all?
	If the ratio of the side lengths of two squares is 1:2, what is the ratio of the square to the larger square? Express your answer as a common fraction.
in boxes of 40. Prish	The You'll Walk All Over Us tile store sells 4-inch by 4-inch ceramic tiles na purchased the minimum number of 4-inch by 4-inch ceramic tiles needed to cover a How many boxes did she buy?
Countdown 4 old is Theo now?	Ten years from now, Theo will be twice as old as he was 4 years ago. How



Countdown 7	A convex polygon has an unknown number of sides. When all the diagonals
from a single vertex are	drawn, seven non-overlapping triangles are created. How many sides does the
polygon have?	
Countdown 9	The local cooking school offers five classes each Friday. Each class lasts 1
hour and 15 minutes. T	here is a 20-minute break between classes. If the first class begins at 8:00am, how
many minutes past noor	n is it when the final class finishes?
Countdown 10	Four pumpkins have an average weight of 15 pounds, and the average
weight of three of those	pumpkins is 13 pounds. How many pounds does the fourth pumpkin weigh?
(Remember: "average" of divided by 3.)	of four numbers is their sum divided by 4; average of three numbers is their sum
Countdown 11	There are two distinct (different) numbers twice as far from 15 as they are
from 75. What is the su	um of those two numbers?
Countdown 12	A triangular number is a positive integer that can be written in the form
$\frac{n(n+1)}{2}$ , where n is an int	seger. In 1796, Carl Friedrich Gauss proved that every positive integer is the sum
of at most three trianguto 40?	lar numbers. What is the greatest of the 3 distinct triangular numbers that sum
Countdown 13	For what value of x do the points $(x, x - 2)$ , $(x - 3, x)$ , and $(0, 0)$ lie on
the same line? Express	your answer as a common fraction.
Countdown 14	What is the positive value of x that satisfies $\sqrt{\sqrt{x} + 600} = 25$ ?
Countdown 16	Gabriel and his two brothers went to the aquarium and spent a total of
\$116. Gabriel spent \$9 a	more than Mario, and Ernesto spent \$4 less than Mario. How many dollars did
Ernesto spend?	
Countdown 17	Virginia rides her bike every day. She rides 12 miles every Monday, 5
miles every Tuesday, 15	miles every Saturday, and 6 miles every other day of the week. Given that May
1,2023 was a Monday, h	now many miles did Virginia ride in May of 2023?





Countdown 37	Randy is the youngest of four brothers whose ages are all distinct positive
integers. The average of years?	the four brothers' ages is 10 years. What is Randy's greatest possible age, in
Countdown 41	A restaurant sells Nepali momo dumplings in baskets of 5 or 8. What is
the greatest exact number	er of momos that <i>cannot</i> be purchased with whole baskets?
Countdown 43	The distance between the centers of two circles is 42 inches, and the
	circles is 27 inches. What is the sum of the lengths of the radii of the circles, in lural of "radius," half the diameter. Hint: draw a picture!)
Countdown 46 $x + y$ ?	The arithmetic mean of 10, 9, 3, $x$ and $y$ is 5. What is the value of
Countdown 47 the two numbers?	Two numbers have a sum of 36. What is the greatest possible product of
	Justin, Pierce and Eli are running a race. Justin runs twice as fast as Eli, nes as fast as Eli. If Justin finishes the race in 36 minutes, how many minutes
does it take Pierce to fini	·
Countdown 54	How many positive perfect squares have fewer than four digits?
Countdown 56	Fran builds a fence around her square-shaped backyard to keep her new
puppy safe. If the area of Fran will need to enclose	her backyard is 1024m <sup>2</sup> , what is the minimum length of fencing, in meters, that her backyard?
Countdown 60	What is the absolute difference between the mean and the median of the
prime numbers less than	20? Express your answer as a common fraction.
Countdown 61	If three carpenters can build three fences in three days, then how many
days doos it take one car	penter to build two fences?



Countdown 63	If n is a two-digit integer for which $n+1, \frac{n}{2}+1, \frac{n}{3}$ , and $\frac{n}{6}+1$ are all
perfect squares, what is	the value of $n$ ?
Countdown 66	If $f(x) = x + 3$ and $g(x) = 3x^2 - 2x + 7$ , what is the value of $g(f(5))$ ?
Countdown 71	A shop sells all teacups at one price and all saucers at another price.
Carson pays \$67 for three	ee teacups and two saucers. Daylon pays \$57 for a teacup and five saucers. How
many dollars will Eidan	pay for one teacup?
Countdown 72	Devlyn made a batch of between 50 and 70 cupcakes. When they are
packaged in groups of 3,	4 or 5 cupcakes, there is always one cupcake left over. How many cupcakes will
	ackaged in groups of 7 cupcakes?
Countdown 75	How many distinct arrangements are there of the letters in the word
ENGINEER?	