

CS 553

CRYPTOGRAPHY

Lecture 21

Keyed Hashing MAC

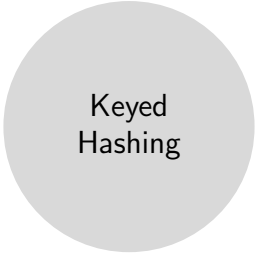
Instructor
Dr. Dhiman Saha



Kecak Dance

Keyed Hash Functions

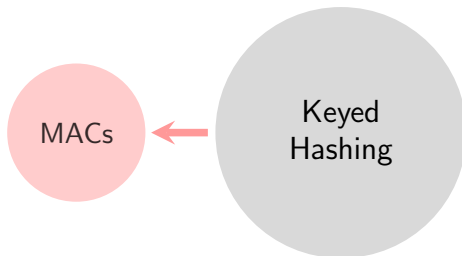
Hashing with secret keys



Keyed
Hashing

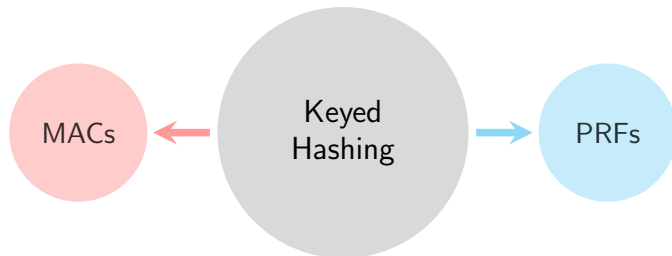
Keyed Hash Functions

Hashing with secret keys

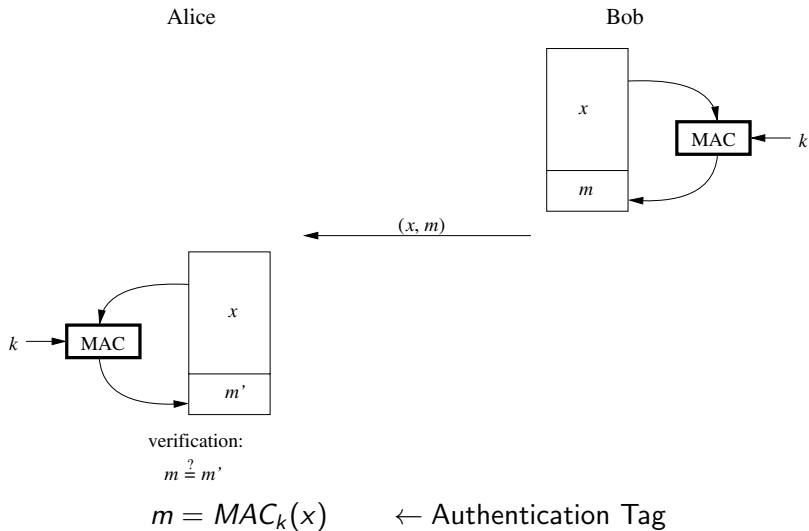


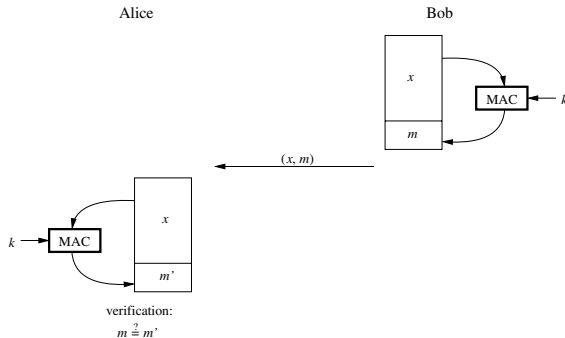
Keyed Hash Functions

Hashing with secret keys



Message Authentication Codes





Integrity

Alice knows that the message wasn't corrupted in transit

Authenticity

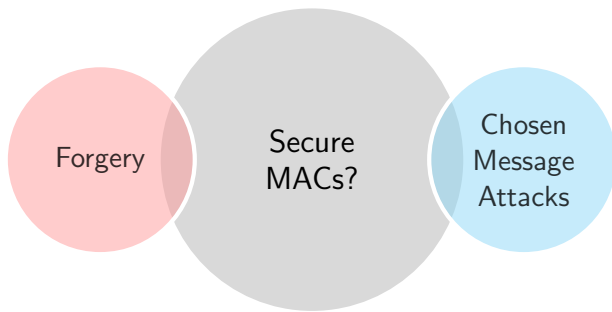
Alice knows that Bob sent that message

Generate a MAC for each network packet transmitted

- ▶ Internet Protocol Security (IPSec)
- ▶ Secure Shell (SSH)
- ▶ Transport Layer Security (TLS)

Ciphertext expansion adds overhead

- ▶ MAC not generated in 3G and 4G mobile telephony standards
- ▶ Whats the implication?



Forgery

- Generating new message/tag pair

Attack Model

- Known Message Attack
- Chosen Message Attack

- ▶ What's a replay attack?



Why?

- ▶ MACs vulnerable to replay attacks
- ▶ What's the strategy to handle this?

Pseudorandom Functions (PRFs)

A PRF is a function that uses a secret key to return $PRF(K, M)$ such that the output looks random.

Used as part of other cryptographic primitive

- ▶ To make block ciphers
- ▶ Key derivation schemes
- ▶ Identification schemes
 - ▶ Generate a response from a random challenge.

Security Notion

Indistinguishability from a random function.

How?

MACs have weaker security requirements

Any secure PRF is also a secure MAC

If a PRF's outputs can't be distinguished from random strings, the implication is that their values can't be guessed which implies **unforgeability** and hence a secure MAC.

► Is the converse true?

Example (PRF \rightarrow PRF2 from secure PRF \rightarrow PRF1)

$$PRF2(K, M) = PRF1(K, M) || 0$$

Keyed Hashes \leftarrow Unkeyed Hashes

The Secret-Prefix Construction

$$\text{Hash}(K \parallel M)$$

Vulnerabilities

- ▶ Length Extension Attacks
- ▶ Different Key Lengths (HomeWork)

The Secret-Suffix Construction

$$\text{Hash}(M \parallel K)$$

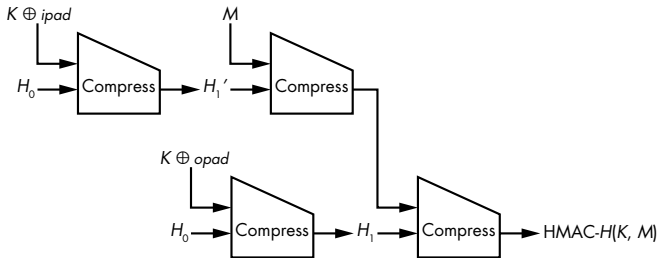
Vulnerabilities

- ▶ ~~Length Extension Attacks~~
- ▶ Colliding Messages \implies forgery

Keyed Hashes \leftarrow Unkeyed Hashes

The HMAC Construction

$$\text{Hash}((K \oplus \text{opad}) \parallel \text{Hash}((K \oplus \text{ipad}) \parallel M))$$



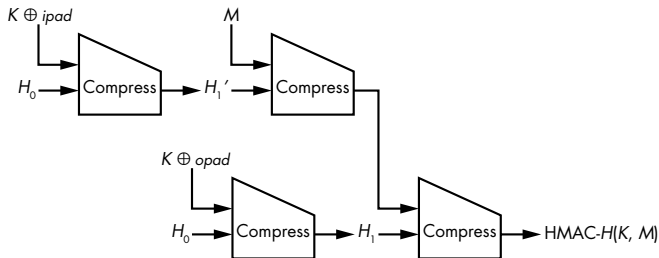
Envelope Mode

$$\text{Hash}(K \parallel M \parallel K)$$

Keyed Hashes \leftarrow Unkeyed Hashes

The HMAC Construction

$$\text{Hash}((K \oplus \text{opad}) \parallel \text{Hash}((K \oplus \text{ipad}) \parallel M))$$



Envelope Mode

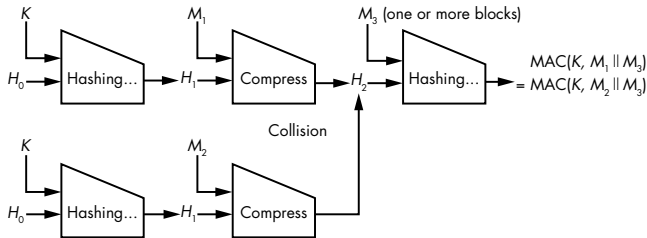
$$\text{Hash}(K \parallel M \parallel K)$$

Generic Attack Against Hash-Based MACs

Cost?

$2^{\frac{n}{2}}$ MAC Tags

Use a hash collision to get a collision of MACs



The principle of the generic forgery attack on hash-based MACs

How?

HomeWork

This attack will work even if the hash function is **not** vulnerable to length extension, and it will work for **HMAC**, too.

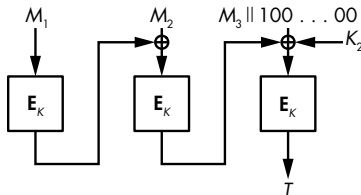
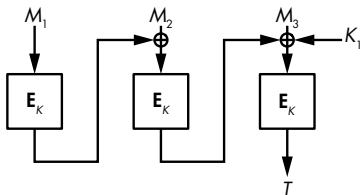
CMAC

Cipher-based MAC

- ▶ CMAC \rightarrow successor of CBC-MAC
- ▶ Recall CBC mode of operation
- ▶ What is the problem with CBC-MAC?

- ▶ Forgery with CBC-MAC

Based on M being a sequence of integral blocks or not



Note

Unlike the CBC encryption mode, CMAC does not take an IV as a parameter and is deterministic. Can you justify this?

HomeWork

- ▶ Side Channel Attacks on MACs