



### Controlled Re-execution for Disjunctive Predicates

EE 382N Distributed Systems
Term Project
Fall 2015

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### **Motivation**

Mo•ti•va•tion /modə'vāSH(ə)n/

The driving force by which humans achieve their goals

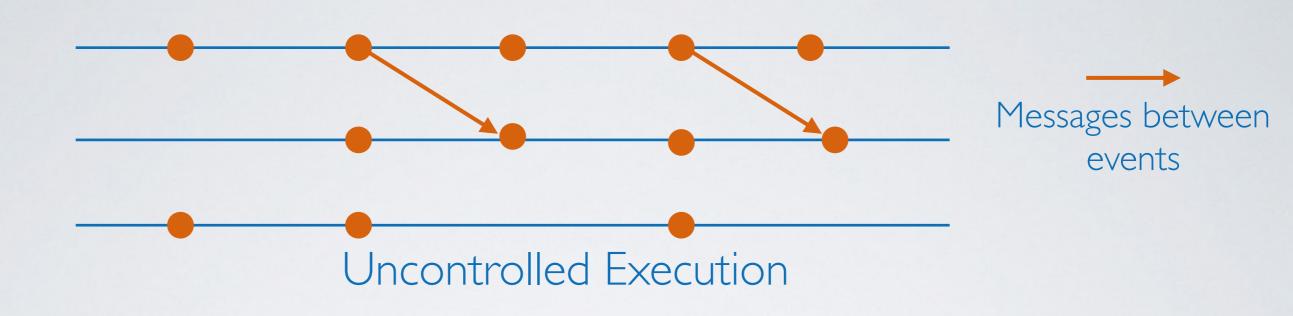
Proliferation of distributed computations

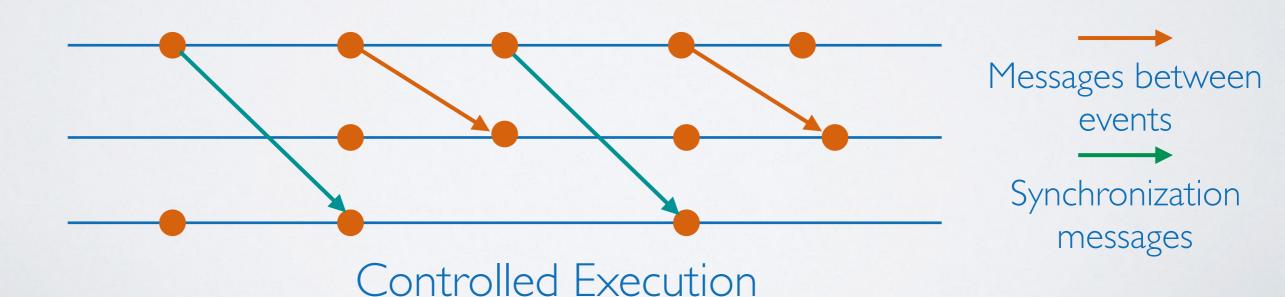
Non-deterministic nature of distributed computations

Present bugs are difficult to reproduce

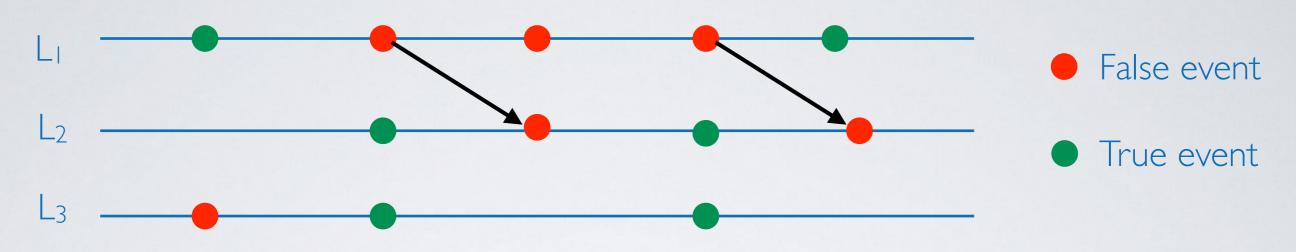
Need to control a distributed computation

### **Control Re-execution**





### Disjunctive Predicates



Global predicate B is a disjunction of local predicates on processes  $B = L_1 \vee L_2 \vee L_3$ 

#### Problem Statement

Given a distributed computations and a predicate B, we aim to control the execution by adding synchronization messages to the computation so that B is always satisfied.

 $B = at least one process is alive at any time <math>\Rightarrow B = alive(P_1) \vee alive(P_2) \dots \vee alive(P_n)$ 

B = mutual exclusion for two processes  $\Rightarrow$  B =  $\neg CS(P_1) \lor \neg CS(P_2)$ 

## Admissible Sequence

For a given computation and a predicate, an admissible sequence of events  $\alpha$  captures some safe execution of events S, where  $S \subseteq E$ 

### Properties of admissible sequence

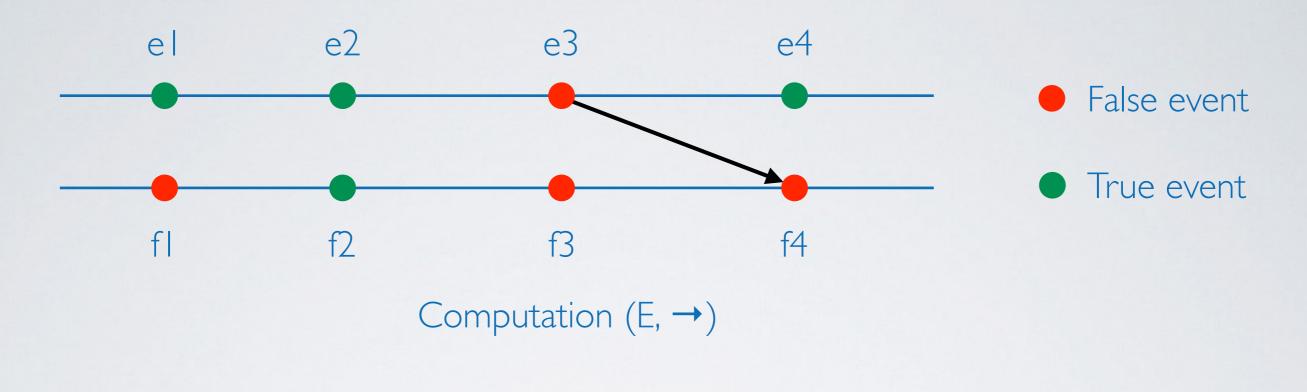
- Agreement: an admissible sequence α should be consistent with the happened before relation →
  - $\forall i, j : i < j \Rightarrow \alpha_j \not\rightarrow \alpha_i$
- 2. Boundary Condition: an admissible sequence must start with an initial event and end in a final event  $(\alpha_0 \in E.\bot) \land (\alpha_{n-1} \in E.T)$
- 4. Continuity: an admissible sequence must be continuous  $\forall (\alpha_j, \alpha_i \in \alpha) \land (\alpha_j, \alpha_i \notin E.T) \land (\alpha_i, \text{succ} \rightarrow \alpha_j) \Rightarrow \alpha_{i+1} = \alpha_i.\text{succ}$
- 5. Safety:  $\alpha$  must be a safe execution. legal(C, E,  $\alpha$ )  $\wedge$  ( $\exists \alpha_i \in \alpha \wedge \alpha_i \in \text{frontier}(C, E)$ )  $\Rightarrow$  C(B) = True

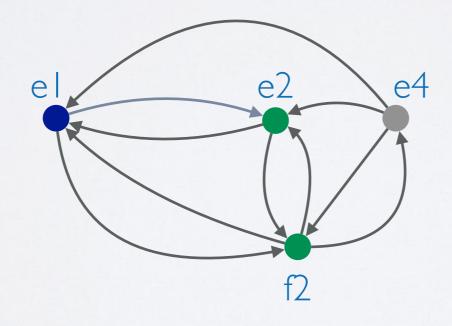
### True Event Graph

For a given computation  $(E, \rightarrow)$  and a predicate B, a true event graph is defined as:

- 1. An event e An event e belongs to the true event graph if the local predicate for the process e.procc is true at the event e.
- 2. There exists an edge between two events e and f if e.succ +> f
- 3. An event e in the true event graph is labeled as initial if  $e \in E.\bot$
- 4. An event e in the true event graph is labeled as "final: if  $e \in E.T$

### True Event Graph





True Event Graph

- True event
- Initial Event
- Final Event

### **Theorems**

#### Theorem I

A predicate B is controllable in a computation  $(E, \rightarrow)$  iff there exists an admissible sequence of events with respect to the predicate B and the computation  $(E, \rightarrow)$ 

#### Theorem 2

Let G (v, E) be the true event graph corresponding to the computation (E,  $\rightarrow$ ) and a predicate B. The shortest path in G, if it exists, corresponds to the admissible sequence of events in the computation

#### Theorem 3

Let G (v, E) be the true event graph corresponding to the computation (E,  $\rightarrow$ ) and a predicate B. B is controllable if in the computation (E,  $\rightarrow$ ) then there exists a permissible path in G.

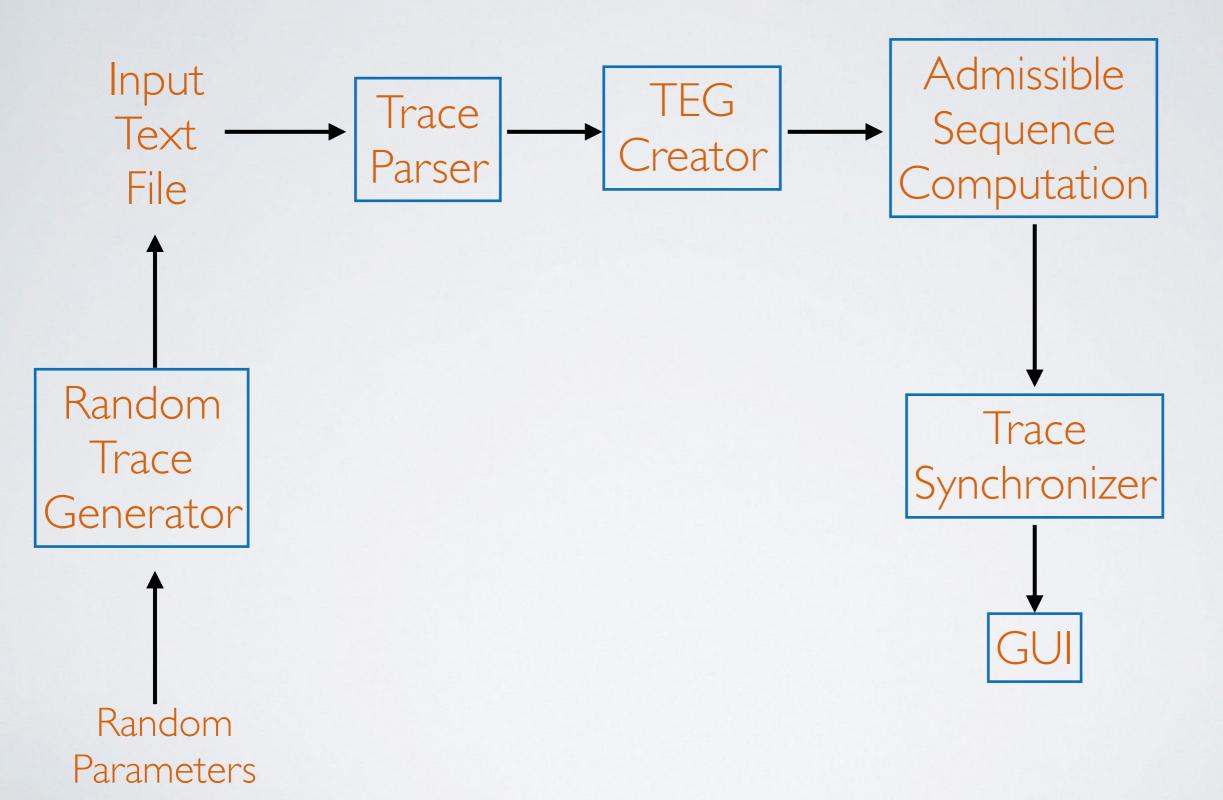
### Solution

Computation Trace

True Event Graph

Admissible Sequence

Recompute Controlled Computation Trace



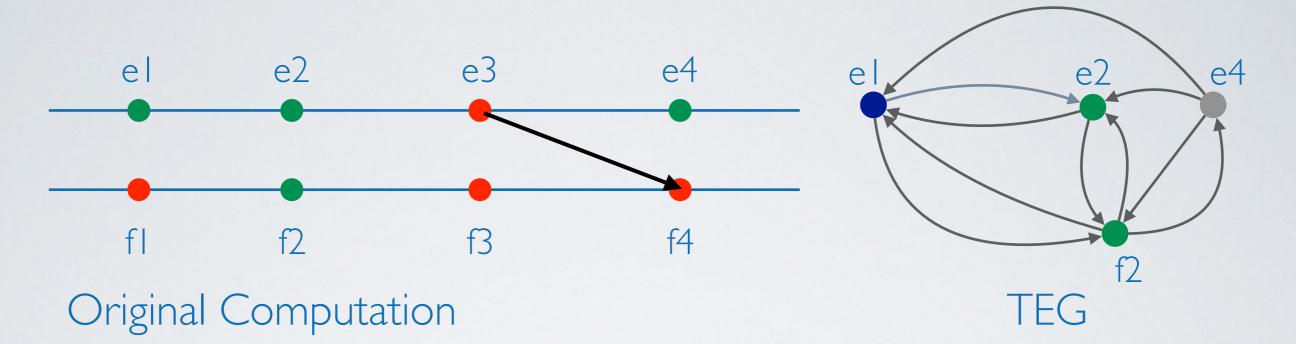
# Admissible Sequence Algorithm

```
findAdmissibleSequence(trace):
graph = constructTEG(trace)
admissible seq = NULL
min length = INFINITY
for e in graph.initial nodes
 for f in graph.final nodes
  path = graph.shortest path(e, f)
  if (length(path) < min length)</pre>
  admissible seq = path;
  min length = length(admissible seq)
  end if
 end for
end for
return admissible seq
        Time Complexity: O((nm)^3)
        Space Complexity: O((nm)^2)
```

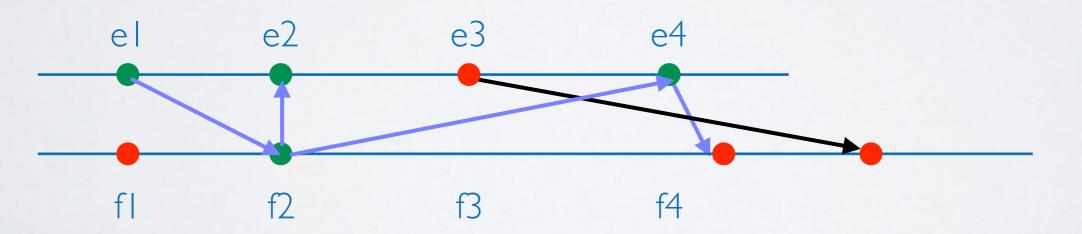
## Trace Synchronizer Algorithm

```
addSyncrhonizationMessages (admissibleS
seq):
// add messages from set A in section
TT
for i in [0, |\alpha|)
  for j in (i, |\alpha|)
  if (\alpha_i.process \neq \alpha_j.process)
   addSyncMessage (\alpha_i, \alpha_j)
  end if
 end for
end for
 // add messages from set B in section
TT
for i in [0, |\alpha|-1)
  if (\alpha_i.process \neq \alpha_{i+1}.process)
  addSyncMessage (\alpha_{i+1}, \alpha_{i}.next)
 end if
end for
```

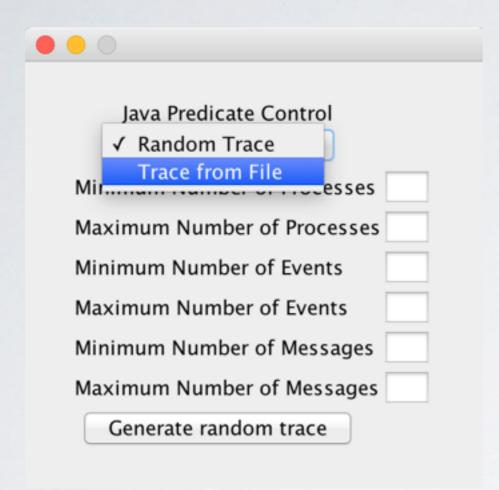
### True Event Graph

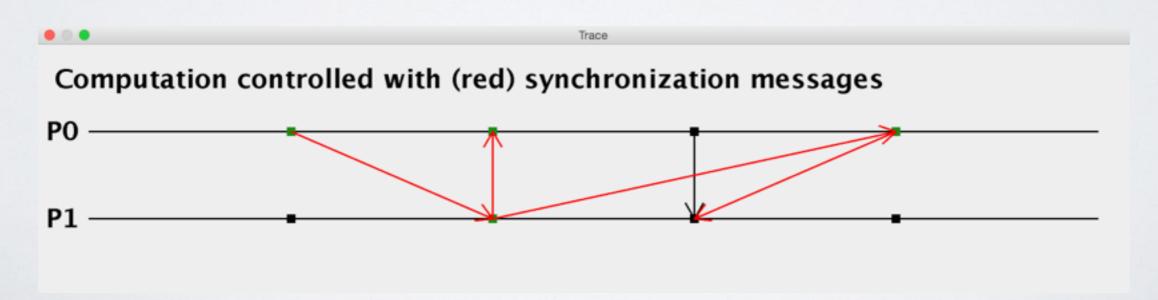


Admissible Sequence: e1, f2, e4

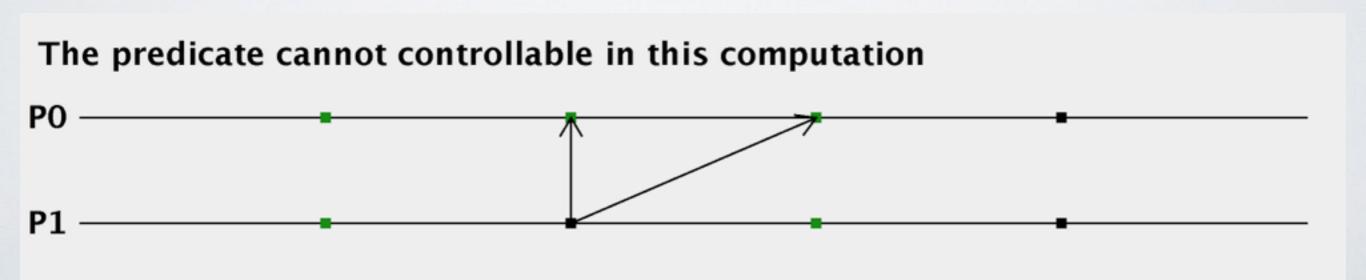


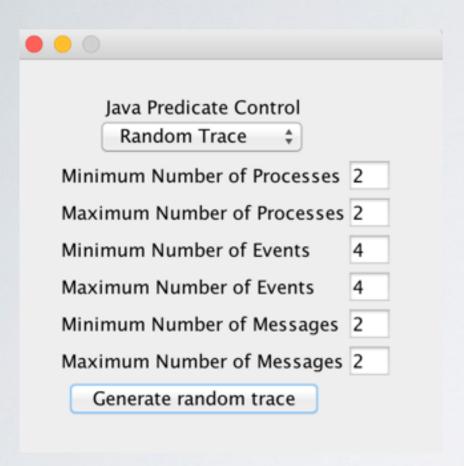
Controlled Computation

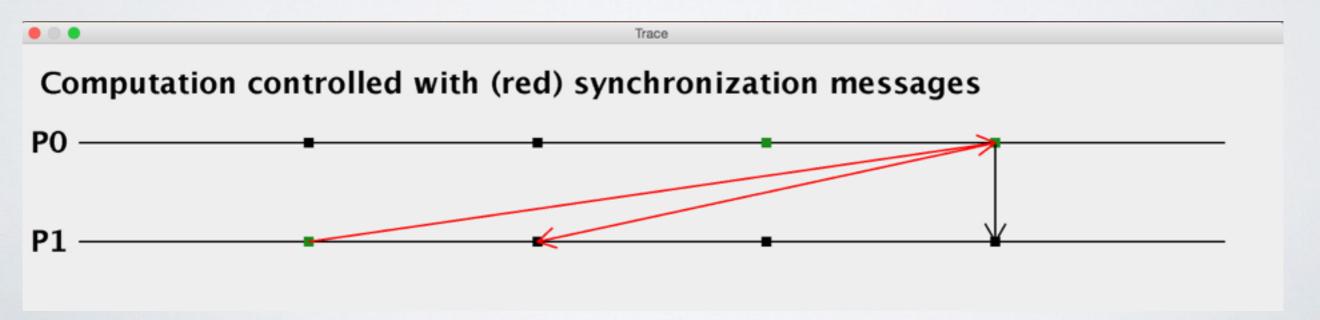












### Thank You!