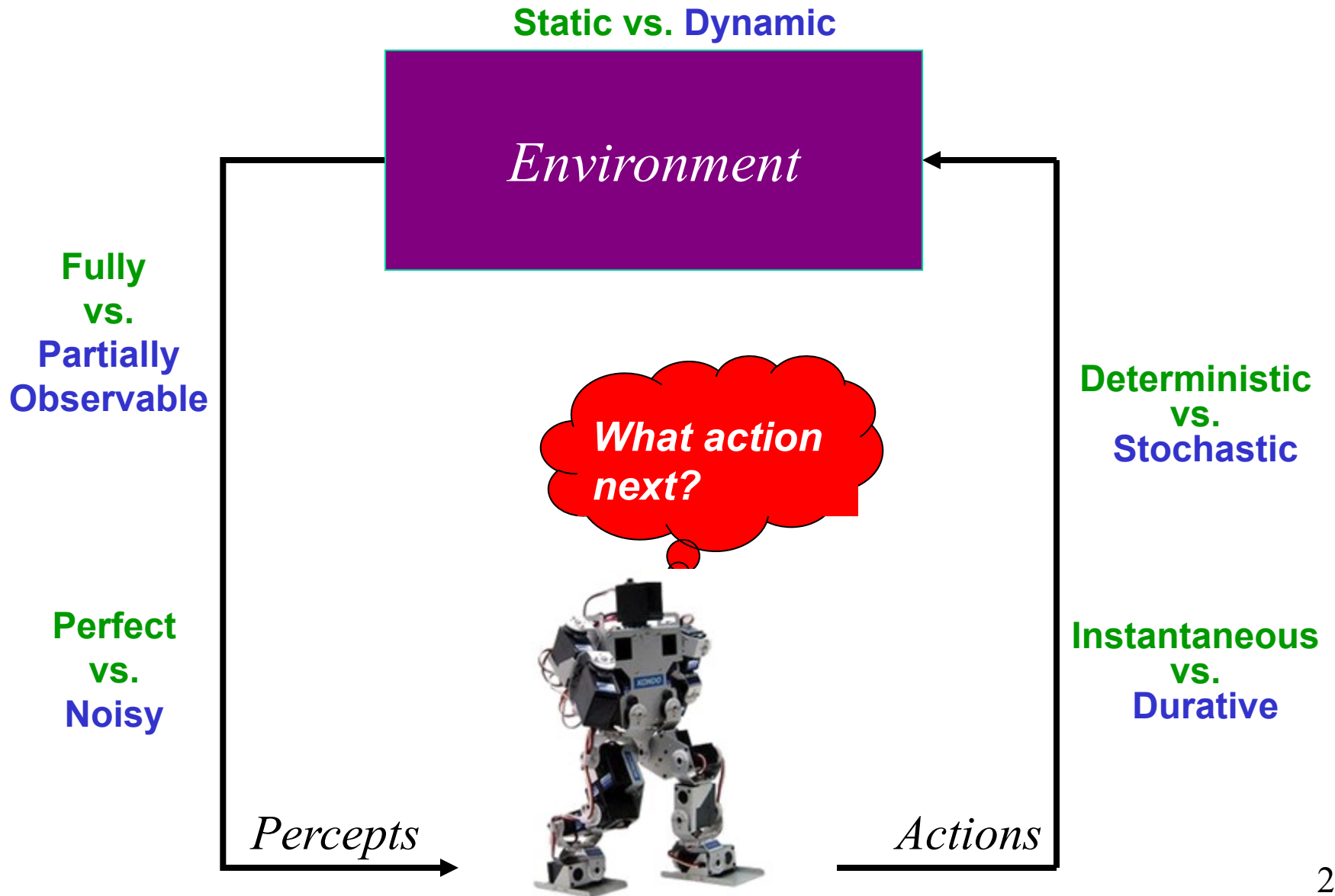


# Markov Decision Processes

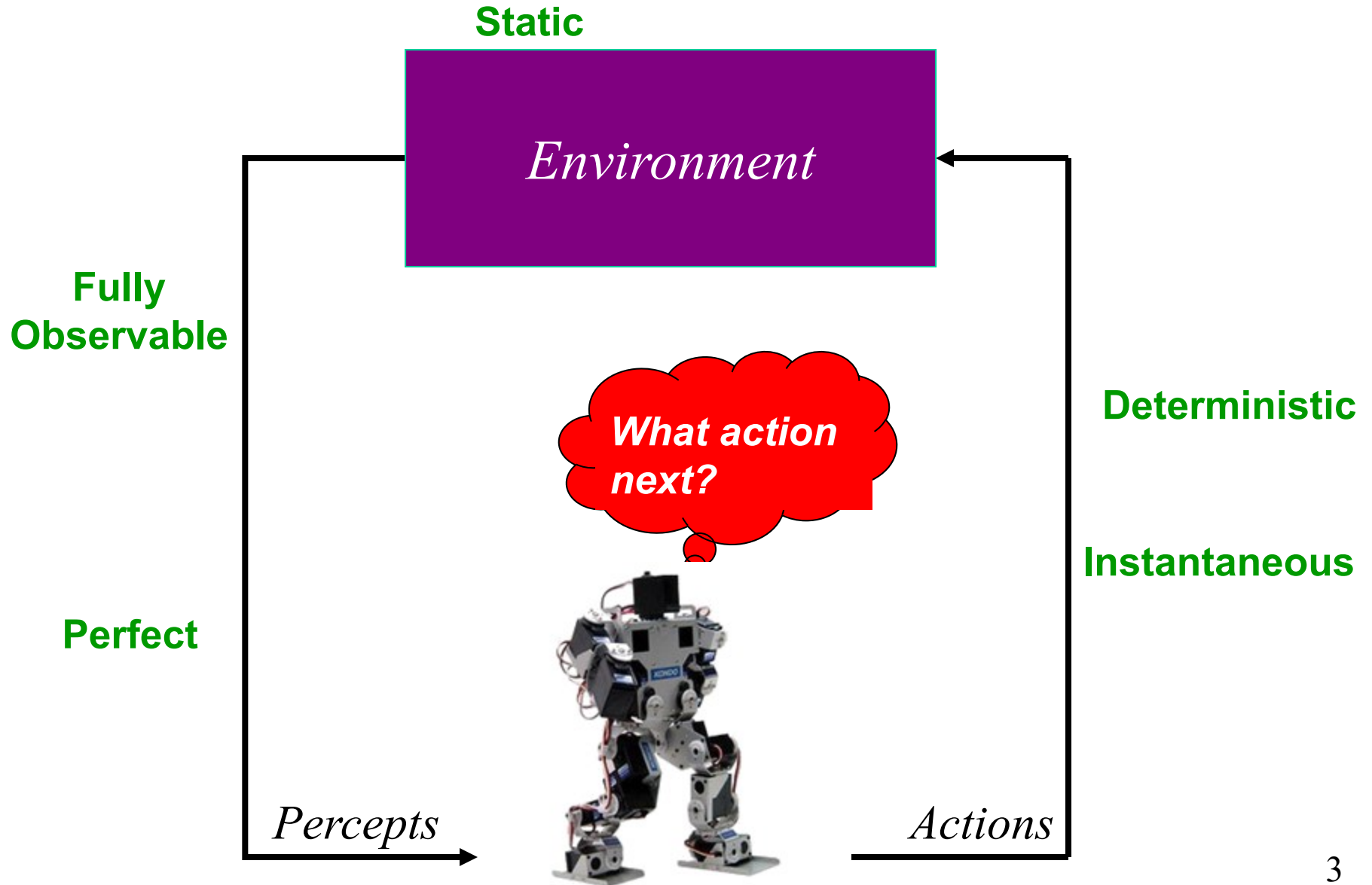
## Chapter 17

Mausam

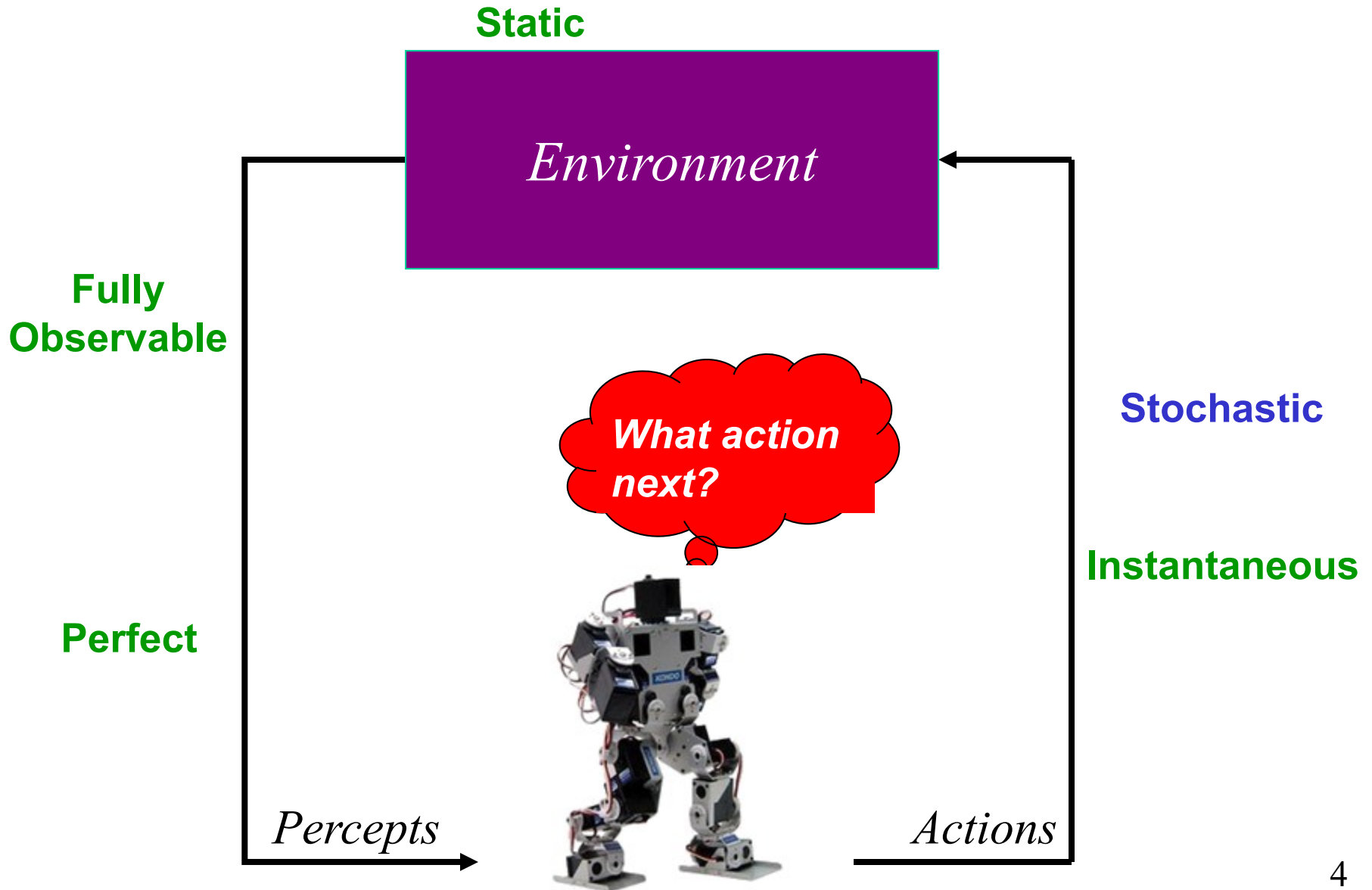
# Planning Agent



# Search Algorithms



# Stochastic Planning: MDPs



## MDP vs. Decision Theory

- Decision theory - episodic
- MDP -- sequential

# Markov Decision Process (MDP)

- $S$ : A set of states
- $A$ : A set of actions
- $\mathcal{T}(s,a,s')$ : transition model
- $\mathcal{C}(s,a,s')$ : cost model
- $\mathcal{G}$ : set of goals
- $s_0$ : start state
- $\gamma$ : discount factor
- $\mathcal{R}(s,a,s')$ : reward model

factored

Factored MDP

absorbing/  
non-absorbing

# Objective of an MDP

- Find a policy  $\pi: \mathcal{S} \rightarrow \mathcal{A}$
- which optimizes
  - minimizes  $\left[ \begin{array}{c} \text{discounted} \\ \text{or} \\ \text{undiscount.} \end{array} \right]$  expected cost to reach a goal
  - maximizes  $\left[ \begin{array}{c} \text{discounted} \\ \text{or} \\ \text{undiscount.} \end{array} \right]$  expected reward
  - maximizes  $\left[ \begin{array}{c} \text{discounted} \\ \text{or} \\ \text{undiscount.} \end{array} \right]$  expected (reward-cost)
- given a \_\_\_\_\_ horizon
  - finite
  - infinite
  - indefinite
- assuming full observability

## Role of Discount Factor ( $\gamma$ )

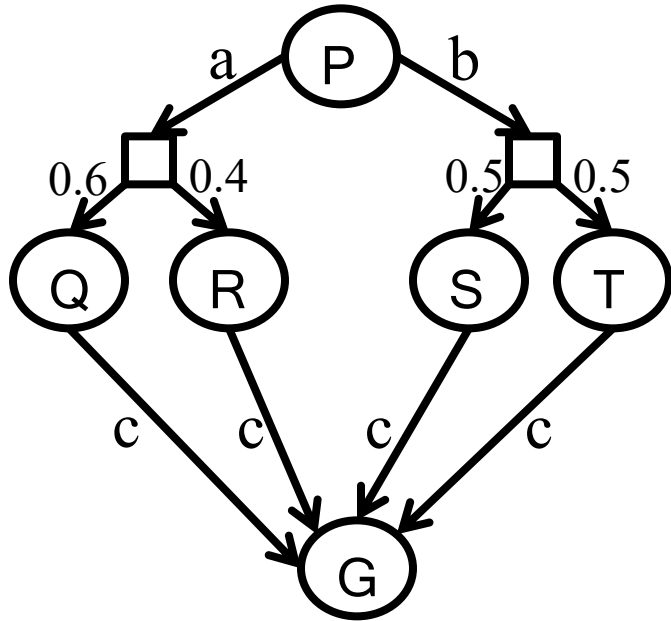
- Keep the total reward/total cost finite
  - useful for infinite horizon problems
- Intuition (economics):
  - Money today is worth more than money tomorrow.
- Total reward:  $r_1 + \gamma r_2 + \gamma^2 r_3 + \dots$
- Total cost:  $c_1 + \gamma c_2 + \gamma^2 c_3 + \dots$



# Examples of MDPs

- Goal-directed, Indefinite Horizon, Cost Minimization MDP
  - $\langle \mathcal{S}, \mathcal{A}, \mathcal{T}, \mathcal{C}, \mathcal{G}, s_0 \rangle$
  - Most often studied in planning, graph theory communities
- Infinite Horizon, Discounted Reward Maximization MDP **most popular**
  - $\langle \mathcal{S}, \mathcal{A}, \mathcal{T}, \mathcal{R}, \gamma \rangle$
  - Most often studied in machine learning, economics, operations research communities
- Oversubscription Planning: Non absorbing goals, Reward Max. MDP
  - $\langle \mathcal{S}, \mathcal{A}, \mathcal{T}, \mathcal{G}, \mathcal{R}, s_0 \rangle$
  - Relatively recent model

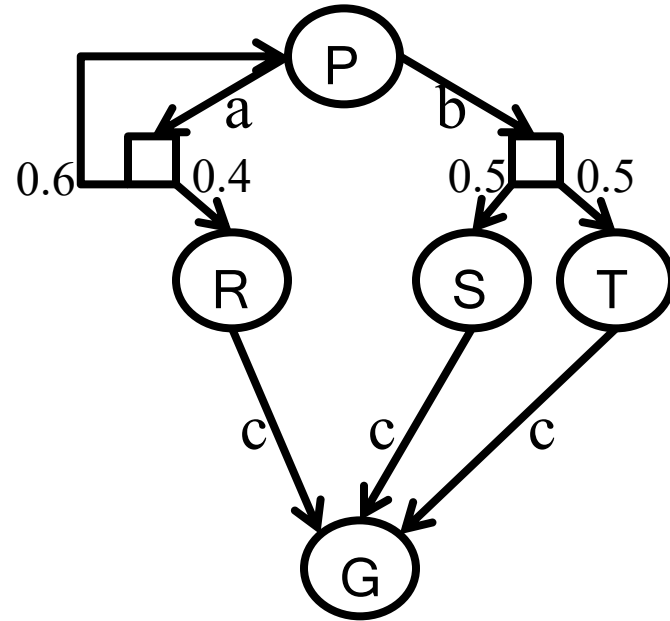
## Acyclic vs. Cyclic MDPs



$C(a) = 5, C(b) = 10, C(c) = 1$

Expectimin works

- $V(Q/R/S/T) = 1$
- $V(P) = 6$  – action a



Expectimin doesn't work

- infinite loop
- $V(R/S/T) = 1$
- $Q(P,b) = 11$
- $Q(P,a) = \text{????}$
- suppose I decide to take a in P
- $Q(P,a) = 5 + 0.4 \cdot 1 + 0.6 Q(P,a)$
- $\rightarrow = 13.5$