

[illegible]

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,9,9,9,8,9,7,7,9,9,9,9,9,9,8,7,9,9,4,5,7,7,4,4,7,9,6,9,6,9,6,7,9,6,5,6,9,9,6,7,7,5,8,5,7,5,6,7,3,
4,6,7,9,5,6,6,9,7,9,4,6,7,5,4,7,6,3,4,6,5,5,8,9,8,7,8,8,7,7,6,5,5,8,6,5,4,9,8,4,5,3,8,9,9,5,4,9,3
,7,2,8,8,7,1,3,9,3,2,3,1,2,1,3,4,1,3,1,3,1,3,2,4,7,5,7,5,7,7,7,4,4,4,8,9,4,4,4,1,8,3,7,7,4,4,4,8,
1,5,6,7,5,8,5,5,8,9,5,3,7,8)
> z5 <- c(4,5,7,7,5,7,7,4,8,9,8,7,9,8,9,9,8,9,9,7,9,9,7,7,9,9,6,7,8,3,6,9,7,5,8,7,6,7,9,4,9,8,1,3
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9,7,5,6,9,7,4,5,7,6,3,5,9,7,3,9,9,6,6,8,9,6,8,8,9,8,7,8,9,7,9,8,4,4,6,4,4,4,8,4,3,9,7,4,7,5,9,7,8
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5,5,6,1,1,5,4,3,4,7,5,2,4,7,4,1,5,7,2,2,4,7,4,4,7,7,3,6,6,8,4,7,9,7,8,5,7,6,8,6,9,4,7,6,6,7,5,6,7
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2,3,7,7,4,5,6,4,4,4,4,3,3,5)
> z6 <- c(4,5,5,3,6,2,7,8,1,7,7,4,3,5,9,6,3,6,6,4,5,7,6,4,4,8,8,3,3,6,4,3,4,4,1,3,4,3,9,5,4,1,5,7
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,3,1,4,3,4,3,4,1,7,3,3,4,7,4,4,1,2,3,1,2,4,1,1,3,1,1,2,1,1,3,1,4,1,1,3,1,2,1,1,1,3,2,1,1,1,1,1,1,
3,4,4,1,3,4,5,2,3,6,4,4,9,8,4,5,7,9,4,8,8,9,9,9,9,5,6,9,8,5,5,9,9,5,8,9,4,6,8,8,7,6,9,8,6,5,9,8,6
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5,8,8,2,8,9,7,5,8,8,7,5,9,7)
> z7 <- c(8,7,8,9,5,9,7,8,6,9,9,8,7,9,8,5,7,9,6,7,5,8,9,5,5,9,9,7,5,8,8,3,5,6,5,3,7,6,3,6,8,6,1,5
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8,9,6,5,6,8,4,7,3,5,8,7,6,9,5,7,8,8,9,7,9,5,8,9,7,6,7,8,8,5,8,7,4,7,7,5,5,5,7,7,7,5,6,7,5,3,8,7,3
,5,7,7,4,7,6,4,3,7,9,4,7,3,5,6,3,5,8,7,3,9,7,5,4,7,9,7,8,8,9,8,8,9,8,8,9,6,9,7,5,8,9,9,6,9,8,
5,7,7,9,9,8,9,9,9,8,8,9,7,9,8,8,5,9,8,8,5,9,9,6,4,8,8,5,6,7,4,3,5,8,9,4,5,8,8,5,4,7,7,4,4,8,5,1,8
,7,9,5,6,1,1,8,6,5,6,6,4,4,6,8,5,5,4,7,5,5,5,5,1,3,5,5,3,4,4,4,4,4,5,3,1,1,3,4,5,5,4,3,4,2,6,6,4,
6,2,5,4,7,5,8,8,6,3,4,3,4,2)
> z8 <- c(2,1,4,5,4,4,4,8,4,9,6,4,8,8,8,5,9,9,7,6,9,9,8,9,9,8,9,9,7,9,8,9,9,9,9,8,8,6,7,8,6,4,4,4
,5,2,1,2,1,4,1,1,2,1,1,1,1,1,1,4,1,3,1,2,2,1,4,4,3,4,3,8,3,4,4,6,4,4,2,1,4,1,1,1,1,1,1,2,1,1,1,1,
4,1,3,1,1,1,1,1,1,1,1,1,1,1,1,3,1,5,1,2,3,4,1,3,6,2,4,7,8,5,4,8,9,5,9,8,9,9,9,9,5,7,9,8,5,6,9,8,6,8
,9,4,7,9,8,7,7,9,9,5,5,8,8,7,5,9,8,3,7,7,7,3,9,8,4,5,9,9,7,7,4,8,8,3,5,9,7,4,9,9,7,7,9,9,6,8,9,8,
8,8,8,9,8,8,8,8,9,8,9,7,5,7,5,7,8,3,8,9,8,5,8,8,8,7,9,8,8,8,8,9,8,9,8,8,7,9,8,8,8,9,9,5,8,9,5,6,7
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5,6,7,8,6,7,9,6,7,7,9,7,6,9)
> z9 <- c(8,7,8,9,7,8,9,8,6,8,9,5,4,6,9,4,6,4,6,7,7,7,9,5,7,9,8,9,7,9,6,8,9,7,6,8,9,7,5,8,8,4,7,7
,5,5,5,7,8,8,7,6,7,6,4,8,8,4,5,7,8,4,7,7,5,4,7,8,6,7,4,5,7,1,3,8,7,3,8,7,5,3,7,9,8,8,8,9,8,8,9,8,
9,8,8,9,6,9,7,6,8,9,9,6,9,8,5,8,8,9,9,8,9,9,9,9,8,9,8,9,8,9,5,9,8,7,4,9,9,6,4,8,8,5,7,9,4,4,6,9,9
,4,4,8,8,5,4,7,8,4,5,7,6,4,8,7,9,6,7,2,4,9,6,5,6,6,4,4,6,8,5,5,4,6,6,5,4,5,4,6,3,4,4,6,3,6,5,5,5,
3,1,1,4,4,4,4,4,3,4,2,7,7,4,6,5,6,8,8,5,3,5,7,3,3,3,5,9,3,6,5,4,5,3,3,3,2,4,1,3,3,5,5,5,4,5,4,9,6
,5,7,6,8,5,8,9,7,7,8,9,9,9,9,8,9,8,9,9,9,9,8,9,6,6,7,7,3,4,4,4,1,1,1,2,1,3,2,2,2,1,1,3,3,2,
6,4,1,3,1,4,1,1,2,3,3,5,1,1)
> z10 <- c(4,7,2,4,2,1,1,1,1,1,1,1,1,1,1,3,1,2,4,3,2,3,5,3,5,8,8,4,5,8,9,4,8,9,9,9,9,9,6,6,9,8,4,
5,9,9,5,8,9,5,5,9,9,8,7,9,9,7,6,9,7,6,4,9,8,3,8,8,8,2,9,8,4,5,9,9,7,8,4,8,8,3,5,9,7,3,9,9,8,5,9,9
,5,9,9,9,8,9,9,9,8,9,8,9,9,9,9,8,6,7,6,8,9,3,9,9,7,5,9,8,8,8,9,9,9,9,9,9,7,9,8,9,6,9,9,9,8,9,8,5,
8,9,5,6,6,8,9,5,5,9,9,6,6,9,9,3,6,7,7,2,9,7,3,6,8,5,3,5,7,6,9,4,4,1,2,3,3,3,4,4,5,5,4,4,4,6,6,7,3
,4,9,5,4,9,8,7,9,6,5,7,8,7,7,8,7,8,7,9,7,7,9,9,7,8,9,9,8,9,8,5,9,9,5,5,8,9,3,6,4,5,7,7,5,9,4,7,9,
7,9,7,9,6,9,9,8,6,9,9,8,4,8,8,4,6,8,5,4,6,8,6,4,7,9,6,5,6,6,3,8,7,3,4,8,6,4,7,7,4,3,6,9,5,7,4,5,7
,3,4,8,7,3,9,7,5,4,6,9,7,8,8)
> z11 <- c(9,8,8,9,9,8,8,9,9,5,9,7,5,9,9,9,5,9,9,6,8,8,9,9,8,8,9,9,9,9,8,9,8,8,4,9,8,8,4,9,9,7,
5,9,8,4,7,8,4,4,5,9,9,8,4,5,8,8,4,4,8,7,5,5,8,5,3,8,7,9,5,5,1,3,9,6,5,7,5,4,5,5,5,5,4,5,7,4,5,4,7,5
,4,6,4,6,1,7,5,8,5,7,5,4,5,5,6,6,2,2,2,1,1,2,1,1,2,3,5,3,3,4,5,4,3,2,4,9,4,4,5,4,4,5,5,5,5,5,7,4,
4,2,2,4,1,4,4,2,1,1,3,1,2,2,1,1,1,2,2,3,2,2,2,3,3,3,6,6,5,3,8,4,4,7,7,3,7,5,7,6,6,9,7,6,8,7,7,8,8
,9,8,8,8,9,9,8,9,3,8,9,5,4,9,8,6,8,5,8,5,7,9,5,9,9,8,6,8,8,6,7,7,8,4,5,9,8,4,6,9,6,6,7,7,3,7,9,6,
8,6,7,8,5,4,9,7,6,6,8,7,3,7,8,7,5,9,9,5,8,7,4,5,4,3,6,3,2,9,8,2,6,8,8,3,7,9,6,4,8,9,4,9,8,7,8,7,6
,9,9,8,7,8,7,6,8,6,5,9,9,5,8)
> z12 <- c(8,8,8,8,6,9,6,8,9,7,8,7,9,7,9,7,8,6,9,9,6,5,9,8,4,9,8,6,4,8,9,8,5,5,9,9,5,4,7,9,5,3,6,
7,3,5,6,5,4,7,4,3,5,8,1,3,1,4,1,1,3,2,3,8,5,2,3,7,5,4,5,6,5,7,1,4,5,4,3,5,7,4,6,4,8,5,6,7,6,8,8
,8,8,9,8,7,9,8,4,3,5,8,3,8,5,4,4,4,8,9,6,7,8,8,7,5,7,6,5,9,7,5,6,9,9,4,5,9,4,4,7,9,5,1,3,3,4,7,
5,3,5,7,4,1,9,5,1,3,5,5,2,5,7,4,4,6,9,9,5,8,5,5,4,4,1,5,4,7,5,5,5,7,3,6,8,5,4,5,9,4,7,5,5,6,6,4,7
,7,7,7,5,5,6,8,3,5,8,4,4,4,9,6,5,6,6,7,6,9,8,8,7,8,9,9,6,7,7,9,5,8,9,5,9,7,9,4,9,9,6,5,8,9,3,7,5,
7,3,5,5,9,4,4,6,7,7,5,7,6,1,3,4,3,3,6,5,2,3,4,1,2,5,4,3,1,4,1,1,3,1,3,3,3,1,1,2,2,1,1,1,6,4,5,8,4
,5,2,8,7,2,3,8,8)
> z <- c(z0,z1,z2,z3,z4,z5,z6,z7,z8,z9,z10,z11,z12)
>
> library(PResiduals)
> partial_Spearman(x | y ~ z)
      est      stderr      p lower CI  upper CI
partial Spearman 0.3469682 0.01600981 5.101425e-88  0.31521 0.3779503
Fisher Transform: TRUE
Confidence Interval: 95%
Number of Observations: 3894
>
```