

## Problem 1. Part 1 Attitude Disturbance Analysis

Do calculations for the disturbances present for equatorial circular orbits at 200km and 350km. Consider a cube with two different halves. One half has twice the density (and therefore twice the mass) as the other. We will only be concerned with rotations about the axis out of the page.

### Part (a)

1. Drag Find the disturbance torque on the cube about the mass center (use  $CD = 2.2$ )

$$\underline{T} = \sum \underline{r}_i \times \underline{F}_i$$

$$\underline{F}_i = \frac{1}{2} \rho V^2 C_D \left( \hat{n}_i \hat{V} \right) A_i \left( -\hat{V} \right)$$

### Part (b)

2. Solar Pressure Find the disturbance torque on the cube about the mass center. Assume that the entire surface is covered in solar panels ( $f_s \approx 0.21$ ,  $f_d \approx 0.1$ )

$$\underline{T} = \sum \underline{r}_i \times \underline{F}_i$$

$$\underline{F}_i = a_i \hat{s} + b_i \hat{n}_i$$

$$a_i = -PA_i \left( 1 - f_{s,i} \right) \cos \theta_i$$

$$b_i = -2PA_i \left( f_{s,i} \cos \theta_i + \frac{1}{3} f_{d,i} \right) \cos \theta_i$$

### Part (c)

3. Gravity Gradient Find the disturbance torque on the cube about the mass center

$$\underline{T} = \sum \underline{r}_i \times \underline{F}_i$$

$$\underline{F}_i = \frac{\mu m_i}{r_i^2} (-\hat{r})$$

### Part (d)

4. Magnetic Dipole Find the disturbance torque on the cube about the mass center for two configurations

$$\underline{T} = \sum \underline{M}_i \times \underline{B}$$

$$\underline{M}_i = nIA\hat{c}$$

## Problem 2. Part 2 Reaction Wheel and Thruster Analysis

Assume a maximum constant on orbit disturbance torque of  $1 \times 10^{-5}$  Nm on a single axis. Size a reaction wheel to keep a craft pointed despite this disturbance. Assume a saturation speed of 6000rpm for the wheel. It should be capable of eliminating the maximum on orbit disturbance without desaturating for two weeks.

$$H_{storage} = \int \frac{dH}{dt} = \int T_{disturbance,max} dt = T_{disturbance,max} t$$

$$\int \frac{dH}{dt} = \int I_{wheel} \alpha dt = I_{wheel} \omega_{saturated}$$

$$I_{wheel} \omega_{saturated} = \int I_{wheel} \alpha dt = \int \frac{dH}{dt}$$

$$= \int T_{thrusters} dt = T_{thrusters} t$$

## Problem 3. Part 3 Hubble Slew Problem

Either use published inertia values for Hubble or the estimates you made in the dynamics assignment. Assume torquers are aligned with the principle axis.

$$I_{xx} \dot{\Omega}_x + H_{spin} \Omega_y = T_x$$

$$I_{yy} \dot{\Omega}_y + H_{spin} \Omega_x = T_y$$

$$H_{spin} = I_{wheel} \omega_{wheel}$$

### Part (a)

1. Two axis torques Find the required variable torques (x and y) to constantly accelerate the angular precession by  $0.1 \text{ deg/s}^2$  on the x axis while trying to keep the angular precession on the y-axis at a constant  $0.1 \text{ deg/s}$ .

### Part (b)

2. Two axis torques Find the required variable torque (x) to constantly accelerate the angular precession by  $0.1 \text{ deg/s}^2$  on the x axis while applying no torque to the y axis.