

University of California, Davis  
Dept. of Mechanical and Aerospace Engineering  
MAE 275

**Homework Assignment 3**

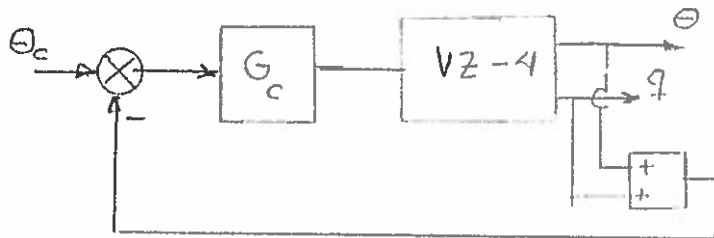
**Due: Thursday, April 30**

Consider the VZ-4 "Doak" vehicle in the hover flight condition given in Appendix A of the reader. Concentrate on the longitudinal motion.

- 1.) Determine the open-loop eigenvalues. How many modes of motion are there?
- 2.) Using MATLAB, determine the following transfer functions:  $\frac{\theta}{\delta e}(s)$  and  $\frac{q}{\delta e}(s)$

Note that, in hover, the action of the "elevator" is replaced by the force generated by the rear thruster.

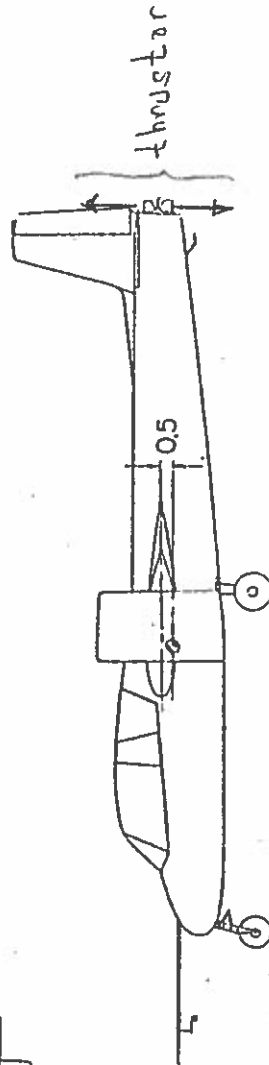
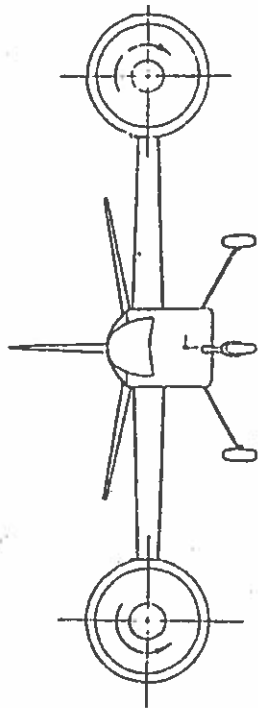
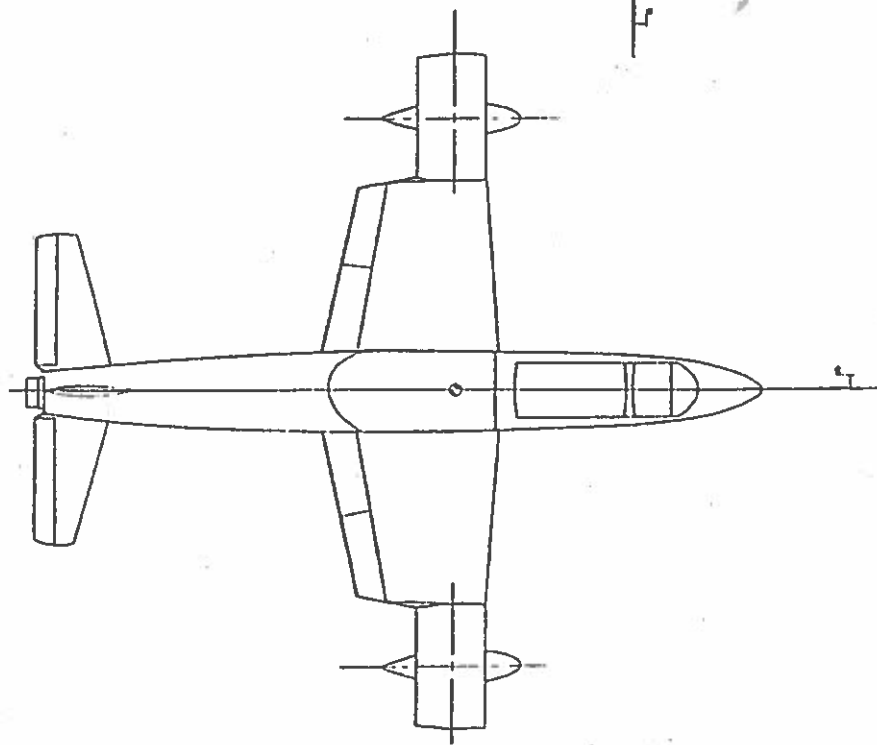
- 3.) Assume that an attitude gyro and a rate gyro are available to measure  $\theta(t) + q(t)$ . The control system below is to be designed and simulated, with the determination of  $G_c$  as the design objective.



- a.) Using loop-shaping principles, determine  $G_c$  such that:
  - i.) The closed-loop system is stable
  - ii.) The  $G_c$  has more poles than zeros.
  - iii.) The closed-loop bandwidth (-3 dB criterion) is at least 5 rad/sec
  - iv.) The gain and phase margins are at least 6 dB and 40 deg. Sketch the Nyquist diagram and show these margins (which can be determined from the open-loop Bode diagram).
  - v.) There is zero steady-state error to a step input  $\theta_c$
- 4.) Create a Simulink simulation of your system and demonstrate the pitch attitude response to a pitch attitude command of 5 deg (5/57.3 rad). Filter your step command with a filter given by  $10^2/(s^2+20s+10^2)$ . Note that the pitch attitude command can be considered as coming from the pilot's control stick.

Your solution should include

- 1.) the A, B, C, D matrices of the vehicle with no feedback.
- 2.) Open-loop eigenvalues and determination of number of modes
- 3.) Appropriate open and closed-loop Bode plots with the compensated open-loop Bode diagram showing the gain and phase margins
- 4.) Nyquist plot sketch indicating the gain and phase margins
- 5.)  $G_c$
- 6.) Simulink diagram
- 7.) Step response



VZ-4

