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CSC600-02
HOMEWORK 2

```
/**
```

HW2 QUESTION 1

The array `a(1..n)` contains sorted integers. Write a function `maxlen(a,n)` that returns the length of the longest sequence of identical numbers (for example, if `a=(1,1,1,2,3,3,5,6,6,6,6,7,9)` then `maxlen` returns 4 because the longest sequence 6,6,6,6

contains 4 numbers. Write a demo main program for testing the work of `maxlen`. Explain your solution, and insert comments in your program. The solution should have time complexity $O(n)$.

```
**/
```

```
#include <iostream>
using namespace std;
```

```
//create an array maxlen of a specific size
```

```
int maxlen (int newArg[], int size){
```

```
    //create a variable which will be the streak number and a
    comparing count
```

```
    int streakNumber=0, count=0;
```

```
    //To check the previous number in the array we declare it to a
    variable
```

```
    int previousNum = newArg[0];
```

```
    //Iterating through the array to compare it with the previous
    number is the array.
```

```
    for(int index=1; index<size; index++)
    {
```

```
        //since we started comparing from the next number in the array
        we initialise it to a variable
```

```
        int currentNumber = newArg[index];
```

```
        //check if they the previous number and the current number are
        same and if not then count remains the same
```

```
        if(previousNum == currentNumber)
        {
```

```
            count++;
```

```
            //check if the count is incremented if yes then make that
            as the streakNumber
```

```
            if(count > streakNumber){streakNumber = count;}
```

```
        }else{count = 1;}
```

```
        previousNum = currentNumber;
```

```
    }
```

```
    return streakNumber;
```

```
}
```

```
//Testing code above with a testing array for the longest streak of
numbers
int main(){
    int testingArray[10] = {1,1,1,1,2,3,4,5,5,5};
    cout << "The longest streak is: " << maxlen (testingArray,10);
    return 0;
}
/**
Since we use only one for loop in the code with iteration to n, this
seems to be the most efficient code
to find the longest streak in an array with time complexity of O(n).
**/
```

MY OUTPUT

```
"/Users/karangupta/Desktop/CSC600_hw2/cmake-build-debug/CSC600_hw2"
The longest streak is: 3
Process finished with exit code 0
```

/**

HW 2 QUESTION 2

We know three points on a curve: (x_1, y_1) , (x_2, y_2) , (x_3, y_3) .
 You have to create a program that for any value $x_1 \leq x \leq x_3$
 computes the
 corresponding value y assuming that the segment of curve can be
 approximated with the parabola $y = ax^2 + bx + c$.
 Write a function that can be called as $y(x_1, y_1, x_2, y_2, x_3, y_3, x)$
 and a main program that reads $x_1, y_1, x_2, y_2, x_3, y_3$ and then displays
 $y(x_1, y_1, x_2, y_2, x_3, y_3, x)$ in $n=40$ equidistant x points between x_1 and
 x_3 .
 Solve this problem in the following two ways:
 (a) Insert points (x_1, y_1) , (x_2, y_2) , (x_3, y_3) in parabola $y(x) =$
 $ax^2 + bx + c$. You
 will get three linear equations; solve them and find a, b, c . Then,
 display the table of
 function $y(x)$ from x_1 to x_3 .
 (b) Solve the same problem using Lagrange interpolation formula.
 (c) Compare your two solutions and show your conclusions.
 **/

```
#include <iostream>
```

```

using namespace std;

//Form a function for parabola and its equidistant point
void y(double x1, double y1, double x2, double y2, double x3, double
y3, float x){
    int a,b,c;
    //Using the Lagrange interpolation formula
    a = (((y1-y2)*(x1-x3)) - ((x1-x2)*(y1-y3)))/(((x1*x1 - x2*x2)*(x1-
x3)) - ((x1-x2)*(x1*x1 - x3*x3)));
    b = ((y1-y2)-(((x1*x1) - (x2*x2))*a))/(x1-x2);
    c = y1 - ((x1*x1)*a) - (x1*b);
    //Print the parabola function and its equidistant point
    cout << "The equation is: y(x) = " << a << "x^2 + " << b << "x + "
<< c << endl;
    cout << "Equidistant point: " << ((x3-x1)/40.0) << endl;
    //We have to use a for loop to increment through and print
    for(int index = 0; index < 40; index++){
        float newCount = (float)index;
        x = x1 + ((x3-x1)/40.0) * newCount;
        printf("(%.2f, %.2f) \n", x, (a*x*x + b*x + c));
    }
}

// Test the parabola by asking for input and then call the above void
function
int main(){
    int x1, y1, x2, y2, x3, y3;
    float x;
    //systematically ask for 6 inputs for the function to work
    cout<<"Please enter the following: \nx1:";
    cin >> x1;
    cout << "y1:";
    cin >> y1;
    cout << "x2:";
    cin >> x2;
    cout << "y2:";
    cin >> y2;
    cout << "x3:";
    cin >> x3;
    cout << "y3:";
    cin >> y3;
    y(x1,y1,x2,y2,x3,y3,x);
    return 0;
}
/**

```

According to me this solution solve's all that was asked and in the most efficient way.

I broke the question into parts and the commented what I thought was right then I wrote

the main method so that I could test my code if it was wrong. After

writing the comments

and the main method then I wrote the function. I had to refer internet to revise what

Lagrange interpolation formula was before approaching it.

*/

MY OUTPUT

```
"/Users/karangupta/Desktop/csc600_hw2_part_2/cmake-build-debug/CSC600_hw2_part_2"
Please enter the following:
x1:
y1:
x2:
y2:
x3:
y3:
The equation is: y(x) = 0x^2 + 1x + 2
Equidistant point: 0.1
(2.00, 4.00)
(2.10, 4.10)
(2.20, 4.20)
(2.30, 4.30)
(2.40, 4.40)
(2.50, 4.50)
(2.60, 4.60)
(2.70, 4.70)
(2.80, 4.80)
(2.90, 4.90)
(3.00, 5.00)
(3.10, 5.10)
(3.20, 5.20)
(3.30, 5.30)
(3.40, 5.40)
(3.50, 5.50)
(3.60, 5.60)
(3.70, 5.70)
(3.80, 5.80)
(3.90, 5.90)
(4.00, 6.00)
(4.00, 6.00)
(4.10, 6.10)
(4.20, 6.20)
(4.30, 6.30)
(4.40, 6.40)
(4.50, 6.50)
(4.60, 6.60)
(4.70, 6.70)
(4.80, 6.80)
(4.90, 6.90)
(5.00, 7.00)
(5.10, 7.10)
(5.20, 7.20)
(5.30, 7.30)
(5.40, 7.40)
(5.50, 7.50)
(5.60, 7.60)
(5.70, 7.70)
(5.80, 7.80)
(5.90, 7.90)

Process finished with exit code 0
```

/**

HW2 QUESTION 3

The array $a(1..n)$ contains arbitrary integers. Write a function

$\text{reduce}(a,n)$ that reduces

the array $a(1..n)$ by eliminating from it all values that are equal to three largest different

integers. For example, if $a=(9,1,1,6,7,1,2,3,3,5,6,6,6,6,7,9)$ then three largest different

integers are 6,7,9 and after reduction the reduced array will be $a=(1,1,1,2,3,3,5)$, $n=7$. The

solution should have time complexity $O(n)$.

```
/**/

#include <iostream>
using namespace std;
// Form a function that finds the largest number takes them out and
the prints the rest with its size
void reduce(int* a, int n){
//We need three variables for large numbers, a number for the left
over size and then an array
    int firstLargest=0, secondLargest=0, thirdLargest=0, size = 0;
    int *newArray=new int[size];

    // iterate through the loop to get the largest 3 value
    for(int index = 0; index< n; index++){
        if(firstLargest < a[index])
            firstLargest = a[index]; // first largest number
        if(secondLargest < a[index] && a[index] < firstLargest)
            secondLargest= a[index]; // second largest number
        if(thirdLargest < a[index] && a[index] < secondLargest)
            thirdLargest= a[index]; // third largest number
    }
    //print the three largest number
    cout<< "Three Largest different Integers: "
        << firstLargest << " " << secondLargest << " " << thirdLargest
    << endl << endl;

    //Form a new array removing the largest numbers and then print it
    cout<<"Array Elements After Reduction: a= ";
    for(int index=0; index< n; index++){
        if((a[index] != firstLargest) && (a[index] != secondLargest)
        && (a[index] != thirdLargest)) {
            newArray[size] = a[index];
            cout<<newArray[size]<<",";
            size++;
            //print the size after the loop ends
        }
    }
    cout<<" n = "<< size << endl;
}

//Test the function above with the same example in the question to be
sure about the output in the main function
int main(){
    int a[]={9,1,1,6,7,1,2,3,3,5,6,6,6,6,7,9};
    //We call the reduce function for separating and printing
    reduce(a, 16);
    return 0;
}

/**/
```

I feel this is the best solution for the problem as it solves what is

asked with the most efficient method. We used total of 2 for loops but not in a nested format therefore the n is iterated once in both for loops that means the efficiency for this is $O(n)$. The first for loop is separating the largest numbers and the second for loop is used for reducing and printing them as sorted.

*/

MY OUTPUT

```
"/Users/karangupta/Desktop/csc600 hw2 part 3/cmake-build-debug/csc600_hw2_part_3"
Three Largest different Integers: 9 7 6

Array Elements After Reduction: a= 1,1,1,2,3,3,5, n = 7

Process finished with exit code 0
```

/**

HW2 QUESTION 4

Write a program BigInt(n) that displays an arbitrary positive integer n using big characters of size 7x7, as in the following example for BigInt(170):

*/

```
#include <iostream>
using namespace std;
//We create a function that makes the numbers in a 2D matrix way.
void BigInt(int n){
    //All the numbers created should be in 2D matrix of string
    variable.
    string numbers[7][10] = {
        { " @@@@@" , " @ " , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" },
        { " @@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" },
        { " @@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" },
        { " @@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" },
        { " @@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" },
        { " @@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" },
        { " @@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" }
    };
    , " @ @ " , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" , " @@@@@" }
```

```

" , " @@@@ " } ,
{ " @ " , " , " @ " , " , " @ "
, " @@@@ " , " @ " , " @ " , " @ " , " @ "
, " @ " } ,
{ " @ " , " , " @ " , " , " @ "
, " @ " , " @ " , " @ " , " @ "
, " @ " } ,
{ " @@@@ " , " @@@@ " , " @@@@ " , " @@@@ "
, " @ " , " @@@@ " , " @@@@ " , " @@@@ "
, " @ " }
};

```

// Need to have a while loop so that we could segment the input into the desired number that need to be printed

```

int i = 0, j = 0, allNumbers[10] ;
while(n > 0){
    //We divide the number by 10 which helps us giving us a single
    number to print each time its iterated
    allNumbers[i] = n % 10;
    n /= 10;
    i++;
    j++;
}
// We print the numbers using a nested for loop.
int index, index1;
for(index=0; index<7; index++){
    for(index1= j-1; index1>=0 ; index1--){
        cout<< numbers [index][allNumbers[index1]];
    }
    cout << endl;
}
}

```

// We test the above function in the main function by just giving it a random input which I am taking from the question since we know the output

```

int main(){
    //We call the function with any random output
    BigInt(170);
    return 0;
}

```

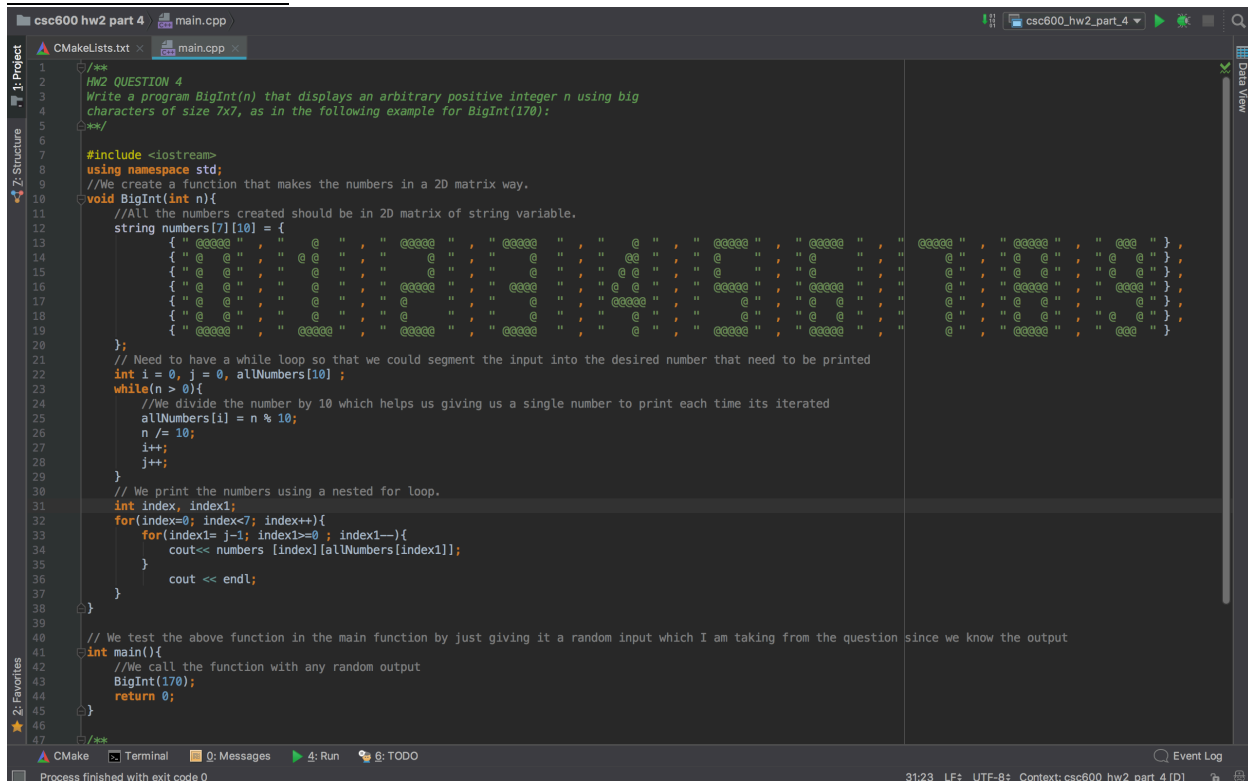
/**

I feel this is the best solution for this question, even though we used a while loop and 2 for loops for dividing the input and printing respectively, even then this is the most efficient code for this question.

I was confused between two approaches for this question, I was first thinking to store the number into switch and each case would represent a number but then I decided to go with 2D matrix and then printing it accordingly

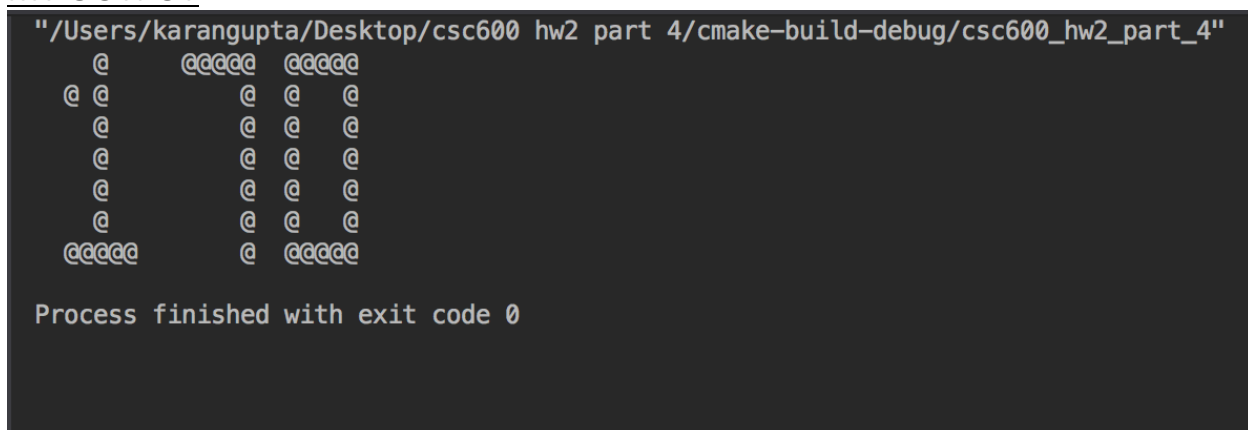
besides calling the switch cases.
**/

MY SOURCE CODE



```
1  /**
2  HW2 QUESTION 4
3  Write a program BigInt(n) that displays an arbitrary positive integer n using big
4  characters of size 7x7, as in the following example for BigInt(170):
5  **/
6
7  #include <iostream>
8  using namespace std;
9  //We create a function that makes the numbers in a 2D matrix way.
10 void BigInt(int n){
11     //All the numbers created should be in 2D matrix of string variable.
12     string numbers[7][10] = {
13         { " @@@@@", " @ ", " @ ", " @ ", " @ ", " @ ", " @ ", " @ ", " @ ", " @ " },
14         { " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ " },
15         { " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ " },
16         { " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ " },
17         { " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ " },
18         { " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ " },
19         { " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ ", " @ @ " },
20     };
21     // Need to have a while loop so that we could segment the input into the desired number that need to be printed
22     int i = 0, j = 0, allNumbers[10];
23     while(n > 0){
24         //We divide the number by 10 which helps us giving us a single number to print each time its iterated
25         allNumbers[i] = n % 10;
26         n /= 10;
27         i++;
28     }
29     // We print the numbers using a nested for loop.
30     int index, index1;
31     for(index=0; index<7; index++){
32         for(index1=j-1; index1>=0; index1--){
33             cout<< numbers [index] [allNumbers[index1]];
34         }
35         cout << endl;
36     }
37 }
38
39 // We test the above function in the main function by just giving it a random input which I am taking from the question since we know the output
40 int main(){
41     //We call the function with any random output
42     BigInt(170);
43     return 0;
44 }
```

MY OUTPUT



```
"/Users/karangupta/Desktop/csc600 hw2 part 4/cmake-build-debug/csc600_hw2_part_4"
@ @@@@ @@@@
@ @ @ @ @
@ @ @ @ @
@ @ @ @ @
@ @ @ @ @
@ @ @ @ @
@@@@ @ @@@@

Process finished with exit code 0
```

/**

HW2 QUESTION 5

Make a sorted integer array $a[i]=i$, $i=0,\dots,n-1$. Let $bs(a,n,x)$ be a binary search

program that returns the index i of array $a[0..n-1]$ where $a[i]=x$. Obviously, $bs(a,n,x)=x$, and the binary search function can be tested using the loop

```
for(j=0; j<K; j++)
for(i=0; i<n; i++) if(bs(a,n,i) != i) cout << "\nERROR";
```

Select the largest n your software can support and then K so that this loop with an iterative version of bs runs 3 seconds or more. Then measure and compare this run time and the run time of the loop that uses a recursive version of bs . Compare these run times using maximum compiler optimization (release version) and the slowest version (minimum optimization or the debug version). If you use a laptop, make measurements using AC power, and then same measurements using only the battery. What conclusions can you derive from these experiments? Who is faster? Why?

*/

```
#include <iostream>
using namespace std;
```

```
// Binary search function we use a while loop for better efficiency
int bs(int* a,int minimum, int maximum, int x){
```

```
    while (minimum <= maximum) {
        int mid;
        mid = (minimum + maximum) / 2;
        if (a[mid] > x) { maximum = mid - 1;}
        else if (a[mid] == x) { return mid;}
        else { minimum = mid + 1;}
    }
    return -1;
}
```

```
//Recursive version of the search, we dont need any loops to sort.
```

```
int bsRecursive(int* a, int minimum, int maximum, int x){

    if(minimum == maximum) {return -1;}
    else{
        int mid = minimum+((maximum-minimum) / 2);
        if (a[mid] < x) { return bsRecursive(a, mid + 1, maximum, x);}
        else if (a[mid] > x) { return bsRecursive(a,minimum, mid - 1,
x);}
        else { return mid;}
    }
}
```

```
//we use clock per second expression to get the time and initilise it
```

```

to a variable
double seconds(){
    return ((double)clock())/CLOCKS_PER_SEC;
}
//We use the above functions to read its run time in the main
function. We would probably need a nested for loop
int main(){

    int K = 1000000, n= 100, a[n];
    double timeStart; // starting the clock
    double timeEnd; // ending the clock

    // Instatiating the array
    for(int index=0;index<n;index++) {
        a[index] = index;
    }
    // START TIME
    timeStart= seconds();
    //We will go through the above mentioned function and print an
error message if needed
    for(int j=0; j<K;j++){
        for(int i=0;i<n;i++){
            if(bs(a,0,n,i)!=i)
                cout<<"ERROR" << endl;
        }
    }
    //END TIME
    timeEnd = seconds()- timeStart;
    cout<<"Iterative seconds:"<< timeEnd<< endl;

    //START TIME
    timeStart=seconds();
    //We will go through the above mentioned function and print an
error message if needed
    for(int j=0; j<K;j++){
        for(int i=0;i<n;i++){
            if(bs(a,0,n,i)!=i)
                cout<<"\nERROR"<<endl;
        }
    }
    //END TIME
    timeEnd= seconds()- timeStart;
    cout<<"Recursive seconds:"<< timeEnd<< endl;

    return 0;
}

```

/**

I feel this code can find time needed and it first explains both binary search function and then recursive function

then we create the function of time. In the main file we use our function to test for time. According to me recursive method has proved itself to be a faster approach than other iterative method. I also tried testing it and I feel that it does when the charger is plugged than it is just on the battery.

*/

MY OUTPUT

```
"/Users/karangupta/Desktop/csc600_hw2_part_5/cmake-build-debug/csc600_hw2_part_5"
```

```
Iterative seconds:5.05003
```

```
Recursive seconds:4.99763
```

```
Process finished with exit code 0
```