- (b,3), (b,b)}
  (b,3), (b,b)}
  - (a)  $\Gamma = \{(a,b), (a,b), (b,b), (b,b), (b,b)\}$
- (2) Let A be the event that a randomly choosen person is a cigarette smoker and let B be the event that the person is eiger smoker
  - P(A) = 0.28, P(B) = 0.07, P(ANB) = 0.05
  - P(AUB) = P(A) + P(B) P(ANB) = 0.28 + 0.07 0.05= 0.30.
- (a) 1-P(AUB) = 0.70. So 70/. smore neither.
- (b)  $P(A^{CB}) = P(B) P(ANB) = 0.07 0.05 = 0.02$ . Here 2½ snows eigans but not eigannettes.
  - (3) 1.521 = 36.

    A be the event that the sum is 7.  $A = \{(3,4), (5,2), (2,5), (6,1), (1,6), (4,3)\}$

P(A) = 436 = Y6.

Let A denote the event that at least one psychologist chosen.

AC - no psychologist Unosen

 $P(A) = 1 - P(A^{c}) = 1 - \frac{\binom{3.6}{3}}{\binom{54}{3}} = 0.8363.$ 

) Let A be the required 6-W 5-B.

 $P(A) = \frac{\binom{6}{1}\binom{5}{2}}{\binom{11}{2}}$  is the required prob.

Then  $P(A) = \frac{\binom{13}{5}\binom{39}{8}}{\binom{52}{13}}$ 

Let E be the event that the committee have 3 men and 2 women.

 $P(A) = \frac{\binom{6}{3}\binom{9}{2}}{\binom{15}{6}} = 0.2398$ 

choices of birthdays for the set of n peoples.

Let E be the event where we will mit able to find two or more people with the same birthday.

This event is equivalent to saying that the n people have n distinct birth-days. So there are

 $365\times364\times363\times\cdots\times(365-n)=\begin{pmatrix}365\\n\end{pmatrix}$  n! ways that w people can have w distinct birthdays.

 $P(E) = \frac{(365)^{n!}}{(365)^{n}}$ 

So the tequired prob. is = 1-P(E).

 $= 1 - {365 \choose n}^{n!} / (365)^{n}$ 

(9) Let E denotes the Event That the Second value than the text die lands on a higher

 $E = \{ (1,2), -, (1,6), (2,3), (2,4), (4,6), - \}$ 

IEI = 5+4+3+2+1 =15

$$P(E) = \frac{15}{36} = \frac{5}{12}$$

(10) 
$$F = be$$
 the event that two dice land in different  $vo$ .

 $F = be$  the event that at least one  $\delta$ .

$$P(E) = \frac{36}{36} = 56$$
,  $P(F) = \frac{11}{36}$ .

$$P(F|E) = \frac{P(F \cap E)}{P(E)}, \qquad P(F \cap E) = \frac{10}{36}$$

$$= \frac{10}{36} \times \frac{10}{8} = \frac{10}{36}.$$

$$P(E|F) = \frac{P(E \cap F)}{P(F_7)} = \frac{\frac{1}{36}}{\frac{1}{16}} = \frac{\frac{1}{16}}{\frac{1}{16}}$$

$$F_{7} = \left\{ (6,1) \right\}, \quad F_{7} = \left\{ (6,1), (1,6), (5,2), (2,5) \right\}.$$

$$P(E|F_8) = \frac{P(E11f_8)}{P(F_8)} = \frac{\frac{1}{36}}{\frac{1}{6}} = \frac{1}{5}.$$

$$P(E|F_9) = \frac{1}{4}, \quad P(E|F_{10}) = \frac{1}{3}, \quad P(E|F_{11}) = \frac{1}{2}$$

$$P(E|F_{12}) = 1.$$

So the required prob. is P(WBIE) = P(WBNE) = P((WANWBNWE)) U(WANWBNWE))

P(E)

P(F) P(WANWBNWC) + P(WACNWBNWC) P (E) = P (WAN WB NWC) + P (WA NWBN WC) P(MANWBNWC)+P(WANWBNWC)+P(WANWBNWC)  $\frac{2}{6}$ ,  $\frac{8}{12}$ .  $(1-\frac{1}{4})$  +  $(1-\frac{2}{6})$ .  $\frac{8}{12}(\frac{1}{4})$  $\frac{2}{5}$ ,  $\frac{8}{12}$   $\left(1-\frac{1}{4}\right)+\left(1-\frac{1}{6}\right)\frac{8}{12}\cdot\frac{1}{4}+\frac{2}{6}$ ,  $\left(1-\frac{6}{12}\right)$ ,  $\frac{1}{4}$ Let S -> be the event the baby survive cosarean section P(s) = 0.98, P(c) = 0.15P(s1c°) = 0.96. We have to find P(s1c°) P(s) = P(s/c) P(c) + P(s/c) P(c) = 0.96 x 0.15 + P(s|cc) x 0.85 > P(SIC) = 0.9835.

P(I) = 0.46, P(L) = 0.30, P(c) = 0.24.

Alt 
$$V \rightarrow be$$
 the event that a person voted.

P(VII) = 0.35, P(VIL) = 0.62, P(VIC) = 0.58

$$P(I|V) = \frac{P(V|I)P(I)}{P(V|I)P(L)+P(V|C)P(C)}$$

$$= \frac{0.35 \times 0.46}{0.35 \times 0.46 + 0.62 \times 0.3 + 0.58 \times (0.25)}$$

One coin is selected at random

$$P(E) = P(F) = P(G) = \frac{1}{3}$$

Let the selected coin is tossed. Let the event that hald receiv

went that hald reconstruct that hald reconstruct 
$$P(H|E) = 1$$
,  $P(H|E) = \frac{1}{2}$ ,  $P(H|G) = 0.75$ 

$$P(H|E) = \frac{1}{2}$$
,  $P(H|E)P(E) = \frac{1}{2}$ 

$$P(H|E) = \frac{1}{P(H|E)P(E)} = \frac{P(H|E)P(E)}{P(H|E)P(E) + P(H|F)P(F) + P(H|G)P(G)} = \frac{1}{3} \cdot \frac{$$

$$P(E) = 0.2$$
,  $P(F) = 0.5$ ,  $P(G) = 0.3$   
Let  $K$  be the event that  $\infty$  a person got an accident

$$p(K|E)=0.05$$
,  $P(K|F)=0.15$ ,  $P(K|G)=0.15$ ,

$$P(E) = P(K|E) P(E) + P(K|F) P(F) + P(K|G) P(G)$$

$$= 0.175$$

$$P(E|K^{c}) = \frac{P(E \cap K^{c})}{P(K^{c})} = \frac{P(K^{c}|E)P(E)}{P(K^{c})}$$

$$= \frac{0.95 \times 0.2}{0.825} = 0.230.$$

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## For this case a, b, c -> 1, 2, 3, ... 6

 $ax^{2}+bx+c=0$  has real roof is  $b^{2}-4ac>0$ =)  $b^{2}/4ac$ 

bo	b2	(a,c)	1	
1	1		Causes	
2_	4	(11)	1	
3	9	(1,1), (1,2), (2,1)	3	
4	16	(1,1), (1,2), (2,1), (2,2)	8	A -1 mgs are
5	25	(1,4), (4,1), (1,3), (3,1) (1,1), (1,2), (2,1), (2,2) (1,4), (4,1), (1,3), (3,1)	14	neal
د د	3-6	(1,5), (5,1), (1,6), (6,1) (43), (3,2), 14+ (2,4), (4,2) (3,3)	17	
			43	

$$P(A) = \frac{43}{63} = \frac{43}{216}$$