

# Introduction to Computer Graphics

## 5. Clipping

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Textbook: E. Angel, D. Shreiner Interactive Computer Graphics, 6th Ed., Pearson  
Ref: D.D. Hearn, M. P. Baker, W. Carithers, Computer Graphics with OpenGL, 4th Ed., Pearson

# Objectives

- ▶ Introduce basic implementation strategies
- ▶ 2D Clipping
  - ▶ Lines
  - ▶ Polygons
- ▶ Clipping in 3D

# Clipping

盡量避免float計算

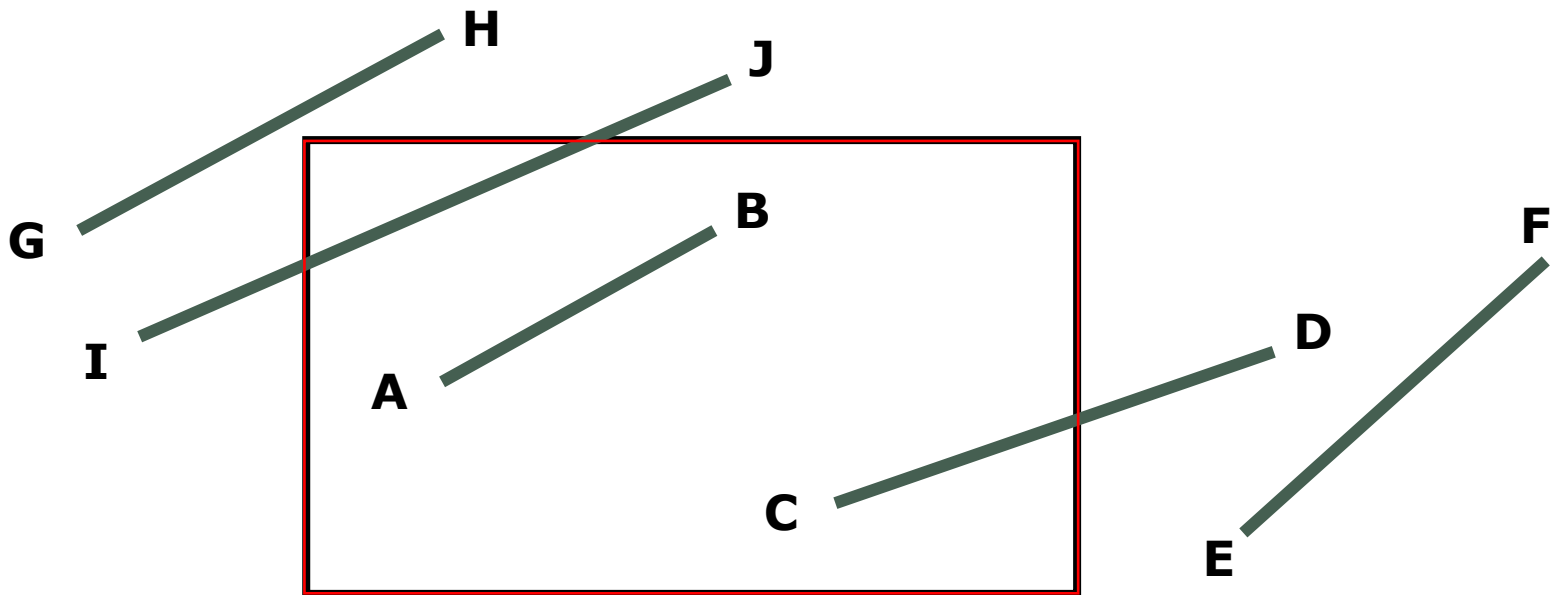
判斷是否在frame buffer裡 : floating point -> if/else  
-> bitwise operation (AND, OR) 與 prediction 效率有關

- ▶ 2D against clipping window
- ▶ 3D against clipping volume
- ▶ Easy for line segments polygons 線與框框的交點
- ▶ Hard for curves and text
  - ▶ Convert to lines or polygons first



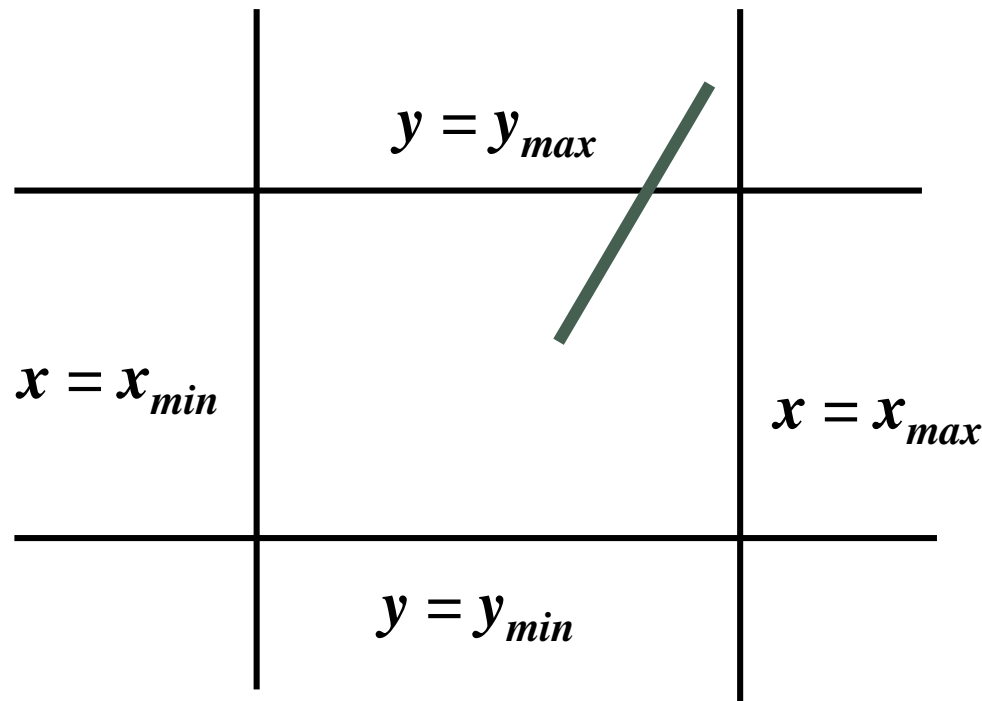
# Clipping 2D Line Segments

- ▶ Brute force approach: compute intersections with all sides of clipping window 和每個邊做相交，一條線要做四次intersection
- ▶ Inefficient: one division per intersection 應減少float computation



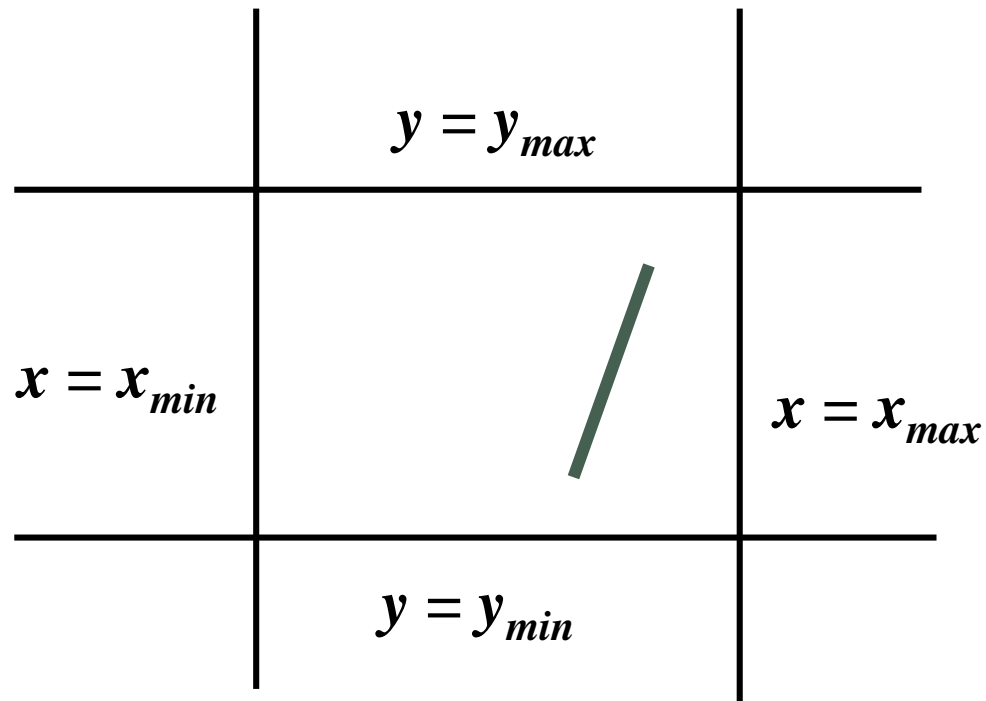
# Cohen-Sutherland Algorithm

- ▶ Idea: eliminate as many cases as possible without computing intersections 有些可以用if/else來避開float computation
- ▶ Start with four lines that determine the sides of the clipping window



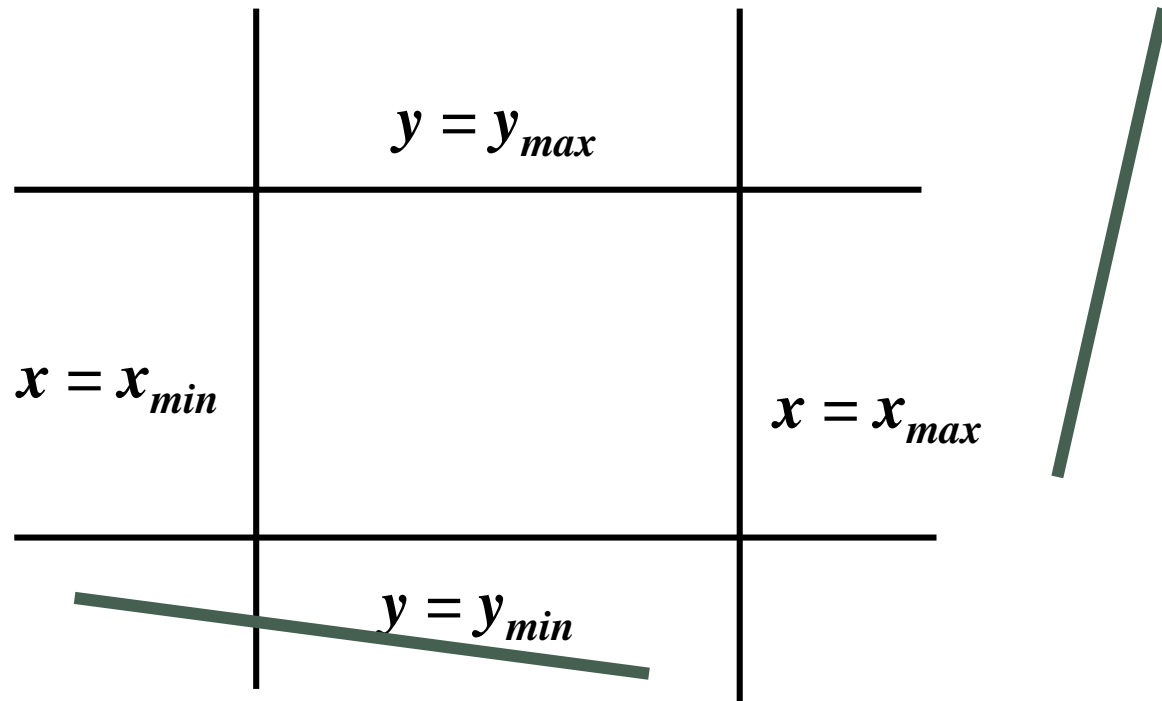
## Case 1 完全不需要做intersection

- ▶ Case 1: both endpoints of a line segment inside all four lines
  - ▶ Draw (accept) the line segment as is



## Case 2 完全在某一個平面或某一條線外面

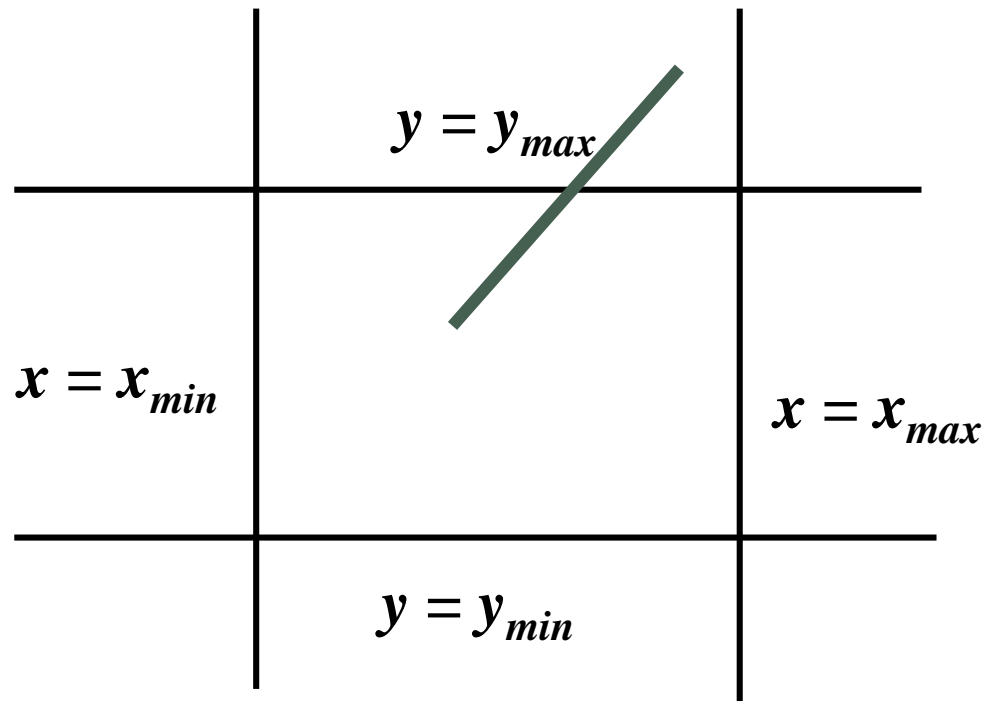
- ▶ Case 2: both endpoints outside all lines and on same side of a line
  - ▶ Discard (reject) the line segment



## Case 3

對於某邊，這條線一個點在裡面一個點在外面=>算一次交點

- ▶ One endpoint inside, one outside
  - ▶ Must do at least one intersection



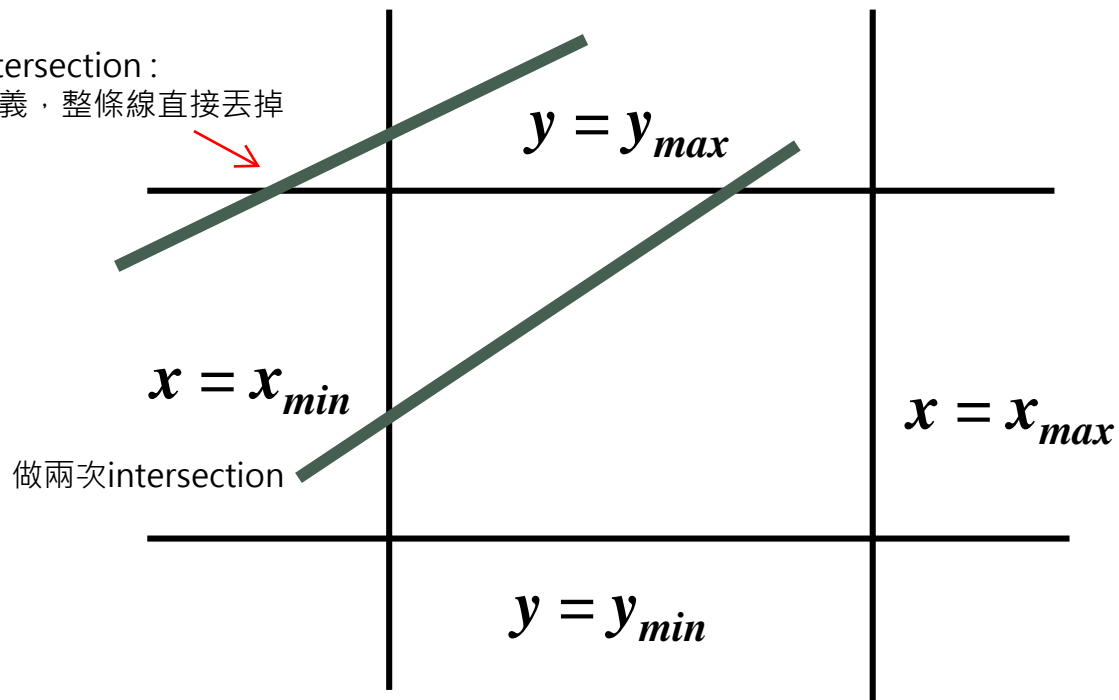


## Case 4

跨兩個區域=>至少要做一次intersection

- ▶ Both outside
  - ▶ May have part inside
  - ▶ Must do at least one intersection

做一次intersection：  
交點無意義，整條線直接丟掉



# Defining Outcodes

- ▶ For each endpoint, define an outcode
  - ▶ [b0 b1 b2 b3]
- ▶ Outcodes divide space into 9 regions
- ▶ Computation of outcode requires at most 4 subtractions

1001	1000	1010
0001	0000	0010
0101	0100	0110

b0 = 1 if  $y > y_{\max}$ , 0 otherwise

b1 = 1 if  $y < y_{\min}$ , 0 otherwise

b2 = 1 if  $x > x_{\max}$ , 0 otherwise

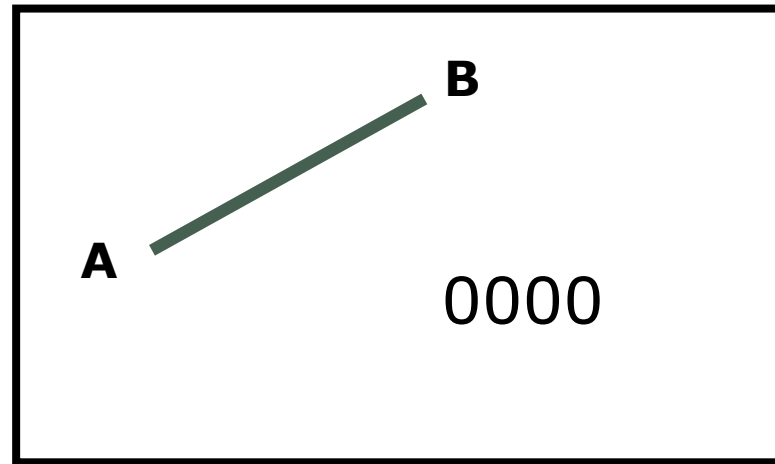
b3 = 1 if  $x < x_{\min}$ , 0 otherwise

## Case 1 Using Outcodes bitwise operation

兩個點進來會自帶outcode

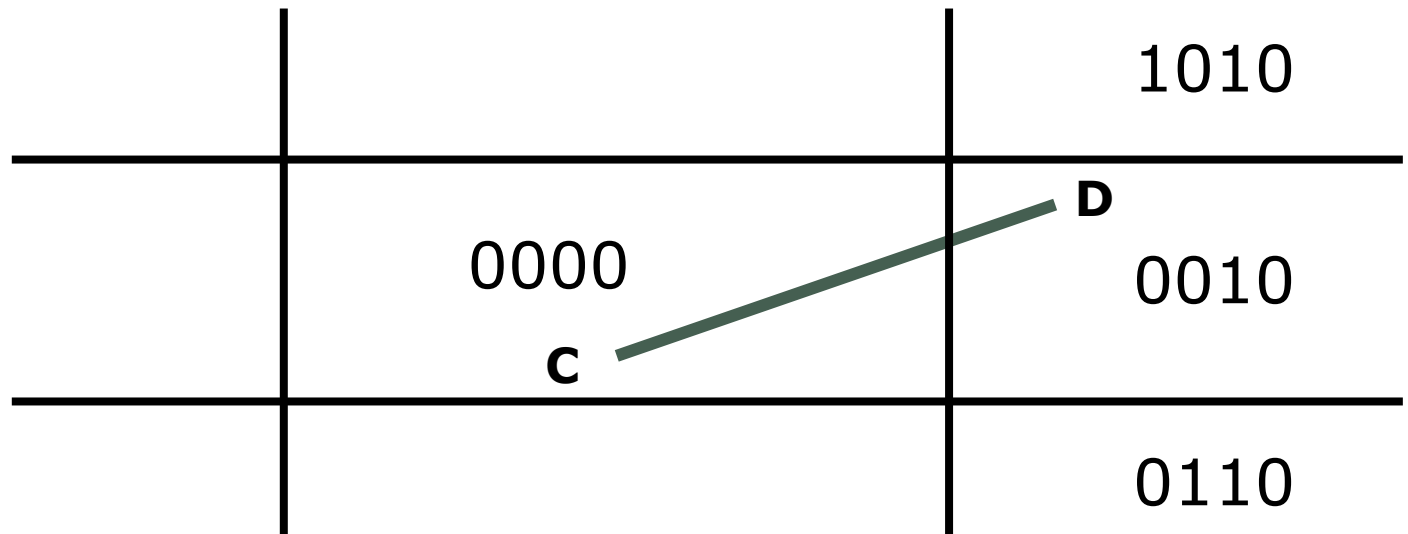
▶ AB:  $\text{outcode}(A) = \text{outcode}(B) = 0$

▶ Accept the line segment



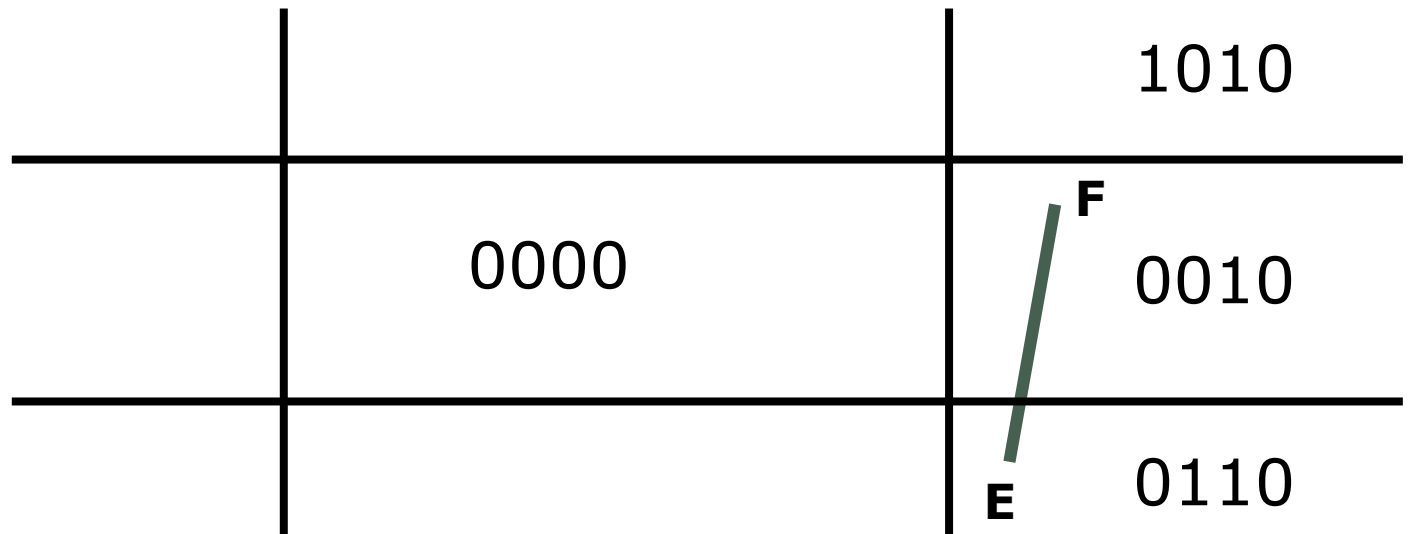
# Using Outcodes

- ▶ CD: outcode (C) = 0, outcode(D)  $\neq$  0
  - ▶ Compute intersection
  - ▶ Location of 1 in outcode(D) determines which edge to intersect with
  - ▶ Note if there were a segment from C to a point in a region with 2 ones in outcode, we might have to do two intersections



# Using Outcodes

- ▶  $EF$ : outcode( $E$ ) logically ANDed with outcode( $F$ ) (bitwise)  $\neq 0$ 
  - ▶ Both outcodes have a 1 bit in the same place
  - ▶ The line segment is outside of corresponding side of clipping window  
會留下某一個數值(AND起來是0010): 剛好對某一條線會全部在外面(不是0000)
  - ▶ reject



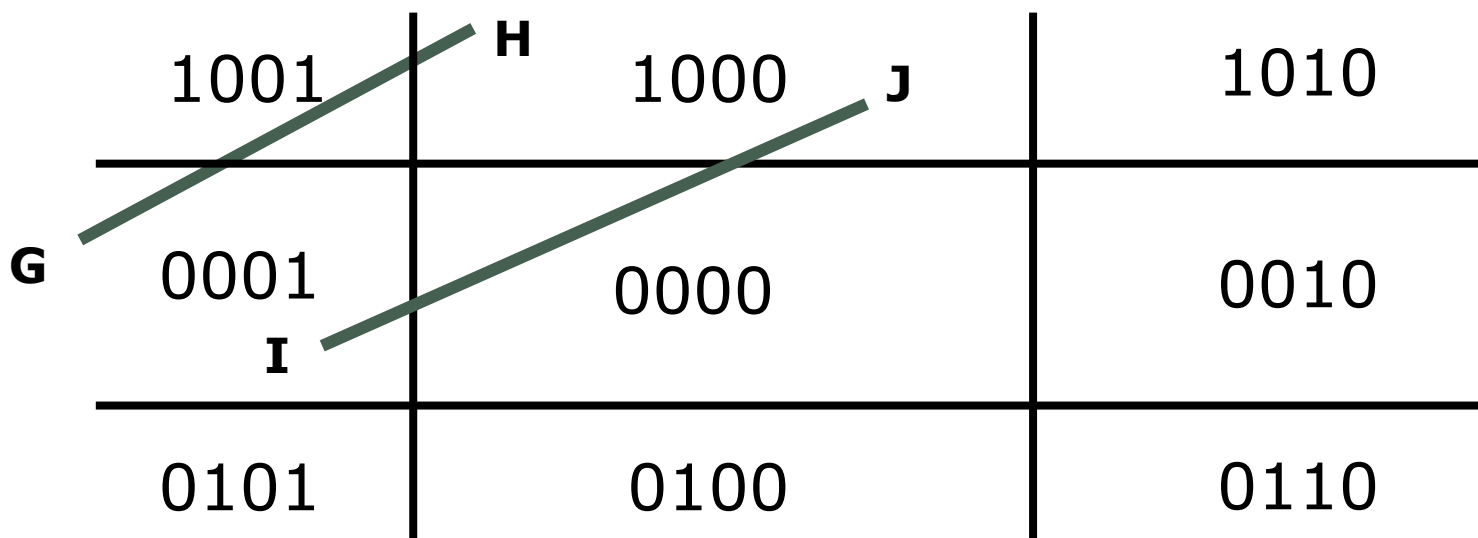
# Using Outcodes

檢查其中一個交點來判斷是哪一種

- ▶ GH and IJ: same outcodes, neither zero but logical AND yields zero

雖然AND之後是0000，但兩條都不是0000

- ▶ Shorten line segment by intersecting with one of sides of window
- ▶ Compute outcode of intersection (new endpoint of shortened line segment)
- ▶ Re-execute algorithm

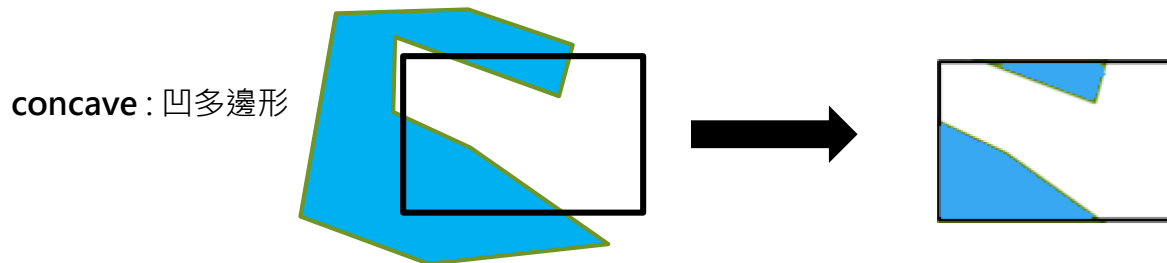


# Efficiency

- ▶ In many applications, the clipping window is small relative to the size of the entire data base
  - ▶ Most line segments can be eliminated based on their outcodes.
- ▶ Inefficiency when code has to be re-executed for line segments that must be shortened in more than one step

# Polygon Clipping

- ▶ Not as simple as line segment clipping
  - ▶ Clipping a line segment yields at most one line segment
  - ▶ Clipping a polygon can yield multiple polygons



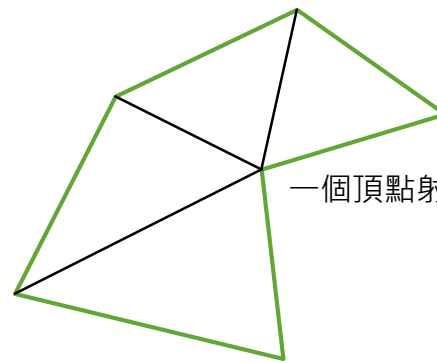
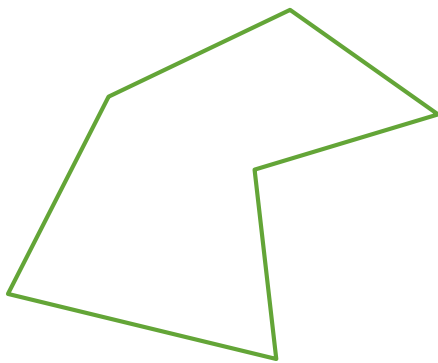
- ▶ However, clipping a convex polygon can yield at most one other polygon



# Tessellation and Convexity

凹邊形要先打斷

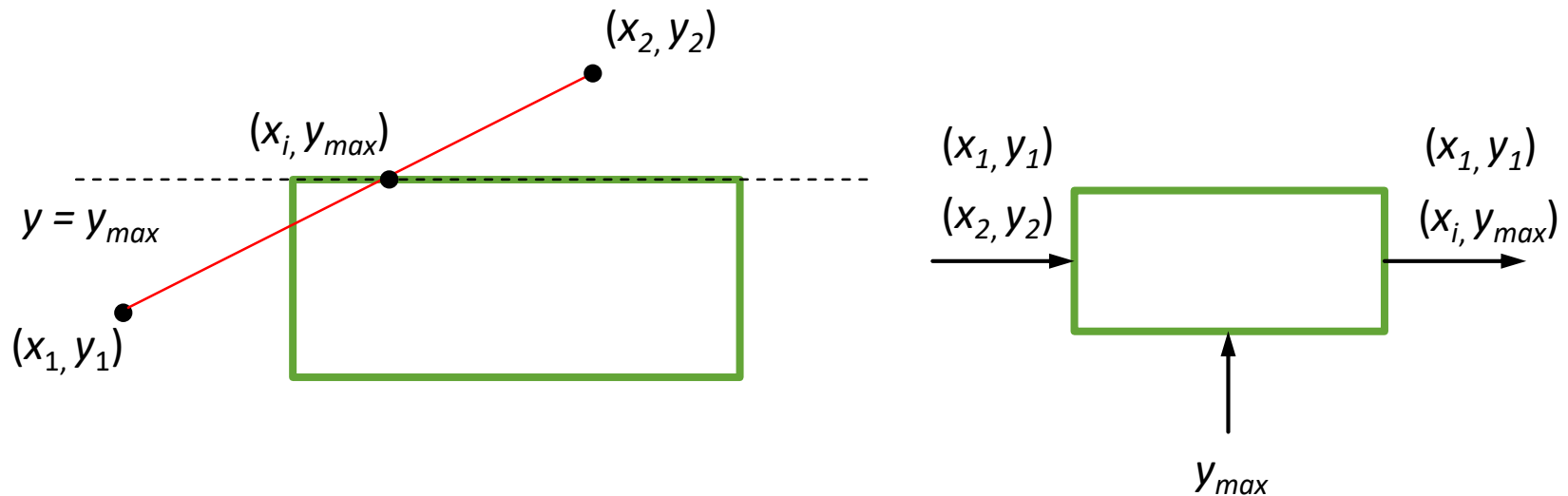
- ▶ One strategy is to replace nonconvex (concave) polygons with a set of triangular polygons (a tessellation)
- ▶ Also makes fill easier



一個頂點射線出去分割凹多邊形

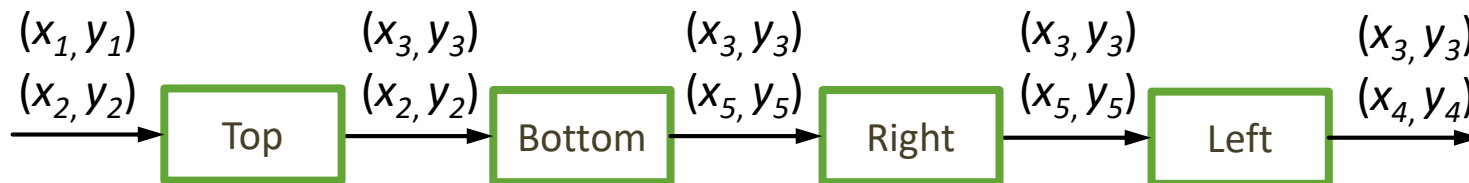
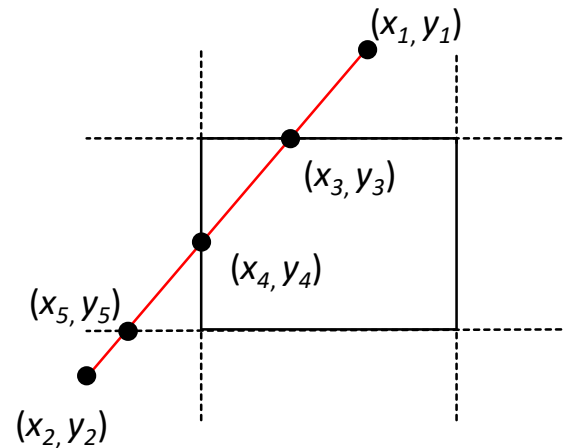
# Clipping as a Black Box pipeline

- Consider line segment clipping as a process that takes in two vertices and produces either no vertices or the vertices of a clipped line segment.



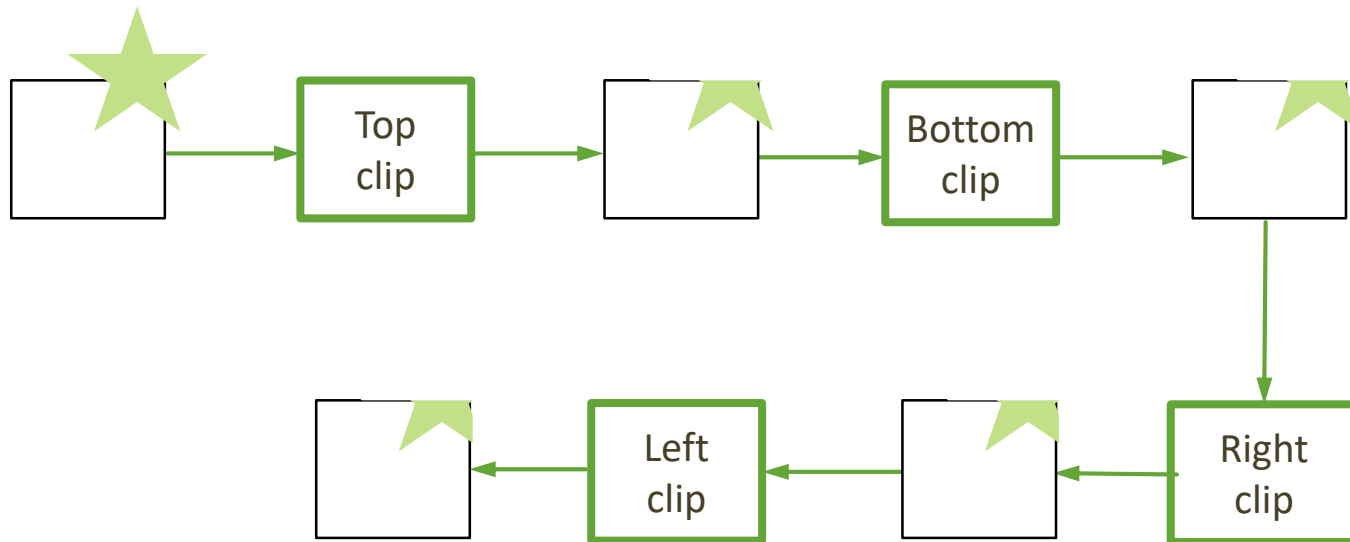
# Pipeline Clipping of Line Segments

- ▶ Clipping against each side of window is independent of other sides
- ▶ Can use four independent clippers in a **pipeline** 分成四個stage，在每一階段砍一刀  
可能會做多餘的事情，在數量多的時候還算有效率



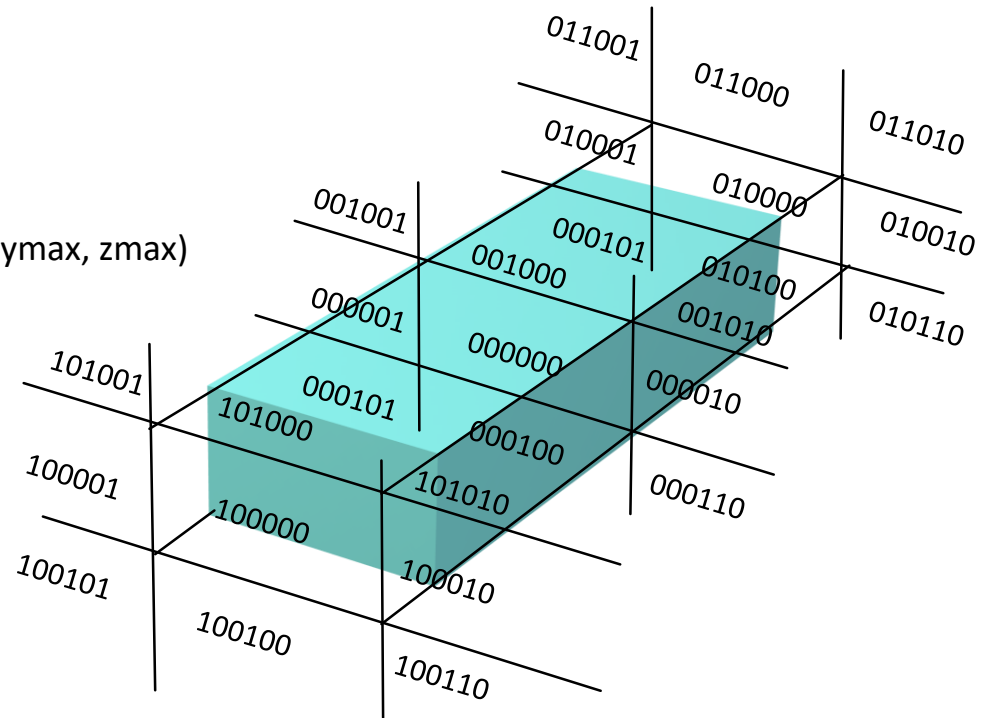
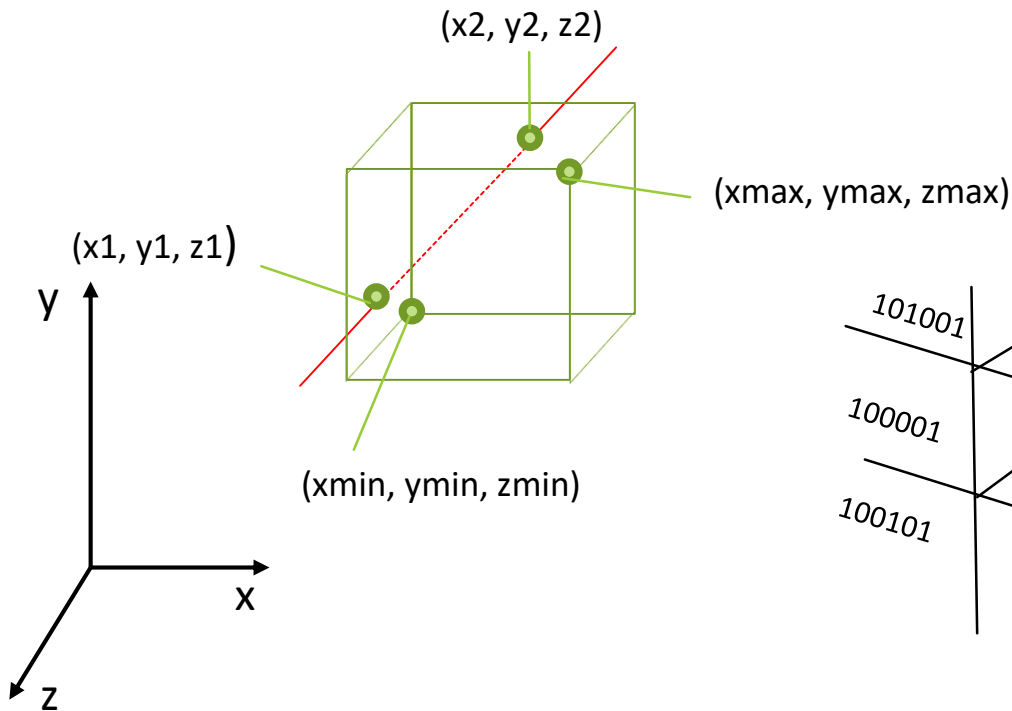
# Pipeline Clipping of Polygons

- ▶ Sutherland-Hodgman algorithm
- ▶ Strategy used in SGI Geometry Engine
- ▶ Small increase in latency



# Cohen-Sutherland Method in 3D

- Use 6-bit outcodes
  - When needed, clip line segments against planes



# Cohen-Sutherland Method in 3D clipping做在normalized space

Check for outcodes:

$$-1 \leq x_p \leq 1, -1 \leq y_p \leq 1, -1 \leq z_p \leq 1$$

Since

$$\begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} \xRightarrow{\text{SRT...}} \begin{bmatrix} x_h \\ y_h \\ z_h \\ h \end{bmatrix} \xRightarrow{\text{Divide h}} \begin{bmatrix} x_h/h \\ y_h/h \\ z_h/h \\ 1 \end{bmatrix} = \begin{bmatrix} x_p \\ y_p \\ z_p \\ 1 \end{bmatrix}$$

To avoid unnecessary float division, We can check

$$-h \leq x_h \leq h, -h \leq y_h \leq h, -h \leq z_h \leq h$$

# Cohen-Sutherland Method in 3D

- ▶ If  $\text{outcode}(A) == \text{outcode}(B) == 0$ 
  - ▶ Accept the whole line segment.
- ▶ If  $(\text{outcode}(A) \text{ and } \text{outcode}(B)) \neq 0$ 
  - ▶ Reject the line segment.

## ▶ Other cases

- ▶ Calculate an intersection (according to outcode bits)
- ▶ Then check outcode again

- ▶ Note: use parametric forms

$$x_h = x_{ha} + (x_{hb} - x_{ha})u$$

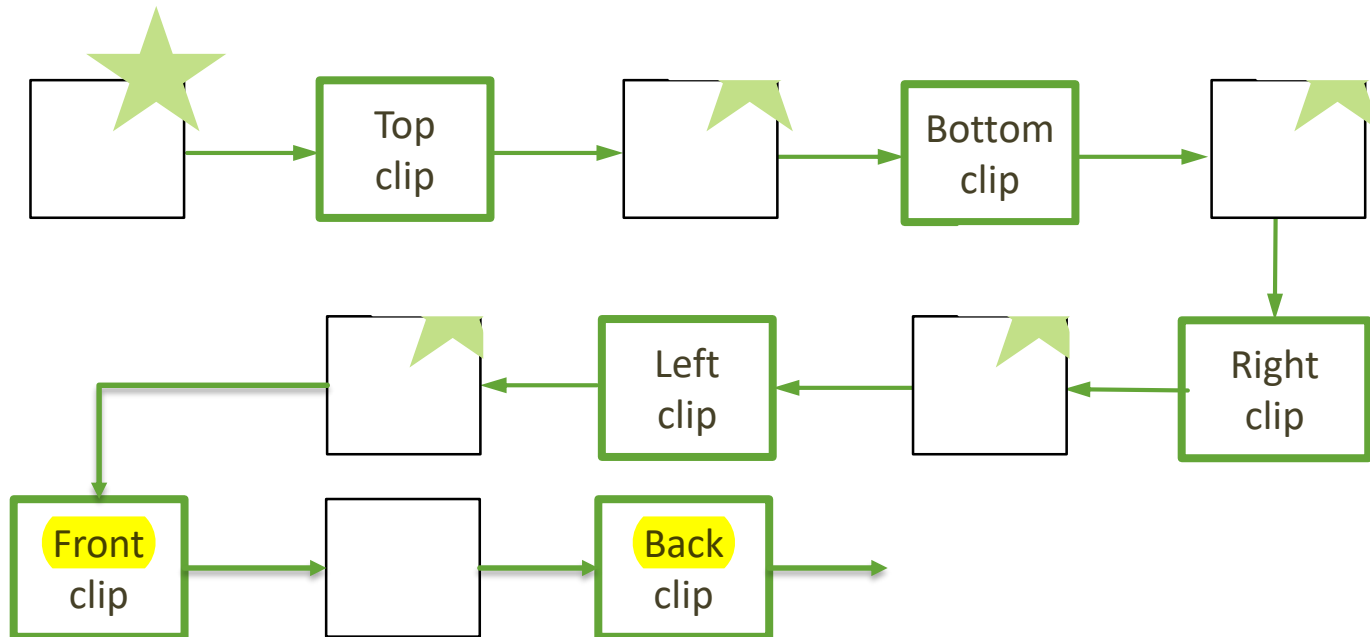
$$y_h = y_{ha} + (y_{hb} - y_{ha})u$$

$$z_h = z_{ha} + (z_{hb} - z_{ha})u$$

$$h = h_a + (h_b - h_a)u$$

# Polygon Clipping in 3D

- ▶ Similar to 2D clipping
  - ▶ Bounding box
  - ▶ Clipping with each clipping plane
  - ▶ Etc.....

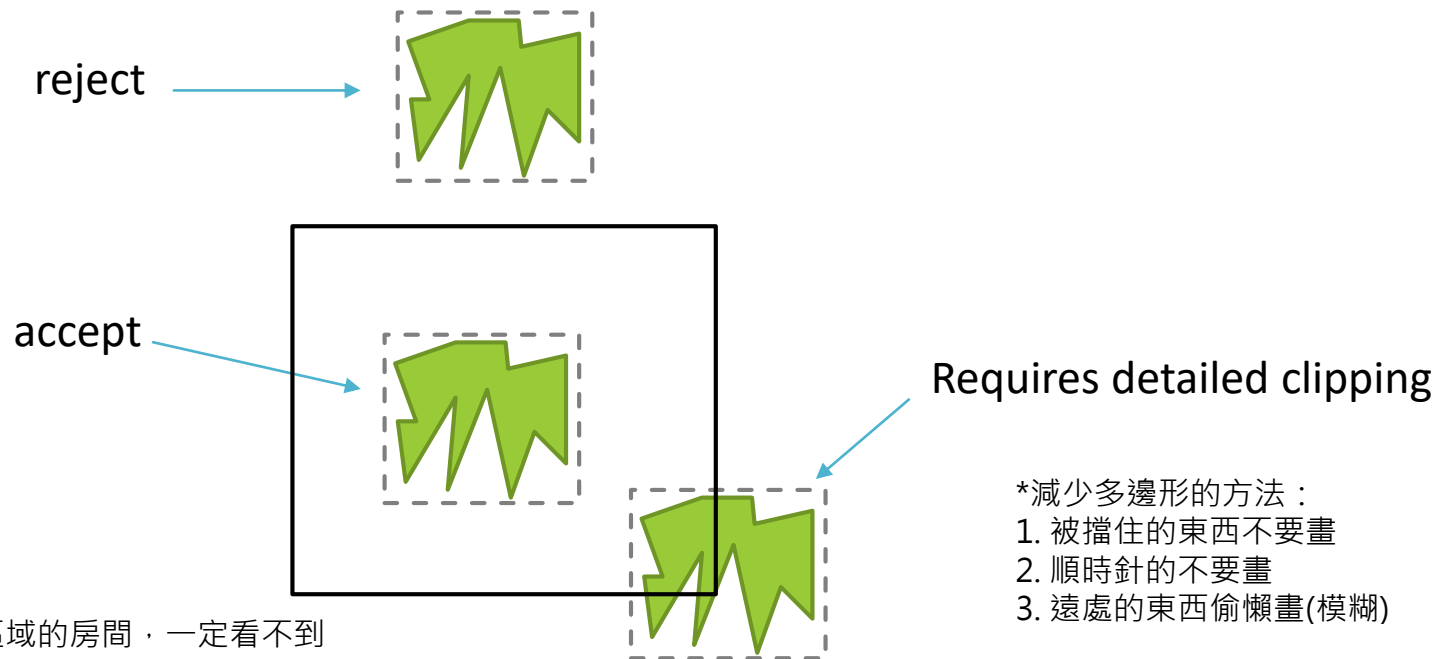




# Bounding Boxes

\*把物件用一個多邊形框住(不會真正畫出來) · 兩個立體去做intersection  
=>可以直接用min/max踢掉frame box以外的物件

- ▶ Rather than doing clipping on a complex polygon, we can use an **axis-aligned** bounding box or extent
  - ▶ Smallest rectangle aligned with axes that encloses the polygon
  - ▶ Simple to compute: max and min of x and y



\*地下城->不渲染不同區域的房間，一定看不到