

R version 4.3.1 (2023-06-16 ucrt) -- "Beagle Scouts"  
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Platform: x86\_64-w64-mingw32/x64 (64-bit)

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[Previously saved workspace restored]

```
> rm(list = ls())
> x0 <- c(2.140561697,1.059497736,1.400870473,1.059315165,1.044773009,1.264290916,1.066033039,0.3
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> x1 <- c(2.018663981,1.999996941,1.744490887,1.667490165,1.400862504,2.025163446,1.899351552,0.7
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482830782,1.251884896,1.942640821,3.163062706,3.925678952)
> x <- c(x0,x1)
> y0 <- c(9.391811581,9.683842779,15.80590066,18.93927034,16.99352399,12.87795684,12.22992791,13.
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1.898468293,1.332823134,1.451257254,1.552825913,1.000296472,0.5940375,0.989730405,1.377803789)
> y1 <- c(0.803819766,0.395028741,0.452981303,0.561235148,0.936592234,1.367158686,1.017229473,0.5
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006368846,1.02010978,1.943973173,2.181809599,5.403819076)
> y <- c(y0,y1)
> cor.test(x, y,alternative = "two.sided", method = "spearman", exact=FALSE )
```

Spearman's rank correlation rho

```
data:  x and y
S = 9828234, p-value < 2.2e-16
alternative hypothesis: true rho is not equal to 0
sample estimates:
      rho
0.3901953

> # ---- Confidence interval ----
> if(!"RVAideMemoire" %in% installed.packages()){install.packages("RVAideMemoire")}
> library(RVAideMemoire)
*** Package RVAideMemoire v 0.9-83-3 ***
> spearman.ci(x,y)
```

Spearman's rank correlation

```
data:  x and y
1000 replicates

95 percent confidence interval:
 0.3036685 0.4648156
sample estimates:
      rho
0.3901953
```

>