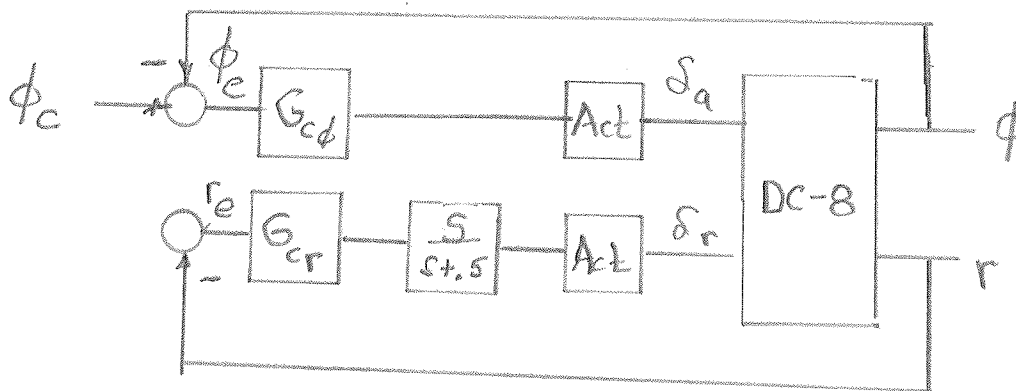


MAE-275

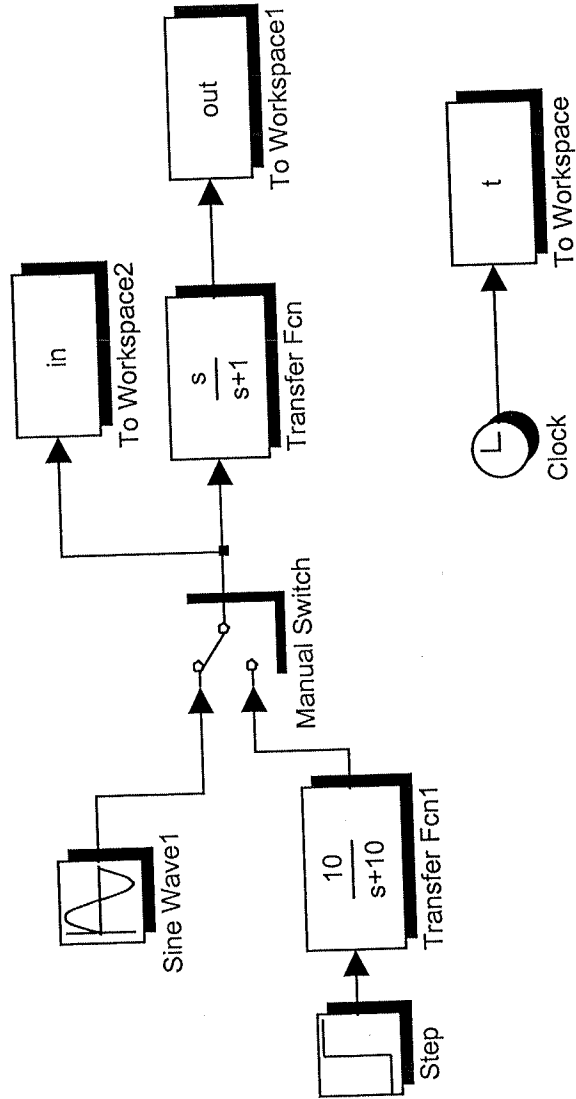
Design Example

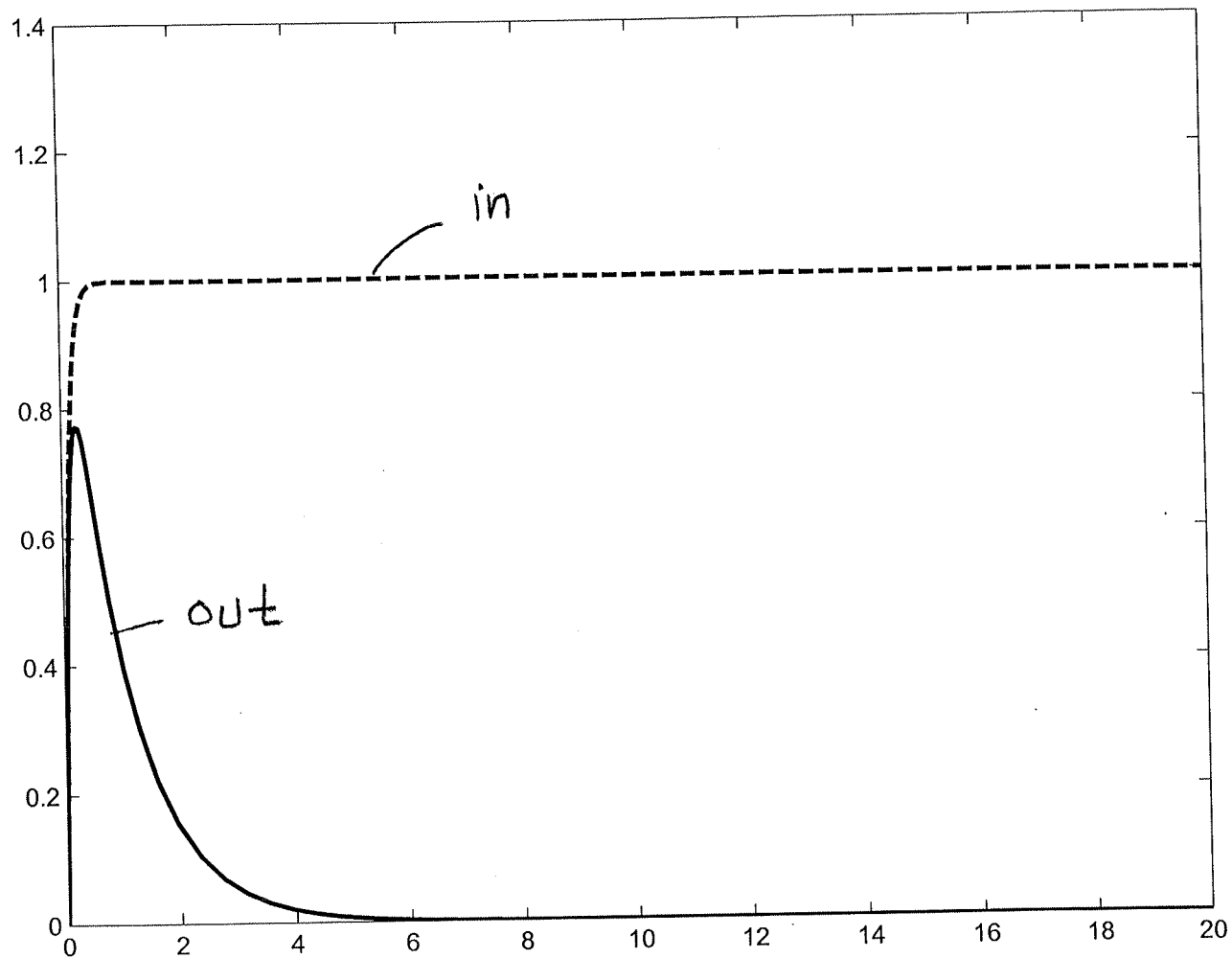


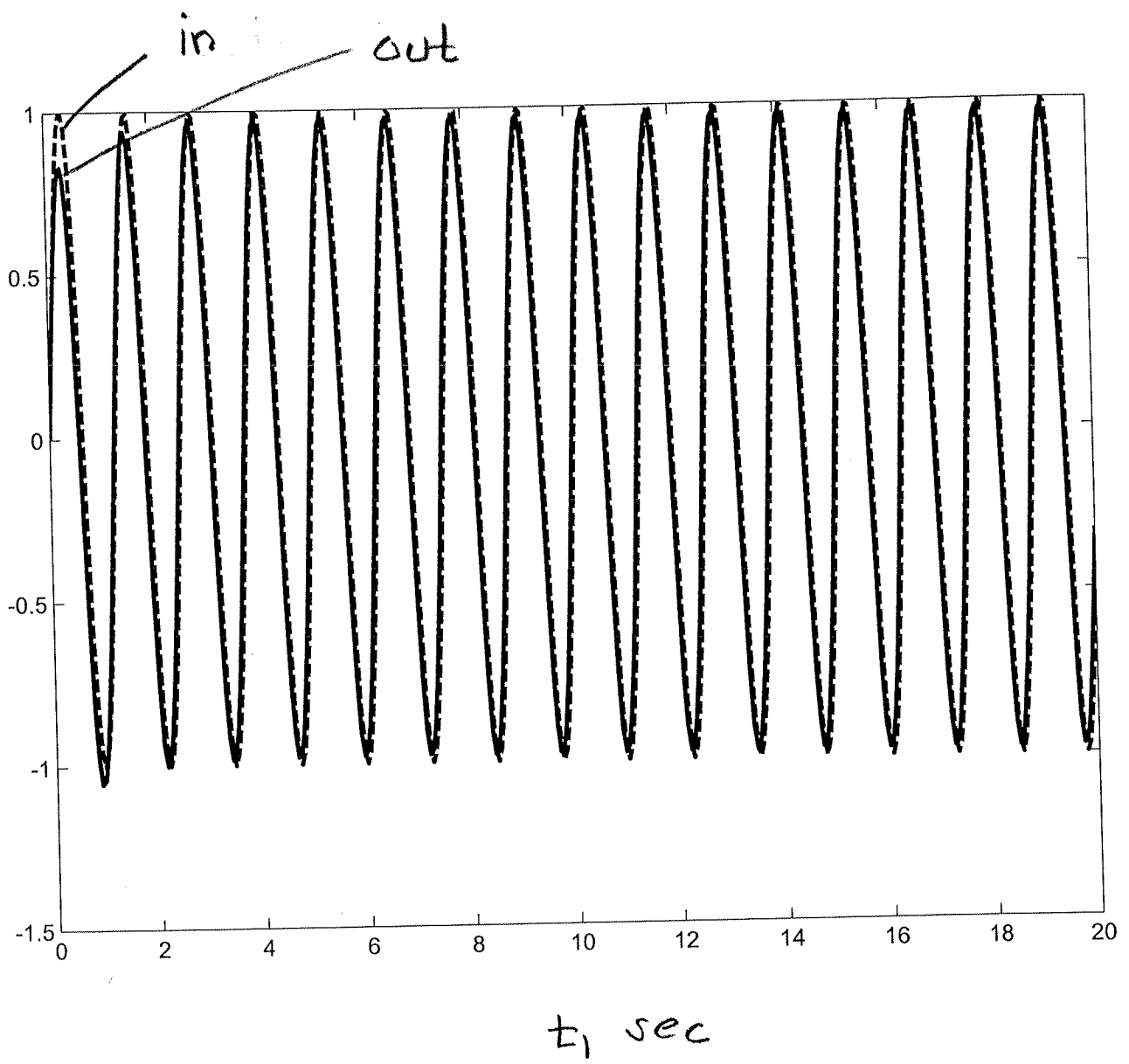
$$\omega_{B\phi} \approx 6 \text{ rad/sec}$$

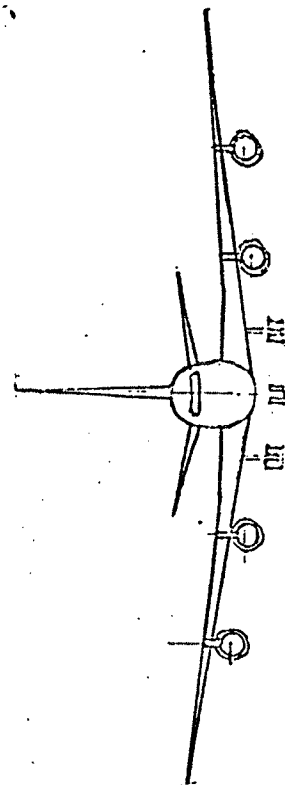
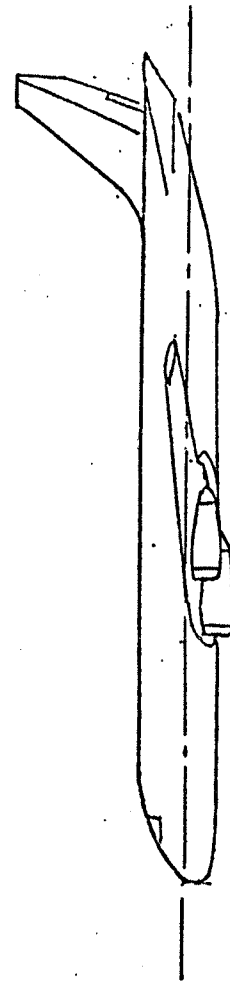
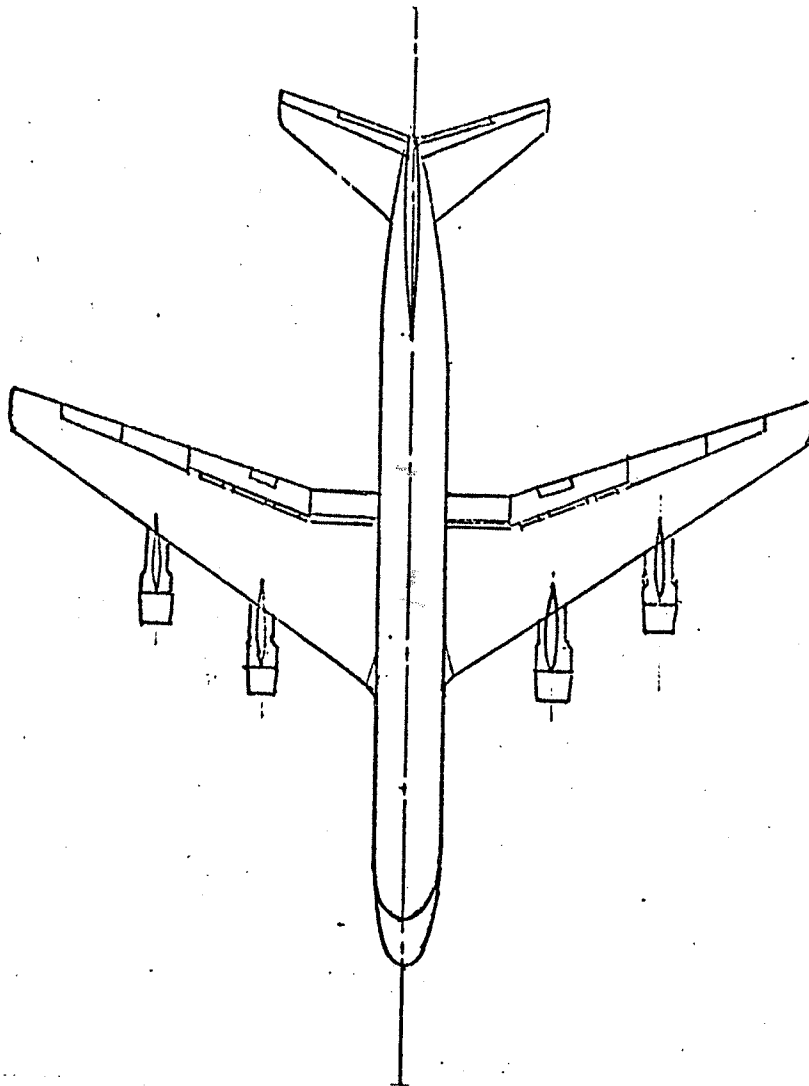
$$\omega_{B_r} \approx 2 \text{ rad/sec}$$

WASHOUT.









DC-8

TABLE A-5

A. GEOMETRICAL AND INERTIAL PARAMETERS FOR THE DC-8

Note: Data are for body-fixed stability axes

$$s = 2600 \text{ ft}^2, \quad b = 142.3 \text{ ft}, \quad c = 23 \text{ ft}, \quad \gamma_0 = 0 \text{ deg}$$

	FLIGHT CONDITION			
	8001 APPROACH	8002 HOLDING	8003 CRUISE	8004 V_{NE}
h (ft)	0	15,000	33,000	33,000
M (-)	0.219	0.443	0.84	0.88
a (ft/sec)	1117	1058	982	982
ρ (slugs/ft ³)	0.002378	0.001496	0.000795	0.000795
V_{T_0} (ft/sec)	243.5	468.2	824.2	863.46
$\bar{q} = \rho V^2/2$ (lb/ft ²)	71.02	163.97	270.0	296.36
W (lb)	190,000	190,000	230,000	230,000
m (slugs)	5900	5900	7143	7143
I_x (slug-ft ²)	3,090,000	3,110,000	3,770,000	3,770,000
I_y (slug-ft ²)	2,940,000	2,940,000	3,560,000	3,560,000
I_z (slug-ft ²)	5,580,000	5,880,000	7,130,000	7,130,000
I_{xz} (slug-ft ²)	28,000	-64,500	45,000	53,700
$x_{c.g./\bar{c}}$	0.15	0.15	0.15	0.15
θ_0 (deg)	0	0	0	0
U_0 (ft/sec)	243.5	468.2	824.2	863.46
W_0 (ft/sec)	0	0	0	0
δ_F (deg)	35	0	0	0

D. LATERAL DIMENSIONAL DERIVATIVES FOR THE DC-8

Note: Data are for body-fixed stability axes

	FLIGHT CONDITION			
	8001	8002	8003	8004
h (ft)	0	15,000	33,000	33,000
M (-)	0.219	0.443	0.84	0.88
Y_v (1/sec)	-0.1113	-0.1008	-0.0868	-0.0931
Y_β [(ft/sec ²)/rad]	-27.1	-47.2	-71.5	-80.4
Y_{δ_a} [(ft/sec ²)/rad]	0	0	0	0
$Y_{\delta_a}^*$ [(1/sec)/rad]	0	0	0	0
Y_{δ_r} [(ft/sec ²)/rad]	5.79	13.48	18.33	20.12
$Y_{\delta_r}^*$ [(1/sec)/rad]	0.0238	0.0288	0.0222	0.0233
L_β (1/sec ²)	-1.335	-2.68	-4.43	-5.05
L_p (1/sec)	-0.95	-1.233	-1.18	-1.289
L_r (1/sec)	0.612	0.391	0.336	0.35
L_{δ_a} (1/sec ²)	-0.726	-1.62	-2.11	-2.3
L_{δ_r} (1/sec ²)	0.1848	0.374	0.559	0.63
L_β' (1/sec ²)	-1.328	-2.71	-4.41	-5.02
L_p' (1/sec)	-0.951	-1.232	-1.181	-1.29
L_r' (1/sec)	0.509	0.397	0.334	0.346
L_{δ_a}' (1/sec ²)	-0.726	-1.62	-2.11	-2.3
L_{δ_r}' (1/sec ²)	0.1813	0.392	0.549	0.612
N_β (1/sec ²)	0.763	1.271	2.17	2.47
N_p (1/sec)	-0.1192	-0.048	-0.01294	-0.00744
N_r (1/sec)	-0.268	-0.252	-0.23	-0.252
N_{δ_a} (1/sec ²)	-0.0496	-0.0365	-0.0519	-0.0615
N_{δ_r} (1/sec ²)	-0.39	-0.86	-1.168	-1.282
N_β' (1/sec ²)	0.757	1.301	2.14	2.43
N_p' (1/sec)	-0.124	-0.0346	-0.0204	-0.01715
N_r' (1/sec)	-0.265	-0.257	-0.228	-0.25
N_{δ_a}' (1/sec ²)	-0.0532	-0.01875	-0.0652	-0.0788
N_{δ_r}' (1/sec ²)	-0.389	-0.864	-0.01164	-1.277

» A

A =

-0.1000	0	-468.2000	32.2000	0
-0.0058	-1.2320	0.3970	0	0
0.0028	-0.0346	-0.2570	0	0
0	1.0000	0	0	0
0	0	1.0000	0	0

» B

B =

0	13.4800
-1.6200	0.3920
-0.0187	-0.8640
0	0
0	0

$$\underline{y} = \begin{Bmatrix} \Delta z \\ \Delta p \\ \Delta r \\ \Delta \phi \\ \Delta \psi \end{Bmatrix}$$

$$\underline{y} = \begin{Bmatrix} \Delta \delta_a \\ \Delta \delta_r \end{Bmatrix}$$

» C

C =

r	0	0	1.0000	0	0
ϕ	0	0	0	1.0000	0
β	0.0021	0	0	0	0

» D

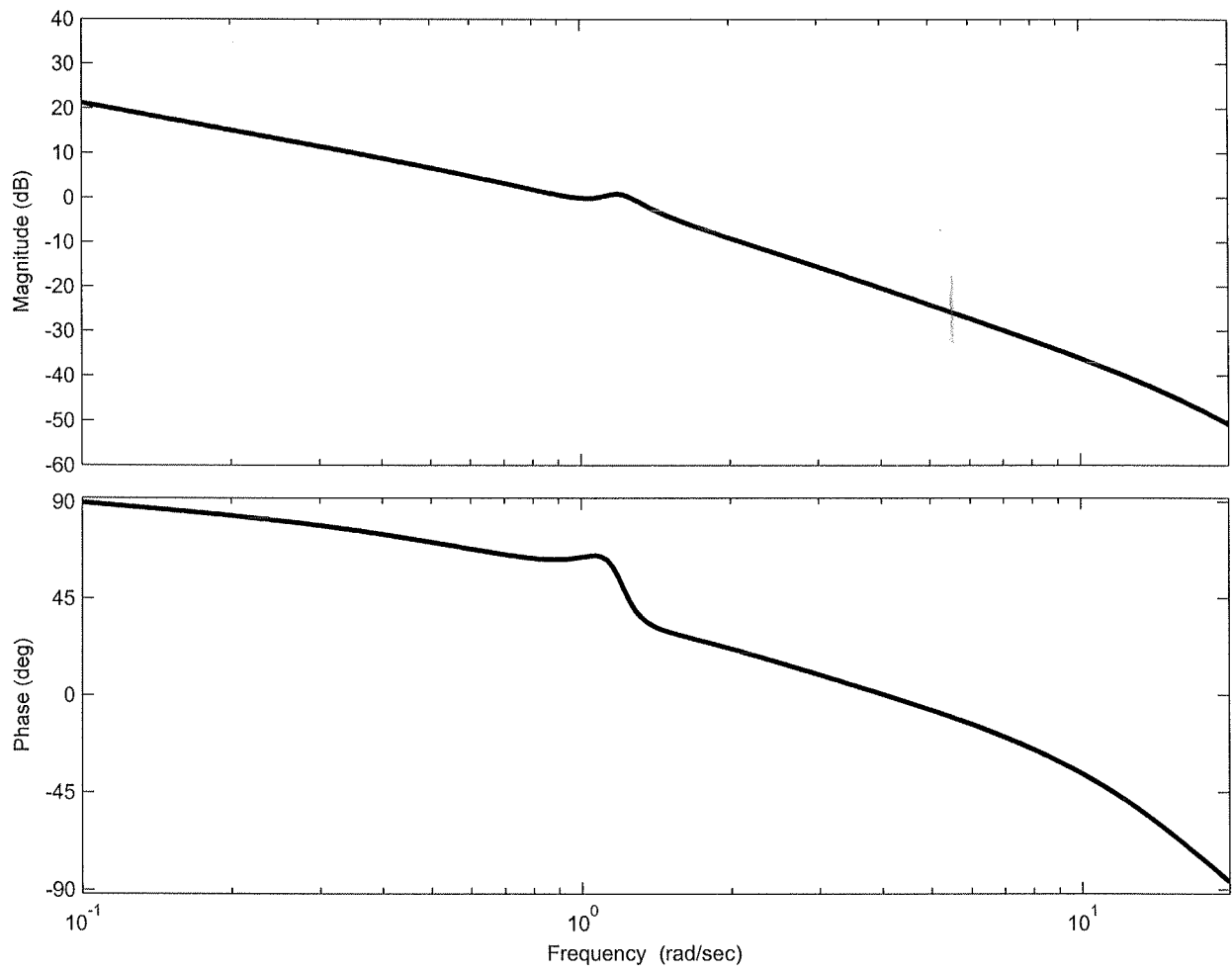
D =

0	0
0	0
0	0

»

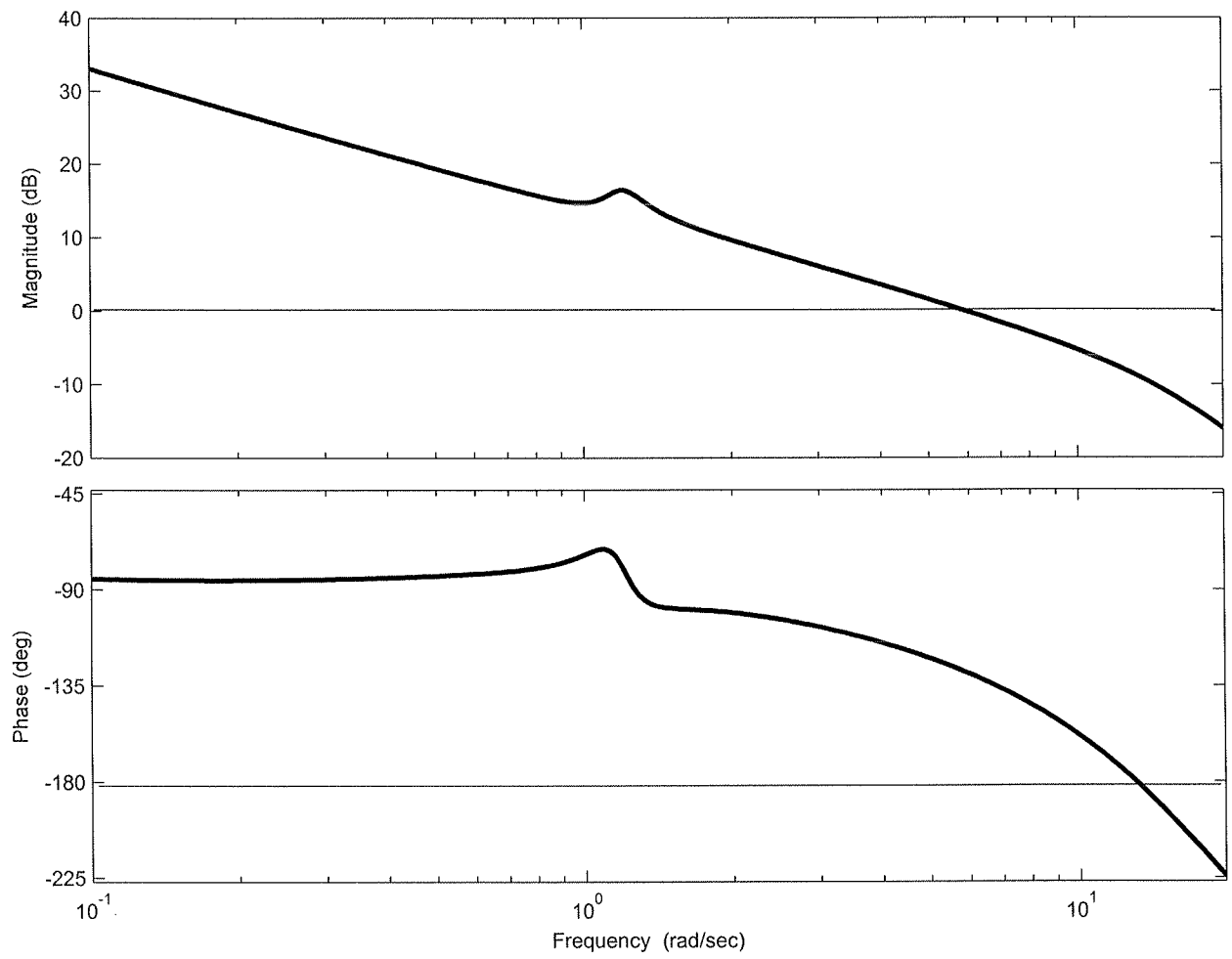
$$\frac{\phi}{s_a}$$

Bode Diagram



$$\frac{\phi}{\phi_e}$$

Bode Diagram



```
>> zpk(phi_phie)
```

Zero/pole/gain:

8.5265e-014 (s+8.391e005) (s+1) (s^2 + 0.3615s + 1.359) (s^2 - 8.391e005s + 7.04e011)

(s+20) (s+1.329) (s+0.006784) (s^2 + 0.2533s + 1.433) (s^2 + 28.28s + 400)

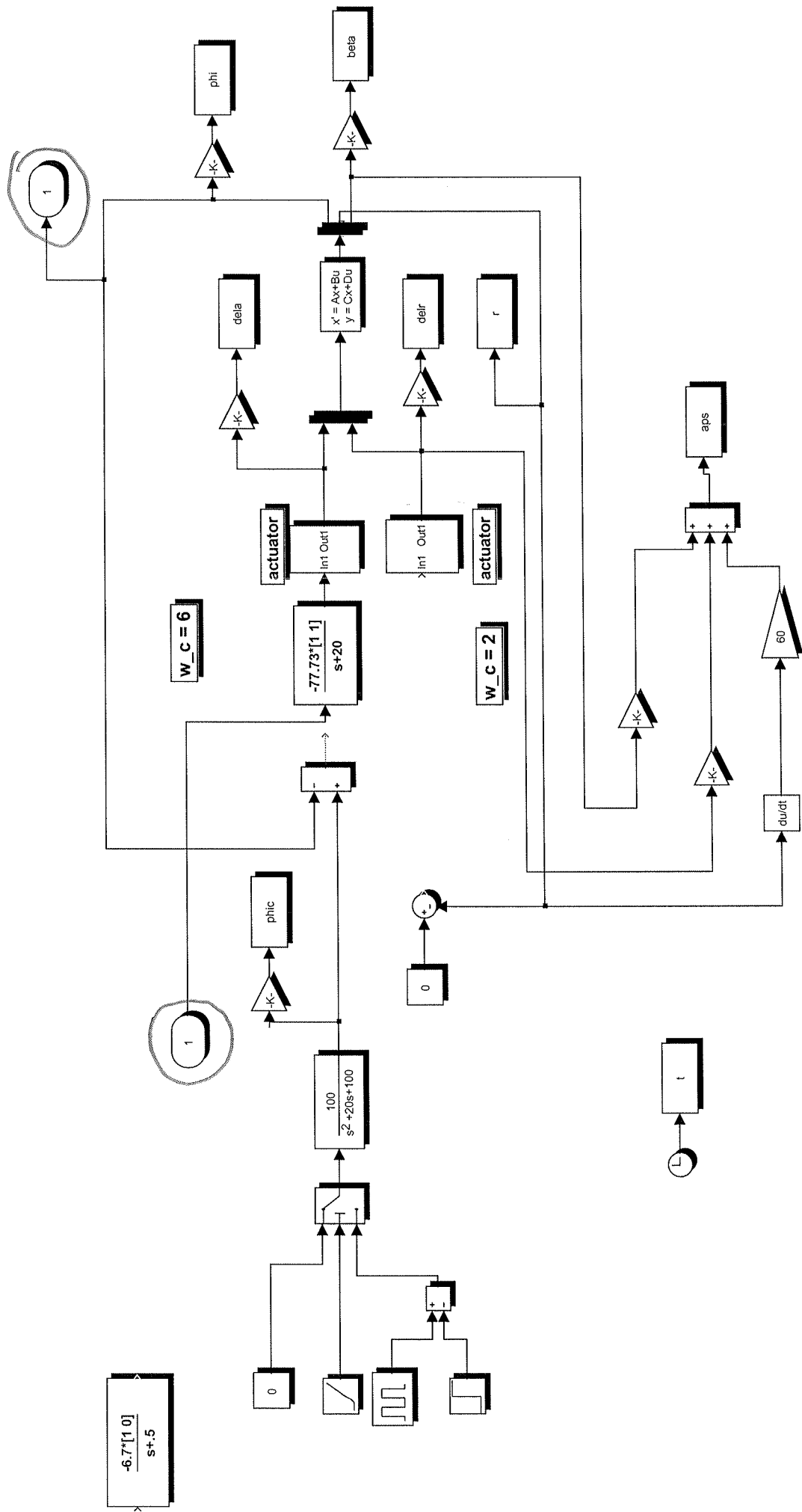
not real

$\frac{d}{\phi_e}$

$n=0$

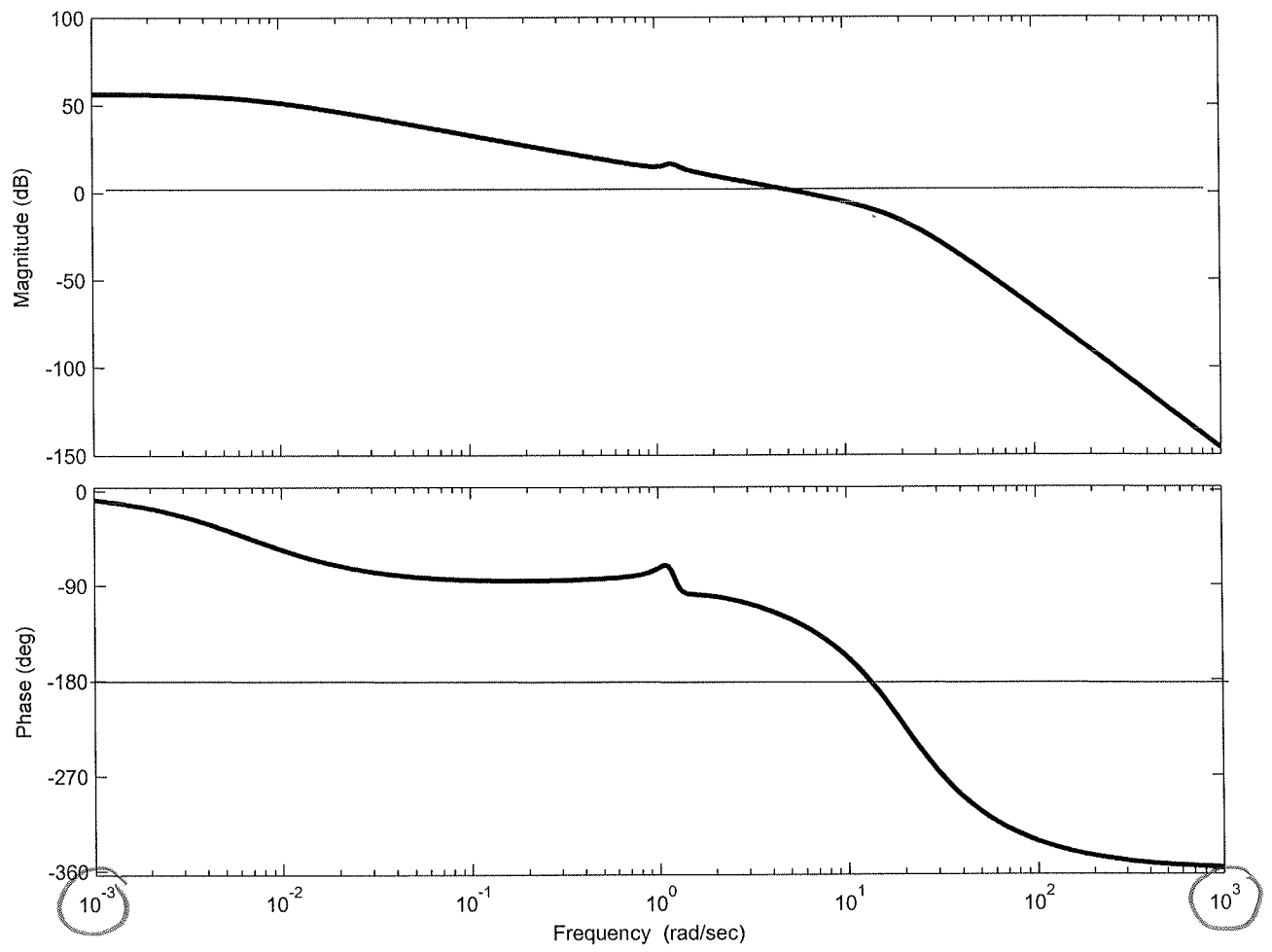
$m=0$

$p=0$

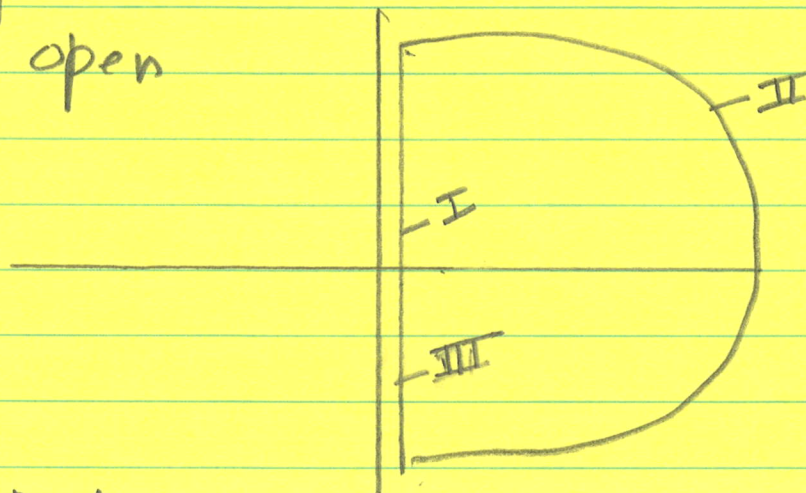


$\frac{\phi}{\phi_c}$

Bode Diagram



ϕ -loop with
r-loop open



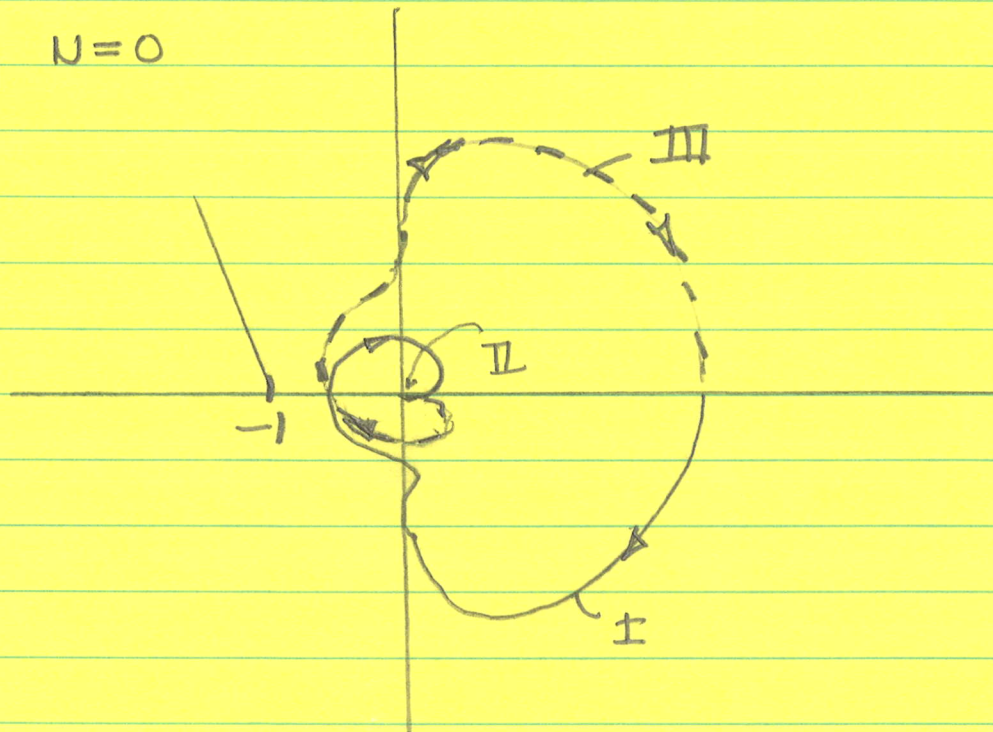
I from Bode

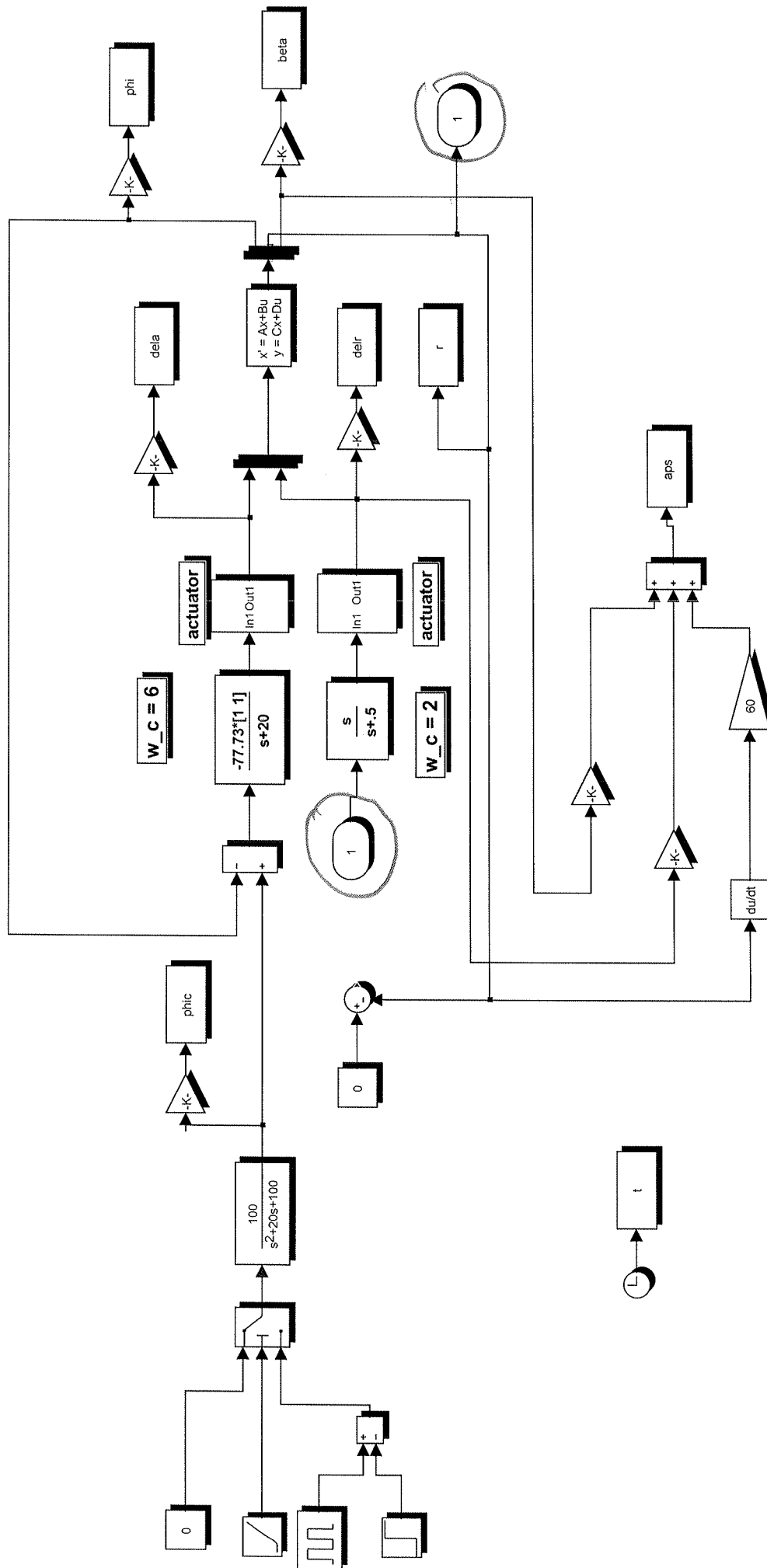
III

$$N = Z - P; \quad N = 0$$

$$P = 0$$

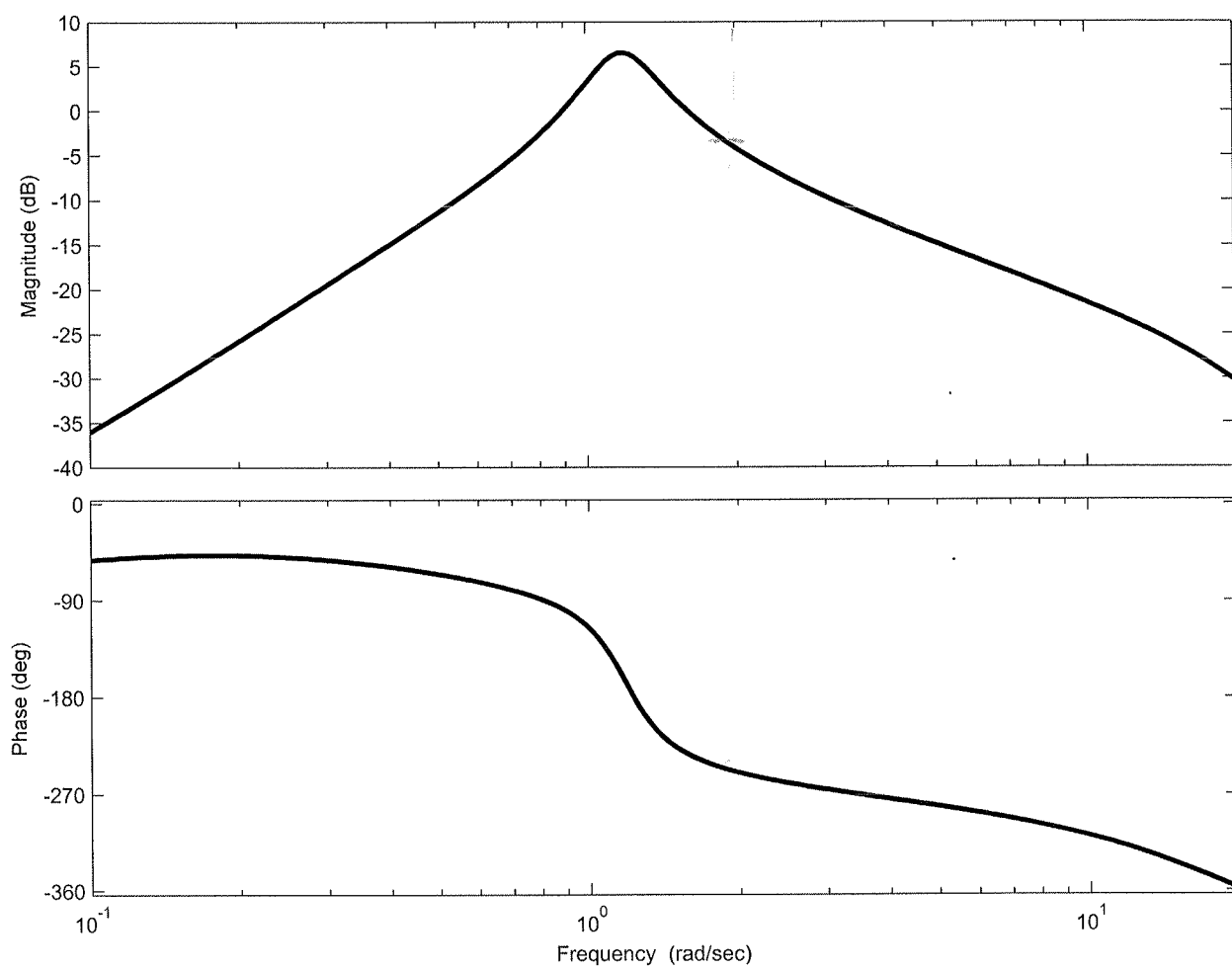
$$\therefore Z = 0$$

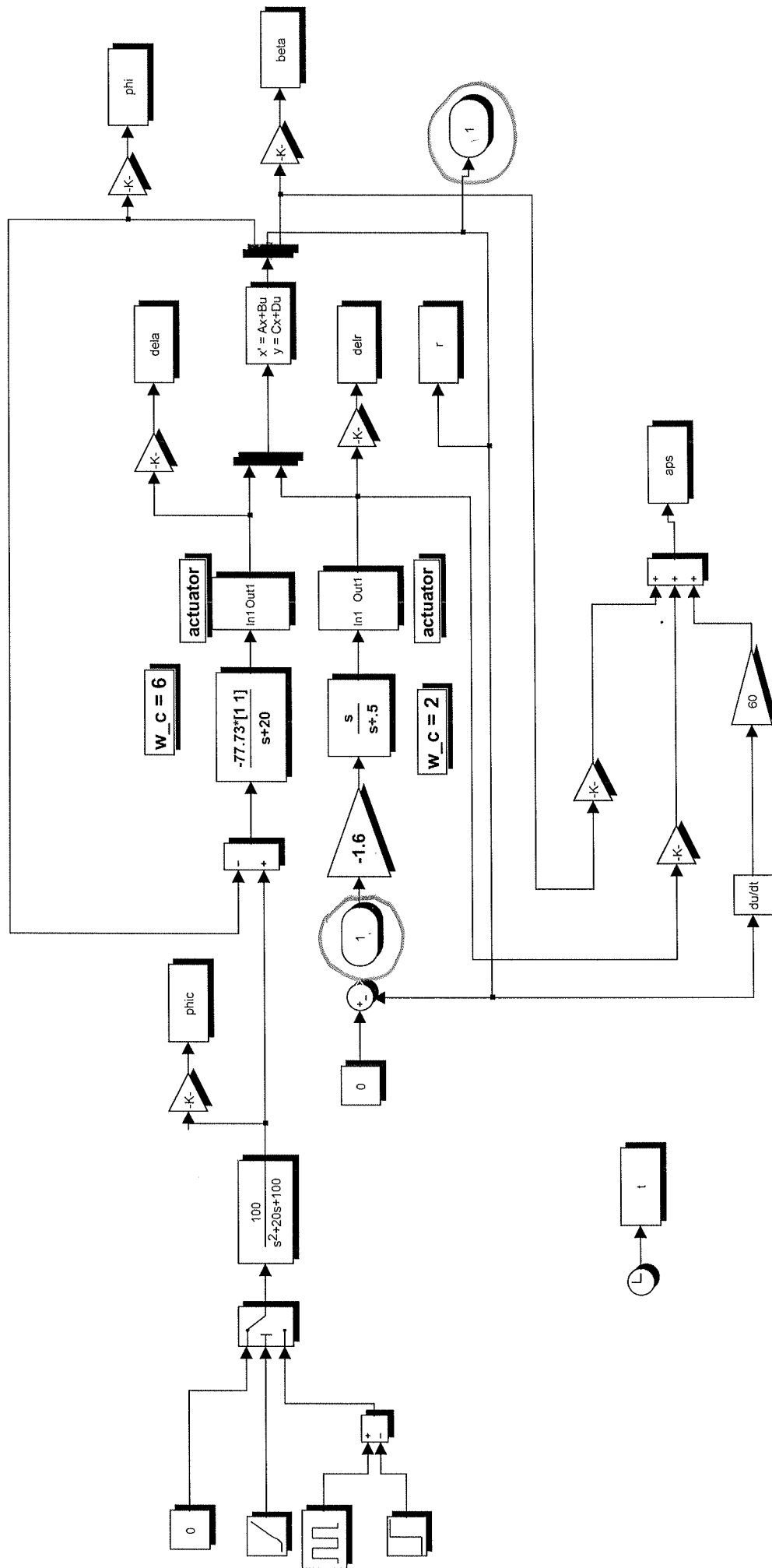




$$\frac{s/s_r}{\phi - \sigma_a}$$

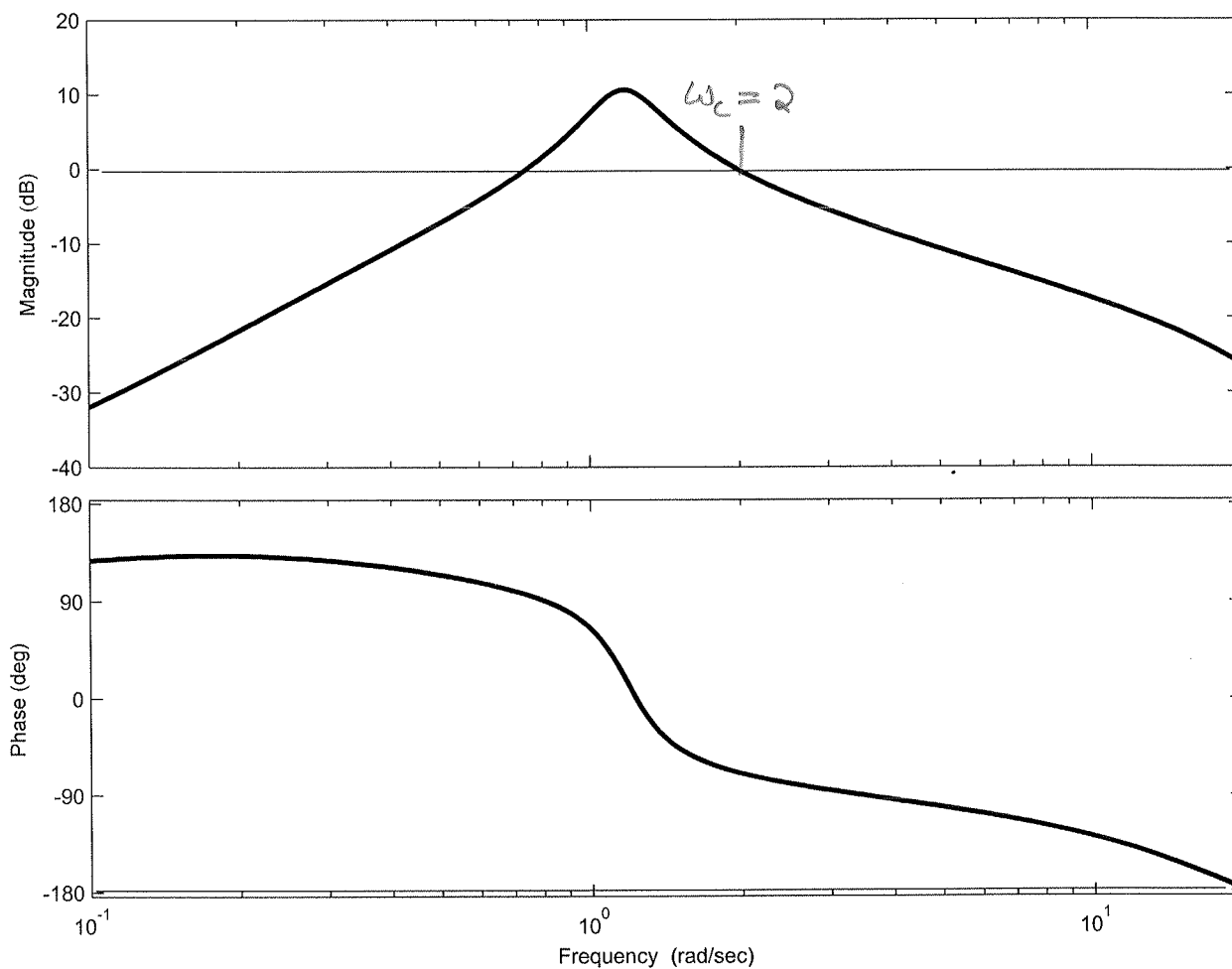
Bode Diagram





$\frac{5}{s} \bigg|$
 $\phi - \delta a$

Bode Diagram



```
>> zpk(r_re)
```

```
Zero/pole/gain:
```

```
-1.4211e-014 s (s+1.973e008) (s-1.973e008) (s+0.9351) (s+0.08107)
```

```
(s^2 + 7.924s + 93.43) (s^2 + 40.64s + 563.7)
```

```
-----
(s+0.9442) (s+0.5) (s^2 + 0.3768s + 1.39) (s^2 + 7.955s + 92.87)
```

```
(s^2 + 40.59s + 562.4) (s^2 + 28.28s + 400)
```

$\frac{F}{r_c} \Big|_{\theta = \delta_a}$

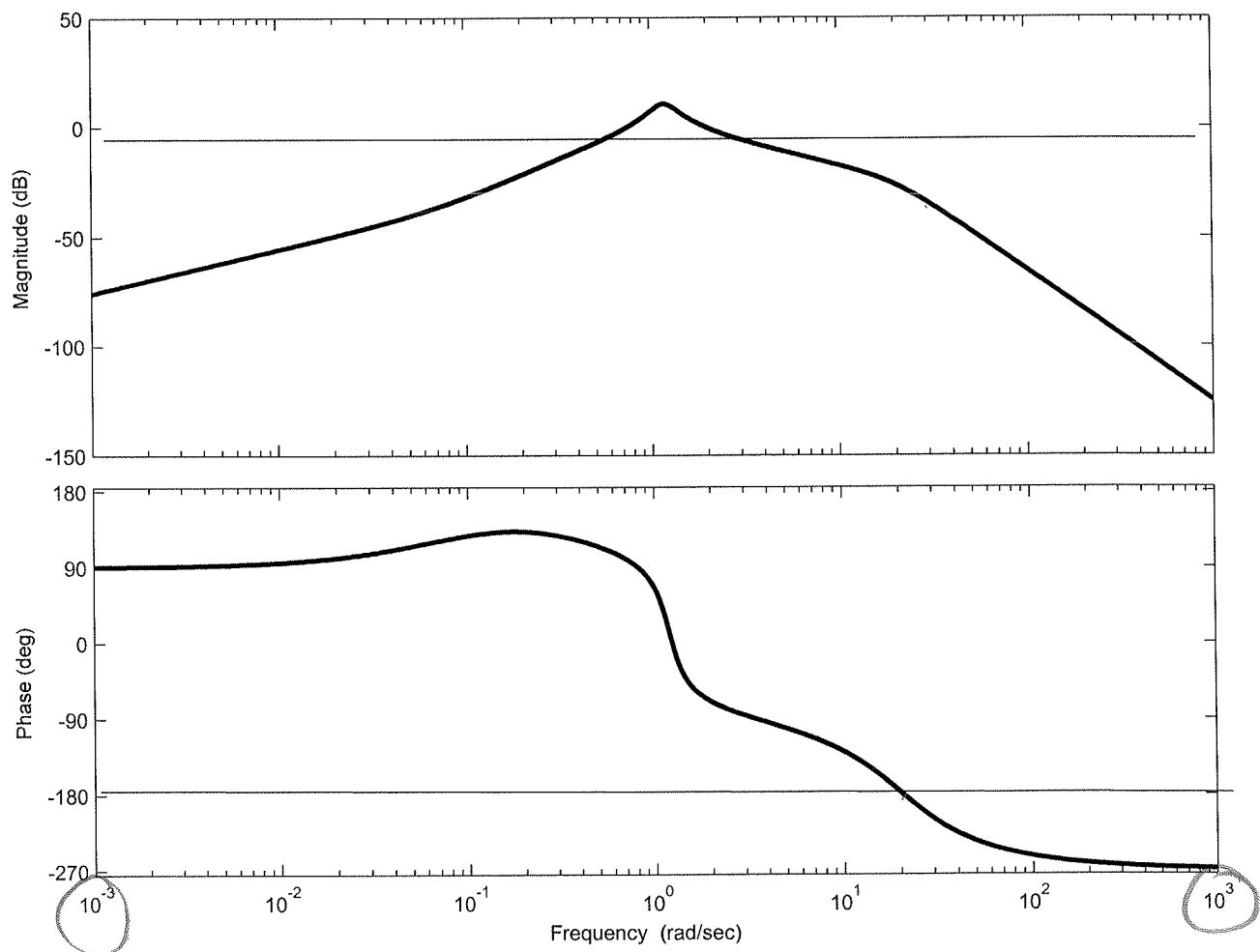
$n = 0$

$p = 1$

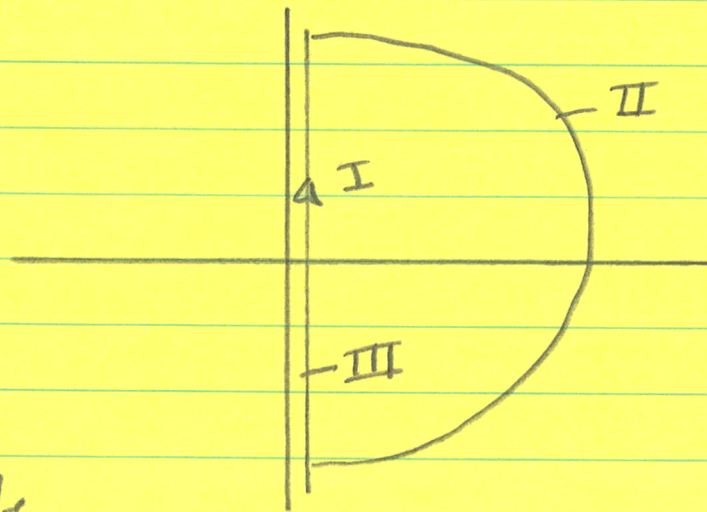
$m = 1$

$\frac{r}{e}$
 $\phi - \delta a$

Bode Diagram



r-loop with ϕ -loop closed

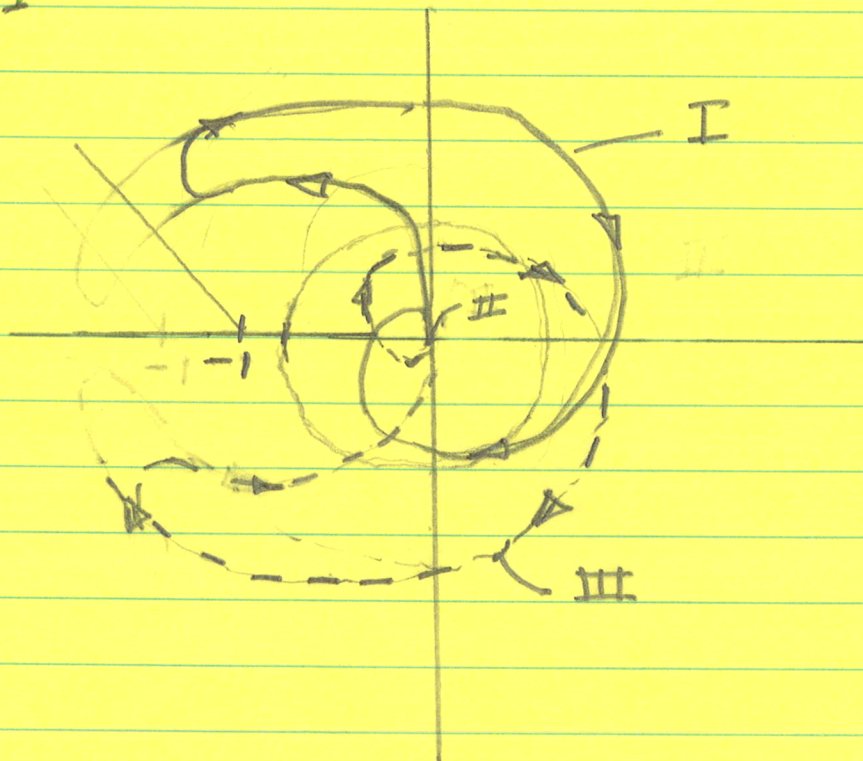


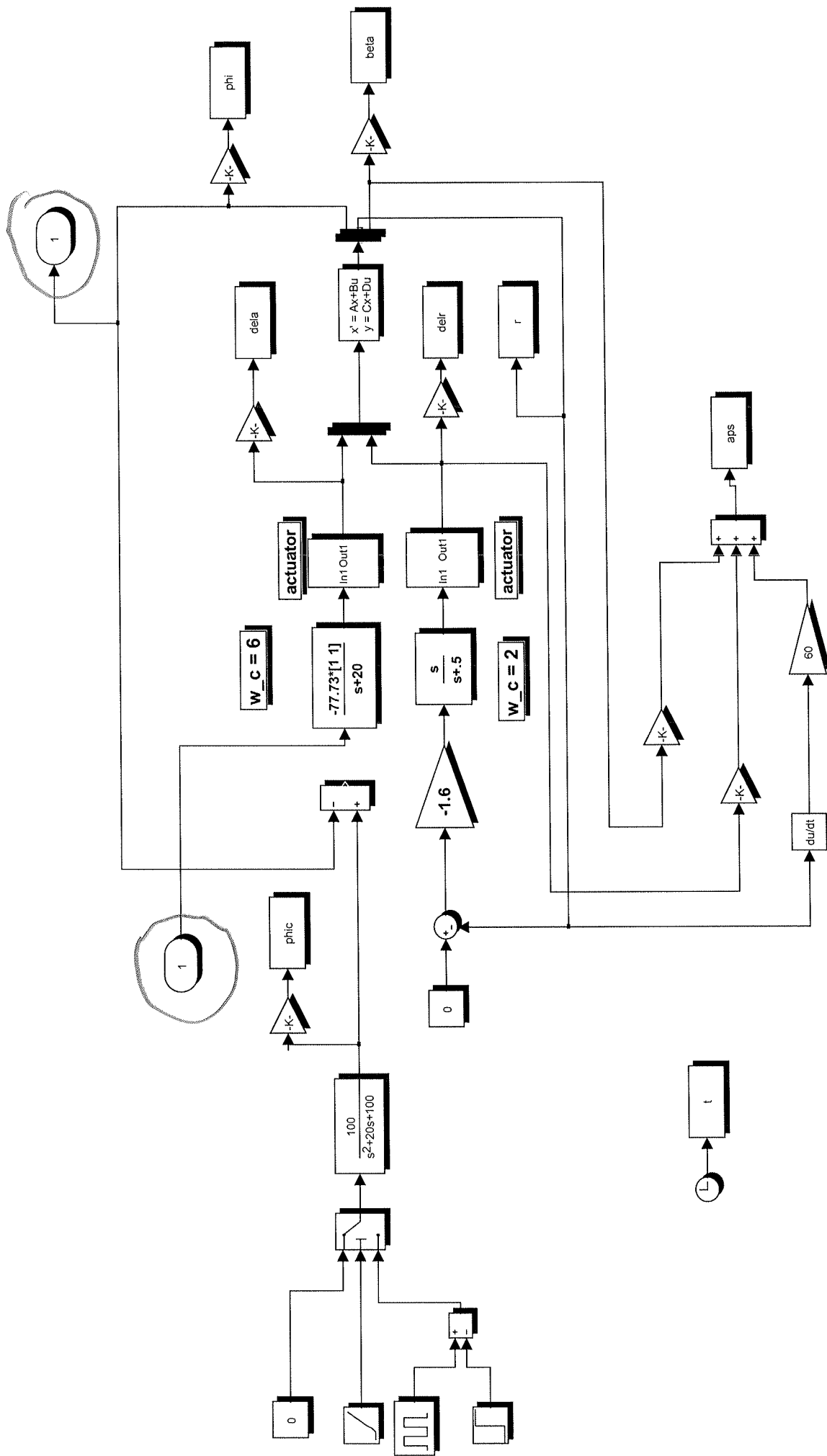
I: from Bode

$$N = Z - P$$

$$P = 0$$

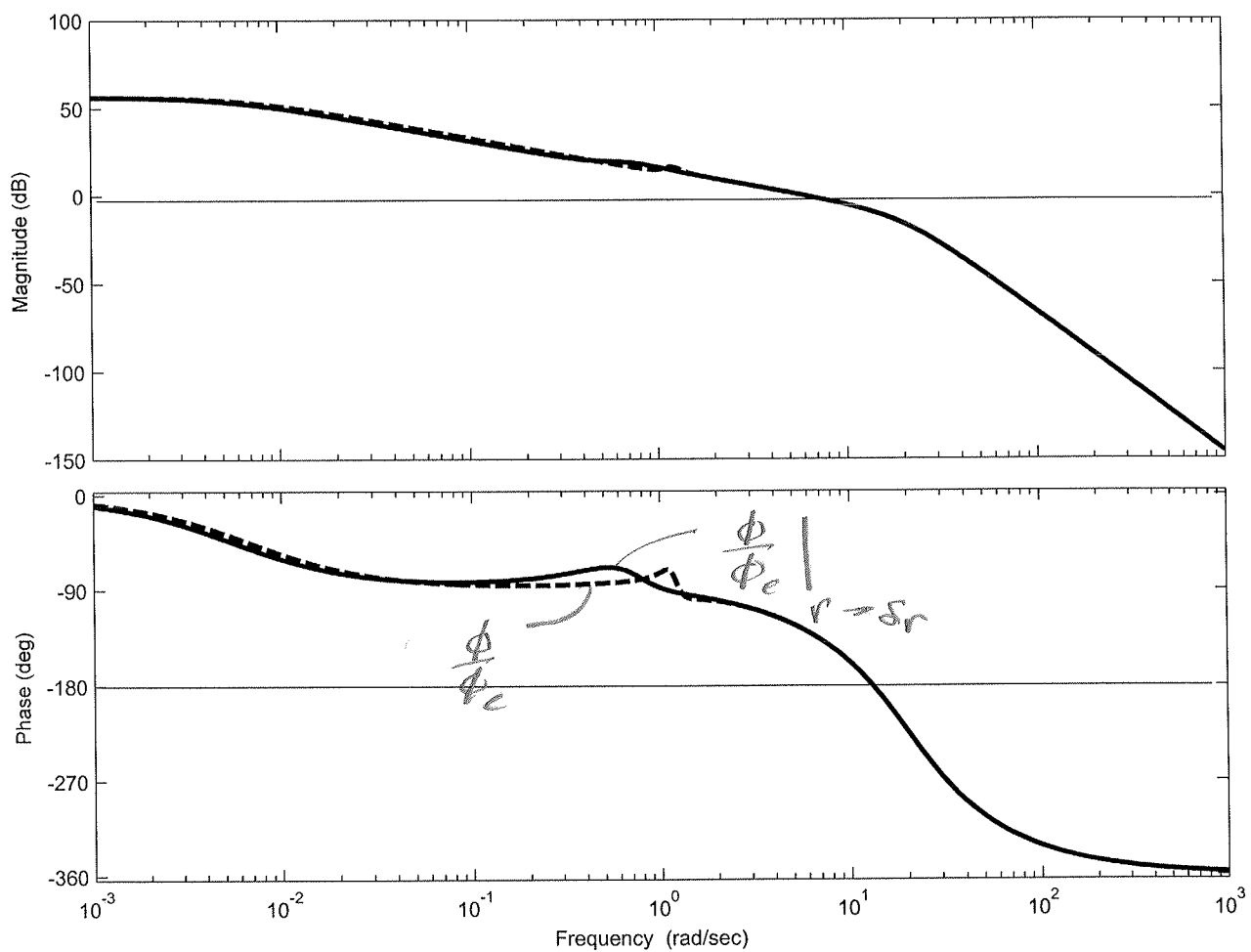
$$Z = 0$$





$$\frac{\phi}{\phi_e} \approx \frac{\phi}{\phi_e} \bigg|_{r \rightarrow \delta r}$$

Bode Diagram




```
>> zpk(gfinal)
```

```
Zero/pole/gain:
```

```
5.6843e-014 (s+9.605e005) (s+1.71) (s+1) (s^2 + 0.797s + 0.4449)
          (s^2 + 26.63s + 357.3) (s^2 - 9.605e005s + 9.225e011)
-----
(s+20) (s+1.713) (s+1.364) (s+0.005584) (s^2 + 0.6389s + 0.5537)
          (s^2 + 26.65s + 357.6) (s^2 + 28.28s + 400)
```

$= \frac{\phi}{\phi_e}$
 $r \rightarrow s_n$

```
>> zpk(phi_phie)
```

```
Zero/pole/gain:
```

```
8.5265e-014 (s+8.391e005) (s+1) (s^2 + 0.3615s + 1.359) (s^2 - 8.391e005s + 7.04e011)
-----
(s+20) (s+1.329) (s+0.006784) (s^2 + 0.2533s + 1.433) (s^2 + 28.28s + 400)
```

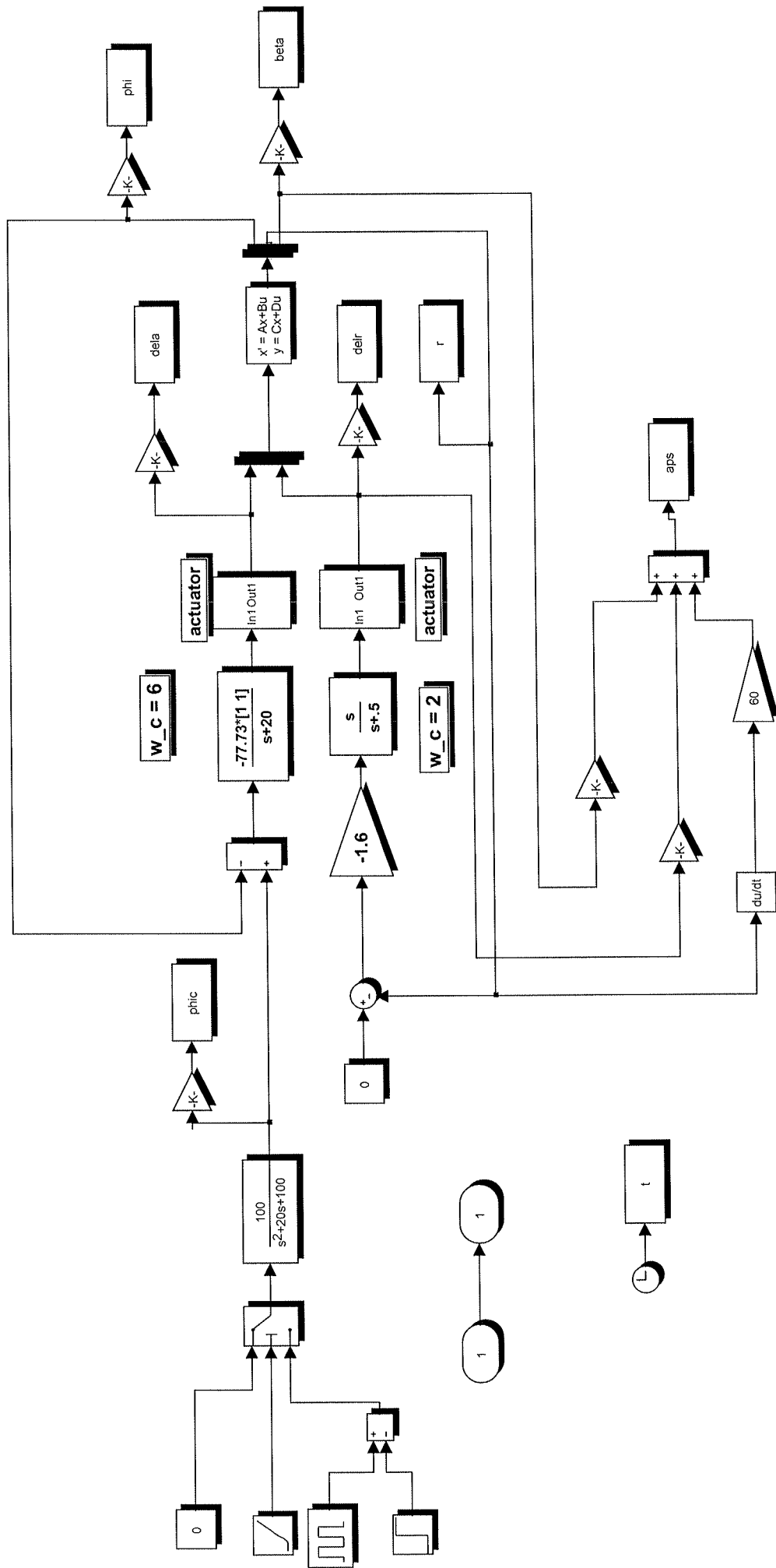
not real

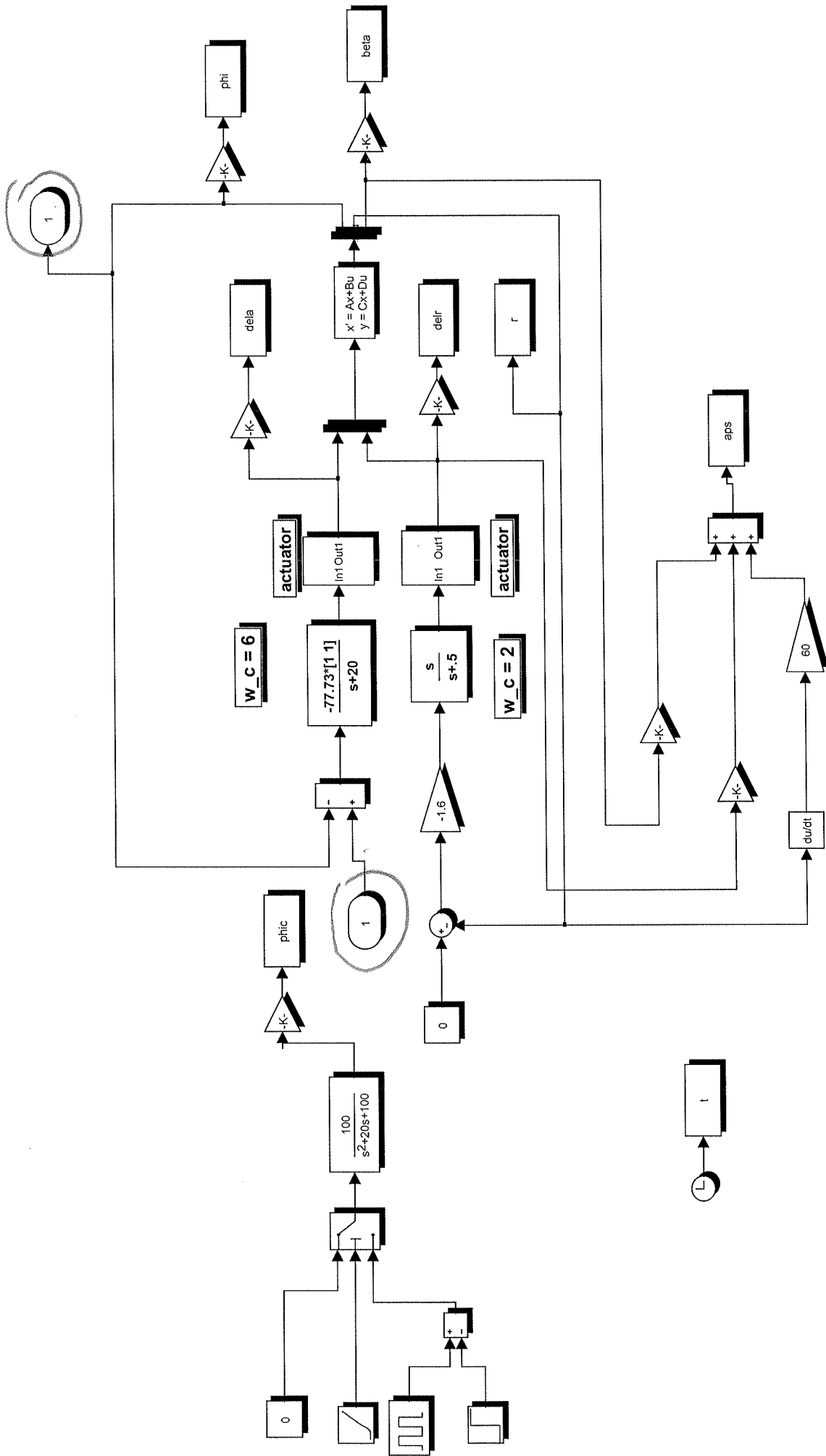
$= \frac{\phi}{\phi_e}$

$n=0$

$m=0$

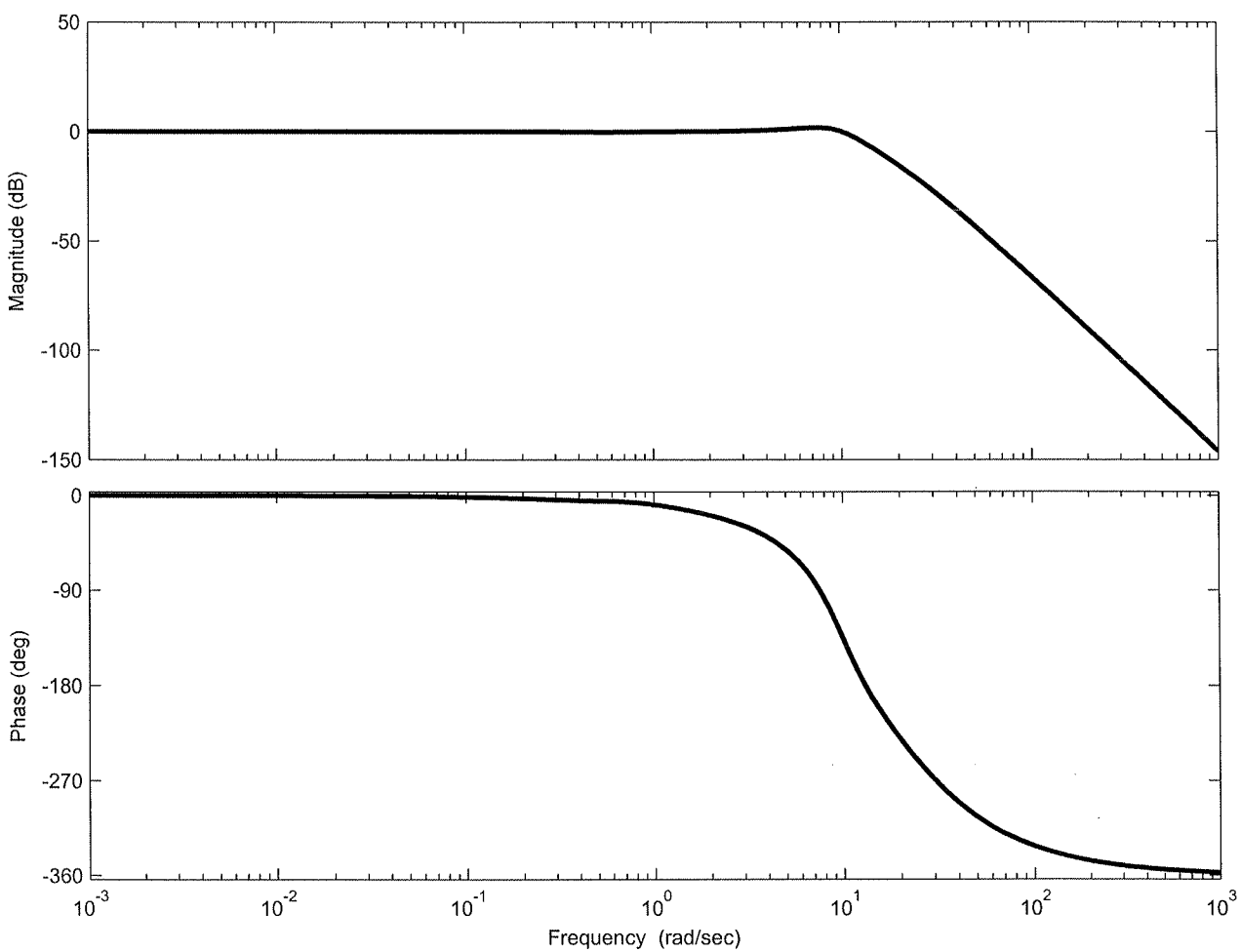
$p=0$





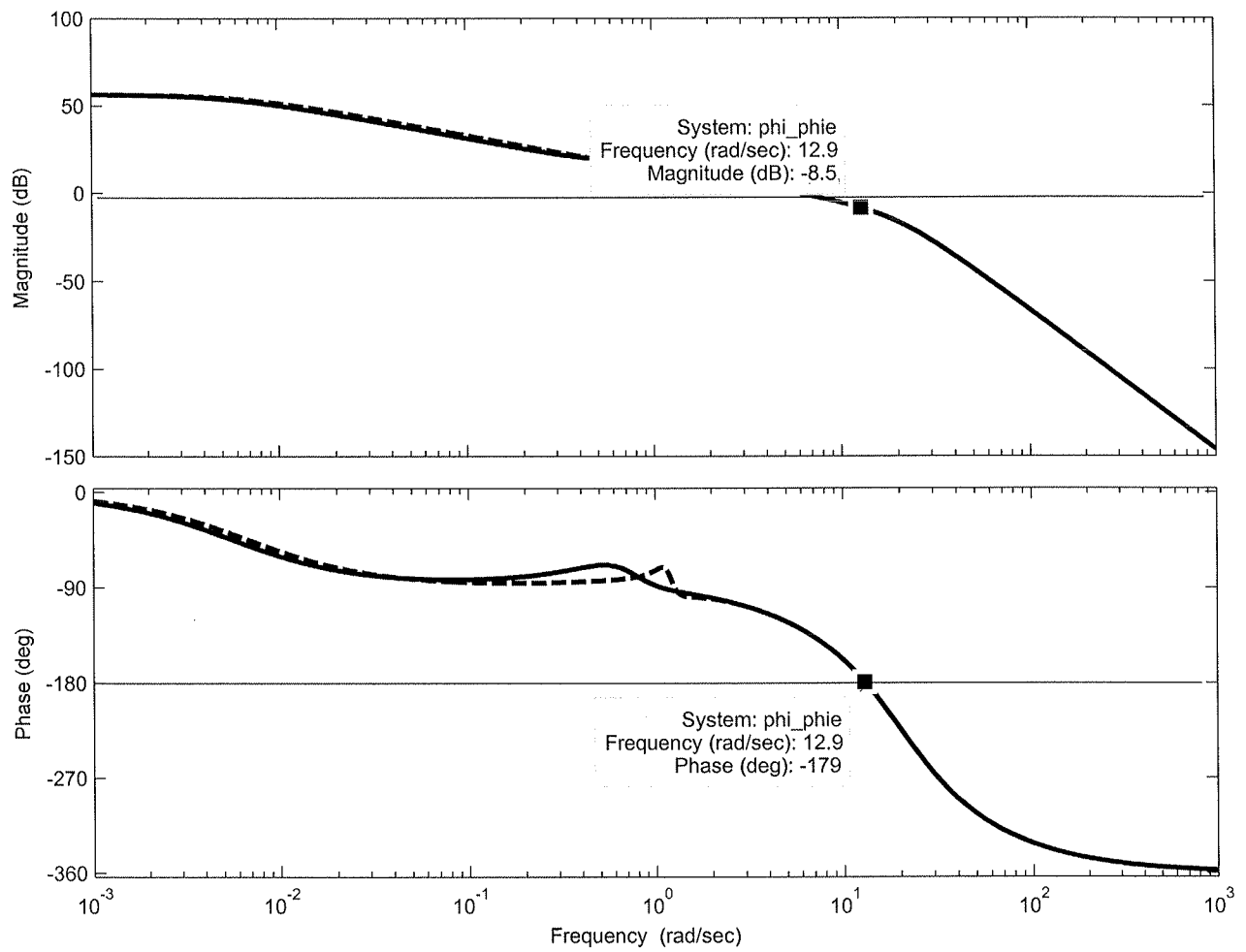
$$\frac{\phi}{\phi_c} \Big|_{r=\delta r}$$

Bode Diagram



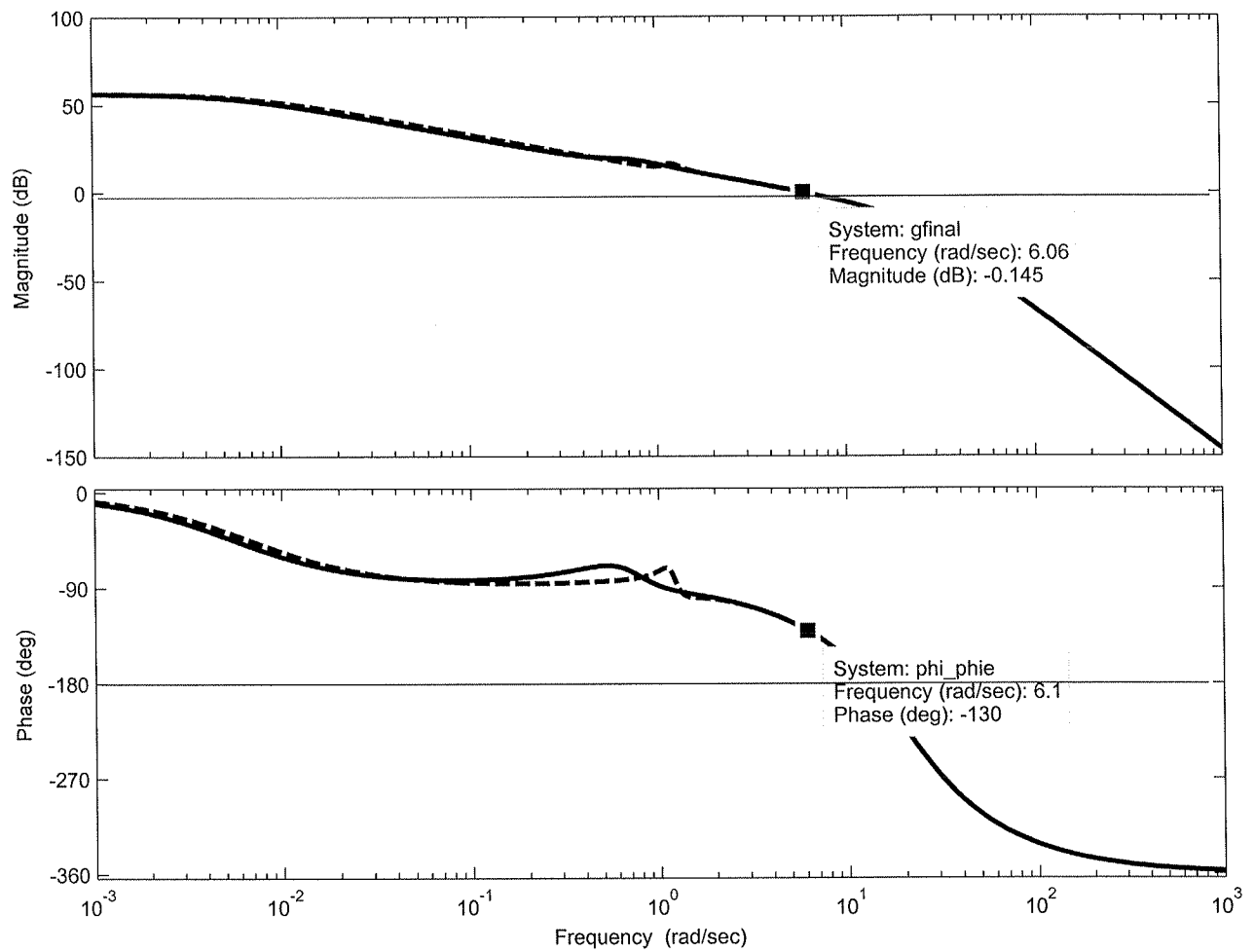
ϕ -loop gain margin = 8.5 dB

Bode Diagram



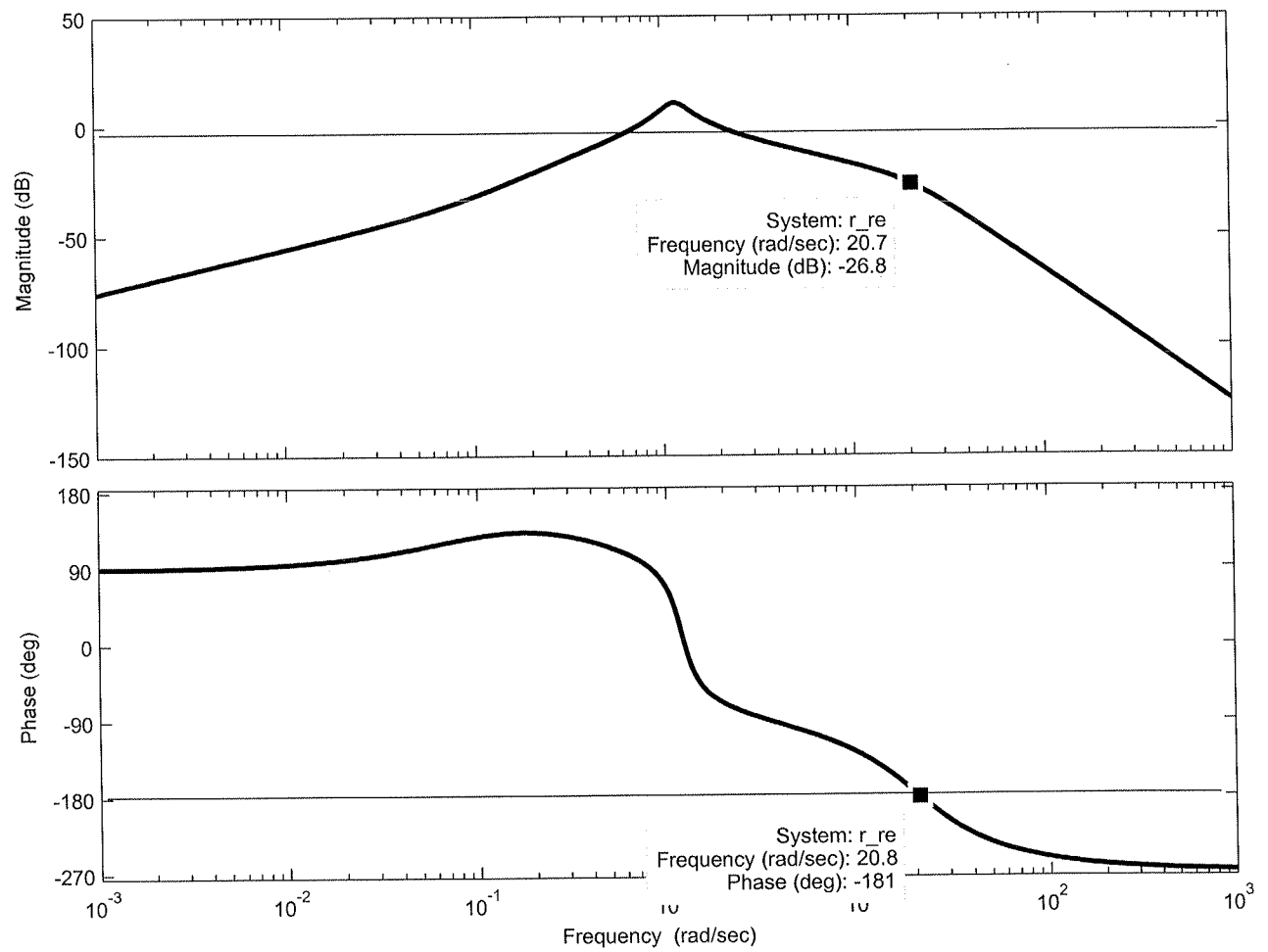
$$\phi\text{-loop phase-margin} = 180 - 130 = 50^\circ$$

Bode Diagram



r-loop gain-margin = 26.8dB

Bode Diagram



r-loop Phase margin = 111°

Bode Diagram

