

CS251: Introduction to Language Processing

Top-Down Parsing

Vishwesh Jatala

Department of CSE

Indian Institute of Technology Bhilai

vishwesh@iitbhilai.ac.in



2023-24-M

Acknowledgement

- Today's slides are modified from that of
 - *Stanford University:*
 - <https://web.stanford.edu/class/archive/cs/cs143/cs143.112>
8/

LL(1) Tables with ϵ

Num \rightarrow **Sign Digits**

Sign \rightarrow **+** | **-** | **ϵ**

Digits \rightarrow **Digit More**

More \rightarrow **Digits** | **ϵ**

Digit \rightarrow **0** | **1** | ... | **9**

LL(1) Tables with ϵ

Num \rightarrow **Sign Digits**

Sign \rightarrow **+** | **-** | **ϵ**

Digits \rightarrow **Digit More**

More \rightarrow **Digits** | **ϵ**

Digit \rightarrow **0** | **1** | ... | **9**

	+	-	#	\$
Num				
Sign				
Digits				
More				
Digit				

LL(1) Tables with ϵ

Num → **Sign Digits**

Sign → **+** | **-** | **ϵ**

Digits → **Digit More**

More → **Digits** | **ϵ**

Digit → **0** | **1** | ... | **9**

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num				
Sign				
Digits				
More				
Digit				

LL(1) Tables with ϵ

Num → **Sign Digits**

Sign → **+** | **-** | **ϵ**
Digits → **Digit More**

More → **Digits** | **ϵ**

Digit → **0** | **1** | ... | **9**

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num				
Sign				
Digits				
More				
Digit				

LL(1) Tables with ϵ

Num → **Sign Digits**

Sign → **+** | **-** | **ϵ**
Digits → **Digit More**

More → **Digits** | **ϵ**

Digit → **0** | **1** | ... | **9**

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num	Sign Digits	Sign Digits	Sign Digits	
Sign				
Digits				
More				
Digit				

LL(1) Tables with ϵ

Num \rightarrow **Sign Digits**
Sign \rightarrow + | - | ϵ
Digits \rightarrow **Digit More**
More \rightarrow **Digits** | ϵ
Digit \rightarrow 0 | 1 | ... | 9

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num	Sign Digits	Sign Digits	Sign Digits	
Sign				
Digits				
More				
Digit				

LL(1) Tables with ϵ

Num → **Sign Digits**
Sign → + | - | ϵ
Digits → **Digit More**
More → **Digits** | ϵ
Digit → 0 | 1 | ... | 9

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num	Sign Digits	Sign Digits	Sign Digits	
Sign	+	-		
Digits				
More				
Digit				

LL(1) Tables with ϵ

Num \rightarrow **Sign Digits**

Sign \rightarrow **+** | **-** | **ϵ**

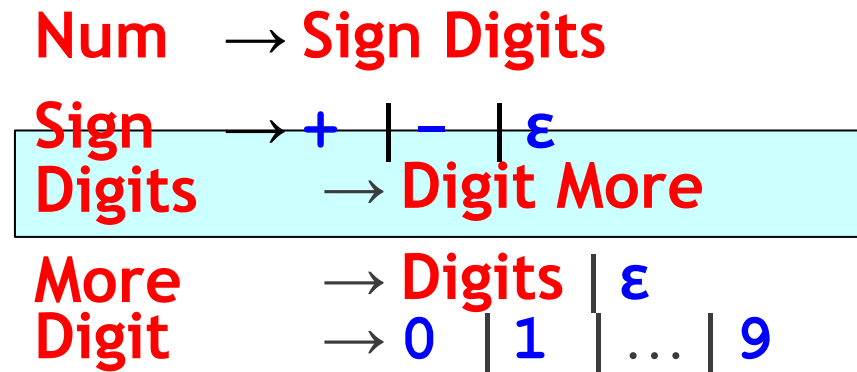
Digits \rightarrow **Digit More**

More \rightarrow **Digits** | **ϵ**
Digit \rightarrow **0** | **1** | **...** | **9**

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num	Sign Digits	Sign Digits	Sign Digits	
Sign	+	-		
Digits				
More				
Digit				

LL(1) Tables with ϵ



Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num	Sign Digits	Sign Digits	Sign Digits	
Sign	+	-		
Digits			Digits More	
More				
Digit				

LL(1) Tables with ϵ

Num → **Sign Digits**

Sign → **+** | **-** | **ϵ**

Digits → **Digit More**

More → **Digits** | **ϵ**

Digit → **0** | **1** | ... | **9**

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num	Sign Digits	Sign Digits	Sign Digits	
Sign	+	-		
Digits			Digits More	
More				
Digit				

LL(1) Tables with ϵ

Num → **Sign Digits**

Sign → **+** | **-** | **ϵ**

Digits → **Digit More**

More → **Digits** | **ϵ**

Digit → **0** | **1** | ... | **9**

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num	Sign Digits	Sign Digits	Sign Digits	
Sign	+	-		
Digits			Digits More	
More			Digits	
Digit				

LL(1) Tables with ϵ

Num → **Sign Digits**

Sign → **+** | **-** | **ϵ**

Digits → **Digit More**

More → **Digits** | **ϵ**

Digit → **0** | **1** | ... | **9**

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num	Sign Digits	Sign Digits	Sign Digits	
Sign	+	-		
Digits			Digits More	
More			Digits	
Digit				

LL(1) Tables with ϵ

Num → **Sign Digits**

Sign → **+** | **-** | **ϵ**

Digits → **Digit More**

More → **Digits** | **ϵ**

Digit → **0** | **1** | ... | **9**

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num	Sign Digits	Sign Digits	Sign Digits	
Sign	+	-		
Digits			Digits More	
More			Digits	
Digit			#	

LL(1) Tables with ϵ

Num → **Sign Digits**

Sign → **+** | **-** | **ϵ**

Digits → **Digit More**

More → **Digits** | **ϵ**

Digit → **0** | **1** | ... | **9**

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num	Sign Digits	Sign Digits	Sign Digits	
Sign	+	-		
Digits			Digits More	
More			Digits	
Digit			#	

LL(1) Tables with ϵ

Num → **Sign Digits**

Sign → **+** | **-** | **ϵ**
Digits → **Digit More**

More → **Digits** | **ϵ**

Digit → **0** | **1** | ... | **9**

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num	Sign Digits	Sign Digits	Sign Digits	
Sign	+	-		
Digits			Digits More	
More			Digits	
Digit			#	

LL(1) Tables with ϵ

Num \rightarrow **Sign Digits**

Sign \rightarrow **+** | **-** | **ϵ**

Digits \rightarrow **Digit More**

More \rightarrow **Digits** | **ϵ**

Digit \rightarrow **0** | **1** | ... | **9**

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num	Sign Digits	Sign Digits	Sign Digits	
Sign	+	-		
Digits			Digits More	
More			Digits	
Digit			#	

LL(1) Tables with ϵ

Num \rightarrow **Sign Digits**

Sign \rightarrow **+** | **-** | **ϵ**

Digits \rightarrow **Digit More**

More \rightarrow **Digits** | **ϵ**

Digit \rightarrow **0** | **1** | ... | **9**

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num	Sign Digits	Sign Digits	Sign Digits	
Sign	+	-	ϵ	
Digits			Digits More	
More			Digits	
Digit			#	

LL(1) Tables with ϵ

Num \rightarrow **Sign Digits**

Sign \rightarrow **+** | **-** | **ϵ**

Digits \rightarrow **Digit More**

More \rightarrow **Digits** | **ϵ**
Digit \rightarrow **0** | **1** | ... | **9**

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num	Sign Digits	Sign Digits	Sign Digits	
Sign	+	-	ϵ	
Digits			Digits More	
More			Digits	
Digit			#	

LL(1) Tables with ϵ

Num → **Sign Digits**

Sign → **+** | **-** | **ϵ**

Digits → **Digit More**

More → **Digits** | **ϵ**

Digit → **0** | **1** | ... | **9**

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num	Sign Digits	Sign Digits	Sign Digits	
Sign	+	-	ϵ	
Digits			Digits More	
More			Digits	
Digit			#	

LL(1) Tables with ϵ

Num → **Sign Digits**

Sign → **+** | **-** | **ϵ**

Digits → **Digit More**

More → **Digits** | **ϵ**

Digit → **0** | **1** | ... | **9**

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num	Sign Digits	Sign Digits	Sign Digits	
Sign	+	-	ϵ	
Digits			Digits More	
More			Digits	ϵ
Digit			#	

LL(1) Tables with ϵ

Num → **Sign Digits**
Sign → **+** | **-** | **ϵ**
Digits → **Digit More**
More → **Digits** | **ϵ**

Digit → **0** | **1** | ... | **9**

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9								ϵ

	+	-	#	\$
Num	Sign Digits	Sign Digits	Sign Digits	
Sign	+	-	ϵ	
Digits			Digits More	
More			Digits	ϵ
Digit			#	

LL(1) Tables with ϵ

Num → **Sign Digits**
Sign → **+** | **-** | **ϵ**
Digits → **Digit More**
More → **Digits** | **ϵ**
Digit → **0** | **1** | ... | **9**

Num		Sign		Digit		Digits		More	
+	-	+	-	0	5	0	5	0	5
0	5	ϵ		1	6	1	6	1	6
1	6			2	7	2	7	2	7
2	7			3	8	3	8	3	8
3	8			4	9	4	9	4	9
4	9							ϵ	

	+	-	#	\$
Num	Sign Digits	Sign Digits	Sign Digits	
Sign	+	-	ϵ	
Digits			Digits More	
More			Digits	ϵ
Digit			#	

The Final LL(1) Table Algorithm

- Compute $\text{FIRST}(\mathbf{A})$ and $\text{FOLLOW}(\mathbf{A})$ for all nonterminals \mathbf{A} .
- For each rule $\mathbf{A} \rightarrow \omega$, for each terminal $\mathbf{t} \in \text{FIRST}^*(\omega)$, set $T[\mathbf{A}, \mathbf{t}] = \omega$.
 - Note that ϵ is not a terminal.
- For each rule $\mathbf{A} \rightarrow \omega$, if $\epsilon \in \text{FIRST}^*(\omega)$, set $T[\mathbf{A}, \mathbf{t}] = \omega$ for each $\mathbf{t} \in \text{FOLLOW}(\mathbf{A})$.

A Formal Characterization of LL(1)

- A grammar is LL(1) if there are no conflicts in the table.
 - Every entry in the LL(1) table is unique

Exercise

- Construct the LL(1) parser table

$S \rightarrow SA \mid b \mid \epsilon$

$A \rightarrow (A) \mid a$

Exercise

- Construct the LL(1) parser table

$S \rightarrow SA | b | \epsilon$

$A \rightarrow (A) | a$

	FIRST	FOLLOW
S	{b, ϵ , a, (}	{(, a, \$}
A	{(, a}	{), (, a, \$}

Exercise

- Construct the LL(1) parser table

$S \rightarrow SA \mid b \mid \epsilon$

$A \rightarrow (A) \mid a$

	a	b	()	\$
s	$S \rightarrow SA$ $S \rightarrow \epsilon$	$S \rightarrow b$	$S \rightarrow SA$ $S \rightarrow \epsilon$		$S \rightarrow \epsilon$
A	$A \rightarrow a$		$A \rightarrow (A)$		

Exercise

- Construct the LL(1) parser table

$A \rightarrow Ab \mid c$

A Grammar that is Not LL(1)

- Consider the following (left-recursive) grammar:

$$A \rightarrow Ab \mid c$$

- $\text{FIRST}(A) = \{c\}$

-

-

	b	c
A		$A \rightarrow Ab$ $A \rightarrow c$

A Grammar that is Not LL(1)

- Consider the following (left-recursive) grammar:

$$A \rightarrow Ab \mid c$$

- $\text{FIRST}(A) = \{c\}$

-

-

	b	c
A		$A \rightarrow Ab$ $A \rightarrow c$

- Cannot uniquely predict production!
- This is called a **FIRST/FIRST conflict**.

Eliminating Left Recursion

- In general, **left recursion** can be converted into **right recursion** by a mechanical transformation.

Consider the grammar

- $$A \rightarrow A\omega \mid a$$

This will produce a followed by some number of

- ω 's.

Can rewrite the grammar as

- $$A \rightarrow aB$$
$$B \rightarrow \epsilon \mid \omega B$$

The Strengths of LL(1)

- LL(1) is straightforward
 - Can be implemented quickly with a table-driven design.
- LL(1) is Fast
 - Can parse in $O(n |G|)$ time, where n is the length of the string and $|G|$ is the size of the grammar.

Exercises

- Text book:
 - Example 4.27
 - Example 4.29
 - Example 4.33

Summary

- **Top-down parsing** tries to derive the user's program from the start symbol.
- **Leftmost BFS** is one approach to top-down parsing; it is mostly of theoretical interest.
- **Leftmost DFS** is another approach to top-down parsing that is uncommon in practice.
- **LL(1) parsing scans** from **left-to-right**, using one token of lookahead to find a leftmost derivation.

FIRST sets contain terminals that may be the **first symbol** of a production.

FOLLOW sets contain terminals that may **follow a nonterminal** in a production.

Left recursion **cause LL(1) to fail** and can be **mechanically eliminated** in some cases.

Questions?