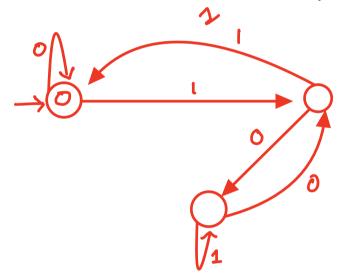
# Some more examples of DFAS

### Example:

Let  $L = \{ W \in (O+1)^{\frac{1}{4}} | W \text{ is a 6 inary} \}$ Trepresentation of an integer divisible by 3 }

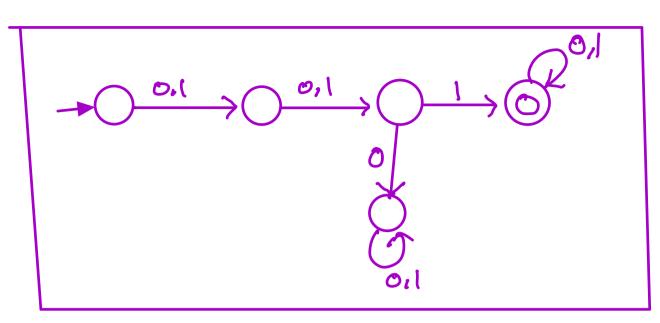


Example 1 Let L= [WE [0+1]\* | the

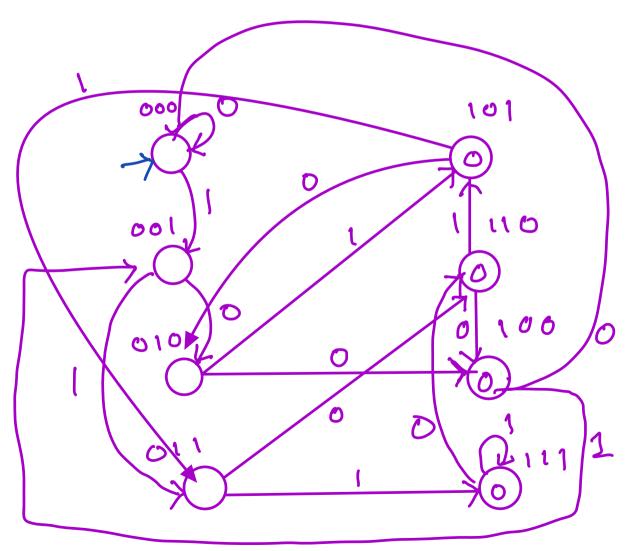
third Symbol I

w from the left
is 13

Example 2 Design a DFA for 2R.



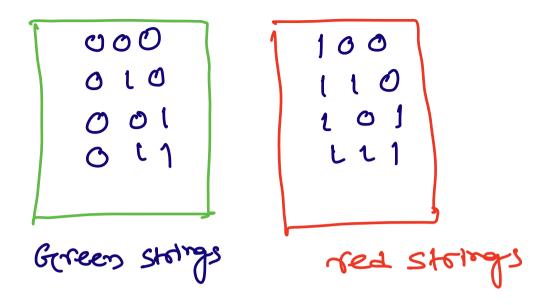
DFA for 2



Theorem Prove that
it is not possible
to design a DFA with
ST States that
accept LR.

Proof Suppose that there exists a DFA with 18 States that accepts LR-

consider the following strings



Since there are atmost

7 States, at least two

9 the acove string

90es to the same state

after the automata

finish scanning the input.

is it possible that a green string and a red string goes to the same state

Ams:

No. ogreen strings must go to a non-accepting stake

and a red storing must go to an accepting stoke 92 is it possible that the same state? Ans NO, take any two Stong 2, y from green Set. or, y differs in attent one 694 -> if the second bit to different, then consider the strings 20, 40

they cannot go to the same state as one of them is 17 2k and the other is not

or if the third bit to different

consider the strings

200 and y00

one of them El and the other & l.

Can two strings from Red Set go to the same State?

Ans NO, Take two strings noy

> second 61+ to different,

take 200, 40

> Lest 6it is different

- -> let M be a DFA. The Set of Stongs accepted by M in denoted by L (M).
- -> A Language L, is colled tragular

  if there exists a DFA M

  Such that L(M)=L

In the previous lecture, we have said that tregular longuages are those which can be trepresented as tregular expressions.

Later We will show that, for every neghbor expression, there is an equivolent DFA.

#### closure properties of regular longuages

- (1) Every language with finite number 3strings is always negation.
- (2) If L is a regulate language, then
  so is 1.º.
- (3) If Li 2 L2 are negater languages,
  then so is LiUL2 and LIOL2
- (4) If  $L_1 \supset L_2$  are negative tongression. then So to  $L_1 \cdot L_2$ .
  - (5) If Li is a Regular language than
    So to 27

Proof
(2) If L in Megnet, So 15

Proof: Let 'L 10 regular.

Therefore there exists a DFA

M=(9, 5, 20, 8, F) that

accepts L.

we constant a DFA M'from M as follows  $M' = (Q, \Sigma, 20, S, Q, F)$ 

claim L(M')= Le

(3) Li, L2 regulate => LIUL2 **Proof** MI= (9, 5, 8, 2, Fi) Let M2= (R1, Z, S2, 8/2, F2) We define M as follows Mz (91x92, 2, S, (9,7), F) Define S((2,8),2) = (2',8') 4 81(2,2) = 21 2 SZ(TIN) = 5) for all MES F = { (2,5) | 26 Fi or reFz}

elaim . L (M) = 1, U22
Proof Homework.

(4) For L1, L2 regular, then so is 2,022

ROOM

The construction of the DFA Is Similar to

the DFA for LIUZZ

other than the final

State. The final state
defined ion this case is  $F = \{22,7\} \mid 26Fi \ 376Fz\}$ 

## (3) L1, L2 regular, So is 2,=22

Before we proceed to prof the above feet, we introduce a 'more relaxed' youratron of Finite entomator.

## Non determistic finite antomaton.

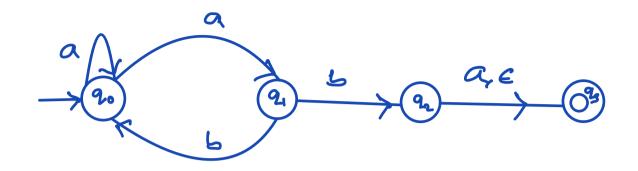
Although at a first glance, the above automaton works like a DFA, there are some

## Significant differences.

- multiple transitions than one state (0,1 or many)
- another without reading an input
- Accept on input string if some Path leas to a final state.
- The machine may 'hang' for an input that must be reserved.

#### Example

What happens is the string ab is given as input in the Automaten given in the worm-up examples !!



Possible end states for a 6

(1) 020 (20 2) 21 20)

(2) 02 (20 2) 21 202

(3) 03 (20 2) 21 202

(4) hangs at 21

one of the above Path reaches to a final state.

therefore, the Stoling as is a coepied.

What about abb ??

Passible and states for abb

(17 it hangs at 90

(2) it hangs at 90

(3) it hangs at 92

(4) it hangs at 93

None of the above possibilities ends subject of the entire input a ends

Hence a 65 & L(M)

## Definition (NFA)

A non-deterministic finite automotion to a s-super (9, 2, 8, 20, F) where

g + A set of states

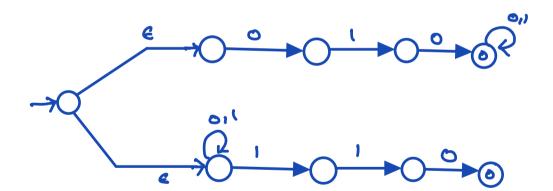
Z + a finite alphabet

 $S: \mathcal{G} \times (\Sigma \times \{E\}) \rightarrow 2^{\mathcal{G}}$ 

where 29 denotes power set 9 9.

Example Find on NFA that accepts
the set of bloary strings
having a substring ool

Find an NFA that accepts the set of whory strings beginning one of with 110



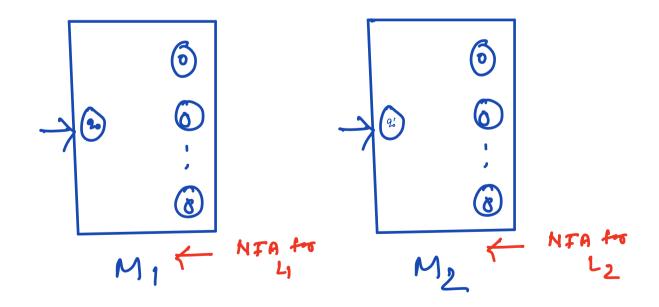
Facts	Geiven NFA'S for
two	Geiven NFAS for Longrages Li D 12
CI)	construct on NFA
(2)	Construct on FA for L1. L2
(3)	construct an NFA for Li

Proof ideas are given below. For the detailed Proof, see book "lewis 2 Papadimitrion", Page 75

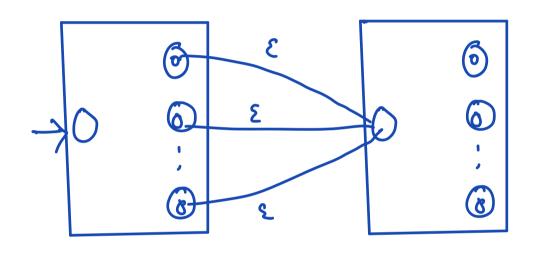
# (1) Add a new Start State S and add trongstrong S(S,E) = {S1,S2}



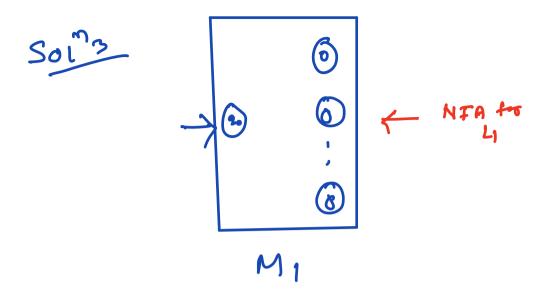
501 2. NFA for L1. L2

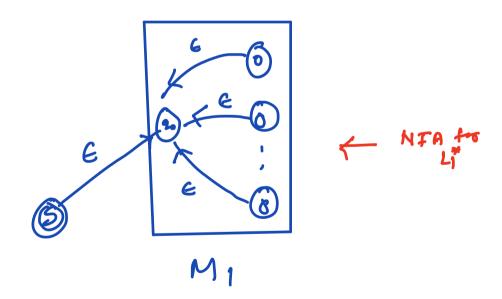


# (1) for every find state $f \in M_1$ , and transitions $g(f, c) = q'_0$



NJA for LIUZ





## Summary of the topics till lecture 3

- \* Discussions on alphabet, string,
  - \* String operations U,., \*
  - \* Regular expression.
  - Deterministic finite automotors or conquege occeptor.
    - + Non-deterministic finite automaton.