
An Observation of the Sleeping Situation of PSU students by a Two-factor ANCOVA Analysis

Jiarong Ye
College of Engineering
The Pennsylvania State University
State College, PA 16801
jxy225@psu.edu

Abstract

The motivation of this report is to observe the sleeping situation of PSU students and study the relations between the average sleeping hours of students and influence factors including their class standing, majors, the interaction term of class standing and majors and the number of dues they have every week, which is considered the covariate in the experiment. The experimental units are PSU students including freshmen, sophomore, junior and senior majoring in Engineering, Business and Liberal Arts. And the data model applied to the experiment is the Two-Factor ANCOVA model.

1 Introduction

As students get heavier workload and higher stress level when the final month approaches, their sleeping condition is affected as well. And the effect differs for students in different class standing and majors. For example, compared with freshmen, seniors are more likely to take on a heavier workload and have more responsibilities such as academic research or job searching. And the majors students are in play an important role as well. Engineering students usually have more academic obligations such as experiments, labs, group projects, technical papers that they need to work on. So are the students in the smeal college of business studying finance, accounting and marketing where case studies require lots of work. In comparison, Liberal Arts students might have a more flexible class schedule and not be as busy as their peers in Engineering and Business. Therefore in order to confirm this speculation, a Two-Factor ANCOVA Model is constructed to test the relations between the response (average sleeping hours per week), two factors (class standing and major) and one covariate (number of dues per week).

2 Data Set

The dataset for the experiment is randomly collected from 60 full-time PSU students taking a bio-behavioral health general education class through informal surveys I conducted at the beginning of each class in November. The response from 48 students are used, among which 16 of them major in Engineering, 16 of them major in Business and 16 of them major in Liberal Arts, and 4 students in each major are in each class stand-

ing respectively (freshmen, sophomore, junior, senior). Their average sleeping hours and the total number of dues in that specific week are collected. The attributes contained in the dataset include:

- **Class standing**
- **Major**
- **Number of dues per week (covariate)**
- **Average sleeping hours per week**

df	class	major	num_of_dues_per_week	avg_sleep_hrs_per_week
1	freshmen	Engineering	5	7.1
2	freshmen	Engineering	4	7.5
3	freshmen	Engineering	6	7.2
4	freshmen	Engineering	7	6.9
5	freshmen	Business	4	7.1
6	freshmen	Business	3	7.6
7	freshmen	Business	3	7.4
8	freshmen	Business	5	7.1
9	freshmen	Liberal Arts	2	8.5
10	freshmen	Liberal Arts	3	8.3
11	freshmen	Liberal Arts	4	8.0
12	freshmen	Liberal Arts	4	8.1
13	sophomore	Engineering	6	7.0
14	sophomore	Engineering	5	7.4
15	sophomore	Engineering	8	6.4
16	sophomore	Engineering	7	6.7
17	sophomore	Business	6	7.3
18	sophomore	Business	3	8.0
19	sophomore	Business	4	6.4
20	sophomore	Business	6	7.5
21	sophomore	Liberal Arts	4	8.0
22	sophomore	Liberal Arts	3	8.3
23	sophomore	Liberal Arts	3	8.2
24	sophomore	Liberal Arts	4	7.9
25	junior	Engineering	4	6.5
26	junior	Engineering	6	6.6
27	junior	Engineering	4	7.0
28	junior	Engineering	5	7.2
29	junior	Business	5	7.5
30	junior	Business	4	7.7
31	junior	Business	6	7.8
32	junior	Business	4	7.8
33	junior	Liberal Arts	4	7.1
34	junior	Liberal Arts	5	7.7
35	junior	Liberal Arts	5	7.8
36	junior	Liberal Arts	4	7.6
37	senior	Engineering	6	6.4
38	senior	Engineering	5	6.9
39	senior	Engineering	5	5.9

df	class	major	num_of_dues_per_week	avg_sleep_hrs_per_week
40	senior	Engineering	7	6.1
41	senior	Business	6	6.5
42	senior	Business	4	7.3
43	senior	Business	5	6.8
44	senior	Business	6	6.4
45	senior	Liberal Arts	4	7.4
46	senior	Liberal Arts	2	8.0
47	senior	Liberal Arts	3	7.3
48	senior	Liberal Arts	3	7.8

3 Exploratory Data Analysis

Next we look at the data multivariately with figures:

3.1 Weekly Average Sleeping Hours

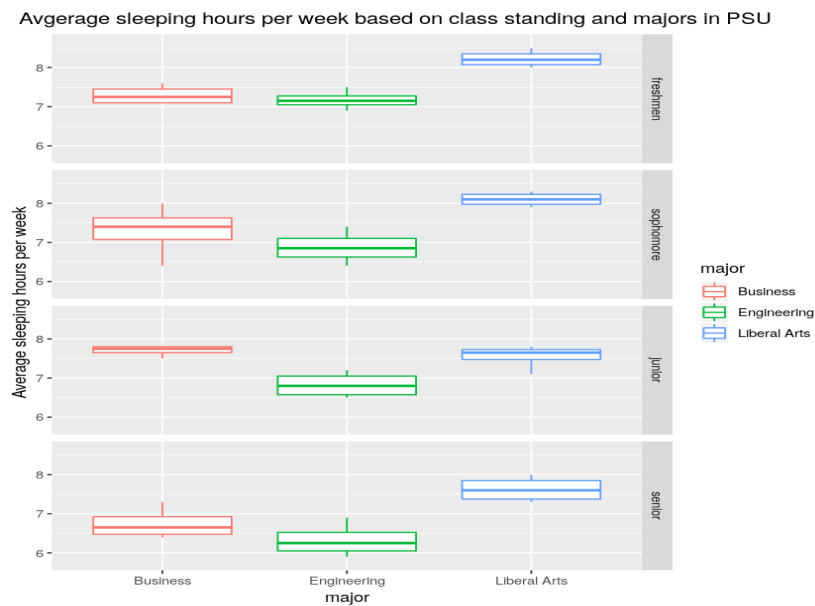


Figure 1: Average sleeping hours per week of different majors

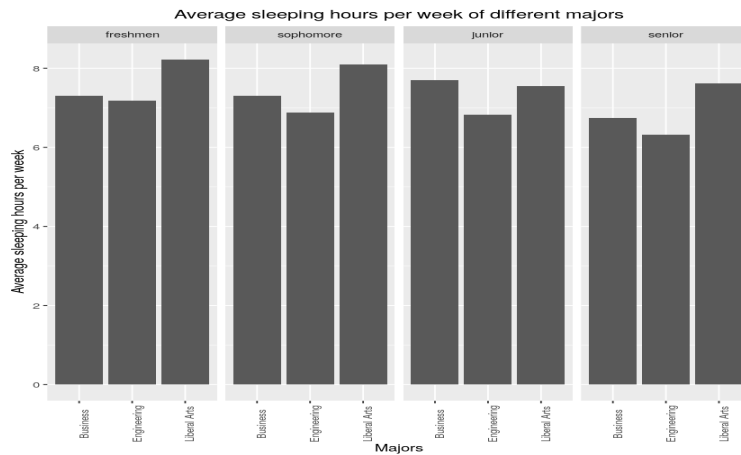


Figure 2: Average sleeping hours per week of different majors

The apparent pattern we observe from the side-by-side bar plot as well as the boxplot is that Liberal Arts students get the longest sleeping hours from freshmen to senior, compared with students majoring in Engineering and Business. And the tendency as the class standing increases among all three majors is similar, freshmen obviously get more sleeping time than juniors and seniors.

3.2 Weekly Number of Dues

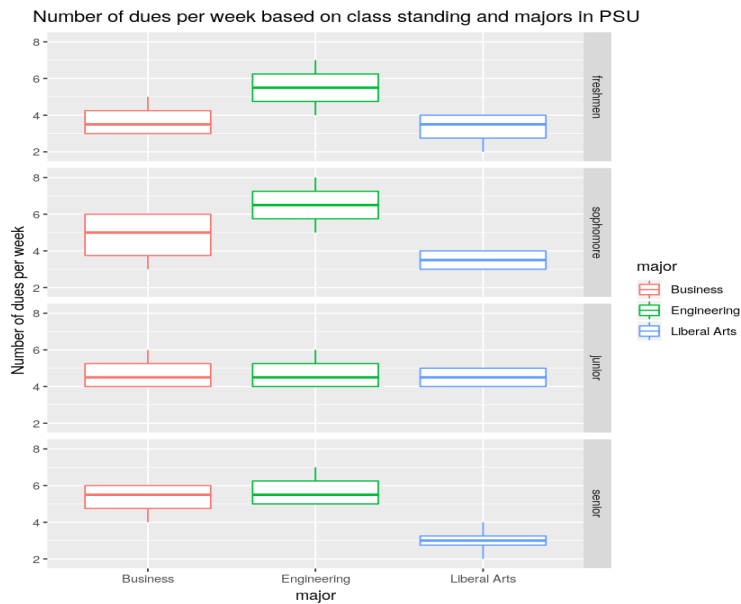


Figure 3: Number of dues per week based on class standing and majors

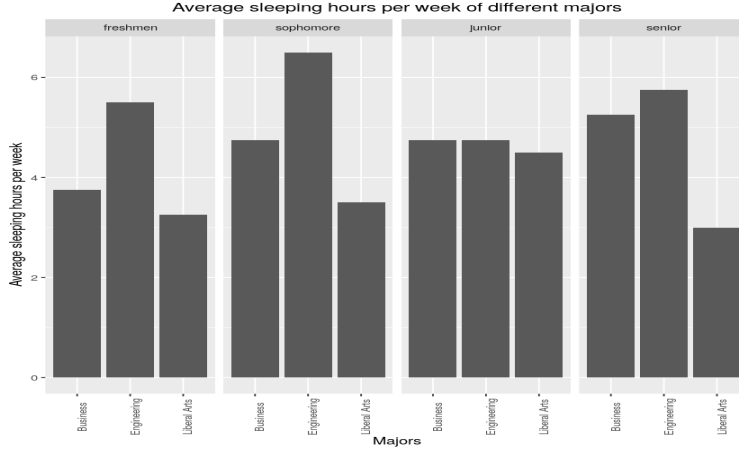


Figure 4: Number of dues per week of different majors

Similar to the average sleeping hours, the number of dues per week share the same tendency that that Liberal Arts students have the least amount of workload from freshmen to senior, compared with students majoring in Engineering and Business. However unlike the relation of average sleeping hours and class standing presented in the figures above, the weekly dues number does not seem to differ significantly based on class standing.

4 Modeling

4.1 Description

In the experiment, firstly, the hypothesis of linearity and equal slope assumption of the covariate will be tested in order to confirm the assumption is actually valid. Secondly, the hypothesis regarding the significance of the interaction term (**class_standing:major**) will be tested. If it is proven to be significant, then the pairwise differences of the interaction of class_standing and major are tested to determine how the interactive term is significant; if it is proven to be not significant, then the interaction term is dropped and pairwise differences of single factor (class_standing and major, respectively) will be tested.

4.2 Data Model

The Two-factor covariance data model for this experiment is:

$$Y_{ijt} = \mu + \alpha_i + \beta_j + (\alpha\beta)_{ij} + \gamma(X_{ijt} - \bar{X}_{...}) + \epsilon_{ijt}, \quad \epsilon_{ijt} \stackrel{iid}{\sim} N(0, \sigma^2)$$

α : The fixed effect of the **Class Standing** factor (Freshmen, Sophomore, Junior, Senior)

β : The fixed effect of the **Major** factor (Engineering, Business, Liberal Arts)

X : The number of dues per week

Y : The average sleeping hours per week

$i = 1, 2, 3, 4, j = 1, 2, 3, t = 1, 2, 3, 4$

4.3 Analysis Before Model Building

4.3.1 Test of Interactions Between Factor and Covariate

1. The interaction between *class standing* and *number of dues per week*

- 1. ANOVA(I(x -mean(x)) + class)
- 2. ANOVA(I(x-mean(x))*class)

anova	Res.Df	RSS	Df	Sum of Sq	F	Pr(>F)
1	43	7.94571416749420				
2	40	7.02215422440894	3	0.923559943085267	1.75361180927449	0.171576450358816

2. The interaction between *major* and *number of dues per week*

- 1. ANOVA(I(x -mean(x)) + major)
- 2. ANOVA(I(x-mean(x))*major)

anova	Res.Df	RSS	Df	Sum of Sq	F	Pr(>F)
1	44	7.83107894736842				
2	42	7.81652126882414	2	0.0145576785442874	0.0391109086658986	0.96167902939109

We can observe from there ANOVA contrast table that after adding the interaction term **I(num_of_dues_per_week-mean(num_of_dues_per_week))*class** and **I(num_of_dues_per_week-mean(num_of_dues_per_week))*major** to the ANOVA model, the new p value become 0.1715765 which is > 0.05 and 0.961679, which is also > 0.05 , indicating the additional interaction term between **num_of_dues_per_week** and **class standing** is not significant, and the additional interaction term between **num_of_dues_per_week** and **major** is not significant either. Therefore it's safe to conclude that the interaction between **class standing** and **number of dues per week**, and **major** and **number of dues per week** are not significant, hence the issue of interaction between covariate and main factors could be dropped later in the two-factor covariate model building without any transformation to the response.

4.3.2 Diagnostics of Linearity and Equal Slopes Assumptions

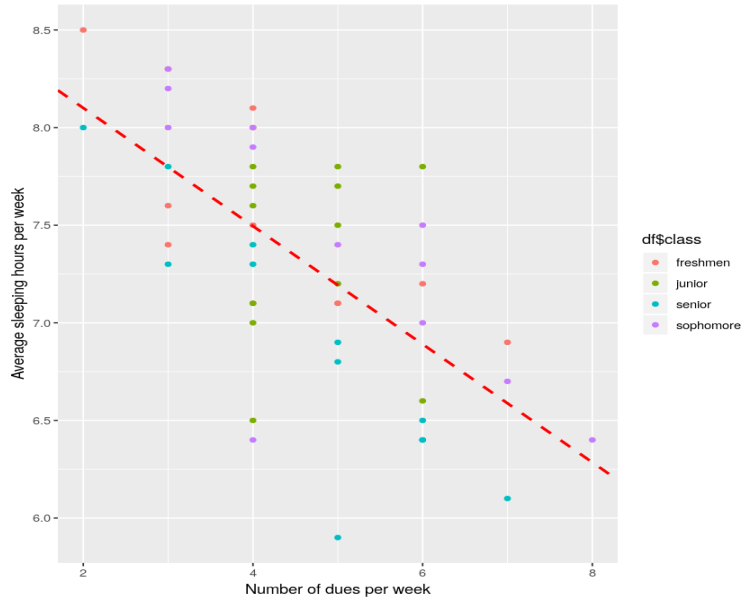


Figure 5: Average sleeping hours per week vs. Number of dues per week

It appears that both the linearity and equal slopes assumptions required for ANCOVA are valid.

4.4 ANCOVA Model

4.4.1 Interaction Term

The first test is for the significance of interaction terms:

Null Hypothesis:

$$H_0 : (\alpha\beta)_{ij} = 0 \text{ for all } i, j$$

Alternative Hypothesis:

$$H_a : (\alpha\beta)_{ij} \neq 0 \text{ for all } i, j$$

ANOVA Table:

(Note* : denote x : num_of_dues_per_week)

anova	Df	Sum Sq	Mean Sq	F value	Pr(>F)
class	3	2.99416666666667	0.998055555555556	9.81822073619254	7.68501150692738e - 05
major	2	9.30500000000000	4.65249999999999	45.76826582535172	1.70770191448029e - 10
I(x - mean(x))	1	1.13158208020050	1.13158208020050	11.13176774848383	2.01977445976904e - 03
class:major	6	1.56388212561606	0.260647020936010	2.56407568850839	3.64868969776764e - 02
Residuals	35	3.55786912751677	0.101653403643336		

Check Residuals Normality and Variance Constance Violation

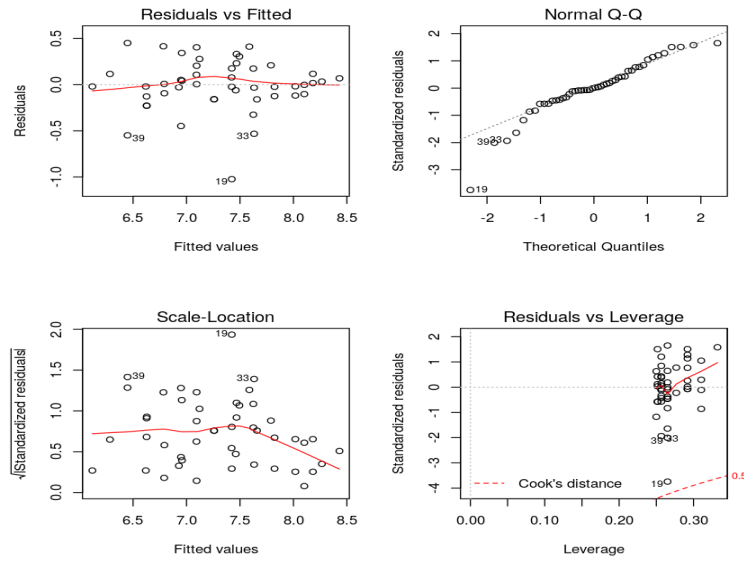


Figure 6: Residual vs. Fitted Value Plot and QQ Plot

From the diagnostic plots above we can see that the assumptions of normality and the constancy of variance of residuals are not violated. Therefore no transformation of variables is needed for this experiment.

Therefore, from the ANCOVA table, we can see that the P value of **class:major** is 0.0364869, and since $0.0364869 < 0.05$, therefore under the significance level of 5%, we are confident enough to reject the null hypothesis and conclude that the interaction term is significant.

Confirm the significant interaction with interaction plot:

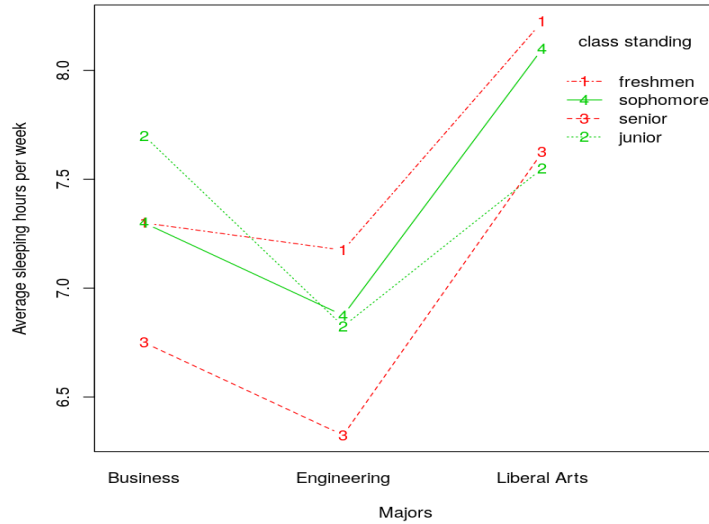


Figure 7: Interaction Plot

The interaction plot shows a strong interaction, with the lines for class standing=Freshmen, class standing=Sophomore, class standing=Junior, class standing=Senior not being parallel with each other.

4.4.2 Pairwise Difference Between Interactive Combinations

Since there are significant interactions, then we can't interpret the effects of each factor individually, and we move directly to the testing for pairwise differences between all interaction of class standing and majors.

Null Hypothesis:

$$H_0 : \tau_{ij} - \tau_{kl} = 0, \text{ for all } i, j, k, l, \text{ where } (i, j) \neq (k, l)$$

Alternative Hypothesis:

$$H_a : \tau_{ij} - \tau_{kl} \neq 0$$

$$\text{Note}^* : \tau_{ij} = \alpha_i + \beta_j + (\alpha\beta)_{ij}$$

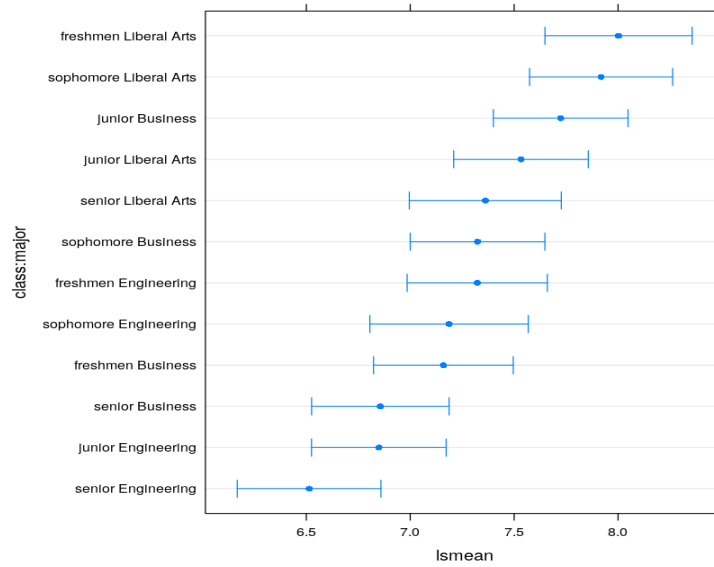


Figure 8: Contrast Plot

Contrast table:

contrast	estimate	SE	df	t.ratio	p.value
freshmen,Business - junior,Business	-0.5644	0.2314	35	-2.439	0.4084
freshmen,Business - senior,Business	0.3034	0.2387	35	1.271	0.9777
freshmen,Business - sophomore,Business	-0.1644	0.2314	35	-0.711	0.9999
freshmen,Business - freshmen,Engineering	-0.1628	0.2433	35	-0.669	0.9999
freshmen,Business - junior,Engineering	0.3106	0.2314	35	1.342	0.9670
freshmen,Business - senior,Engineering	0.6461	0.2485	35	2.600	0.3174
freshmen,Business - sophomore,Engineering	-0.0272	0.2673	35	-0.102	1.0000
freshmen,Business - freshmen,Liberal Arts	-0.8428	0.2270	35	-3.713	0.0294
freshmen,Business - junior,Liberal Arts	-0.3733	0.2288	35	-1.631	0.8855
freshmen,Business - senior,Liberal Arts	-0.2017	0.2288	35	-0.881	0.9989
freshmen,Business - sophomore,Liberal Arts	-0.7589	0.2258	35	-3.361	0.0689
junior,Business - senior,Business	0.8678	0.2270	35	3.824	0.0222
junior,Business - sophomore,Business	0.4000	0.2254	35	1.774	0.8205
junior,Business - freshmen,Engineering	0.4017	0.2288	35	1.755	0.8300
junior,Business - junior,Engineering	0.8750	0.2254	35	3.881	0.0191
junior,Business - senior,Engineering	1.2106	0.2314	35	5.231	0.0004
junior,Business - sophomore,Engineering	0.5372	0.2433	35	2.208	0.5548
junior,Business - freshmen,Liberal Arts	-0.2784	0.2387	35	-1.166	0.9884
junior,Business - junior,Liberal Arts	0.1911	0.2258	35	0.846	0.9993
junior,Business - senior,Liberal Arts	0.3628	0.2433	35	1.491	0.9333
junior,Business - sophomore,Liberal Arts	-0.1945	0.2347	35	-0.829	0.9994

contrast	estimate	SE	df	t.ratio	p.value
senior,Business - sophomore,Business	-0.4678	0.2270	35	-2.061	0.6513
senior,Business - freshmen,Engineering	-0.4661	0.2258	35	-2.064	0.6494
senior,Business - junior,Engineering	0.0072	0.2270	35	0.032	1.0000
senior,Business - senior,Engineering	0.3428	0.2270	35	1.510	0.9277
senior,Business - sophomore,Engineering	-0.3305	0.2347	35	-1.408	0.9540
senior,Business - freshmen,Liberal Arts	-1.1461	0.2485	35	-4.613	0.0026
senior,Business - junior,Liberal Arts	-0.6767	0.2288	35	-2.957	0.1650
senior,Business - senior,Liberal Arts	-0.5050	0.2542	35	-1.986	0.6989
senior,Business - sophomore,Liberal Arts	-1.0622	0.2433	35	-4.366	0.0052
sophomore,Business - freshmen,Engineering	0.0017	0.2288	35	0.007	1.0000
sophomore,Business - junior,Engineering	0.4750	0.2254	35	2.107	0.6215
sophomore,Business - senior,Engineering	0.8106	0.2314	35	3.503	0.0493
sophomore,Business - sophomore,Engineering	0.1372	0.2433	35	0.564	1.0000
sophomore,Business - freshmen,Liberal Arts	-0.6784	0.2387	35	-2.842	0.2065
sophomore,Business - junior,Liberal Arts	-0.2089	0.2258	35	-0.925	0.9983
sophomore,Business - senior,Liberal Arts	-0.0372	0.2433	35	-0.153	1.0000
sophomore,Business - sophomore,Liberal Arts	-0.5945	0.2347	35	-2.533	0.3540
freshmen,Engineering - junior,Engineering	0.4733	0.2288	35	2.068	0.6465
freshmen,Engineering - senior,Engineering	0.8089	0.2258	35	3.582	0.0407
freshmen,Engineering - sophomore,Engineering	0.1356	0.2314	35	0.586	1.0000
freshmen,Engineering - freshmen,Liberal Arts	-0.6800	0.2542	35	-2.675	0.2799
freshmen,Engineering - junior,Liberal Arts	-0.2106	0.2314	35	-0.910	0.9986
freshmen,Engineering - senior,Liberal Arts	-0.0389	0.2605	35	-0.149	1.0000
freshmen,Engineering - sophomore,Liberal Arts	-0.5961	0.2485	35	-2.399	0.4326
junior,Engineering - senior,Engineering	0.3356	0.2314	35	1.450	0.9442
junior,Engineering - sophomore,Engineering	-0.3378	0.2433	35	-1.388	0.9583
junior,Engineering - freshmen,Liberal Arts	-1.1534	0.2387	35	-4.832	0.0014
junior,Engineering - junior,Liberal Arts	-0.6839	0.2258	35	-3.028	0.1428
junior,Engineering - senior,Liberal Arts	-0.5122	0.2433	35	-2.106	0.6223
junior,Engineering - sophomore,Liberal Arts	-1.0695	0.2347	35	-4.556	0.0030
senior,Engineering - sophomore,Engineering	-0.6733	0.2288	35	-2.942	0.1699
senior,Engineering - freshmen,Liberal Arts	-1.4889	0.2605	35	-5.715	0.0001
senior,Engineering - junior,Liberal Arts	-1.0195	0.2347	35	-4.343	0.0055
senior,Engineering - senior,Liberal Arts	-0.8478	0.2673	35	-3.171	0.1054
senior,Engineering - sophomore,Liberal Arts	-1.4050	0.2542	35	-5.526	0.0002
sophomore,Engineering - freshmen,Liberal Arts	-0.8156	0.2822	35	-2.890	0.1884
sophomore,Engineering - junior,Liberal Arts	-0.3461	0.2485	35	-1.393	0.9573
sophomore,Engineering - senior,Liberal Arts	-0.1745	0.2903	35	-0.601	1.0000
sophomore,Engineering - sophomore,Liberal Arts	-0.7317	0.2746	35	-2.665	0.2846
freshmen,Liberal Arts - junior,Liberal Arts	0.4695	0.2347	35	2.000	0.6902
freshmen,Liberal Arts - senior,Liberal Arts	0.6411	0.2258	35	2.839	0.2078
freshmen,Liberal Arts - sophomore,Liberal Arts	0.0839	0.2258	35	0.371	1.0000
junior,Liberal Arts - senior,Liberal Arts	0.1716	0.2387	35	0.719	0.9998
junior,Liberal Arts - sophomore,Liberal Arts	-0.3856	0.2314	35	-1.666	0.8712
senior,Liberal Arts - sophomore,Liberal Arts	-0.5572	0.2270	35	-2.455	0.3987

P value adjustment: tukey method for comparing a family of 12 estimates

From the p values of contrast table of interaction terms, we could make the following conclusions:

- Freshmen majoring in Business sleep significantly less than freshmen majoring in Liberal Arts;
- Junior majoring in Business sleep significantly more than senior majoring in Business;
- Junior majoring in Business sleep significantly more than junior majoring in Engineering;
- Junior majoring in Business sleep significantly more than senior majoring in Engineering;
- Senior majoring in Business sleep significantly less than freshmen majoring in Liberal Arts;
- Senior majoring in Business sleep significantly less than sophomore majoring in Liberal Arts;
- Sophomore majoring in Business sleeps significantly more than senior majoring in Engineering;
- Freshmen majoring in Engineering sleeps significantly more than senior majoring in Engineering;
- Junior majoring in Engineering sleeps significantly less than freshmen majoring in Liberal Arts;
- Senior majoring in Engineering sleeps significantly less than freshmen majoring in Liberal Arts;
- Senior majoring in Engineering sleeps significantly less than junior majoring in Liberal Arts;
- Senior majoring in Engineering sleeps significantly less than sophomore majoring in Liberal Arts;
- No other comparisons are significantly different than zero.

5 Conclusion

From the Two-Factor ANCOVA analysis above to study the sleeping condition of PSU students of different class standing and different majors in November (the month before the finals) we learn that the linearity and equal slope assumption between the covariate and the response is valid and there exists a significant interaction effect between class standing and major. Specifically, from the contrast table of the interactive combination of class standing and major, juniors and seniors who are majoring in Engineering sleep significantly less than freshmen and sophomore majoring in Liberal Arts, which confirms the speculation made in the introduction that Engineering students are more likely to shoulder more workload and that affects their sleeping conditions.

6 Appendix: R Code

Listing 1: dataset for experiment

```
class=c(rep("freshmen", 12),
        rep("sophomore", 12),
        rep("junior", 12),
        rep("senior", 12))
major=c(rep(c(rep("Engineering", 4),
                rep("Business", 4),
                rep("Liberal Arts", 4)),
            4))
num_of_dues_per_week = c(5, 4, 6, 7,
```

```

4, 3, 3, 5,
2, 3, 4, 4,
6, 5, 8, 7,
6, 3, 4, 6,
4, 3, 3, 4,
4, 6, 4, 5,
5, 4, 6, 4,
4, 5, 5, 4,
6, 5, 5, 7,
6, 4, 5, 6,
4, 2, 3, 3)
avg_sleep_hrs_per_week=c(7.1, 7.5, 7.2, 6.9,
7.1, 7.6, 7.4, 7.1,
8.5, 8.3, 8.0, 8.1,
7.0, 7.4, 6.4, 6.7,
7.3, 8.0, 6.4, 7.5,
8.0, 8.3, 8.2, 7.9,
6.5, 6.6, 7.0, 7.2,
7.5, 7.7, 7.8, 7.8,
7.1, 7.7, 7.8, 7.6,
6.4, 6.9, 5.9, 6.1,
6.5, 7.3, 6.8, 6.4,
7.4, 8.0, 7.3, 7.8)
df=data.frame(class , major , num_of_dues_per_week , avg_sleep_hrs_per_week)

```

Listing 2: Average sleeping hours per week of different majors

```

library(ggplot2)
library(plyr)
df_sleep <- ddply(df, .(class), transform, pos = cumsum(avg_sleep_hrs_per_week)
- (0.5 * avg_sleep_hrs_per_week))
df_sleep$class_adjusted = factor(df_sleep$class,
levels=c('freshmen','sophomore', 'junior','senior'))
ggplot(df_sleep, aes(x = major, y = avg_sleep_hrs_per_week*0.25)) +
geom_bar(stat="identity") +
facet_grid(.~class_adjusted) +
ylab('Average sleeping hours per week') +
xlab('Majors') +
ggtitle('Average sleeping hours per week of different majors') +
theme(plot.title = element_text(hjust = 0.5)) +
theme(axis.text.x = element_text(angle = 90, size = 8))

```

Listing 3: Average sleeping hours per week based on class standing and majors in PSU

```

ggplot(df_sleep, aes(x=major, y=avg_sleep_hrs_per_week, color=major)) +
geom_boxplot() +
facet_grid(vars(class_adjusted)) +
ylab('Average sleeping hours per week') +
ggtitle('Average sleeping hours per week based on class standing and majors') +
theme(plot.title = element_text(hjust = 0.2)) +
ylim(min(df$avg_sleep_hrs_per_week)-0.2,
max(df$avg_sleep_hrs_per_week)+0.2)

```

Listing 4: Number of dues per week of different majors

```

df_due <- ddply(df, .(class), transform,
               pos = cumsum(num_of_dues_per_week) - (0.5 * num_of_dues_per_week))
df_due$class_adjusted = factor(df_due$class,
                               levels=c('freshmen', 'sophomore', 'junior', 'senior'))
ggplot(df_due, aes(x = major, y = num_of_dues_per_week*0.25)) +
  geom_bar(stat="identity") +
  facet_grid(.~class_adjusted) +
  ylab('Average sleeping hours per week') +
  xlab('Majors') +
  ggtitle('Number of dues per week of different majors') +
  theme(plot.title = element_text(hjust = 0.5)) +
  theme(axis.text.x = element_text(angle = 90, size = 8))

```

Listing 5: Number of dues per week based on class standing and majors in PSU

```

ggplot(df_due, aes(x=major, y=num_of_dues_per_week, color=major)) +
geom_boxplot() +
  facet_grid(vars(class_adjusted)) +
  ylab('Number of dues per week') +
  ggtitle('Number of dues per week based on class standing and majors') +
  theme(plot.title = element_text(hjust = 0.2)) +
  ylim(min(df$num_of_dues_per_week)-0.2, max(df$num_of_dues_per_week)+0.2)

```

Listing 6: The interaction between major/class standing and number of dues per week

```

mod1 <- aov(avg_sleep_hrs_per_week ~ I(num_of_dues_per_week
  -mean(num_of_dues_per_week)) + class, data = df)
mod2 <- aov(avg_sleep_hrs_per_week ~ I(num_of_dues_per_week
  -mean(num_of_dues_per_week))*class, data = df)
anova(mod1, mod2)

mod1 <- aov(avg_sleep_hrs_per_week ~ I(num_of_dues_per_week
  -mean(num_of_dues_per_week)) + major, data = df)
mod2 <- aov(avg_sleep_hrs_per_week ~ I(num_of_dues_per_week
  -mean(num_of_dues_per_week))*major, data = df)
anova(mod1, mod2)

```

Listing 7: Diagnostics of linearity and equal slopes assumptions

```

qplot(x = df$num_of_dues_per_week,
      y = df$avg_sleep_hrs_per_week,
      col = df$class,
      xlab = 'Number of dues per week',
      ylab = 'Average sleeping hours per week') +
  geom_abline(intercept = 8.7053,
              slope = -0.3025,
              color="red",
              linetype="dashed",
              size=1)

```

Listing 8: Residuals Normality and Constance of Variance Violation Check Plot

```

par(mfrow=c(2,2))
plot(aov.sleep)

```

Listing 9: Interaction Plot

```
interaction.plot(x.factor = df$major, trace.factor = df$class,
                 response = df$avg_sleep_hrs_per_week, type = "b", col = 2:3,
                 xlab = "Majors",
                 ylab = "Average sleeping hours per week",
                 trace.label = "class standing")
```

Listing 10: Pairwise Differences of allinteractive combinations

```
lsminter=lsmmeans(aov.sleep, ~ class:major)
contrast(lsminter, method="pairwise")
contrast_inter = cld(lsminter, alpha=0.05)
plot(contrast_inter)
```
