

DAE PROJECT

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PRESENTATION

INSTRUCTOR - NIL KAMAL HAZRA

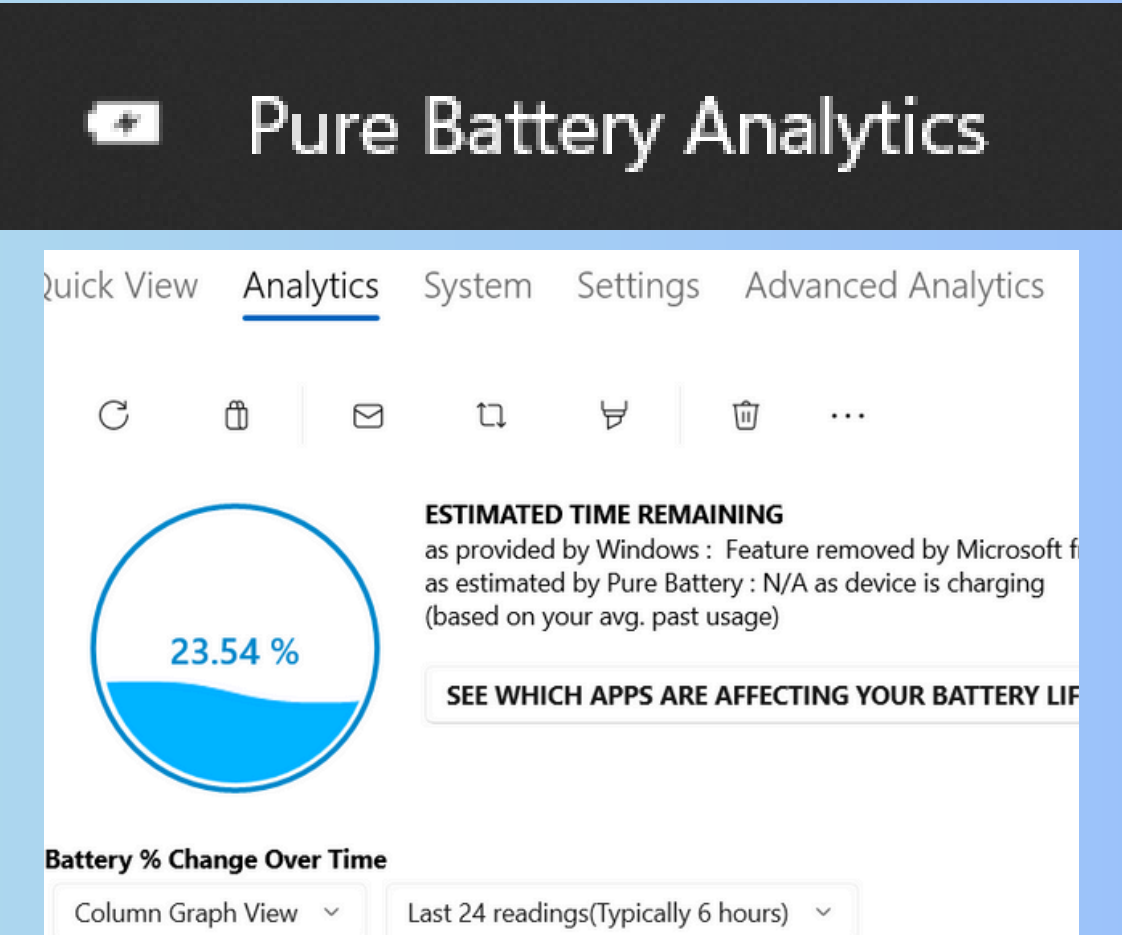
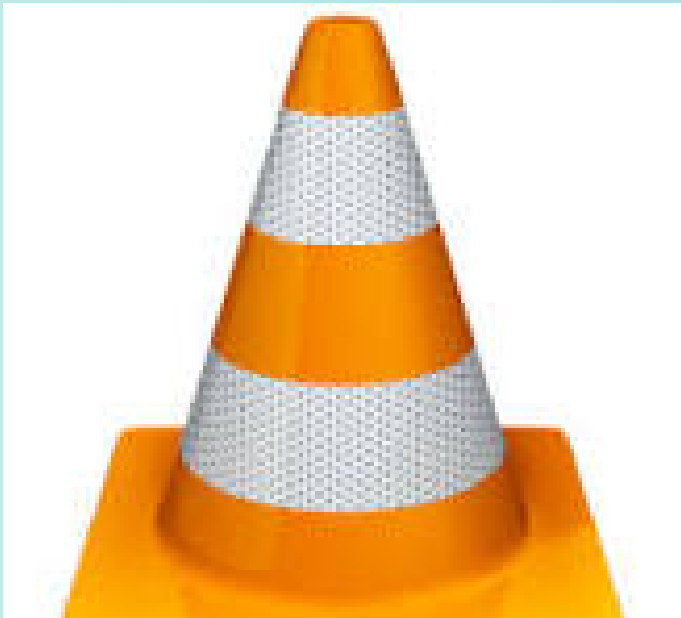
GROUP 6

GROUP MEMBERS

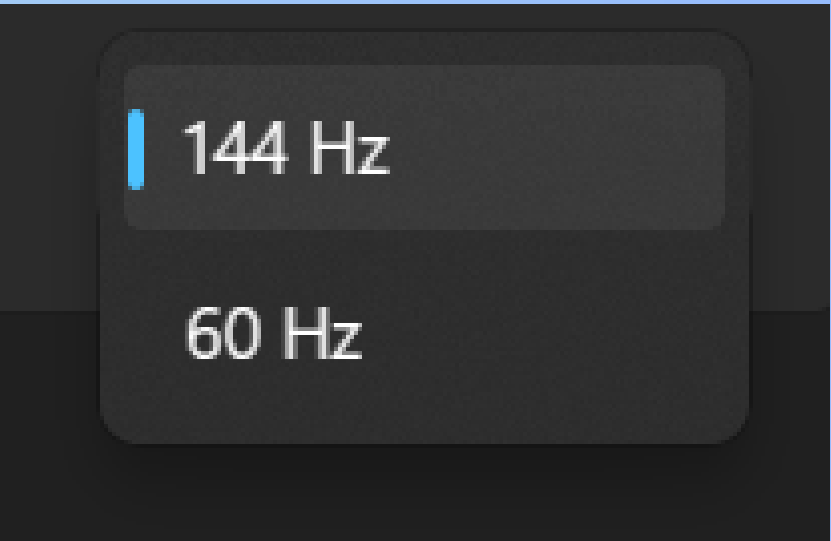
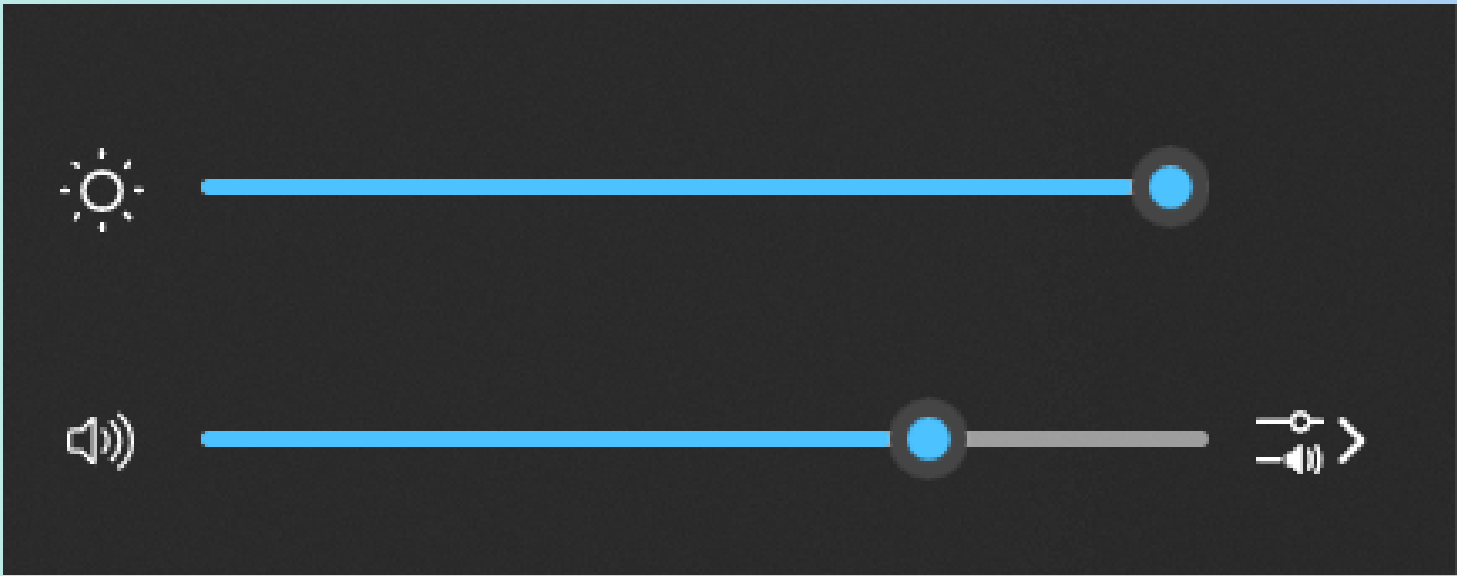
TEAM MEMBERS :

1. Aditya Anand (B21ES003)
2. Vinit (B22ES026)
3. Aditya Padhy (B22ES005)
4. Harsh (B22ES027)
5. Karan (B22ES019)
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7. Girish (B22CY002)

EXP - INTRO



- 1920 × 1080 (Recommended)
- 1760 × 990
- 1680 × 1050
- 1600 × 900
- 1366 × 768
- 1280 × 1024
- 1280 × 720
- 1128 × 634
- 1024 × 768
- 800 × 600



Objective: Analyzing various factors and their impact on LAPTOP Battery life .

Through our experiment we came across various factors which affect the battery life of the laptop , but we will be considering **refresh rate, brightness, resolution and speaker** for our experiment.

Tools Used:

- RStudio
- Battery Analytics Application
- Stopwatch
- Hp Laptop

NOTATIONS:

- A = Refresh Rate
- B = Brightness
- C = RESOLUTION
- D = SPEAKER VOL.

	A-Refresh Rate		B-Brightness		C-RESOLUTION		D-SPEAKER.		RATE
	60Hz(Low)	144Hz(High)	0(Low)	100(High)	900x600p	1920x1080p	NO(MUTE)	YES(VOL)	(%DISCHARGE /Hrs.)
1									31.08
a									39.84
b									37.68
ab									59.68
c									31.32
ac									37.32
bc									35.4
abc									56.72
d									34.2
ad									43.08
bd									38.52
abd									61.36
cd									32.76
acd									39
bcd									37.08
abcd									60.04

There are 4 factors and 2 levels of each high on low.
Based on different combination of factor levels the observations have been made.

INDICATORS :

LOW LEVELHIGH LEVEL

As it can be seen in the table when all the factors are high the battery drainage is highest and least when all are at low level.

```
> Design.matrix
```

	I	A	B	AB	C	AC	BC	ABC	D	AD	BD	ABD	CD	ACD	BCD	ABCD	Rate
(1)	1	-1	-1	1	-1	1	1	-1	-1	1	1	-1	1	-1	-1	1	31.08
a	1	1	-1	-1	-1	-1	1	1	-1	-1	1	1	1	1	-1	-1	39.84
b	1	-1	1	-1	-1	1	-1	1	-1	1	-1	1	1	-1	1	-1	37.68
ab	1	1	1	1	-1	-1	-1	-1	-1	-1	-1	-1	1	1	1	1	59.68
c	1	-1	-1	1	1	-1	-1	1	-1	1	1	-1	-1	1	1	-1	31.32
ac	1	1	-1	-1	1	1	-1	-1	-1	-1	1	1	-1	-1	1	1	37.32
bc	1	-1	1	-1	1	-1	1	-1	-1	1	-1	1	-1	1	-1	1	35.40
abc	1	1	1	1	1	1	1	1	-1	-1	-1	-1	-1	-1	-1	-1	56.72
d	1	-1	-1	1	-1	1	1	-1	1	-1	-1	1	-1	1	1	-1	34.20
ad	1	1	-1	-1	-1	-1	1	1	1	1	-1	-1	-1	-1	1	1	43.08
bd	1	-1	1	-1	-1	1	-1	1	1	-1	1	-1	-1	1	-1	1	38.52
abd	1	1	1	1	-1	-1	-1	-1	1	1	1	1	-1	-1	-1	-1	61.36
cd	1	-1	-1	1	1	-1	-1	1	1	-1	-1	1	1	-1	-1	1	32.76
acd	1	1	-1	-1	1	1	-1	-1	1	1	-1	-1	1	1	-1	-1	39.00
bcd	1	-1	1	-1	1	-1	1	-1	1	-1	1	-1	1	-1	1	-1	37.08
abcd	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	60.04

This is the design matrix for our experiment

A design matrix organizes data for regression analysis. Rows represent observations, columns represent predictors, and one column is for the response variable. It helps estimate coefficients for predictors and interpret their relationship with the response.

```
> eff=cbind(Ieff,Feff)
```

```
> eff
```

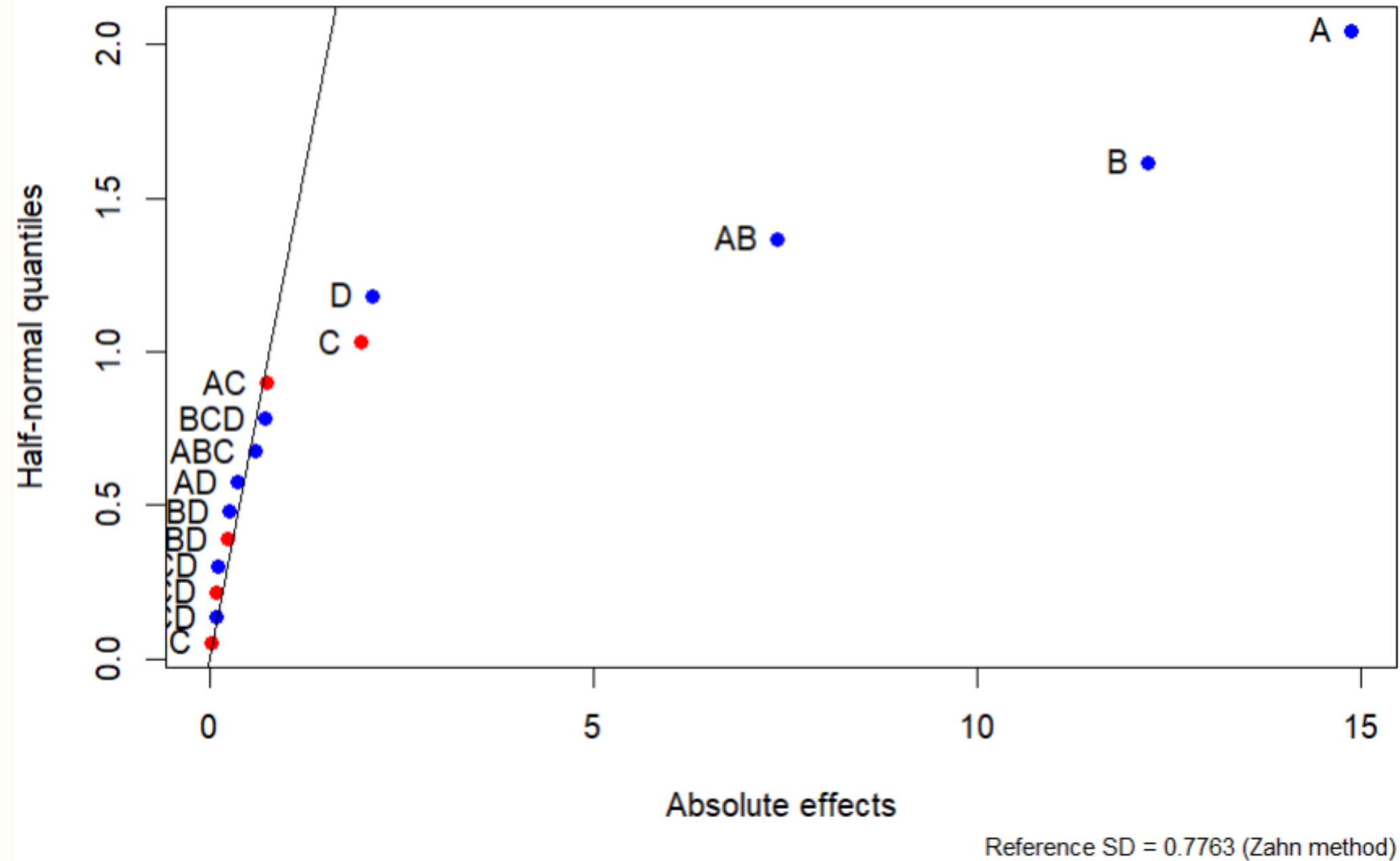
	I	A	B	AB	C	AC	BC
Rate	42.1925	14.875	12.235	7.405	-1.975	-0.745	-0.025

ABC	D	AD	BD	ABD	CD	ACD	BCD	ABCD
0.605	2.125	0.355	-0.245	0.265	-0.095	0.115	0.715	0.085

>> FROM ABOVE RESULT WE CAN SEE WE HAVE BOTH +VE AND -VE EFFECT OF FACTORS ON RATE OF DISCHARGE

TO GET VISUAL DIFF. WE USE Half normal plot

A half-normal plot assesses if data follow a normal distribution. Points form a straight line if data are normal. Deviations suggest non-normality, requiring further examination or alternative methods.



Half normal plot

The **red points** in the plot show that the factors have Negative effects. The **blue points** in show that the factors have Positive effects.

From the obtained plot, we get that the main factor **effects A and B are highly significant. Others C & D are less significant**

The Interaction **Effect AB** is also far from the line to be considered as significant Here

```

> pilotEff
      A      B      AB      C      AC      BC      ABC      D      AD      BD      ABD      CD      ACD      BCD      ABCD
14.875 12.235  7.405 -1.975 -0.745 -0.025  0.605  2.125  0.355 -0.245  0.265 -0.095  0.115  0.715  0.085
attr(,"mean")

42.1925
> hnplot(pilotEff,ID=0)

```

Regression Model

Factor effects refer to the influence or impact that each factor has on the response variable.

In a regression model, the coefficients indicate how much the response variable is expected to change for a one-unit change in the corresponding factor, while holding all other factors constant. Hence the coefficients turn out to be (factor effect)/2.

For example, in a 2^2 factorial design (where $k = 2$), if you have factors A and B, the regression model might look like this:

$$\underline{Y = \beta_0 + \beta_1 A + \beta_2 B + \beta_{12} AB + \epsilon}$$

Here, β_0 represents the intercept, β_1 represents the effect of factor A, β_2 represents the effect of factor B, and β_{12} represents the interaction effect between factors A and B.


```

Call:
lm.default(formula = Factors ~ B * A, data = data.rate)

Residuals:
    Min       1Q   Median       3Q      Max
-2.73  -1.08   0.13   0.78   3.27

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)  42.1925     0.4595   91.822  < 2e-16 ***
B             6.1175     0.4595   13.313 1.51e-08 ***
A            7.4375     0.4595   16.186 1.62e-09 ***
B:A          3.7025     0.4595    8.058 3.49e-06 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.838 on 12 degrees of freedom
Multiple R-squared:  0.9768,    Adjusted R-squared:  0.9709
F-statistic: 168.1 on 3 and 12 DF,  p-value: 4.585e-10

```

In this case

$yp = 42.1925 + 7.4375 x_1 + 6.1175 x_2 + 3.7025 x_1 x_3$

Here x_1 , x_2 are levels of A and B respectively for each exp.

>Residuals are the differences between the observed values and the predicted values from the regression model that represent the errors or unexplained variance

|
>> $e(x) = y_{actual} - y_{predicted}$

```

> residuals=mod$res
> residuals

```

```

     1     2     3     4     5     6     7     8     9    10    11    12    13
-1.26  0.03  0.51  0.23 -1.02 -2.49 -1.77 -2.73  1.86  3.27  1.35  1.91  0.42
    14    15    16
-0.81 -0.09  0.59

```

**Low P-value means
the null hypothesis
that coefficients of
model is zero is
rejected.**

The coefficient of **multiple determination R^2** is defined by

$$\underline{R^2 = SSR/SST = 1 - SSE/SST} \quad (\text{Given value for the model} = \mathbf{0.9768})$$

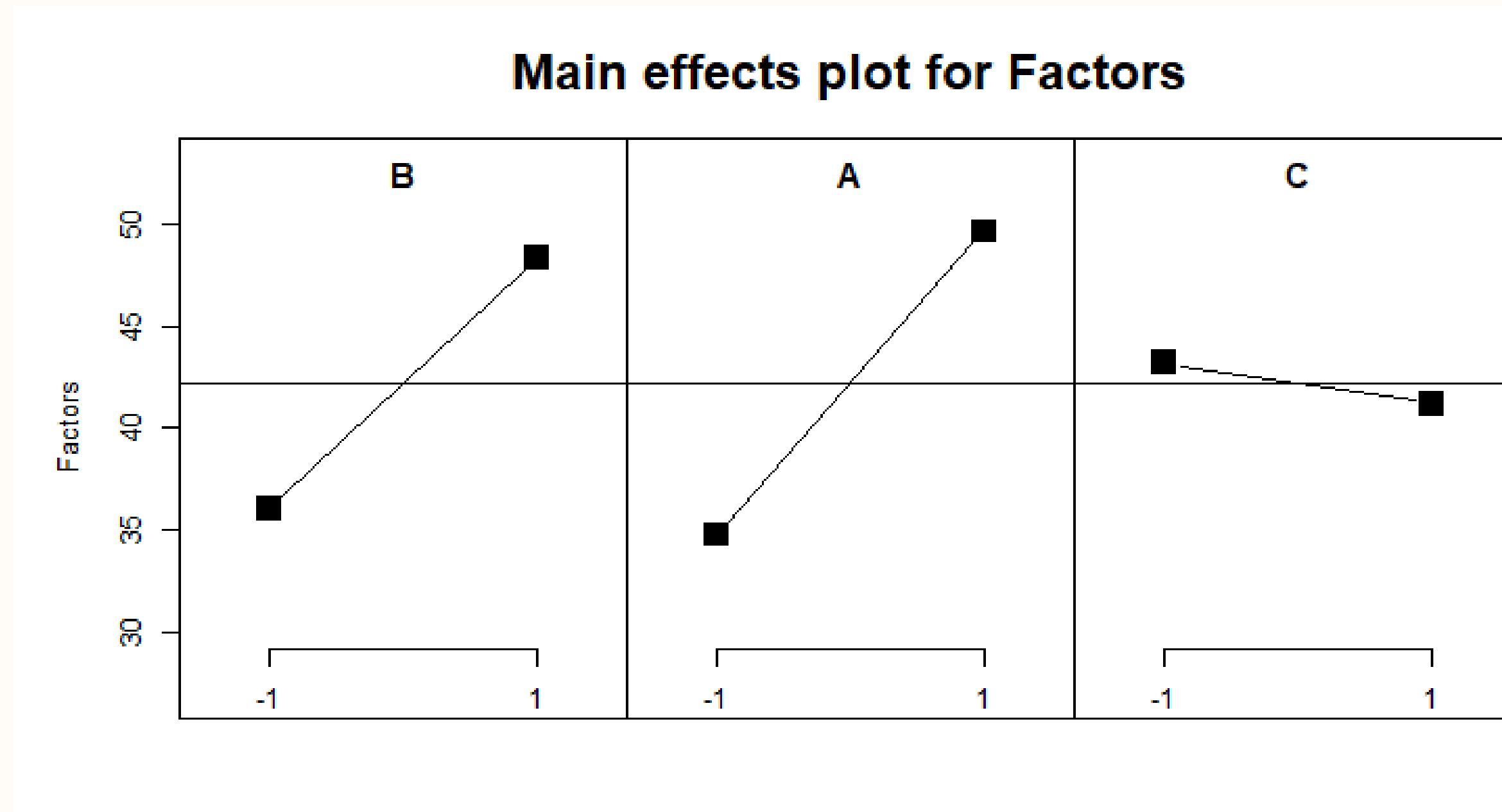
.Drawbacks: A large value of R^2 does not necessarily imply that the regression model is a good one. Adding a variable to the model will always increase R^2 , regardless of whether the additional variable is statistically significant or not.

The coefficient of **adjusted R^2** is defined by

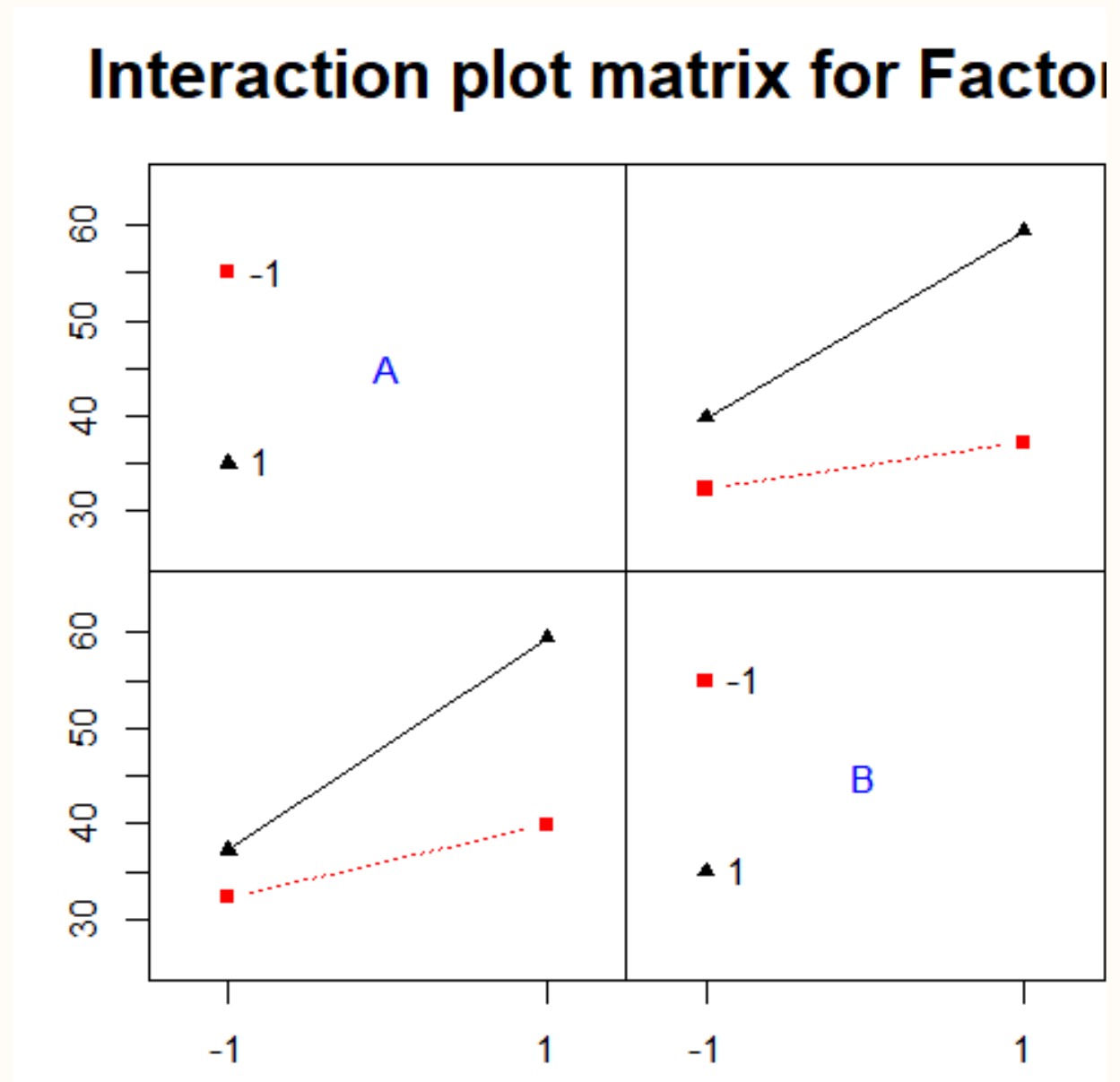
$$\underline{R^2 = 1 - SSE/SST * (n-1)/(n-k-1)} \quad (\text{Given value for the model} = \mathbf{0.9709})$$

R^2 adj will increase only by adding a variable that reduces the MSE , i.e., enhances MSR i.e., the addition of the variable has a significant contribution in the response.

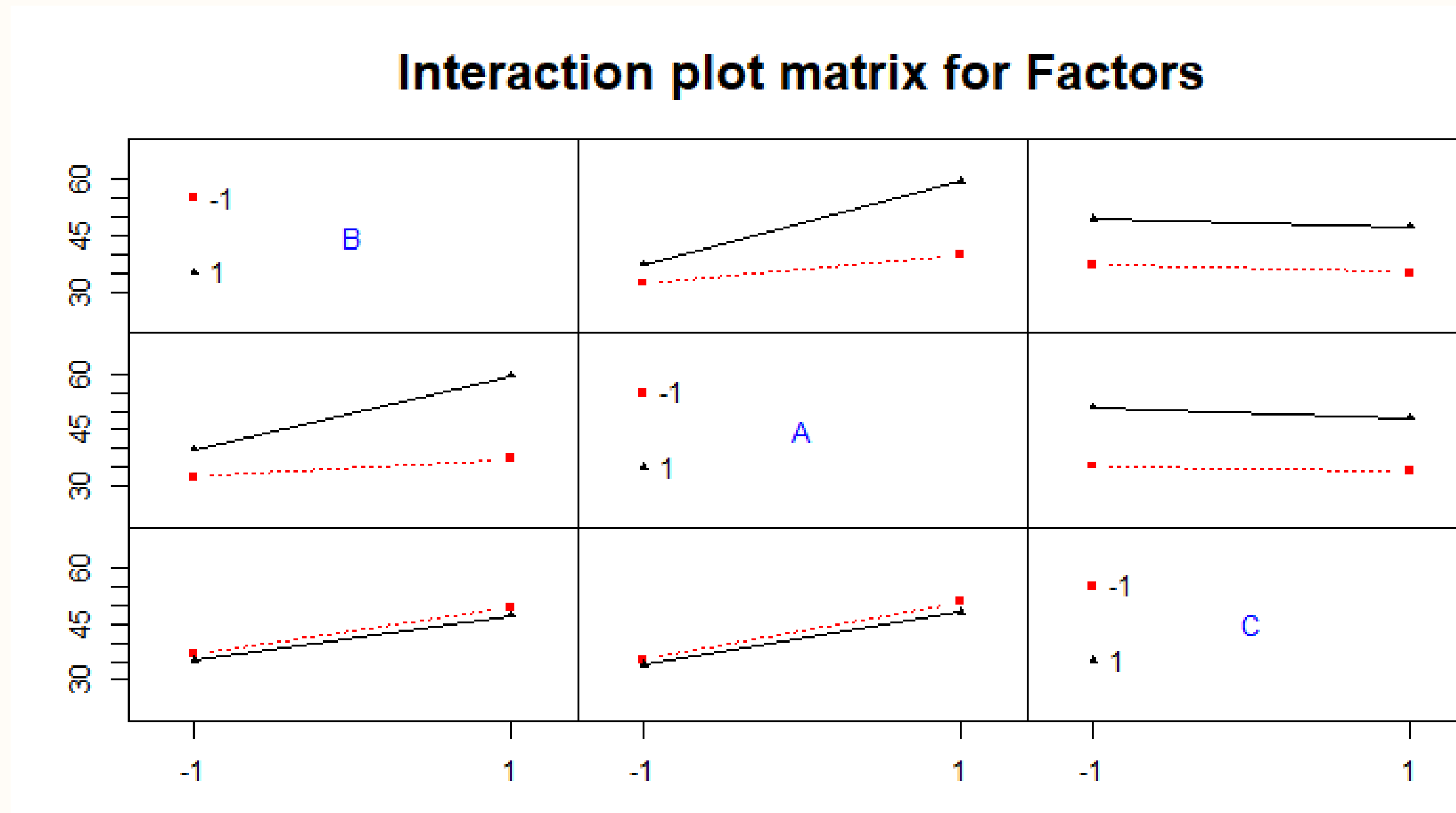
Factor C(Resolution) has a Negative effect Surprising. Means better resolution is good for battery life. May be due to inbuilt internal optimization



Here also we see that the factor C has lesser (as compared to A and B) and inverse impact on the battery drainage.



- In GRAPHS, the **black line signifies the high level of factor A and B respectively .**
The red line signifies the low level of factor A and B respectively .
- OBSERVATION says as in each block, as **the lines are not parallel to each other,**
hence, the interactions between these factors A and B are significant.



- Here we see that keeping B constant at low level when A is changed from -1 to 1 the difference in response is not that large. It is significant when B is high and vice versa.
- Here we see that A and C, also B and **C don't interact much as the lines are quite parallel.**

Design Projection ANOVA(by omitting factors C and D)

```
##### Design Projection #####
values <- matrix(c(31.08, 31.32, 34.2, 32.76,
                  39.84, 37.32, 43.08, 39,
                  37.68, 35.4, 38.52, 37.08,
                  59.68, 56.72, 61.36, 60.04), byrow = TRUE, ncol = 4)
dimnames(values) <- list(c("(1)", "a", "b", "ab"), c("Rep1", "Rep2", "Rep3", "Rep4"))
```

```
> data.mat <- data.frame(A, B, as.vector(values))
> model <- aov(as.vector(values) ~ A*B, data = data.mat)
> summary(model)
```

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
A	1	885.1	885.1	261.99	1.62e-09 ***
B	1	598.8	598.8	177.24	1.51e-08 ***
A:B	1	219.3	219.3	64.92	3.49e-06 ***
Residuals	12	40.5	3.4		

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Above, shows factors A and B are highly significant.

USING MULTIPLE LEVEL FOR FACTOR A and B

HIGH, MID, LOW

Multiple levels of significant factors			
A-Refresh Rate	B-Brightness		
RATE	L1-0	L2 -50	L3 -100
144	42.44	50.11	63.2
90	36.3	42.1	49.8
60	34.1	35.7	37.89

```
> data.rate
refresh_rate brightness_level rate
1          144Hz           L1 42.44
2           90Hz           L1 36.30
3           60Hz           L1 34.10
4          144Hz           L2 50.11
5           90Hz           L2 42.10
6           60Hz           L2 35.70
7          144Hz           L3 63.20
8           90Hz           L3 49.80
9           60Hz           L3 37.89
```

```
> summary(rate.aov)
              Df Sum Sq Mean Sq F value Pr(>F)
refresh_rate    2  387.7   193.86  10.398 0.0260 *
brightness_level 2  244.8   122.39   6.565 0.0545 .
Residuals       4   74.6    18.64
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

**FROM Above results we find that compared to Brightness (B) Refresh Rate (A)
is more significant**

LSD

LSD, or Least Significant Difference, is used to compare means of different groups after an ANOVA test. It determines if the difference between two group means is statistically significant.

>>If the difference is larger than the LSD value, it suggests a significant difference.

**Obtained the rates into groups
are as follows into a,b & ab**

Where $\alpha = 0.05$

```
$comparison
NULL

$groups
      rate groups
63.2  63.20      a
50.11 50.11     ab
49.8  49.80     ab
42.44 42.44      b
42.1  42.10      b
37.89 37.89      b
36.3  36.30      b
35.7  35.70      b
34.1  34.10      b

attr(,"class")
[1] "group"
>
```


TUKEY HSD

Tukey's HSD (Honestly Significant Difference) compares means of different groups after ANOVA, determining if differences are statistically significant.

\$refresh_rate					
	diff	lwr	upr	p	adj
90Hz-60Hz	6.836667	-5.728199	19.40153	0.2424679	
144Hz-60Hz	16.020000	3.455134	28.58487	0.0226806	
144Hz-90Hz	9.183333	-3.381532	21.74820	0.1224995	

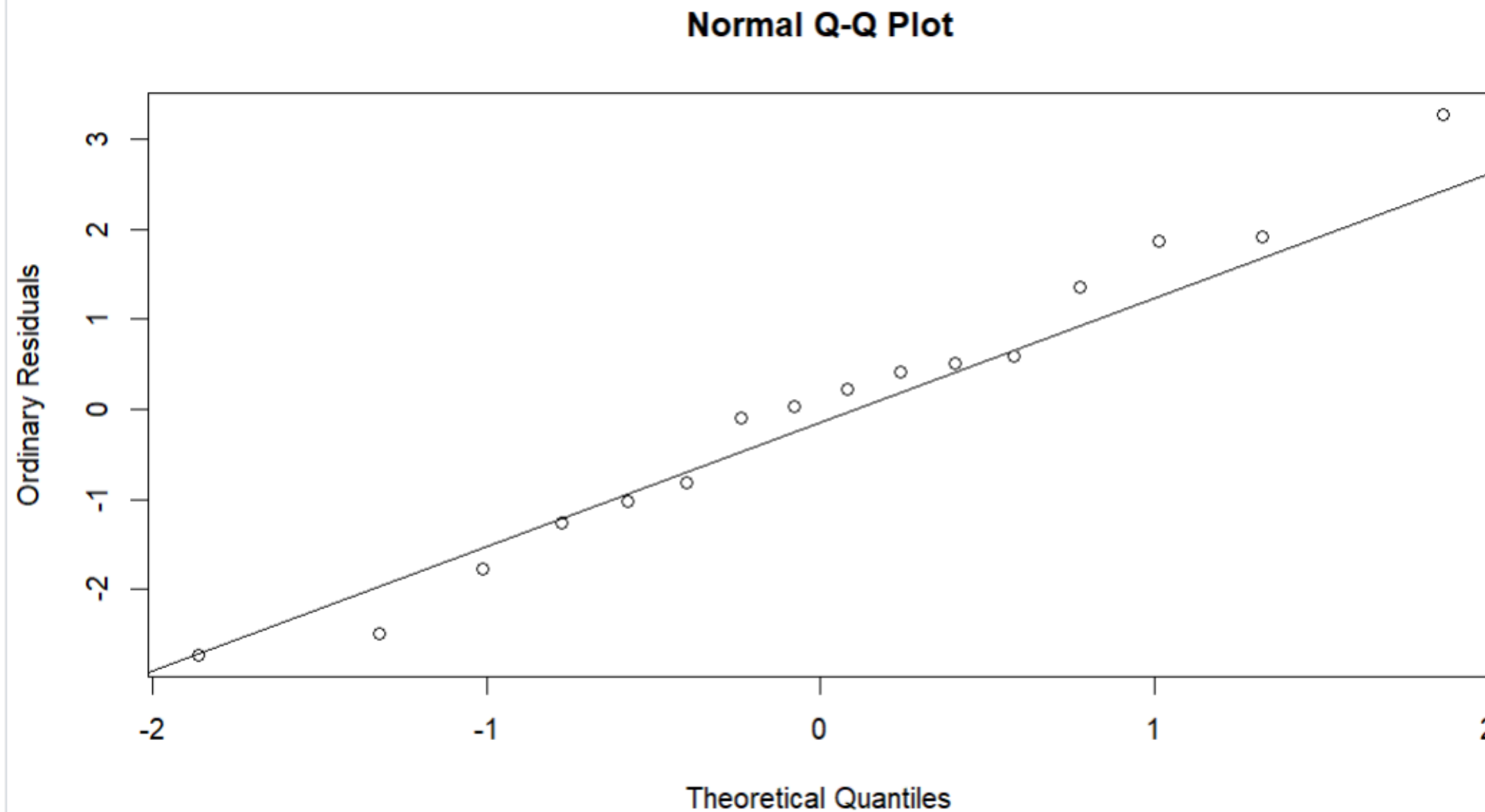
\$brightness_level					
	diff	lwr	upr	p	adj
L2-L1	5.023333	-7.5415323	17.58820	0.4122775	
L3-L1	12.683333	0.1184677	25.24820	0.0485634	
L3-L2	7.660000	-4.9048657	20.22487	0.1901441	

Above, shows factors A & B have impact on each level where conf. Level = 0.95

- For Factor A-Refresh rate : there more difference between mid to high than low to mid shows there is higher variation on high Refresh rate .
- For Factor B-Brightness level : there more difference between mid to high than low to mid shows there is higher variation on high Brightness . >>**NOT LINEARLY INCREASING**
- Rate of Discharging: 144Hz > 90Hz > 60Hz & L3>L2>L1

qq-plot

A Q-Q plot compares the quantiles of a dataset to those of a theoretical distribution.



Deviations from the line indicate departures from the expected distribution, such as heavier or lighter tails. Outliers may also be identified.

Above , The residuals Exactly follow the normal distribution.

Dunnnett's Test

```
> dunnnett= DunnnettTest(data.rate$rate,g, control="144Hz", conf.level=0.95)
> dunnnett
```

```
Dunnnett's test for comparing several treatments with a control :
  95% family-wise confidence level
```

```
$`144Hz`
```

	diff	lwr.ci	upr.ci	pval
60Hz-144Hz	-16.020000	-33.09204	1.052035	0.0625 .
90Hz-144Hz	-9.183333	-26.25537	7.888702	0.2830

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

**144 Hz is our control Group at
95% confidence Interval.**

- In Dunnnett's test, the control group is used to assess whether there are significant differences between the control and other treatments.
- The test compares treatments with a control group and calculates differences, confidence intervals, and p-values for each comparison. Low p-values w.r.t confidence interval suggest significant differences, while high p-values indicate treatments are comparable to the control.

CONCLUSIONS OF ANALYSIS

Effects of Refresh Rate & Brightness are highly significant. Others RESOLUTION & SOUND are less significant .

Factor C(Resolution) has a Negative effect. Means better resolution is good for battery life.

Compared to Brightness (B) Refresh Rate (A) is more significant.

Rate of Discharging: 144Hz > 90Hz > 60Hz & L3>L2>L1

NOT LINEARLY INCREASING

IDEAL CONDITION TO SET FACTORS

REFRESH RATE - 60Hz

RESOLUTION - HIGH (RECOMMENDED)

BRIGHTNESS - ON LOWER SIDE

SPEAKER VOL - NOT MATTER MUCH