

The sequence generation function has a time complexity of  $O(n(\log n)^2)$ . There is one for loop nested within another for loop. The nested for loop repeatedly runs one time more than the previous iteration. Hence the big O is  $n(\log n)^2$ .

For space complexity of this function is equal to  $O(n)$ , because we malloc-ed  $n$  to the array that contains the sub array sequence. Even though the array will not every need this much space, it ensures that the array never overflows.

Shell Insertion sort			
Input Size	Time (sec)	comparisons	moves
15	0	93	15
1,000	0	35730	4543
10,000	0	623628	71109
100,000	0	9611932	1004825
1,000,00	2	137680165	13479446

Shell Selection sort			
Input Size	Time (sec)	comparisons	moves
15	0	473	45
1,000	0	1554965	13629
10,000	0	150943093	213327
100,000	22	15014392012	3014475
1,000,00	N/A	N/A	N/A

As we can see from the table above, as the number of inputs grew, the time taken to sort the numbers grew at an increasing rate.

The shell insertion sort has a time complexity equal to  $O(n^2/\log(n))$  and a space complexity equal to  $O(1)$ . No space is allocated in this function besides that allocated in the function call to the sequence generation function.

The shell selection sort has a time complexity equal to  $O(n^2)$  and a space complexity equal to  $O(1)$ . No space is allocated in this function besides that allocated in the function call to the sequence generation function.