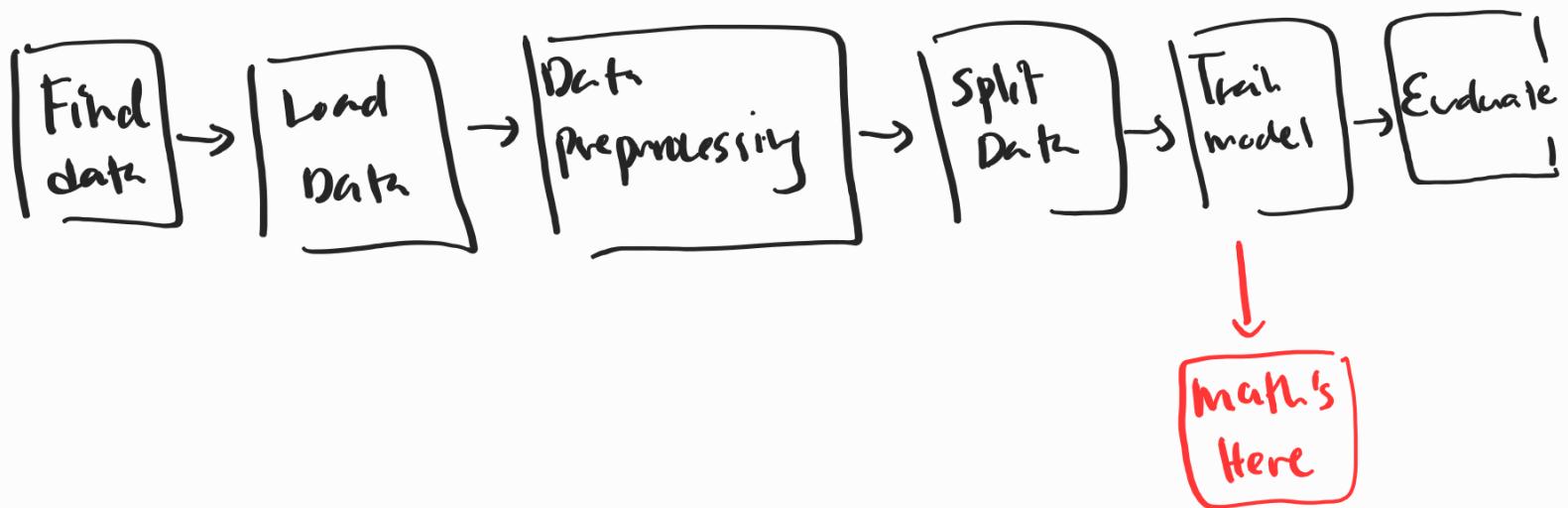


Machine Learning Flow (works for any algo)



Naïve Bayes: The Maths

Consider this situation. You have a friend, named Ali. He comes to class. Sometimes he comes by car, sometimes by bus. You've noticed that when he comes by car, he is usually early. When he comes by bus, he is often late.

$$P(\text{Bus}) = 0.4 \quad : \text{Probability of Ali taking Bus}$$

$$P(\text{Car}) = 0.6 \quad : \quad \begin{matrix} " & " & " & " & " \end{matrix} \quad \text{car}$$

↳ Prior probability.

$$P(\text{Early} | \text{Bus}) = 0.25 \quad \leftarrow \text{Conditional probability}$$

$P(x | \text{condition})$

The probability of Ali coming to class Early given that we know he took the Bus.

$$P(\text{Marry supermodel}) \quad \downarrow 0.01$$

$$P(\text{Marry supermodel} | \begin{matrix} \text{Rich like oil} \\ \text{tycoon} \end{matrix}) = 0.4$$

Given information

$$\underline{P(\text{Bus}) = 0.4}$$

$$\underline{P(\text{Car}) = 0.6}$$

$$\underline{P(\text{Early} \mid \text{Bus}) = 0.25}$$

$$\underline{P(\text{Late} \mid \text{Bus}) = 0.75}$$

Intuitive,
common
sense,
logic

$$\underline{P(\text{Early} \mid \text{car}) = 0.75}$$

$$\underline{P(\text{Late} \mid \text{car}) = 0.25}$$

Joint Probability

$$P(X, Y) = \frac{P(X|Y) P(Y)}{\text{or}} \quad \frac{P(Y|X) P(X)}{\downarrow}$$

The probability of 2 events
happening

$$P(\text{Late, Bus})$$

$$= P(\text{Late} \mid \text{Bus}) P(\text{Bus}) = (0.75)(0.4)$$

$$= \underline{\underline{0.3}}$$



$$P(\text{Late, Car})$$

$$= P(\text{Late} \mid \text{Car}) P(\text{Car})$$

$$= (0.25)(0.6) = \underline{\underline{0.15}}$$

Marginal Probability

$$P(X) = \sum_{Y} P(X, Y)$$

$$= \sum_{Y} P(X|Y) P(Y)$$

~~Continue with our example~~

$$\bullet P(\text{Early, Bus})$$

$$= P(\text{Early} \mid \text{Bus}) \cdot P(\text{Bus}) = (0.25)(0.4) = \underline{\underline{0.1}}$$

$$\bullet P(\text{Early, car})$$

$$= P(\text{Early} \mid \text{Car}) P(\text{Car}) = 0.75 \times 0.6 = \underline{\underline{0.45}}$$

$$\bullet P(\text{Early}) = P(\text{Early, Bus}) + P(\text{Early, car}) = 0.1 + 0.45 = \underline{\underline{0.55}}$$

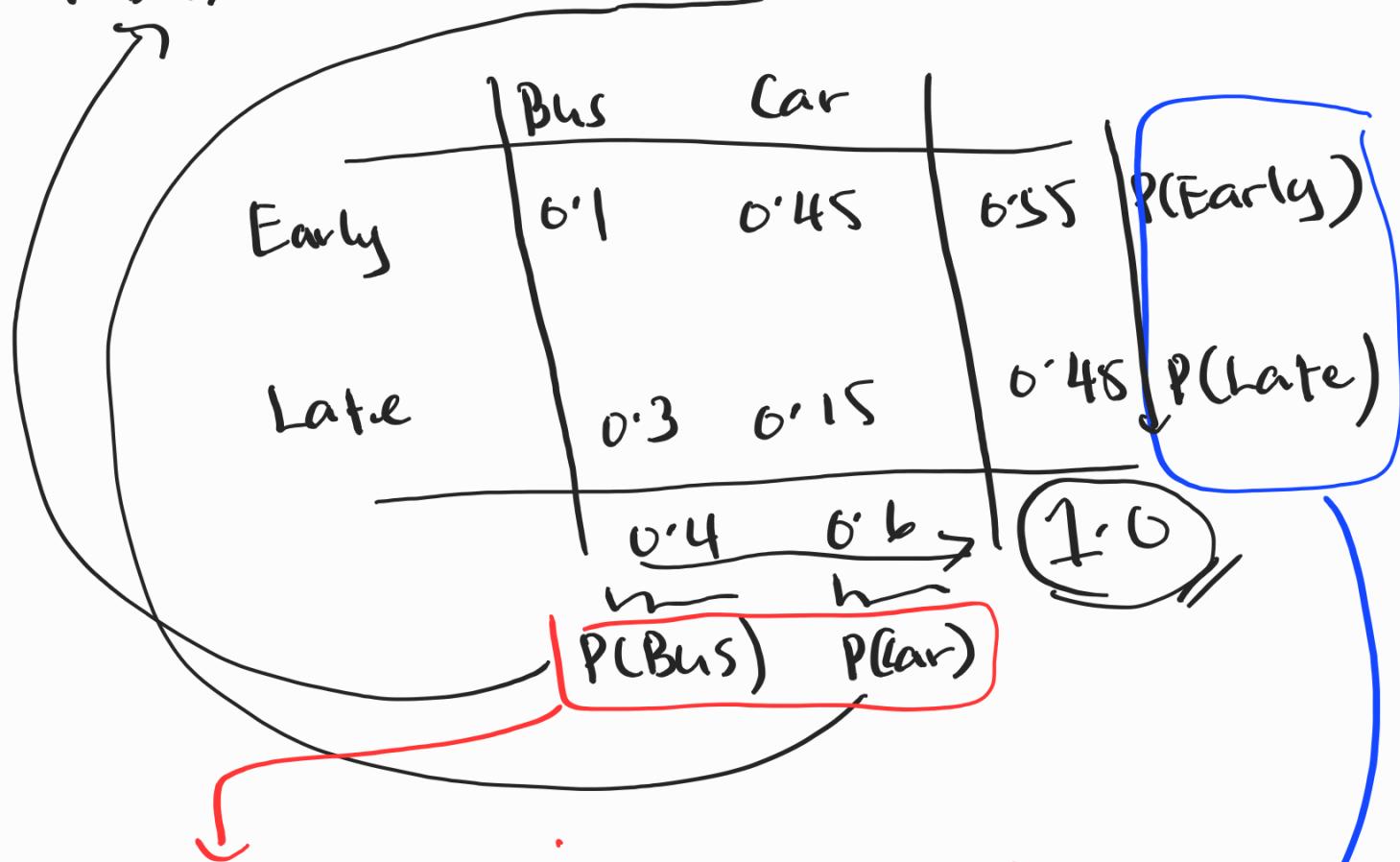
Let's put everything
together

		Bus	Car	
		Early	Late	Total
Early	Bus	0.1	0.45	0.55
	Car	0.3	0.15	0.45
Total		0.4	0.6	1.0
		P(Late, Bus)		

Summary

- ✓ Prior Probability : Given earlier
- ✓ Conditional " :
- ✓ Joint Probability
- ✓ Marginal Probability

$$P(\text{Bus}) = 0.4 \quad P(\text{Car}) = 0.6$$



Prior : The probability that is given earlier. Or something that we know beforehand

Marginal : $P(\text{Early})$: Probability of Ali being early regardless of the mode transports

Back to ML

What does the dataset look like?

Day	Attributes / Features		Target / output
	Bus	Car	
1	YES	No	Early
2	YES	No	Late
3	No	YES	Early
:	:	:	:
365	:	:	:

} Samples / Observations

- From the dataset above, you can calculate the conditional probabilities → Refer slides on how to calculate from a table.

$$\begin{array}{ll} P(\text{Early} \mid \text{Bus}) & P(\text{Late} \mid \text{Bus}) \\ P(\text{Early} \mid \text{Car}) & P(\text{Late} \mid \text{Car}) \end{array}$$

- The ML Question

CLASSIFICATION

Given a new row of information like below, what is the prediction for Ali?

Day	Bus	Car	Early / Late	Predict
367	YES	No	? Late	↓

- Posterior Probability , Bayes Theorem

$$P(\text{Bus} \mid \text{Late}) = \frac{P(\text{Late} \mid \text{Bus}) \cdot P(\text{Bus})}{P(\text{Late})}$$

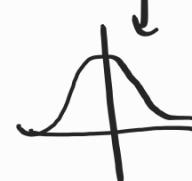
Posterior Probability

- $P(\text{Bus} | \text{Late}) = \frac{P(\text{Late} | \text{Bus}) P(\text{Bus})}{P(\text{Late})}$
- $P(\text{Bus} | \text{Early}) = \frac{P(\text{Early} | \text{Bus}) P(\text{Bus})}{P(\text{Early})}$
- $P(\text{Car} | \text{Late})$
- $P(\text{Car} | \text{Early})$

When we look at the slides, it will tell you, in practical we use the Gaussian Probability

$$P(\text{Bus Late}) = \frac{P(\text{Late} | \text{Bus}) P(\text{Bus})}{P(\text{Late})}$$

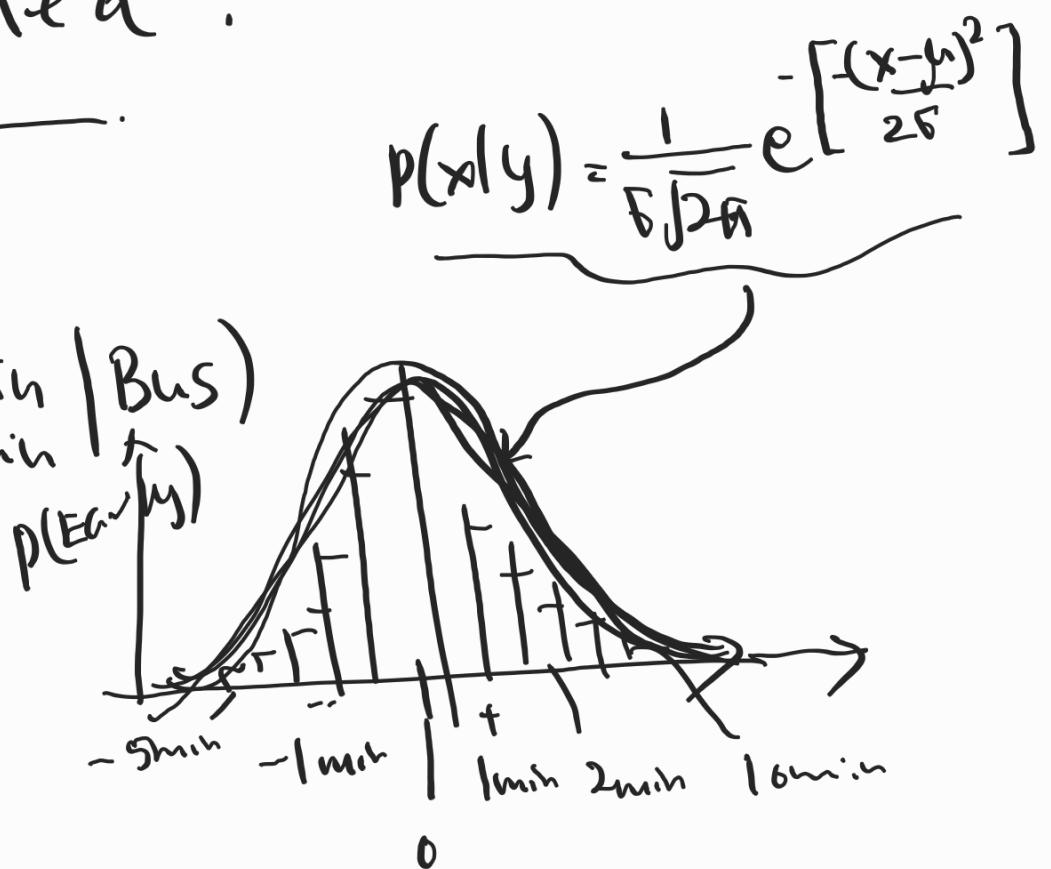
Likelihood \downarrow Prior \leftarrow

 Posterior \downarrow

 Marginal \uparrow


Both the posteriors and likelihood
are assumed to be normally
distributed.

- Example

$$P(\text{Early} = +1\text{min} | \text{Bus})$$



Day	Bus	Car	Early (By minutes)
Day 1	1	0	+1 min
2	0	1	+2 min
:	:	:	+0
:	:	:	-1 min
:	:	:	-10 mins
365	.	.	

$P(\text{Early} | \text{Bus})$

$$P(\text{Early} | \text{Bus}) = \frac{1}{\sqrt{2\pi}} e^{-\left[\frac{-(\text{Early} - \mu)^2}{2\sigma^2}\right]}$$