# Predicting Weather Forecast

# Kruger 60 A

Research Skills: Programming with R

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#### Introduction

Weather forecasting has been attempted to be predicted formally since 19th century (wikipedia). Traditionally, this has been done through physical simulations in which the atmosphere is modeled as a fluid (Holmstrom, Liu & Vo, 2016). The samples from the present state of atmosphere are collected and prediction has been done by computing the numerical equations fluid dynamics & thermodynamics with the samples collected. Later on, a lot work and methods have been used to predict weather forecast with machine learning models since they are more robust to perturbations. In this project, a few different machine learning models are attempt to predict whether it'll rain tomorrow or not and the amount of rain that will rain tomorrow.

# **Data Description**

The dataset used was retrieved from the competition website Kaggle. The original dataset contains 24 different variables about weather in Australia. Every observation represents one day at an Australian city and 20 of the variables represent specific measurements like humidity, wind speed, minimum and maximum temperature and so on. The dataset contains two target variables as presented as a challenge by Kaggle: a binary variable that states if it would rain the next day and a continuous variable that states the amount of rain that would fall the next day.

# Research Questions

For the two target variables presented in the previous section, two separate research questions were constructed:

- R1: Which weather features can most accurately predict whether it will rain tomorrow?
- R2: How accurate can weather measurements from today predict the amount of rain that will fall tomorrow?

For both research questions, different types of modeling and feature selection methods were tried to find the optimal solution.

#### Packages Used

caret was used to make a test en training set for our dataset. Furthermore, we build a KNN model to predict research question 1. tidyverse is used to benefit from dplyr packages which is used to select and made new variables, subsetting or deleting certain unnecessary variables and also benefit from ggplot2 which is used for visualization both in modelling and EDA parts, besides we followed tidy data principles with "%>% " in tidyverse package. ggfortify was needed for the PCA analysis. The package assists the ggplot2 package and makes it possible to use the autoplot() function. The function made it possible to easily

plot the PCA graph. leaps and MASS are used by Caret to do the forward and backward feature selection methods. MLmetrics was used to get the mean squared error for all linear models tried to answer research question 2, to be able to compare the model performances. neuralnet The package neuralnet was used to build a simple neural network to answer question 2 and compare the results with the simple linear regression models. Boruta package is built to find important variables based on Boruta algorithm which is a wrapper built around random forest classification algorithm. It tries to bring variables as important, unimportant and tentative. We used the package to answer research question 1.

```
rm(list=ls(all=TRUE))
library(caret)
library(dplyr)
library(tidyverse)
library(ggplot2)
library(ggfortify)
library(leaps)
library(MASS)
library(mice)
library(MLmetrics)
library(neuralnet)
library(Boruta)
```

# **Data Processing**

First the data is loaded and structure is viewed to see what type of variables are available.

```
weather <- read.delim("weatherAUS.csv", sep=",", stringsAsFactors = FALSE)
str(weather) # dataset has int, num and chr values</pre>
```

```
'data.frame':
                    145460 obs. of 24 variables:
                          "2008-12-01" "2008-12-02" "2008-12-03" "2008-12-04" ...
##
   $ Date
                   : chr
                          "Albury" "Albury" "Albury" "Albury" ...
##
   $ Location
                   : chr
##
  $ MinTemp
                   : num
                          13.4 7.4 12.9 9.2 17.5 14.6 14.3 7.7 9.7 13.1 ...
##
  $ MaxTemp
                          22.9 25.1 25.7 28 32.3 29.7 25 26.7 31.9 30.1 ...
                   : num
##
   $ Rainfall
                   : num
                          0.6 0 0 0 1 0.2 0 0 0 1.4 ...
##
                          NA NA NA NA NA NA NA NA NA ...
   $ Evaporation : num
## $ Sunshine
                   : num
                          NA NA NA NA NA NA NA NA NA ...
## $ WindGustDir : chr
                          "W" "WNW" "WSW" "NE" ...
##
   $ WindGustSpeed: int
                          44 44 46 24 41 56 50 35 80 28 ...
##
                          "W" "NNW" "W" "SE" ...
  $ WindDir9am
                   : chr
##
  $ WindDir3pm
                   : chr
                          "WNW" "WSW" "WSW" "E" ...
##
   $ WindSpeed9am : int
                          20 4 19 11 7 19 20 6 7 15 ...
##
   $ WindSpeed3pm : int
                          24 22 26 9 20 24 24 17 28 11 ...
##
   $ Humidity9am : int
                          71 44 38 45 82 55 49 48 42 58 ...
   $ Humidity3pm
                  : int
                          22 25 30 16 33 23 19 19 9 27 ...
   $ Pressure9am
##
                  : num
                          1008 1011 1008 1018 1011 ...
##
   $ Pressure3pm
                  : num
                          1007 1008 1009 1013 1006 ...
##
  $ Cloud9am
                   : int
                          8 NA NA NA 7 NA 1 NA NA NA ...
##
   $ Cloud3pm
                   : int
                          NA NA 2 NA 8 NA NA NA NA NA ...
   $ Temp9am
                          16.9 17.2 21 18.1 17.8 20.6 18.1 16.3 18.3 20.1 ...
##
                   : num
##
   $ Temp3pm
                          21.8 24.3 23.2 26.5 29.7 28.9 24.6 25.5 30.2 28.2 ...
                   : num
##
  $ RainToday
                   : chr
                          "No" "No" "No" "No" ...
   $ RISK MM
                   : num
##
                          0 0 0 1 0.2 0 0 0 1.4 0 ...
                          "No" "No" "No" "No" ...
   $ RainTomorrow : chr
```

#### • Variable classes

The variables as presented in the original dataset were all integer, numerical and character values. We decided to convert all variables that contained character values to factors, except for the variable Date. This was done as character values are difficult to use in further analysis to answer the research questions.

```
weather$RainToday <- factor(weather$RainToday)
weather$RainTomorrow <- factor(weather$RainTomorrow)
weather$WindDir3pm <- factor(weather$WindDir3pm)
weather$WindDir9am <- factor(weather$WindDir9am)
weather$WindGustDir <- factor(weather$WindGustDir)
weather$Location <- factor(weather$Location)</pre>
```

#### • Adding new variables

As the Date variable is coded like *yyyy-mm-dd*, it was not very helpful to use this variable as a predictor, therefore we decided to break the variable down and make two new variables with it: *Month* and *Season*. First, we added the column Month by taking a substring from the *Date* column, after that we wrote our own function (conver\_season) to convert a column with month numbers to the Australian season and we saved those in a new column: *Season*.

```
#Creating a new column with only the month number
weather$Season <- substr(weather$Date, 6, 7)
weather$Season <- as.numeric(weather$Season)
weather$Season [weather$Season == 12] <- 0

convert_season <- function(Month) {
    Month[Month <= 2] <- "Summer"
    Month[Month >= 3 & Month <= 5] <- "Autumn"
    Month[Month >= 6 & Month <= 8] <- "Winter"
    Month[!(Month %in% c("Autumn", "Winter", "Summer"))] <- "Spring"
    Month
}

weather$Season <- convert_season(weather$Season)
weather$Season <- factor(weather$Season)</pre>
```

#### • Missing data

The dataset contained quite a lot of missing data, especially for four of the variables: Evaporation, Sunshine, Cloud9am and Cloud3pm. Values of those four variables were missing for more than one third of the observations. Before deleting those variables from the dataset, we looked at some graphs to see if the variables could be good predictors for the target variables. Although Cloud9am and Cloud3pm seemed to be reasonably good predictors we decided to delete all four of them from consideration, as the fraction of data missing was too big.

For the other variables we tried to impute the missing values with multiple imputation using the mice package. Unfortunately, due to the size of the dataset the imputation was very computationally expensive so we decided to omit the observations that contained missing values. This still resulted in a dataset of **112.925 observations** (against 145.460 observations from the original dataset), which we think should be enough to get reasonable good results.

```
sapply(weather, function(x) sum(is.na(x))) # shows absolute numbers of missing values
```

Rainfall	${\tt MaxTemp}$	MinTemp	Location	Date	##
3261	1261	1485	0	0	##
WindDir9am	WindGustSpeed	WindGustDir	Sunshine	Evaporation	##
10566	10263	10326	69835	62790	##
Humidity3pm	Humidity9am	WindSpeed3pm	WindSpeed9am	WindDir3pm	##
4507	2654	3062	1767	4228	##

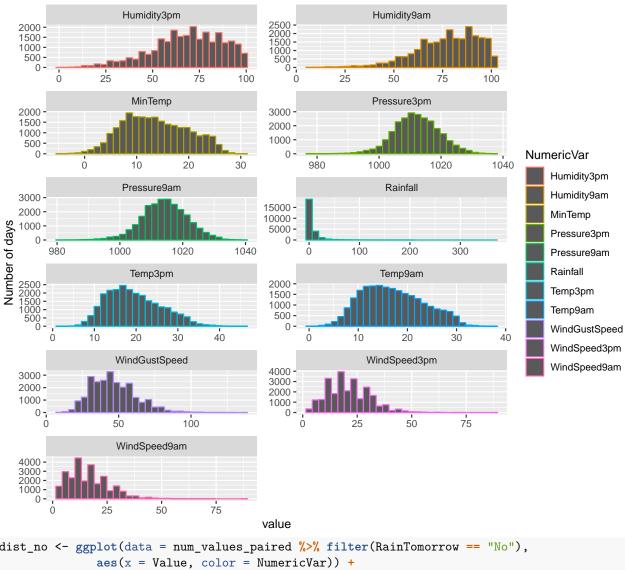
```
##
     Pressure9am
                    Pressure3pm
                                      Cloud9am
                                                     Cloud3pm
                                                                     Temp9am
##
            15065
                          15028
                                         55888
                                                        59358
                                                                         1767
                                       RISK MM RainTomorrow
##
         Temp3pm
                      RainToday
                                                                      Season
            3609
                                                          3267
##
                            3261
                                          3267
                                                                            0
colMeans(is.na(weather)) # shows percentage of missig values per column
##
            Date
                       Location
                                       MinTemp
                                                      MaxTemp
                                                                    Rainfall
##
      0.0000000
                     0.00000000
                                    0.01020899
                                                   0.00866905
                                                                  0.02241853
##
     Evaporation
                       Sunshine
                                   WindGustDir WindGustSpeed
                                                                  WindDir9am
##
      0.43166506
                     0.48009762
                                    0.07098859
                                                   0.07055548
                                                                  0.07263853
##
      WindDir3pm
                   WindSpeed9am
                                  WindSpeed3pm
                                                  Humidity9am
                                                                 Humidity3pm
##
      0.02906641
                     0.01214767
                                    0.02105046
                                                   0.01824557
                                                                  0.03098446
##
     Pressure9am
                    Pressure3pm
                                      Cloud9am
                                                     Cloud3pm
                                                                     Temp9am
##
      0.10356799
                     0.10331363
                                    0.38421559
                                                   0.40807095
                                                                  0.01214767
##
         Temp3pm
                      RainToday
                                       RISK_MM
                                                RainTomorrow
                                                                      Season
##
      0.02481094
                     0.02241853
                                    0.02245978
                                                   0.02245978
                                                                  0.00000000
weather_clean <- subset(weather, select = -c(Evaporation, Sunshine, Cloud3pm, Cloud9am))</pre>
weather_clean <- na.omit(weather_clean)</pre>
sapply(weather_clean, function(x) sum(is.na(x)))
##
            Date
                       Location
                                       MinTemp
                                                      MaxTemp
                                                                    Rainfall
##
                0
##
     WindGustDir WindGustSpeed
                                    WindDir9am
                                                   WindDir3pm
                                                                WindSpeed9am
##
                0
                                                             0
##
    WindSpeed3pm
                    Humidity9am
                                   Humidity3pm
                                                  Pressure9am
                                                                 Pressure3pm
##
                                                             0
##
         Temp9am
                        Temp3pm
                                     RainToday
                                                      RISK_MM
                                                                RainTomorrow
                                                             0
##
                0
                               0
                                              0
                                                                            0
##
          Season
##
                0
```

## Exploratory Data Analysis (EDA)

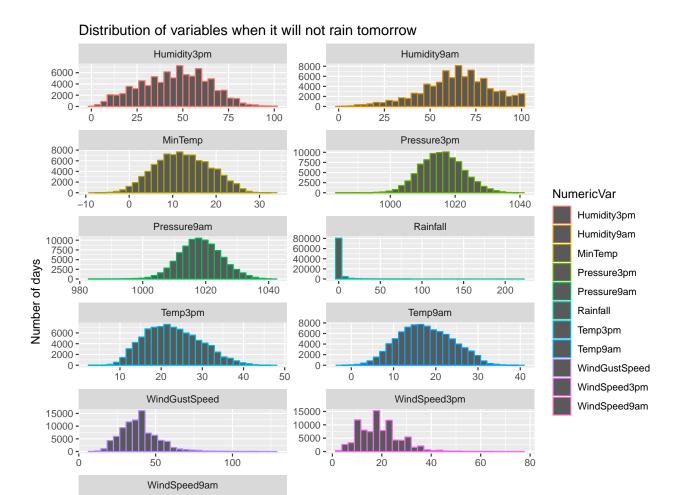
The graphs show the distribution of the numberic values per each binary target value. It can be observed that skewnesses of **Humidity3pm** and **Humidity9am** are changing based on tomorrow is rainy or not. Pressure and temparature distributions are also slightly different. That might help to predict whether it'll rain tomorrow or the amount of rain will it rain.

## `stat bin()` using `bins = 30`. Pick better value with `binwidth`.

## Distribution of variables when it will rain tomorrow



## `stat\_bin()` using `bins = 30`. Pick better value with `binwidth`.



# Modelling Research Question 1

25

15000 -10000 -5000 -0 -

Ö

## 1. Logistic Regression & Burato Algorithm for Feature Selection

75

50

When we approach the problem as a **binary classification proplem** to predict whether it'll rain tomorrow or not, the algorithm will be **logistic regression** to apply on the problem. Since the research question has two predictable outcome which are "yes" or "no".

value

Target variable: RainTomorrow Predictor variables: all columns excluding Date, Rainfall and RISK\_MM

# Splitting data to train and test

```
set.seed(1)
trn_index = createDataPartition(y = weather_clean_r1$RainTomorrow, p = 0.70, list = FALSE)
trn_weather = weather_clean_r1[trn_index, ]
tst_weather = weather_clean_r1[-trn_index, ]
```

#### Fitting training data to logistic regression

```
set.seed(1)
weather_lgr = train(RainTomorrow ~ ., method = "glm",
  family = binomial(link = "logit"), data = trn_weather,
  trControl = trainControl(method = 'cv', number = 5))
weather_lgr
## Generalized Linear Model
##
##
  79049 samples
##
      18 predictor
##
       2 classes: 'Yes', 'No'
##
## No pre-processing
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 63239, 63239, 63240, 63239, 63239
## Resampling results:
##
##
     Accuracy
                Kappa
##
     0.8526104 0.5224735
set.seed(1)
predicted_outcomes <- predict(weather_lgr, tst_weather)</pre>
predicted_outcomes[1:10]
## [1] No No No Yes No No
                                   No
## Levels: Yes No
```

Once the training data is fitted on logistic regression with all features the prediction accuracy is 85% which is kind of good accuracy but definitely could be better by eliminating the unimportant variables which can be noise for the model.

```
accuracy <- sum(predicted_outcomes == tst_weather$RainTomorrow) /
length(tst_weather$RainTomorrow)
accuracy</pre>
```

```
## [1] 0.8559747
```

Zooming a bit more to the accuracy to understand at which class, the logistic resgression is better to predict (yes or no), actually it's more important to know for us when we predict when it'll rain because in the context it makes more sense to be prepared for rain. So, we're more interested in **recall score** (sensitivity) than **accuracy**, meaning that out of all the positive classes, how much we predicted correctly. It should be high as possible. Regarding the model that we fitted, *sensitivity* (52%) is much lower than *accuracy*(85%).

```
weather_confM <- confusionMatrix(predicted_outcomes, tst_weather$RainTomorrow)
weather_confM</pre>
```

```
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                Yes
                        No
##
          Yes
               3913 1287
##
          No
               3592 25084
##
##
                  Accuracy: 0.856
                    95% CI: (0.8522, 0.8597)
##
##
       No Information Rate: 0.7785
```

```
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
                     Kappa: 0.5309
   Mcnemar's Test P-Value : < 2.2e-16
##
##
               Sensitivity: 0.5214
##
##
               Specificity: 0.9512
##
            Pos Pred Value: 0.7525
##
            Neg Pred Value: 0.8747
##
                Prevalence: 0.2215
##
            Detection Rate: 0.1155
      Detection Prevalence: 0.1535
##
##
         Balanced Accuracy: 0.7363
##
##
          'Positive' Class : Yes
##
```

So, to find the important features to increase recall & accuracy, we can use **Boruta** package that will help to classify features as important and unimportant. Then the important ones can be fitted to the linear regression again and see if the scores improve. Then, we'll be able to answer research question 1 by identifying more important variables to predict whether it'll rain tomorrow or not.

## Classifying features as important or unimportant with Boruta

Since Boruta algorithm is a wrapper built on random forest classification, if we use the all data set, it'll be computationally heavy and time-consuming, so, the data will be sampled to make it faster because the original purpose of the project is to demonstrate our R skills rather than computational work.

It seems that Location, Season, WinDir3pm and WindSpeed9am features are unimportant and they'll be removed from the features to fit the model again.

## Fitting only important features to logistic regression again

```
trn_weather = weather_clean_r1[trn_index, ]
tst_weather = weather_clean_r1[-trn_index, ]
set.seed(1)
weather_lgr = train(RainTomorrow ~ ., method = "glm",
  family = binomial(link = "logit"), data = trn_weather,
  trControl = trainControl(method = 'cv', number = 5))
set.seed(1)
predicted_outcomes <- predict(weather_lgr, tst_weather)</pre>
predicted_outcomes[1:10]
## [1] No No No No Yes No No No No
## Levels: Yes No
accuracy <- sum(predicted_outcomes == tst_weather$RainTomorrow) /
  length(tst_weather$RainTomorrow)
accuracy
## [1] 0.8559747
weather_confM <- confusionMatrix(predicted_outcomes, tst_weather$RainTomorrow)
weather_confM
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
                Yes
                       No
##
          Yes 3913 1287
               3592 25084
##
          No
##
##
                  Accuracy: 0.856
                    95% CI: (0.8522, 0.8597)
##
##
       No Information Rate: 0.7785
       P-Value [Acc > NIR] : < 2.2e-16
##
##
##
                     Kappa: 0.5309
##
    Mcnemar's Test P-Value : < 2.2e-16
##
##
               Sensitivity: 0.5214
##
               Specificity: 0.9512
            Pos Pred Value: 0.7525
##
##
            Neg Pred Value: 0.8747
##
                Prevalence: 0.2215
##
            Detection Rate: 0.1155
##
      Detection Prevalence: 0.1535
##
         Balanced Accuracy: 0.7363
##
          'Positive' Class : Yes
##
##
```

After eliminating the unimportant variables based on Burota package, we observed that neither accuracy nor sensitivity score has changed, so it still supports our model that at least it's proved that Location, Season, WinDir3pm and WindSpeed9am features are not important predictors to predict it'll rain tomorrow since it didn't decrease the model accuracy by removing them.

# K-Nearest Neighbor(KNN) & Principal Component Analysis (PCA)

Besides a logistic regression, we also wanted to test other options with our dataset. The idea was to do a PCA for feature selection, and then fit a KNN model.

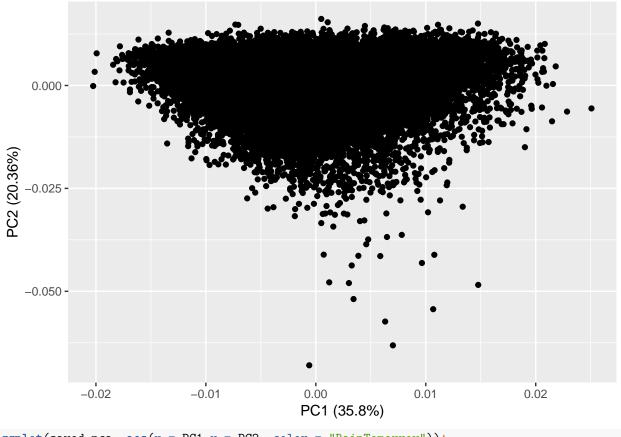
## Splitting data to test and train

```
set.seed(1)
weather_frac = sample_frac(weather_clean, size = 0.2, replace = FALSE)

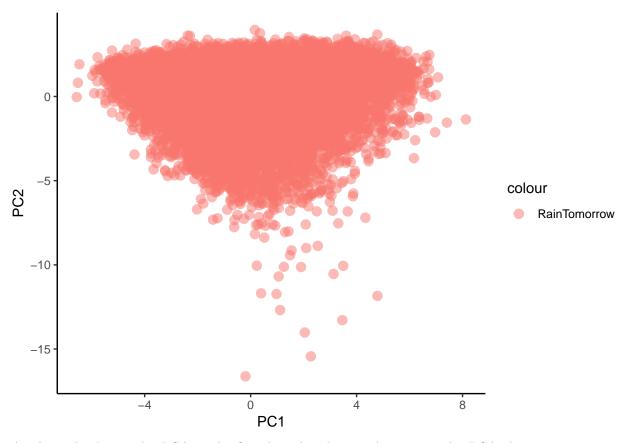
trn_index <- createDataPartition(weather_frac$RainTomorrow, p = 0.7, list = FALSE)
trn_weather <- weather_frac[trn_index, ]
tst_weather <- weather_frac[-trn_index, ]</pre>
```

## PCA for feature selection

```
## Importance of components:
##
                            PC1
                                   PC2
                                           PC3
                                                   PC4
                                                           PC5
                                                                   PC6
                                                                            PC7
## Standard deviation
                          2.157 1.6270 1.3421 1.02957 0.92551 0.83305 0.71411
## Proportion of Variance 0.358 0.2036 0.1386 0.08154 0.06589 0.05338 0.03923
## Cumulative Proportion 0.358 0.5617 0.7002 0.78176 0.84766 0.90104 0.94026
##
                              PC8
                                       PC9
                                              PC10
                                                      PC11
                                                              PC12
                                                                       PC13
                          0.58037 0.51128 0.32782 0.18209 0.16339 0.10488
## Standard deviation
## Proportion of Variance 0.02591 0.02011 0.00827 0.00255 0.00205 0.00085
## Cumulative Proportion 0.96618 0.98628 0.99455 0.99710 0.99915 1.00000
saved_pca <- pca_weather$x[, 1:13]</pre>
saved_pca <- cbind(saved_pca, RainTomorrow = factor(weather_frac$RainTomorrow))</pre>
autoplot(pca_weather) # quick plot without color and edits
```



ggplot(saved\_pca, aes(x = PC1,y = PC2, color = "RainTomorrow"))+
 geom\_point(size=3,alpha=0.5)+
 theme\_classic()



As the code shows, the PCA works fine, but the plotting does not. The PCA shows 13 components. RainTomorrow as factor has a different amount of rows than the saved\_pca variable. This is why the color of the ggplot is off, as we unfortunately unable to fix this properly.

We wanted to follow up with a KNN model. As seen below, this is a regular model without using the PCA components. Multiple error warnings showed that the datapoints of the components were too close together to build a KNN model.

# Fitting the data onto KNN model

```
## Training a basic KNN model for target RainTomorrow
knn_weather <- train(RainTomorrow ~. -Date, method = "knn", data = trn_weather,
                     trControl = trainControl(method = 'cv', number = 10),
                     na.action = na.omit)
knn_weather
## k-Nearest Neighbors
##
##
  15810 samples
##
      20 predictor
##
       2 classes: 'No', 'Yes'
##
## No pre-processing
## Resampling: Cross-Validated (10 fold)
## Summary of sample sizes: 14229, 14229, 14229, 14229, 14229, 14229, ...
##
  Resampling results across tuning parameters:
##
##
       Accuracy
                   Kappa
       0.8756483 0.5918052
##
```

```
## 7 0.8767868 0.5914922

## 9 0.8764073 0.5878667

## ## Accuracy was used to select the optimal model using the largest value.

## The final value used for the model was k=7.

# k=9 proves to be the most accurate (0.892)
```

The regular KNN model has high accuracy on the train set, where k = 9 is the most accurate (0.892).

## Modelling Research Question 2

Different linear models were tried and compared to predict the target variable **RISK\_MM** (amount of rain that will fall tomorrow). First a linear regression model was tried, including all variables of the dataset, except Date. Furthermore, forward and backwards feature selection was tried using leapforward and leapbackward when training a model with the caret package in combination with the leap package. Finally a simple neural network was tried using the neuralnet package, with a minimum amount of steps and repetitions, as a neural network is very computationally expensive.

The data was sampled into a smaller set to decrease running time of the models.

```
set.seed(1)
weather_frac = sample_frac(weather_clean, size = 0.2, replace = FALSE)

weather_frac_r2 <- subset(weather_frac, select = -c(Date, RainTomorrow))

validation_index <- createDataPartition(weather_frac_r2$RISK_MM, p=0.70,
    list=FALSE)

validation <- weather_frac_r2[-validation_index,]
training <- weather_frac_r2[validation_index,]</pre>
```

## Linear Regression Without Feature Selection

```
full_linear <- lm(RISK_MM ~., data= training)
summary(full_linear)
##</pre>
```

```
## Call:
## lm(formula = RISK MM ~ ., data = training)
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
  -32.613 -2.465 -0.662
                             1.110 212.897
##
## Coefficients:
##
                             Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                            39.004927
                                       11.869943
                                                    3.286 0.001018 **
## LocationAlbury
                            -0.171153
                                         0.542923 -0.315 0.752580
## LocationAliceSprings
                             0.783891
                                         0.534482
                                                    1.467 0.142495
## LocationBadgerysCreek
                            -0.413007
                                         0.550498 -0.750 0.453120
## LocationBallarat
                            -2.666379
                                                   -4.877 1.09e-06 ***
                                        0.546768
## LocationBendigo
                            -0.511548
                                         0.517992
                                                   -0.988 0.323384
## LocationBrisbane
                                                  -1.348 0.177612
                            -0.726748
                                        0.539049
## LocationCairns
                            -1.375663
                                         0.568761 -2.419 0.015587 *
## LocationCanberra
                            -0.417340
                                        0.536397 -0.778 0.436555
```

```
## LocationCobar
                              0.757176
                                          0.512455
                                                      1.478 0.139549
## LocationCoffsHarbour
                              0.418198
                                          0.553922
                                                      0.755 0.450274
                                                     -3.563 0.000368 ***
## LocationDartmoor
                              -2.004525
                                          0.562671
## LocationDarwin
                             -1.112891
                                                     -2.038 0.041530
                                          0.545973
## LocationGoldCoast
                              -0.429653
                                          0.555892
                                                     -0.773 0.439589
## LocationHobart
                                                     -3.879 0.000105 ***
                             -2.077852
                                          0.535633
## LocationKatherine
                              -2.894170
                                          0.846453
                                                     -3.419 0.000630 ***
## LocationLaunceston
                             -1.206474
                                          0.618485
                                                     -1.951 0.051111
## LocationMelbourne
                              -1.727594
                                          0.570333
                                                     -3.029 0.002457 **
## LocationMelbourneAirport -1.634892
                                          0.526110
                                                     -3.108 0.001890 **
## LocationMildura
                              0.563324
                                          0.514851
                                                      1.094 0.273907
## LocationMoree
                                                     -0.710 0.477611
                              -0.374715
                                          0.527643
## LocationMountGambier
                             -1.854381
                                          0.524189
                                                     -3.538 0.000405 ***
## LocationNhil
                             -1.205997
                                          0.615163
                                                     -1.960 0.049961 *
## LocationNorahHead
                              -2.293605
                                          0.536456
                                                     -4.275 1.92e-05 ***
## LocationNorfolkIsland
                              -2.465016
                                          0.534269
                                                     -4.614 3.98e-06 ***
                                          0.522240
## LocationNuriootpa
                              -0.865331
                                                     -1.657 0.097547
## LocationPearceRAAF
                              -1.173081
                                          0.541836
                                                     -2.165 0.030402
## LocationPerth
                             -0.441274
                                          0.508916
                                                     -0.867 0.385909
## LocationPerthAirport
                              -0.953912
                                          0.503959
                                                     -1.893 0.058398
## LocationPortland
                              -2.300831
                                          0.521786
                                                     -4.410 1.04e-05 ***
## LocationRichmond
                                                     -1.426 0.153971
                              -0.807413
                                          0.566323
## LocationSale
                                                     -3.525 0.000425 ***
                             -1.895627
                                          0.537829
## LocationSydney
                              -1.035325
                                          0.566155
                                                     -1.829 0.067464
                                          0.534407
## LocationSydneyAirport
                             -1.375220
                                                     -2.573 0.010081 *
## LocationTownsville
                              -1.017379
                                          0.571950
                                                     -1.779 0.075294
## LocationTuggeranong
                                                     -0.410 0.681504
                              -0.225032
                                          0.548296
## LocationUluru
                              -0.316342
                                          0.652150
                                                    -0.485 0.627629
                                                     -0.373 0.709454
## LocationWaggaWagga
                             -0.192413
                                          0.516411
                                          0.548194
## LocationWalpole
                             -2.647451
                                                     -4.829 1.38e-06 ***
## LocationWatsonia
                              -1.545136
                                          0.524573
                                                     -2.946 0.003229 **
## LocationWilliamtown
                             -0.716469
                                          0.559575
                                                     -1.280 0.200431
## LocationWitchcliffe
                             -1.126282
                                          0.550029
                                                     -2.048 0.040608
## LocationWollongong
                              -2.266696
                                          0.529286
                                                     -4.283 1.86e-05 ***
## LocationWoomera
                              0.278131
                                          0.514839
                                                      0.540 0.589047
## MinTemp
                                          0.029142
                                                      0.547 0.584164
                              0.015950
## MaxTemp
                              0.070734
                                          0.054228
                                                      1.304 0.192119
## Rainfall
                                          0.007911
                                                     19.916 < 2e-16 ***
                              0.157547
## WindGustDirENE
                                          0.327482
                                                      0.470 0.638344
                              0.153924
## WindGustDirESE
                              -0.223384
                                          0.326218
                                                     -0.685 0.493501
  WindGustDirN
                              -0.055454
                                          0.358917
                                                     -0.155 0.877215
## WindGustDirNE
                              0.075922
                                          0.353065
                                                      0.215 0.829741
## WindGustDirNNE
                              -0.430003
                                          0.369655
                                                     -1.163 0.244745
## WindGustDirNNW
                              -0.185100
                                                     -0.471 0.637515
                                          0.392839
  WindGustDirNW
                              0.043683
                                          0.371019
                                                      0.118 0.906277
## WindGustDirS
                              0.190929
                                          0.346830
                                                      0.550 0.581986
   WindGustDirSE
                              0.115765
                                          0.326221
                                                      0.355 0.722695
   WindGustDirSSE
                              0.066258
                                          0.341457
                                                      0.194 0.846144
                                                     -0.090 0.928615
## WindGustDirSSW
                              -0.031406
                                          0.350559
## WindGustDirSW
                              -0.126003
                                          0.350228
                                                     -0.360 0.719020
## WindGustDirW
                              -0.262801
                                          0.352528
                                                     -0.745 0.455996
## WindGustDirWNW
                             -0.119912
                                          0.367232
                                                     -0.327 0.744028
## WindGustDirWSW
                              0.073374
                                          0.351230
                                                      0.209 0.834525
## WindGustSpeed
                              0.144344
                                          0.007078
                                                    20.394 < 2e-16 ***
```

```
## WindDir9amENE
                             0.542958
                                         0.310442
                                                    1.749 0.080313 .
## WindDir9amESE
                             0.433296
                                        0.316591
                                                    1.369 0.171134
## WindDir9amN
                            -0.613079
                                        0.316410
                                                  -1.938 0.052689
## WindDir9amNE
                                        0.327133
                             0.514722
                                                    1.573 0.115639
## WindDir9amNNE
                             0.416348
                                        0.331560
                                                    1.256 0.209235
## WindDir9amNNW
                            -0.810917
                                        0.349301
                                                  -2.322 0.020270 *
## WindDir9amNW
                            -0.901689
                                        0.347614
                                                  -2.594 0.009497 **
## WindDir9amS
                            -0.076351
                                        0.326614
                                                  -0.234 0.815169
## WindDir9amSE
                            -0.347962
                                        0.311422
                                                  -1.117 0.263870
## WindDir9amSSE
                            -0.310416
                                        0.320682
                                                  -0.968 0.333066
## WindDir9amSSW
                            -0.606373
                                        0.345027
                                                  -1.757 0.078858
## WindDir9amSW
                            -0.231783
                                        0.348029
                                                  -0.666 0.505429
## WindDir9amW
                            -0.866110
                                        0.352934
                                                  -2.454 0.014137 *
## WindDir9amWNW
                            -0.402991
                                        0.360154
                                                  -1.119 0.263183
## WindDir9amWSW
                                        0.353193
                            -0.371058
                                                  -1.051 0.293467
## WindDir3pmENE
                            -0.881767
                                         0.337792
                                                  -2.610 0.009053 **
## WindDir3pmESE
                            -0.122977
                                        0.327195
                                                  -0.376 0.707032
## WindDir3pmN
                            -0.140311
                                        0.361913
                                                  -0.388 0.698250
## WindDir3pmNE
                            -1.684882
                                        0.348328 -4.837 1.33e-06 ***
## WindDir3pmNNE
                            -1.213031
                                        0.372474
                                                  -3.257 0.001130
## WindDir3pmNNW
                            -0.320688
                                        0.376567
                                                  -0.852 0.394443
## WindDir3pmNW
                                                  -1.221 0.221922
                            -0.456650
                                        0.373849
## WindDir3pmS
                            -0.012308
                                        0.337996
                                                  -0.036 0.970953
## WindDir3pmSE
                            -0.429504
                                        0.318086
                                                  -1.350 0.176947
## WindDir3pmSSE
                            -0.049591
                                        0.339422 -0.146 0.883841
## WindDir3pmSSW
                             0.347042
                                        0.355752
                                                   0.976 0.329318
## WindDir3pmSW
                            -0.166025
                                        0.357681
                                                  -0.464 0.642532
## WindDir3pmW
                             0.039140
                                        0.355787
                                                   0.110 0.912404
## WindDir3pmWNW
                            -0.044210
                                        0.364505 -0.121 0.903466
## WindDir3pmWSW
                             0.051801
                                        0.352493
                                                    0.147 0.883168
## WindSpeed9am
                             0.006768
                                        0.009679
                                                    0.699 0.484401
## WindSpeed3pm
                            -0.096298
                                        0.009731
                                                  -9.896 < 2e-16 ***
## Humidity9am
                            -0.012653
                                        0.006359
                                                  -1.990 0.046636
                                                  22.998
## Humidity3pm
                             0.163588
                                        0.007113
                                                          < 2e-16 ***
## Pressure9am
                                        0.040574
                                                  15.334
                             0.622177
                                                           < 2e-16
## Pressure3pm
                            -0.670817
                                        0.040079 - 16.738
                                                          < 2e-16 ***
## Temp9am
                            -0.053525
                                        0.046088
                                                  -1.161 0.245518
## Temp3pm
                            -0.004542
                                                  -0.076 0.939610
                                        0.059953
## RainTodayYes
                                                    2.714 0.006654 **
                             0.471608
                                        0.173765
## SeasonSpring
                            -0.441409
                                        0.164093
                                                  -2.690 0.007153 **
## SeasonSummer
                             0.217808
                                        0.179485
                                                    1.214 0.224950
## SeasonWinter
                            -0.400754
                                        0.189242 -2.118 0.034218 *
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 6.976 on 15705 degrees of freedom
## Multiple R-squared: 0.2263, Adjusted R-squared: 0.2212
## F-statistic: 44.17 on 104 and 15705 DF, p-value: < 2.2e-16
MSE(y_pred = predict(full_linear, validation), y_true = validation$RISK_MM)
```

## [1] 59.34653

```
\# MSE = 56.87, R2 = 0.27
```

# Stepwise feature selection using Caret, Leaps and MASS

For the simple linear model all variables were included to predict RISK\_MM. We also tried to implement backwards and forwards feature selection to check if leaving out features can lead to better predictions

• 1. Backward feature Selection

```
set.seed(1)
backwards_model <- train(RISK_MM ~. , data = training,</pre>
                    method = "leapBackward",
                    tuneGrid = data.frame(nvmax = 1:18),
                    trControl = trainControl(method = "cv", number = 10),
                    na.action = na.exclude)
## Reordering variables and trying again:
backwards_model$results
##
      nvmax
                RMSE
                       Rsquared
                                      MAE
                                            RMSESD RsquaredSD
```

```
## 1
          1 7.629633 0.05271570 3.176216 1.125572 0.01240481 0.1553364
## 2
          2 7.629352 0.05280321 3.174591 1.125146 0.01239039 0.1550559
## 3
          3 7.625690 0.05360128 3.173745 1.123843 0.01145819 0.1544331
          4 7.621979 0.05454935 3.175074 1.123022 0.01192728 0.1556921
## 4
## 5
          5 7.619561 0.05519086 3.172759 1.124580 0.01214816 0.1570521
          6 7.603028 0.05957518 3.174631 1.127524 0.01353631 0.1570393
## 6
## 7
          7 7.602971 0.05958458 3.174888 1.126441 0.01355569 0.1580846
## 8
          8 7.603390 0.05949559 3.174136 1.126571 0.01365350 0.1584838
         9 7.601737 0.05995186 3.172603 1.122183 0.01339476 0.1592889
## 9
## 10
         10 7.598160 0.06075652 3.172812 1.120851 0.01246855 0.1595194
         11 7.597004 0.06107688 3.171436 1.120116 0.01289170 0.1598675
## 11
## 12
         12 7.597152 0.06104855 3.171816 1.120220 0.01292376 0.1599876
## 13
         13 7.596697 0.06116075 3.170675 1.119754 0.01295282 0.1596706
         14 7.596547 0.06122224 3.170597 1.119727 0.01315491 0.1591900
## 14
## 15
         15 7.594944 0.06161241 3.168480 1.120001 0.01336925 0.1599359
         16 7.594922 0.06169802 3.168058 1.118047 0.01355120 0.1594530
## 16
         17 7.594926 0.06170483 3.167793 1.117793 0.01361541 0.1599390
## 17
## 18
         18 7.592061 0.06252164 3.183630 1.114818 0.01290278 0.1621939
```

The results of the backwards feature selection model show that including all 18 variables leads to the lowest RMSE and the highest R squared score.

The backwards feature selection model has an MSE of

```
MSE(y_pred = predict(backwards_model, validation), y_true = validation$RISK_MM)
```

#### ## [1] 71.514

• 2. Forward Feature Selection

```
forwards_model <- train(RISK_MM ~. , data = training,</pre>
                    method = "leapForward",
                    tuneGrid = data.frame(nvmax = 1:18),
                    trControl = trainControl(method = "cv", number = 10),
                    na.action = na.exclude)
## Reordering variables and trying again:
forwards_model$results
```

```
##
      nvmax
                RMSE
                       Rsquared
                                     MAE
                                            RMSESD RsquaredSD
## 1
          1 7.582508 0.05474692 3.175895 1.433014 0.01735202 0.1779703
## 2
          2 7.582301 0.05483861 3.174417 1.432485 0.01755949 0.1769568
## 3
          3 7.579663 0.05546339 3.169821 1.433044 0.01737813 0.1770036
          4 7.578904 0.05572383 3.170492 1.435021 0.01777857 0.1775136
## 4
          5 7.561437 0.06003377 3.176058 1.428901 0.01761640 0.1828253
## 5
## 6
          6 7.561714 0.05998168 3.177195 1.427612 0.01757299 0.1817460
## 7
          7 7.557641 0.06090816 3.175340 1.428575 0.01724883 0.1834513
          8 7.557522 0.06088972 3.174216 1.429179 0.01714231 0.1852817
## 8
          9 7.551915 0.06267829 3.171645 1.424088 0.01979855 0.1843580
## 9
         10 7.552058 0.06264361 3.171472 1.424110 0.01980318 0.1843688
## 10
## 11
         11 7.551656 0.06271658 3.170792 1.424412 0.01969466 0.1848665
## 12
         12 7.551789 0.06267532 3.171601 1.423692 0.01965477 0.1853148
## 13
         13 7.551474 0.06274626 3.171279 1.424325 0.01963012 0.1855148
## 14
         14 7.551244 0.06282030 3.171416 1.424677 0.01968190 0.1855226
## 15
         15 7.550750 0.06294223 3.170736 1.424176 0.01963997 0.1856800
## 16
         16 7.550631 0.06303957 3.170834 1.422156 0.02000336 0.1849253
## 17
         17 7.550680 0.06301787 3.170906 1.422298 0.01992060 0.1844607
## 18
         18 7.548431 0.06356009 3.171678 1.423294 0.01933368 0.1835269
```

The results of the forward feature selection model also showed that including all 18 variables lead to the best prediction for RISK\_MM, but the R squared score is slightly higher and the RMSE score is slightly lower for forwards feature selection.

The forward feature selection model has an MSE of

```
MSE(y_pred = predict(forwards_model, validation), y_true = validation$RISK_MM)
```

```
## [1] 71.40349
```

Comparing the MSEs of the simple linear model and the models using backwards and forwards feature selection, the simple linear model still performs the best.

## Deep Learning

In the next piece of code a simple neural network is implemented to try to get a smaller MSE score than the simple linear regression model.

• First all factor variables have to become dummy variables

```
n <- names(weather_frac_r2)
formula_bin <- as.formula(paste("~ ", paste(n, collapse= "+")))
binarized_train <- as.data.frame(model.matrix(formula_bin , data = training))
binarized_valid <- as.data.frame(model.matrix(formula_bin, data = validation))
binarized_train$^(Intercept)^<- NULL
binarized_valid$^(Intercept)^<- NULL</pre>
```

• Adding all variables in a formula to use in the neural network. The parameters 'rep' and 'stepmax' are kept very low to speed up the process time.

```
n_bin <-names(binarized_train)</pre>
formula_net <- as.formula(paste("RISK_MM ~", paste(n_bin[!n_bin %in% "RISK_MM"],
                           collapse = "+")))
nn <- neuralnet(formula_net, data=binarized_train, hidden=3, rep=50,</pre>
                linear.output=T, lifesign="full", algorithm="rprop+",
                threshold=0.01, stepmax = 1000)
## hidden: 3
                thresh: 0.01
                                                             48
                                 rep:
                                       1/50
                                                steps:
                                                                   error: 493887.4038
                                                                                        time: 0.71 secs
                thresh: 0.01
## hidden: 3
                                 rep:
                                       2/50
                                                             52
                                                                   error: 493887.4038
                                                                                        time: 0.79 secs
                                                steps:
## hidden: 3
                thresh: 0.01
                                 rep:
                                        3/50
                                                steps:
                                                             52
                                                                   error: 493887.4038
                                                                                        time: 0.79 secs
## hidden: 3
                thresh: 0.01
                                 rep:
                                       4/50
                                                steps:
                                                             57
                                                                   error: 493887.4038
                                                                                        time: 0.89 secs
## hidden: 3
                thresh: 0.01
                                 rep:
                                       5/50
                                                steps:
                                                             62
                                                                   error: 493887.4038
                                                                                        time: 1.13 secs
## hidden: 3
                thresh: 0.01
                                       6/50
                                                             58
                                                                   error: 493887.4038
                                                                                        time: 0.84 secs
                                 rep:
                                                steps:
## hidden: 3
                thresh: 0.01
                                 rep:
                                       7/50
                                                steps:
                                                             65
                                                                   error: 493887.4038
                                                                                        time: 0.92 secs
## hidden: 3
                thresh: 0.01
                                       8/50
                                 rep:
                                                steps: stepmax
                                                                   min thresh: 3959.194317
## hidden: 3
                thresh: 0.01
                                 rep: 9/50
                                                steps:
                                                             54
                                                                   error: 493887.4038
                                                                                        time: 0.8 secs
## hidden: 3
                thresh: 0.01
                                 rep: 10/50
                                                                   min thresh: 120.6535465
                                                steps: stepmax
## hidden: 3
                thresh: 0.01
                                 rep: 11/50
                                                                   error: 493887.4038
                                                                                        time: 0.87 secs
                                                steps:
                                                             50
## hidden: 3
                thresh: 0.01
                                 rep: 12/50
                                                                                        time: 0.74 secs
                                                steps:
                                                             51
                                                                   error: 493887.4038
## hidden: 3
                thresh: 0.01
                                 rep: 13/50
                                                                   error: 493887.4038
                                                                                        time: 0.75 secs
                                                steps:
                                                             52
## hidden: 3
                thresh: 0.01
                                 rep: 14/50
                                                steps: stepmax
                                                                   min thresh: 18.55614134
## hidden: 3
                thresh: 0.01
                                 rep: 15/50
                                                steps:
                                                             68
                                                                   error: 493887.4038
                                                                                        time: 1.08 secs
## hidden: 3
                thresh: 0.01
                                 rep: 16/50
                                                             60
                                                                   error: 493887.4038
                                                                                        time: 1.1 secs
                                                steps:
## hidden: 3
                thresh: 0.01
                                 rep: 17/50
                                                steps:
                                                             61
                                                                   error: 493887.4038
                                                                                        time: 0.94 secs
## hidden: 3
                                                             57
                thresh: 0.01
                                 rep: 18/50
                                                steps:
                                                                   error: 493887.4038
                                                                                        time: 0.93 secs
## hidden: 3
                thresh: 0.01
                                 rep: 19/50
                                                steps:
                                                             62
                                                                   error: 493887.4038
                                                                                        time: 0.89 secs
## hidden: 3
                                 rep: 20/50
                thresh: 0.01
                                                steps:
                                                             59
                                                                   error: 493887.4038
                                                                                        time: 0.89 secs
## hidden: 3
                thresh: 0.01
                                 rep: 21/50
                                                steps:
                                                             56
                                                                   error: 493887.4038
                                                                                        time: 0.85 secs
## hidden: 3
                thresh: 0.01
                                 rep: 22/50
                                                steps:
                                                             57
                                                                   error: 493887.4038
                                                                                        time: 1.07 secs
## hidden: 3
                                                                                        time: 0.69 secs
                thresh: 0.01
                                 rep: 23/50
                                                                   error: 493887.4038
                                                steps:
                                                             47
## hidden: 3
                thresh: 0.01
                                 rep: 24/50
                                                steps: stepmax
                                                                   min thresh: 4301.630098
                thresh: 0.01
## hidden: 3
                                 rep: 25/50
                                                steps: stepmax
                                                                   min thresh: 3641.430109
## hidden: 3
                thresh: 0.01
                                 rep: 26/50
                                                steps:
                                                             58
                                                                   error: 493887.4038 time: 0.87 secs
## hidden: 3
                thresh: 0.01
                                 rep: 27/50
                                                                   min thresh: 4232.506632
                                                steps: stepmax
## hidden: 3
                thresh: 0.01
                                 rep: 28/50
                                                                   error: 493887.4038
                                                steps:
                                                             64
                                                                                        time: 1.03 secs
## hidden: 3
                thresh: 0.01
                                 rep: 29/50
                                                             51
                                                                   error: 493887.4038
                                                                                        time: 0.87 secs
                                                steps:
```

steps:

steps:

steps:

59

73

59

error: 493887.4038

error: 493887.4038

error: 493887.4038 time: 0.86 secs

time: 0.97 secs

time: 1.13 secs

rep: 30/50

rep: 31/50

rep: 32/50

## hidden: 3

## hidden: 3

## hidden: 3

thresh: 0.01

thresh: 0.01

thresh: 0.01

```
## hidden: 3
                 thresh: 0.01
                                 rep: 33/50
                                                steps:
                                                             46
                                                                    error: 493887.4038
                                                                                        time: 0.68 secs
## hidden: 3
                                 rep: 34/50
                                                                                        time: 0.82 secs
                 thresh: 0.01
                                                steps:
                                                             55
                                                                    error: 493887.4038
                                                steps:
## hidden: 3
                 thresh: 0.01
                                 rep: 35/50
                                                             60
                                                                    error: 493887.4038
                                                                                         time: 1.13 secs
## hidden: 3
                 thresh: 0.01
                                 rep: 36/50
                                                steps:
                                                             59
                                                                    error: 493887.4038
                                                                                        time: 0.99 secs
## hidden: 3
                 thresh: 0.01
                                 rep: 37/50
                                                steps:
                                                             78
                                                                    error: 493887.4038
                                                                                         time: 1.2 secs
## hidden: 3
                                 rep: 38/50
                                                steps:
                 thresh: 0.01
                                                             57
                                                                    error: 493887.4038
                                                                                         time: 0.89 secs
## hidden: 3
                 thresh: 0.01
                                 rep: 39/50
                                                steps:
                                                             55
                                                                    error: 493887.4038
                                                                                         time: 1.05 secs
## hidden: 3
                 thresh: 0.01
                                 rep: 40/50
                                                steps:
                                                             58
                                                                   error: 493887.4038
                                                                                         time: 0.98 secs
## hidden: 3
                 thresh: 0.01
                                 rep: 41/50
                                                steps: stepmax
                                                                   min thresh: 0.9297154123
## hidden: 3
                 thresh: 0.01
                                 rep: 42/50
                                                steps:
                                                             51
                                                                   error: 493887.4038
                                                                                         time: 0.74 secs
## hidden: 3
                 thresh: 0.01
                                 rep: 43/50
                                                steps:
                                                                   min thresh: 3645.055923
                                                        stepmax
## hidden: 3
                 thresh: 0.01
                                 rep: 44/50
                                                steps:
                                                             53
                                                                    error: 493887.4038
                                                                                         time: 0.77 secs
## hidden: 3
                 thresh: 0.01
                                 rep: 45/50
                                                steps:
                                                             46
                                                                    error: 493887.4038
                                                                                         time: 0.66 secs
## hidden: 3
                 thresh: 0.01
                                 rep: 46/50
                                                steps:
                                                             57
                                                                    error: 493887.4038
                                                                                         time: 0.82 secs
## hidden: 3
                 thresh: 0.01
                                 rep: 47/50
                                                                                         time: 1.07 secs
                                                steps:
                                                             54
                                                                    error: 493887.4038
## hidden: 3
                 thresh: 0.01
                                 rep: 48/50
                                                steps:
                                                             66
                                                                    error: 493887.4038
                                                                                         time: 1.11 secs
## hidden: 3
                                                             58
                 thresh: 0.01
                                 rep: 49/50
                                                steps:
                                                                    error: 493887.4038
                                                                                         time: 1.03 secs
## hidden: 3
                 thresh: 0.01
                                 rep: 50/50
                                                steps:
                                                             69
                                                                    error: 493887.4038
                                                                                         time: 1.28 secs
```

Removing the target variable from the validation set to make predictions

```
copy_bin_valid <- binarized_valid
copy_bin_valid$RISK_MM <- NULL

pred_nn <- neuralnet::compute(nn, copy_bin_valid)
predicted_values <- pred_nn$net.result</pre>
```

• Simple neural network resulted in a MSE = 75.35

```
MSE(y_pred = predicted_values, y_true = validation$RISK_MM)
```

## [1] 75.35606684

## Conclusion

- Research Question 1 Regarding the logistic regression model and important feature detection method (Burota algorithm), we can predict with 85% accuracy whether it'll rain tomorrow. To answer research question, "Which weather features can most accurately predict whether it will rain tomorrow?", we have 14 important variable that predicts the rain with 85% accuracy and we identified 4 unimportant features as Location, Season, WinDir3pm and WindSpeed9am that they don't change model accuracy. We assume to have better accuracy and recall score by using more advanced classification models which can be computationally heavy and also unsupervised models to identify best predictors.
- Research Question 2

When interpreting the model results for research question 2, the linear regression model including all variables from the dataset performed best in predicting the amount of rain tomorrow. To answer the research question, "how accurate can weather measurements from today predict the amount of rain that will fall tomorrow?", our models did not predict the amount of rain very accurately. The best model had a high mean squared error and the R<sup>2</sup> score was very low, which shows that the model did not explain a lot of variability in the target variable RISK\_MM and thus does not fit the data well. We expect to get more accurate results with a more computationally expensive neural network, when normalizing the numerical variables on beforehand and when increasing the amount of steps and repetitions the network may make.

# Task Distribution

Report writing and data processing have been done together and the seperation of the other tasks are as below;

- Vicky Mekes worked on research question 1 by doing PCA &KNN
- Sema Karan worked on research question 1 by doing EDA, Logistic Reg., Burato feature selection
- Shelly van Erp worked on research question 2 by doing Forward/Backward Selection, Linear Model and Deep Learning.