THESIS TITLE

by

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Abstract

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In this memo, we seek to lay out a case for the use of absorber in an interferometric study of the spatial monopole of the 21cm reionization signature (i.e. the "global signal"). As discussed in previous memos, we believe that the way to optimize the sensitivity to the monopole term comes from the use of absorptive walls between the antennas to impose an artificially high "horizon", or temperature discontinuity, onto the beam of each antenna, thereby pushing the monopole into higher order spatial terms (Kundert 2016). With the new simulation, we are able to manipulate many parameters of our virtual interferometer, including but not limited to the antenna spacing, absorber wall height, and the attenuating properties of the absorber itself. From our exploration of these parameters, we are able to now state with certainty that we are able to detect the monopole term of the sky using a classical interferometer.

To DEDICATED PERSON

This is the dedication.

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Acknowledgments

These are the acknowledgements.

Chapter 1

Introduction

very quick overview of HYPERION and breakdown of what's in each chapter

Chapter 2

The Global Signal – Its Physics and Significance to Cosmology

2.1 Overview of the Epoch of Reionization

In brief, the Epoch of Reionization refers to the period of the universe's history during which its supply of intergalactic hydrogen became reionized. This is important to its evolution, and therefore of interest to astronomers, due to the driving factor of that ionization: the ignition of the first stars, galaxies, and black holes in the universe. A positive detection of the Epoch of Reionization will help astronomers to clarify many open questions of cosmology, such as the properties of the first galaxies, how stars with zero metallicity formed, the physics of early quasars, and more.

In slightly more detail, let us begin at the beginning. At the start of time, the universe was extremely hot and ionized from the Big Bang. Over time, as space itself expanded and the gas within the universe cooled adiabatically at a rate of $T(z) = (1+z)T_0$, the temperature of the universe dropped low enough that the nearly-uniform ionized plasma that made up the universe was able to recombine to form neutral hydrogen. This phase transition, which occurred approximately 380,000 years after the Big Bang at a redshift of $z = 1098$, enabled photons to decouple from the baryonic matter, thus allowing photons to stream freely for the first time in the history of the universe. These important periods of the universe's history are aptly referred to as "photon decoupling" and "the surface of last scattering". The surface of last scattering also marks the horizon of the observable universe, as everything beyond it is simply too opaque to be observable. The radiation released at the surface of last scattering, now referred to as the "Cosmic Microwave Background" (CMB), has a mean temperature of $T_0 = 2.725$ K (Fixsen 2009) and was first observed serendipitously by Arno Penzias and Robert Wilson in 1964 (Penzias & Wilson 1965).

At the point of the CMB, the gravitational force had heretofore always served as second fiddle to the electromagnetic force, and the formation of structure was driven solely by dark matter (Zaroubi 2012). As such, structure had yet to form, and the release of the CMB

led to a period known as the "Dark Ages" – a time when the universe had nothing to do but slowly get to work allowing slight matter over-densities, i.e. approximately 1 part in 10^5 more dense than the mean density of the universe according to COBE observations (Wright 1992), to grow and transform into stars, galaxies, and black holes.

About 100 million years passed and the universe bathed in nothing but the after-glow of the Big Bang. Finally, the first galaxies formed, and along with them bright stars to emit ionizing radiation. Soon, we find small ionized bubbles in the intergalactic medium (IGM), the hydrogen gas filling the space between galaxies. Over time, more galaxies and their bright stars make more ionized bubbles, until eventually the entire universe's supply of loose hydrogen gas has been converted into a proton-electron ionized plasma.

This period, very creatively, is called the Epoch of Reionization – the epoch during which the universe once again became ionized, like it was at the dawn of time.

As of yet, there has been no confirmed[1] direct detection of this time period – either of the objects that drive it nor of the gas behavior itself. This is not for lack of trying. There are currently (or soon to be) observatories looking for high-redshift galaxies and quasars (Gardner 2006), for power-spectrum measurements to find ionized regions around those high-energy objects (DeBoer 2017), and for the microscopic temperature changes in the gas of the universe (Bowman & Rogers 2010). As it turns out, these observations are hard to make – 13 billion light years is a long way for light to travel.

For the sake of brevity and intellectual focus, this thesis (and the experiment proposed within) will be focusing solely on observing the overall average behavior of the intergalactic medium as it evolves throughout this time period. This is referred to as the "global signal".

2.2 Overview of the Global Signal

The global signal of reionization is an observation of the overall average nature of hydrogen throughout this epoch, i.e. the spatially averaged signal from the neutral hydrogen gas, as observed using redshifted 21 cm emission from the intergalactic medium 13 billion years ago. More specifically, global signal experiments seek to observe the relationship between the internal level populations of the neutral hydrogen IGM and the ambient temperature of the universe, as set by the CMB photons. This relationship is written quantitatively in Eq. (2.1).

$$\delta T_b = (T_s - T_\gamma)(1 - e^{-\tau}) \tag{2.1}$$

where δT_b is the observed fluctuation in the 21 cm brightness temperature of the 21 cm line (T_s) relative to the background CMB brightness temperature (T_γ), and τ is the optical depth of the hydrogen through which the CMB is passing.

[1] While there has yet to be a confirmed direct detection of the Epoch of Reionization, the EDGES experiment has announced a possible detection of the 21 cm reionization global signal (Bowman et al. 2018).

Figure 2.1: In the top half of the figure, we see a cartoon of the reionization history of the universe and the development and growth of ionized bubbles over time. In the bottom half, we see a breakdown of T_b, the brightness temperature of the 21 cm global signal, over time. There are five labeled regimes to this plot, each corresponding to the dominance of a different variable in the production of the 21 cm signal. Figure originally published in Pritchard & Loeb 2012.

By observing the evolution of the spin temperature relative to the CMB background temperature, we are able to better understand how and when energy was injected into the gas (Pritchard & Loeb 2010). For example, the X-rays generated by black holes contributed to the heating of the gas, making the gas itself brighter than the ambient photons. Additionally, Lyman-α photons from Population II and III stars modify the coupling of the IGM gas temperature to the 21 cm spin temperature via the Wouthuysen-Field effect, providing a means to track early star formation (Furlanetto et al. 2006).

However, while it's fairly straightforward to observe the 21 cm signal and acquire a measurement of the spin temperature through time, that alone doesn't give us much insight into the driving physics of that signal. First, we must understand what factors contribute to the spin temperature of the gas.

Brief History of the Global Signal

The most important observable quantity of the global signal, and the one that informs us as to the underlying astrophysics at each redshift, is the spin temperature T_s, which can be described as a weighted average of of the ambient CMB photon temperature T_γ, the kinetic temperature of the intergalactic medium T_K, the collisional excitation ratio x_c, and

the Lyman-α excitation ratio x_α, as shown in Eq. (2.2).

$$T_s^{-1} = \frac{T_\gamma^{-1} + (x_c + x_\alpha)T_K^{-1}}{1 + x_c + x_\alpha} \tag{2.2}$$

The collisional and Lyman-α excitation ratios define the fraction of transitions that are being driven by ambient CMB radiation vs. by other physical processes (such as collisions or absorption of high energy Lyman-α photons),

$$x_n = \frac{N_{10}}{A_{10}} \frac{T_*}{T_\gamma} \tag{2.3}$$

where here N_{10} is the excitation rate coefficient of the physical process in question (i.e. the rate at which that particular physical process is driving transitions).

Based on these variables, we can define six main physical regimes believed to have taken place during the process of structure formation and IGM reionization, which can be seen in Fig. 2.1 and are physically detailed below.

- ($200 \leq z \leq 1100$): During this time period, the residual free electron fraction remaining post-recombination and the high gas density allows the thermal and spin temperatures of the gas to remain coupled with the photon background via Compton scatting and collisional excitations. All temperatures are the same, and therefore there will be no detectable 21 cm signal.

- ($40 \leq z \leq 200$): As cosmological expansion continues, Compton scattering no longer couples the thermal temperature of the gas to the CMB photons, and the gas and radiation decouple and go out of equilibrium. Collisional coupling sets the spin temperature $T_S < T_\gamma$, leading to an absorption feature in the 21 cm global signal.

- ($30 \leq z \leq 40$): Expansion continues and collisional interactions are no longer effective at coupling the thermal and spin temperatures of the gas. The excitation levels shift to being set by radiative coupling to the CMB, such that $T_S = T_\gamma$, and there is no detectable 21 cm signal.

- ($15 \leq z \leq 30$): As the first sources (e.g. stars, active galactic nuclei (AGN), etc...) ignite, they begin emitting high energy Lyman-α and X-ray photons. The hyperfine populations couple to the thermal temperature of the cold gas via the Wouthuysen-Field effect, such that $T_S \sim T_K < T_\gamma$, resulting in an absorption feature in the 21 cm global signal.

- ($7 \leq z \leq 15$): The radiation (particularly the X-rays) from bright sources heat the gas, $T_K > T_\gamma$ and we see 21 cm emission in the global signal. Lyman-α coupling is still effective at setting the level populations.

- ($z \leq 7$): Enough ionizing radiation has spread throughout the universe that the IGM has been converted from neutral to ionized, and reionization is complete.

At present, all redshift ranges listed are theoretical, as no confirmed detections have yet been made. However, it is abundantly clear that detection and study of this era of this part of the universe's history is rich with information about our cosmological origins, and could fill many of the gaps in our current knowledge.

Chapter 3

Interferometry

3.1 Brief Overview

Let's start with what they are. An interferometer is any device which superimposes the waves from a coherent light source in order to gain information about the source itself. So what does that mean? Let's look at the most basic case of a Michelson interferometer. In this scenario, we have a coherent light source (typically a laser) pointing at a beam splitter. The splitter splits the light into two identical beams, which travel on separate paths, until they are recombined before entering a detector. The difference in the paths creates a phase difference between the beams. This phase difference is what creates an interference pattern, which is what then gives us the information we seek about the light source, which typically comes in the form of fringes.

What if instead of using mirrors and beam splitters, we built two identical small telescopes that were physically separated in space, then pointed them at the same astronomical source. Because they're not in the same spot but are separated by a "baseline", there must be a difference in the path lengths between the telescopes and the source. This is the fundamental idea behind radio interferometers. Now let's explore the mathematics.

In order to get a handle on the mathematics and theory behind astronomical interferometry, we're going to make some simplifying assumptions. We will consider the case of a two-element interferometer (that is, an interferometer with two antennas and one "baseline" between them) observing a very distant source (so the emissions from the source will come in the form of plane waves and the antennas will point in the same direction on the sky). This interferometer will be fixed in space - so, no rotation or motion of the antennas themselves. We will also be looking at just one frequency, so the signals coming in will be perfectly sinusoidal with one known wavelength. We won't be worrying about anything in the backend, so we'll say that we have no frequency conversions (an RF interferometer) with a single polarization and perfectly idealized electronics (perfectly linear, no amplitude or phase distortions, perfectly identical for both instruments, and no added noise). We'll also assume no propagation distortions, so the plane waves we observe from the source won't be

disturbed by the ionosphere or atmosphere of Earth, and that the source is small enough in angular size that we can approximate the sky as flat and two-dimensional.

What does that leave us? Two identical sensors that are separated by a vector distance $\mathbf{b}$ - this is our baseline. These sensors are both pointed at a quasi-monochromatic source of frequency ν, in the vector direction $\mathbf{s}$. Combining these fundamental numbers, we then get the key quantity $\tau_g = \mathbf{b} \cdot \mathbf{s}/c$, which is the geometric time delay. That's the extra time needed for the signal to reach the more distant antenna. This number will be important to us in order to correlate our signals. We can also find the phase shift in the signal by writing $\Theta = \omega\tau_g = 2\pi\mathbf{b} \cdot \mathbf{s}/\lambda$.

With this knowledge of the phase difference between the paths, we can write out the voltages received by each of the sensors, so we get $V_1 = E\cos[\omega(t - \tau_g)]$, because it has that extra phase delay from the baseline separation, and $V_2 = \cos(\omega t)$. In this case, the path lengths from the sensor to the multiplier are treated as being equal, so we don't need to add any extra phase terms. We then multiply our signals together, and take an average over time, which gives us an averaged product $R_C = P\cos(\omega\tau_g)$. This quantity is dependent on the received power $P = E^2/2$ and the geometric delay τ_g, and hence on the baseline orientation and source direction. We can rewrite R_C to make this relationship more explicit as:

$$R_C = P\cos(2\pi\frac{\mathbf{b} \cdot \mathbf{s}}{\lambda}) \tag{3.1}$$

Note that R_C is not a function of the time of the observation (so long as the source itself is not transient or variable), the physical location of the baseline (provided that the source is in the far field, which is always true of astronomical sources), or the actual phase of the incoming signals. All that matters is the relative phase between the sensors!

In order to get a better understanding of our observed response, let's rewrite some terms. Let us say that $\mathbf{b} \cdot \mathbf{s}/\lambda = u\cos\alpha = u\sin\theta = ul$. In this case, we are defining

$$u \equiv b/\lambda \tag{3.2}$$

which is the baseline length in units of wavelengths, and θ is the angle relative to the zenith. $l = \cos\alpha = \sin\theta$ is the direction cosine. We can then rewrite our response function as $R_C = P\cos(2\pi ul)$. We can now see quite easily that the longer the baseline, the more rapid the frequency of the response function R_C. This is what radio astronomers call "fringes".

We can also begin to see why we want to have many sets of antennas - each baseline will only give us information about one set of fringes. In order to reconstruct a full image of an extended source, we need to be able to observe more than one spatial frequency. The response from an extended source is obtained by summing the responses at each antenna to all emission over the sky, multiplying the two for each pair of antennas, and averaging. Assuming that the source itself is spatially incoherent (e.g. that the emission from one side of the galaxy isn't related to the emission from the other side), the averaging and integrals can be interchanged, giving us

$$R_C = \iint I(\mathbf{s}) \cos(2\pi\nu \mathbf{b} \cdot \mathbf{s}/c) d\Omega \tag{3.3}$$

We can now see the relationship between what we are measuring to what we want to observe - we have linked the source brightness $I_\nu(\mathbf{s})$ to the even interferometer response R_C. To complete the image of the sky, we can observe the odd interferometer response R_S, which is the sinusoidal equivalent of R_C, by slipping in a 90° phase offset along one of the signal paths.

Now we can define a complex function $V = R_C - iR_S = Ae^{-i\phi}$ as our complex visibility from the two independent, real correlator outputs R_C and R_S, where $A = \sqrt{R_C^2 + R_S^2}$ and $\phi = \tan^{-1}(R_S/R_C)$.

We can now rewrite the complex visibility as an integral, giving us:

$$V(\mathbf{b}) = R_C - iR_S = \iint I(\mathbf{s}) e^{-2\pi i \nu \mathbf{b} \cdot \mathbf{s}/c} \, d\Omega \tag{3.4}$$

This is easily recognized as the 2D Fourier transform, when the right geometry is utilized. As it turns out, the earlier definitions of u and l are very convenient coordinates to use, and can be expanded to two dimensions to give us the (u, v) visibility plane and the (l, m) source plane[1].

Additionally, so far we have avoided mentioning any frequency dependence in this relationship or any intrinsic instrumental effects. The fact of the matter is that every astronomical array will have a frequency dependence, either from the response of the instrument itself or from the changing physics of the visible celestial sky (or, more likely, both). Therefore we must in fact calculate visibilities for all the frequencies within our science band (i.e. for each channel, meaning that there will be a level of imprecision and integration of each visibility across a known $\delta\nu$ of frequency space in the science band).

Moreover, we must also account for the fact that no antenna has perfect reception to the entire sky – rather, each antenna has some spatial sensitivity related to its own shape. This shape is often referred to as the "beam" or the "primary beam" of the antenna, and we shall denote it as $A(l, m)$.

Eq. (3.4) can now be rewritten with these coordinates like so:

$$V_\nu(u, v) = \iint I'_\nu(l, m) e^{-2\pi i(ul + vm)} \, dl \, dm \tag{3.5}$$

where $I'_\nu(l, m) = I_\nu(l, m) A_\nu(l, m)$. This is the van Cittert-Zernike theorem, a fundamental equation for interferometry, which relates the brightness of the distant source to the mutual coherence function (or visibility) via the 2D Fourier transform in a convenient set of coordinates for radio astronomy.

[1] In actuality, we don't use the uv-plane, but rather calculate from baselines $\mathbf{b}$ and source direction $\mathbf{s}$ directly, so as to avoid any complications or imprecision due to usage of the flat-sky approximation. See Appendix A for more information on the uv-plane and when it is an appropriate coordinate system to use.

3.2 Spatial Modes and Interferometric Sensitivities

As mentioned above in Section 3.1, interferometry gives you sensitivity to different spatially varying modes based on the physical separation of the antennas or telescope reflecting dishes making the observation. The bigger the separation, the faster the spatial variation observed on the sky, and therefore the higher resolution/smaller the object that can be observed.

It is through this knowledge that we are able to construct instruments that are specifically tuned to different spatial scales. For example, astronomers (and the general public) are fascinated by black holes and want to observe their inner workings. Black holes are very compact objects in the sky, so to be able to resolve them takes incredibly high resolution observations. Under the Rayleigh criterion (Eq. 3.6), radio astronomers can achieve fine resolution (i.e. small θ) by using high frequencies (i.e. small λ, of the order of less than a millimeter) and very large baselines (i.e. large B, on the order of thousands of kilometers).

$$\theta = \lambda / B \tag{3.6}$$

Alternately, if one wanted to observe fluffy galactic clouds or other extended structures, they would instead prefer to construct an interferometer using closely packed antennas and lower frequencies.

By constructing an array using a combination of differing baselines, one can fill in the sampling of the uv-plane. With complete sampling of the uv- plane, one can perform a simple 2D Fourier transform and perfectly recreate the image plane. This relationship between spatial frequency and images, or visibility and brightness, is known as the *spatial Fourier transform*, and is the backbone of all radio interferometry, from the reconstruction of cosmological power spectra all the way to the sophisticated synthesis imaging techniques described above.

In reality, of course, it is impossible to completely sample the uv-plane and recover a perfect image. We must therefore design our instruments to be maximally effective at the observations we wish for them to make. In the cases of general purpose instruments like the Very Large Array (VLA), that means designing the instrument to be very flexible – covering a broad range of frequencies, minimizing redundancy in the baselines, and using different array configurations to better sample different regions of the uv-plane.

However, for smaller scale instruments, astronomers generally wish to build something which is very specifically tailored for the observation they want to be making, leading to creative and highly unique array configurations that make use of the spatial Fourier transform to the best of their ability.

Spatial Fourier Transforms

Much as we can think of the relationship between time and frequency as a Fourier pair, we can also relate the physical separation of the antennas (i.e. the "geometric time delay" τ_g) and the spatial frequency.

Consider the variable u, which is defined as the baseline separation of two antennas measured in wavelengths in Eq. (3.2). Based on Eq. (3.1), we also know that $R_C \approx \cos(2\pi ul)$, meaning that the number of whole fringes imposed across the sky for any given separation will be $N_f = 2u$.

This in turn means that a pair of antennas separated by u wavelengths will be most sensitive to objects with an angular scale of about $\theta = 1/u$, according to Eq. (3.6).

One can relate this to the idea of spherical harmonics, with the harmonics providing us the (l, m) coordinates of our observed brightness, providing us some context for the second member of our spatial Fourier pair. We can thus start visualizing the physical meaning of "spatial variance" and "spatial frequencies".

We can do so by rewriting our interferometric visibility in terms of spherical harmonics. Let's begin by rewriting our visibility equation into the form seen in Eq. (3.4), now factoring in the primary beam and integrating over the full celestial sphere.

$$V(\nu) = \int I(\mathbf{s})A(\mathbf{s})e^{-2\pi i\nu \mathbf{b}\cdot\mathbf{s}/c}\, d\mathbf{s} \tag{3.7}$$

where $I(\mathbf{s})$ is the sky brightness, $A(\mathbf{s})$ is the primary beam of the antenna, and the exponential term is the interferometric "fringe". Now, much in the way that any signal can be decomposed into an infinite series of Fourier frequencies and amplitudes, we can rewrite the terms of Eq. (3.7) to be expressed as a sum of spherical harmonics.

$$I(\mathbf{s}) = \sum_{l,m} I_{lm} Y_l^m(\mathbf{s}) \tag{3.8}$$

and therefore the visibility equation becomes:

$$V(\nu) = \int \Big(\sum_{l,m} I_{lm} Y_l^m(\mathbf{s})\Big) A(\mathbf{s})e^{-2\pi i\nu \mathbf{b}\cdot\mathbf{s}/c}\, d\mathbf{s} \tag{3.9}$$

So now the question is simply: does the integral of the zeroth mode (i.e. the global signal) vanish or not. This term can be written as:

$$V_0(\nu) \equiv I_{00}(\nu) \int Y_0^0(\mathbf{s})A(\mathbf{s})e^{-2\pi i\nu \mathbf{b}\cdot\mathbf{s}/c}\, d\mathbf{s} \tag{3.10}$$

We know that $Y_0^0 = \sqrt{1/4\pi}$, so the remaining question of interest basically boils down to whether or not the beam can break the inherent symmetry of the fringe term, leaving us with a non-zero $V_0(\nu)$.

Figure 3.1: Above, we see a collection of the low-order spherical harmonic functions. This can help us begin to visualize what, physically, the spherical harmonics are and how they can be used to parse spatial information observed on the sky from an interferometer.

3.3 Observing the Spatial Monopole with an Interferometer

At this point, it is a fair enough question to ask how exactly we intend to use an interferometer to observe a spatially invariant signal. Everything we have stated above indicates that interferometers see *changing* signals – they observe the spatial variance that they are sensitive to based upon the separation of the antennas and the frequency they are observing at. They are inherently AC circuits. The one thing they are explicitly not meant to do is to observe what is effectively a DC tone.

So how exactly is this supposed to work?

Well, it turns out there's a couple of things in our favor here. The first thing, as addressed in Presley et al. (2015), is that we're on earth and can't actually see a monopole from the sky – the horizon gets in the way. Furthermore, the antenna itself has a directionally dependent beam, introducing an additional layer of spatial variance. Therefore, what in reality is a monopole signal from the entire universe is instead observed with a spatial cut-off – it's a top-hat. Or, more accurately (with the addition of the primary beam A), it's a bowler hat. And, most importantly for our goals, a top-hat signal doesn't necessarily integrate to zero and therefore may be observable with an interferometer (Venumadhav et al. 2016).

That being said, a top-hat signal that spatially broad still isn't easily observable with an interferometer. From our knowledge of Fourier transformed, we know that a broad spatial cut-off translates into a narrow spread of powers in the visibility domain – i.e. most of the monopole power will remain in very broad, long and low spatial modes. If we want to truly convert the monopole into a signal that we can get at with an interferometer, we're going to have to constrict the scale of our spatial top hat.

What we need to do is artificially push our monopole term into higher modes – modes that we are in control of. Or, in Fourier terminology, we need to apply a top-hat function to our monopole signal.

In doing so, we will generate a visibility sensitivity in the shape of a sinc function – meaning we will have sensitivity to our monopole term in many Fourier modes, rather than just in the $(0, 0)$ or $(0, 1)$ modes. If we control the shape of the top hat imposed, then we know the shape of the sinc function, meaning we can calibrate exactly what our monopole sensitivity should be at any given point in the uv-plane.

So now the question is simply how can we raise the horizon that our antennas see? One option would be to literally raise the horizon – either find or manufacture a deep valley for them to reside within. This would probably be challenging to do well – digging a valley for the whole array would undoubtedly be expensive, and it'd be very hard to find a naturally occurring, rotationally symmetric valley (particularly one deep enough to actually meaningfully raise the horizon of our antennas).

So we must find a way to artificially raise the horizon of our antennas. Moreso, as described in Venumadhav et al. (2016), we must either allow our antennas to freely cross-talk (thereby eliminating the vast majority of benefits gained from using an interferometric

Figure 3.2: This figure shows the Fourier relationship between the two-dimensional top hat function and a Bessel function. This image can be thought of as an idealized cartoon of the aperture and visibility planes of our proposed interferometer. On the left, we see the imposed top-hat, where the yellow portion would be the portion of monopole sky visible to the antenna and the blue would be the perfect absorber. On the right, we have performed a two-dimensional Fourier transform to convert into the visibility plane (i.e. to see the spatial modes to which we are observationally sensitive), and we see this rippling function centered around the zero-spacing mode.

setup) or we must introduce a source of noise from lossy components (e.g. the ground or other signal absorbers, rather than reflectors or transmitters) in order to maintain a sensitivity to the global signal. As described in Section 3.1, the more closely spaced your elements, the larger the spatial scales on the sky your instrument will be sensitive to. We therefore know that we are going to be using a very closely packed array, which will make our system very prone to cross-talk. If we want to avoid that, then we'll have to find some way to ensure that the antennas don't see each other in addition to seeing less of the sky.

All of which leads us to the construction of thin absorptive walls between the antennas – introducing a new horizon in how the antenna sees the sky and maintaining the independence of each antenna's signal from its very nearby neighbors. In order to maximize our sensitivity to the global signal, we will want the absorbers used to be highly efficient at dissipating energy across our frequency spectrum (Venumadhav et al. 2016). This will provide us will a strong "edge" in how our antennas see the sky, in turn creating maximal Fourier leakage into higher modes and best enabling us to make a successful observation of the reionization monopole signal.

Chapter 4

Overview of the Theory of HYPERION

4.1 Absorber – A New Approach to Monopole Interferometry

If you were to wander onto almost any given radio telescope currently active in taking observations, you're almost certain to find some kind of reflective material underneath the antennas (either in the form of a ground screen or a reflective dish). One thing you're not likely to find is any kind of absorptive material – we as astronomers are already fighting an uphill battle on attaining the very fine sensitivities needed to detect celestial sources, we really need all the photons we can get.

However, it is not unheard of. While absorbers have never been used in the element design of a reionization project to date, they have been used by cosmic microwave background (CMB) experiments. Absorptive structures, or baffles, to control pickup from outside the main beam, which can be a source of systemic errors Essinger-Hileman et al. (2016). By surrounding the receiver with an absorptive material, rather an a reflective one as seen in most standard radio telescope designs, one can better control the exact signal that will be seen in the sidelobes of the beam, and thereby better calibrate the system in turn.

This same principle applies in the case of a monopole interferometer, where use of an absorber can not only be beneficial but actually fundamental to the design of the array despite the microscopic signal we aim to detect. By controlling what each antenna sees on the sky, we can accurately calibrate our system and ensure that our reionization signal is indeed signal and not instrumental noise.

Practical Instrumentation

As discussed in Chapter 3, one of the fundamental requirements of a monopole interferometer is close spacing of the antennas, in order to maximize reception of the global sky mode.

However, this close spacing also predisposes the instrument to cross-talk. As discussed in Venumadhav et al. (2016), this isn't necessarily a bad thing – cross-talk is one of two ways that an array of antennas can maintain a sensitivity to the monopole. Each individual antenna will broadcast its reception of the monopole to its neighbors, and that reception will correlate. In this case, one will have a direct view of the monopole term, as you will be correlating the zero-spacing mode seen by one antenna with the zero-spacing mode of another, thus providing the necessary sensitivity to the global signal.

However, that also means that instrumental noise will be broadcast and correlated between antennas, vastly diminishing the useful properties of the interferometer and maintaining many of the pitfalls of single-dish instruments. The risk here comes in the calculus of calibration for the instrument. In particular, it is difficult to properly calibrate the correlated noise between elements as it has a noise bias. This bias means that, while we observe more of the true signal, we also no longer are able to integrate down the instrumental noise, essentially placing a DC offset into our system. The exact value of this offset is a function of frequency and of the exact qualities of the instrument, and will likely vary from element to element. If it is not perfectly calibrated and subtracted off from the data, then traces of this bias will remain in the final data and can easily be mistaken for true science.

So we'd like to avoid cross-talk and other sources of correlated noise between elements as best as we can, while still maintaining a sensitivity to a correlated monopole signal. The only other way for an interferometer to have the capacity to observe the monopole is through the presence of dissipative elements, such as absorbers and/or the ground. Without cross-talk or dissipative elements, the monopole term will integrate to zero in every non-zero spatial mode, making the interferometer completely insensitive to the global signal Venumadhav et al. (2016).

One way to manage cross-talk it to pack the space between antennas with absorber – with a high-enough quality absorber, we can essentially make the antennas invisible to each other by just placing a tall enough wall between them. Ideally, this material would be quite physically thin, so that these absorber walls wouldn't force us to spread the shape of the array at all, thus maintaining a sensitivity to the spatial monopole of the reionization global signal.

In order for this to work, the absorber needs to meet some basic criteria. Most importantly, it will need to be at least optically thick enough that antennas on opposing sides of an absorber wall will not observe the same noise signal from the absorber. If the noise observed from the absorber is coherent between elements, then we will fall into the same pitfalls that arise from cross-talk between elements, described above.

Additionally, the absorber walls need to be shaped in such a way that signal won't reflect and bounce over the barriers – if signals are able to diffract off of one antenna and into the other, then there will still be cross-talk and our calibrations will be flawed. For this reason, we won't be able to build straight walls with sharp cutoffs. Rather, we want to build our walls in a way that signal gets trapped into the absorber or angles out of the array entirely. Ideally, we'd like to build our walls with some kind of pyramidal structure (to capture and dampen the signal within the absorber), and with a curved roll-off at the top edge (to prevent

reflections off of the baffle into multiple antennas).

Manipulating the Spatial Monopole

Another benefit to the use of absorber in our array is how we can use it to manipulate the instrument's sensitivity to the monopole. As discussed in Sec. 3.3, by applying a spatial windowing function to our monopole signal, we can increase our interferometric sensitivity to the global signal. The absorber can impose this windowing function by creating a spatial temperature change in the absorber's field of view, increasing the harmonic content of the monopole signal by imposing non-isotropic terms.

Let's take a closer look at how this is to actually work. In a perfect world, our absorbing material would be 100% effective and no information could be transmitted through it – it would absorb all incident light and re-emit it as thermal radiation. That means that, as per Fig. 4.1 and ignoring the effects of the antenna beam shape, the antenna would see the sky up until an angle of θ off of zenith, and then it would see a perfect blackbody matching the ambient temperature of the array everywhere else.

One way to understand the absorption of the blackbody would be to think in terms of optical depth, and the above case is one in which the absorber has an optical depth of $\tau = \infty$. This thinking also enables us to begin to understand more realistic scenarios, where we don't have perfect absorption between our antennas.

$$I_{obs}(\theta) = I_{sky}\ e^{-\tau_\theta} + S_{abs}\ (1 - e^{-\tau_\theta}) \tag{4.1}$$

where I_{obs} is the observed sky brightness, I_{sky} is the sky brightness, S_{abs} is the thermal brightness from the absorber, and τ is the optical depth of the absorber. This equation is a variation on the radiative transfer equation, where the sky is our source and the absorber is the medium through which the radiation is travelling.

In this quantitative construction of the reception of an element, we can see that the strength of the absorber determines the strength of the spatial cutoff – particularly, in the case of a poor absorber, the above equation shows that there will be a great deal of sky leakage into the "horizon". In particular, for reionization studies, this will be problematic due to the brightness of the sky at these frequencies from galactic synchrotron emission. So a weak absorber will barely put a dent in the sky brightness, diminishing the effectiveness of the imposed window, and keeping the reionization global signal power in the lower, harder to detect spatial modes.

Additionally, if the quality of the absorber is poor, this can increase the confusion between inherent sky structure and windowed monopole sky. Consider the fact that the sky itself will not be a perfect monopole and will therefore have spatial structure. If the quality of the absorber is poor, then more of that structure will be visible across the whole sky. This will exist in addition to the characteristic spatial sensitivity of the monopole portion of the sky. This mixing of intrinsic sky structure and imposed sky structure must be handled carefully, and having a high-performing absorber can help us to better control those parameters.

Figure 4.1: This cartoon shows the basic structure of the proposed absorber walls. Each antenna in the array will be circled by a cylinder of absorber material, creating a uniform temperature cutoff in the antenna's reception of the sky. By increasing the height of the wall, we can change the cutoff angle of the reception of the sky, thereby shrinking the spatial windowing and pushing more of the monopole to higher spatial modes.

Finally, if the absorber is optically thin, then antennas on either side of an absorber baffle will see coherent signal coming from the absorber, contributing to an overall noise bias that may be hard to calibrate for.

4.2 Overview of the Instrumental Design

Let us now consider the design of our interferometer itself. There are two key areas of interest to us: how our sensitivity to the monopole varies with the separation between antennas, and how it changes in the presence of different absorber structures and materials. Another way of viewing it would be: how do the characteristics of the individual elements and of the array design affect our ability to make this measurement.

Let us first consider the array design, i.e. baseline separations. Intuitively, we expect that the sensitivity to the global signal will be maximized with the smallest baseline separations, which correspond to a position in the uv-plane close to the origin, or the zero-spacing mode. The trade-off of this, from a design perspective, comes in the difficulty of ameliorating cross-talk in a densely packed array. We want to optimize our array design to space our antennas as loosely as possible while also maintaining workable sensitivity to the monopole term, as this will best enable us to mitigate systemic problems in our instrument and perform a successful experiment.

The next step is to add the absorber, which can essentially be treated as a modification to the antenna's beam. This calculation is done using Eq. (4.2),

$$B(\theta,\phi,\nu) = 10^{\alpha(\nu)/20}\Big(\frac{1}{2}+\frac{1}{2}\tanh\Big(\frac{\theta-(\frac{1}{2}-\theta_0)}{a}\Big)\Big)+\Big(\frac{1}{2}-\frac{1}{2}\tanh\Big(\frac{\theta-(\frac{1}{2}-\theta_0)}{a}\Big)\Big) \quad (4.2)$$

where $\alpha(\nu)$ is the absorptivity by frequency of the absorber, θ_0 is the cutoff angle of the structure (i.e. θ_0 is the height of the absorber walls), and a is the smoothing parameter that blends the transition between the absorber and the sky.

This term is then combined with the antenna beam, giving us Eq. (4.3).

$$A'(\theta,\phi,\nu) = A(\theta,\phi,\nu)B(\theta,\phi,\nu) \quad (4.3)$$

Chapter 5

Overview of the Logistics of HYPERION

5.1 Methodology of Simulation

For this simulation, we import a model array using the AIPy AntennaArray framework, which enables us to carry around an array with known geometry and baseline separations, along with individual antenna beam patterns and accessible frequencies. With this information and the previously made sky maps, we are now able to calculate our visibilities across many frequencies by using Eq. (3.4).

The AntennaArray framework also enables us to carry around models of the beams of the antennas, which is a convenient way to import absorbers into the simulation. Essentially, within the context of the simulation, the absorbers act as a modification term on the beam pattern, changing the way that each individual antenna sees the sky. This works as follows:

To start, we need a beam. HYPERION uses SARAS-style fat dipole antennas in our instrument, which means we will be using a frequency-invariant dipole beam pattern in our simulation to match (Patra et al. 2013). This is the base beam model used throughout the simulation, calculated using Eq. (5.1).

$$A(\theta, \phi, \nu) = \cos\left(\frac{\frac{\pi}{2}\cos\theta}{\sin\theta}\right) \tag{5.1}$$

The parameters we can play with are the absorptivity of the material (i.e. how much attenuation does the absorber provide at each frequency), the height of the absorber walls, and how smooth the transition from absorber to sky is.

5.2 Absorber Baffles – Initial Results

TALK ABOUT SYSTEM TEMPERATURE, NO NEED TO COOL BAFFLES (memo 1)

To date, we are still relatively early in the testing of our hypothesis that absorber walls or "baffles" between antennas will enable us to better observe the spatial monopole with an interferometer. There have been two main sets of tests performed so far – one in-lab test to measure the absorptivity of various proposed materials, and some brief field tests to gauge the effectiveness of our absorber at mitigating cross-talk between antennas.

The in-lab test was, in essence, a simple antenna return-loss measurement. To conduct the measurements, we started by constructing a large (i.e. 4.5' cube) Faraday cage out of wood and chicken wire, and placed an antenna at its center. From this setup, we could perform a simple return loss measurement and see what the maximum power return to the antenna is.

We could then line the cage with various absorptive materials and take another return-loss measurement, this time with (ideally) much of the power absorbed by the absorber, and see how effective each material is at dissipating energy within our science band. One such measurement is shown in Fig. 5.1, featuring our most promising absorber candidate material, ferrite tiles.

As can be easily seen in the figure, the ferrite tiles have a decent absorptivity profile across the band, and an excellent absorptivity around 120 MHz. However, as described in Section 2.2, the global signal of reionization is rich with physical information that is uniquely tied to its changing amplitude by frequency. The kinds of variations that we see in the absorptivity across the band are dangerous for the well-being of our experiment, as they could translate to tricky or uncertain calibration of our final instrument. We want to ensure that almost everything beyond the global signal has simple and well-defined relations to frequency (e.g. the synchrotron galactic sky, which is well described by a power law), in order to best understand our signal and be sure that instrumental idiosyncracies aren't being mistaken for true signal and science. As such, we would strongly prefer an absorber (or combination of absorbers) that has a more uniform performance across the science band.

Additionally, the ferrite tiles are among the most expensive of the materials we investigated. Even with a very close spacing and therefore relatively small baffle structures, the costs of acquiring enough ferrite to create an array quickly becomes overwhelming to the budget.

Other candidate absorbers include mats of Zotefoam Plastazote®, the AEP-EM low-frequency pyramidal foam absorber from DJM Electronics, and the creation of a grid of resistors designed to match with the free-space impedance (Mahesh et al. 2015). The Zotefoam was appealing due to its low cost compared to the pyramidal foam and ferrite tiles, but unfortunately its performance seemed to scale in proportion to its price tag. The pyramidal foam performed slightly better, but seemed to feature more reflections than the ferrite and overall had a lower absorptivity performance than the ferrite, despite a nearly identical price tag per square foot of coverage. The resistive mesh is still an attractive idea, as it would only cost us an ungodly amount of effort to put together and about $10 worth of resistors. Unfortunately, at the time of writing, only a very introductory level of investigation has been put into the resistive mesh idea, so nothing conclusive can be said about its performance as an absorber material.

Figure 5.1: Here we see the results of a closed-box return loss measurement taken with a densely packed (i.e. 9×9 tiles per wall) configuration of ferrite tiles, evenly spaced along the walls of the testing Faraday cage. The ripples are an artifact from the testing setup, and not inherent to the performance of the ferrite itself. As can be easily seen, the Ferrite performs much better at the high range of our science band, and is optimized around $\sim$ 120 MHz. While this material has the best performance out of all the materials we have looked into so far, we would ideally prefer a material with a more even absorptivity across the band, so as best to avoid inadvertently adding ripples or structure to our sky observations.

At this point in time, there really haven't been any meaningful field tests upon which I could report. However, the most important things for us to investigate in the field would be a) ability of the absorber to mitigate the cross-talk between antennas and b) the efficacy of the baffles' ability to impose a spatial temperature variation from the antenna's point-of-view and how that efficacy evolves over frequency.

In Fig. 5.2, we see one possible arrangement of the absorber materials in order to assess the ability of the absorber at mitigating cross-talk between antennas. In order to perform this test adequately, one would need to take two measurements in the same radio environment – one without the absorber between the antennas, in order to gauge the baseline level of cross-talk, and one with the absorber between, to measure the improvement in power leakage.

Figure 5.2: Shown here is a simple diagnostic field set-up that could be used to evaluate an absorber's ability to mitigate cross-talk between elements. Here we used a densely-packed configuration of ferrite tiles that have been propped up on some of our pyramidal foam absorber for additional height.

Chapter 6

Sensitivity to the Monopole Sky

6.1 Simulated

lay out the case that absorber helps us maximize interferometric sensitivity to monopole, lay out the case that we can use the characteristics of this sensitivity to potentially help us pick out monopole vs. higher order terms (some kind of filtering around sensitivity vs. u mode)

As can be easily seen in Figures 6.1 and 6.2, all interferometers have a non-zero sensitivity to the monopole mode of the sky. As the number of wavelengths of separations increases, that sensitivity also quickly evaporates.

now speak to absorbers that we tried and how they all performed. show results of monopole sky with absorber, compare to without absorber and show that there is greater sensitivity

We can also begin to see a characteristic shape of the sensitivity in the uv-plane, with peaks and nulls placed at regular intervals in uv-space. The predictability of this shape could allow us to use it as a calibration tool, if properly understood. In particular, it could be a valuable way to remove leakage from non-monopole terms into our signal. Given that this characteristic shape derives only from the monopole sky and the shape of the beam, we know that any observational deviations in this shape must come from the sky rather than the system. Therefore, it may be possible to use this information as a way to

Additionally, this shape enables us to do some weighting of our observational data. By knowing exactly what modes we expect to see the monopole term at its brightest and dimmest, we can properly weight and interpret our data at each mode and frequency, enabling us to better compare data points at different points in uv-space and frequency.

6.2 Recovered

Figure 6.1: Shown here is the absolute value of the visibility of a spectrally flat monopole sky with no absorber walls versus frequency. As can be seen already, the interferometer does have non-zero sensitivity to the monopole, though it is plainly clear that the autocorrelation term (shown in blue) is more sensitive than any of the non-zero interferometric baseline pairings.

Figure 6.2: REMAKE THIS FIGURE Shown here is the absolute value of the visibility of a spectrally flat monopole sky with no absorber walls versus uv-baseline. As can be seen already, the interferometer has a non-zero sensitivity to the monopole at non-zero baseline separations.

Chapter 7

Conclusion

review all chapters and results, but pithier

Appendix A

The Flat-Sky Approximation and Its Limitations

In Eq. (3.5), we made one implicit assumption – that we are working in only two dimensions. This, of course, is not true.

In reality, if one is hoping to utilize the nice Fourier nature of the brightness and visibility planes, the van Cittert-Zernicke theorem should be written in terms of *(u,v,w)* coordinates, rather than just *(u,v)*. The full (idealized) measurement equation can thus be written as:

$$V(u,v,w) = \iint I(l,m) e^{-2\pi i(ul+vm+w\sqrt{1-l^2-m^2})} dl dm \tag{A.1}$$

The next step is to assume that l and m are small, such that $\sqrt{1-l^2-m^2} \approx 1$, allowing the $e^{-2\pi i w}$ term to be removed from the integral by applying the proper phasing to the measured visibility and the measurement equation to be simplified to a 2D Fourier transform sampled in the uv-plane. This procedure is called the *flat-sky approximation*.

This approximation works well for many applications in astronomy, particularly in the observation of point sources or small extended sources in the sky (up to about $\pm 10°$ or so, where $l \equiv \sin\theta \approx \theta$). However, as the observed area in the sky gets larger, it becomes impossible to apply an absolutely correct phasor to the 2D integral, and the w-term instead introduces a spatially varying departure from the 2D Fourier transform the further from the phase center you are.

So, obviously, in the case where you're trying to use an interferometer to observe a global phenomenon (such as the reionization global signal), the flat sky approximation simply won't do. In the case that one is attempting to perform sky imaging, then care must be taken to navigate the pitfalls of the flat-sky approximation, including the use of clunky or expensive algorithms such as W-projection. In our case, we are not trying to image the sky at all, rather we're just attempting to understand the distribution of power in the visibility domain. We can therefore avoid the (u,v) to (l,m) confusion entirely and calculate our visibilities directly based on our knowledge of the source direction $\mathbf{s}$ and the baseline separation $\mathbf{b}$.

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