

Duration: 3 Hours

[Max Marks: 80]

N.B: (1) Question No 1 is Compulsory.

(2) Attempt any three questions out of the remaining five.

(3) All questions carry equal marks.

(4) Assume suitable data, if required and state it clearly.

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- a Explain the ways of acceptance by a PDA. [20]
- b Discuss difference in transition function of PDA, TM and FA. [05]
- c Design DFA that accepts Strings that contain "ba" or "ab" as suffix over $\Sigma = \{a, b\}$. [05]
- d Construct CFG to generate the language $L = \{a^i b^j c^k \mid k=i+j, i, j \geq 1\}$ [05]

- 2 a Represent RE epsilon for $L = \{w \mid w \text{ has prefix } bab \text{ and suffix } abb \text{ and } w \text{ is a string over } \{a, b\}\}$. [10]
Design NFA with epsilon moves for accepting L. Convert it to minimized DFA.

- b Explain Pumping Lemma for regular languages. Prove that given language is not a regular language. $L = \{a^n b^{n+1} \mid n \geq 1\}$ [10]

- 3 a The grammar G is $S \rightarrow aB \mid bA, A \rightarrow aAS \mid bAA, B \rightarrow b \mid bS \mid aBB$ [10]
Derive using Left Most Derivation (LMD) and Rightmost Derivation (RMD) for the following string "aaabbb". Draw Parse Tree.

- b Give formal definition of Push Down Automata. Design PDA that accepts odd palindromes over $\{a, b, c\}$, where c exists only at the center of every string. [10]

- 4 a i) Design DFA that accepts Strings that are multiples of 4 $\Sigma = \{0, 1\}$. [10]
ii) Design NFA that accepts strings starting with a and ending with a or starting with b and ending in b.

- b Design a Mealy machine to change every occurrence of 'a' with x, b with y and c is kept unchanged. Convert the same to equivalent Moore machine. [10]

- 5 a Consider following CFG. Is it already simplified? Explain your answer. Convert it to CNF form. [10]

 $S \rightarrow ASB \mid a \mid bb$ $A \rightarrow aSA \mid a$ $B \rightarrow SbS \mid bb$

- b Design a TM for converting a input binary number to its one's complement of a binary [10]

number.

6 Write Short notes (Any Four)

- a Chomsky Hierarchy
- b Post Correspondence Problem
- c Arden's Theorem
- d TM-Halting Problem
- e Variants of Turing Machines

[20]