# 7524 - Teoría de la programación TP Individual

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# Ejercicio 1) - Procesamiento de listas Length <u>Take</u> **Drop Append** <u>Member</u> **Position** Ejercicio 2) - Referencias externas Ejercicio 3) - Ejemplo de ejecución Programa 1 Programa 2 Programa 3 Programa 4 Programa 5 Programa 6 Ejercicio 4) - Case Ejercicio 5) - Recursividad 1. Traducción al lenguaje Kernel 2. "Tail Recursive" 3. Ejecución en la máquina abstracta Implementación básica

Implementación Tail Recursive

# Ejercicio 1) - Procesamiento de listas

## 1. Length

a. Código Oz

```
% Length function
declare fun {Length Xs}
          case Xs of nil then 0
        [] H|T then 1 + {Length T}
        end
    end
```

b. Ejemplos de ejecución

```
Oz Programming Interface (emacs@KARINA-VAIO)
                                                                                  X
File Edit Options Buffers Tools Oz Help
% Length function
declare fun {Length Xs}
           case Xs of nil then 0
           [] H|T then 1 + {Length T}
        end
% invocation examples Length
{Show 'Length examples'}
{Show {Length [1 2 10]}}
{Show {Length [1 2 10 'test']}}
{Show {Length ['a' 'b' 'c']}}
{Show {Length ['a' 'b' 'c' 4 5 6 7 8 9 10]}}
1\**- Oz
                      All L8
'Length examples'
4
3
10
1\**- *Oz Emulator*
                      Bot L9
                                 (Comint:run)
```

#### 2. Take

a. Código Oz

```
% Take function
declare fun {Take Xs N}
    if N == 0 then nil
    else
        case Xs of nil then nil
        [] H|T then H|{Take T N-1}
        end
    end
end
```

```
X
Oz Programming Interface (emacs@KARINA-VAIO)
File Edit Options Buffers Tools Oz Help
                            X 1 1 1 1 1
% Take function
declare fun {Take Xs N}
           if N == 0 then nil
              case Xs of nil then nil
             [] H|T then H|{Take T N-1}
              end
           end
        end
% invocation examples Take
{Show 'Take examples'}
{Show {Take [1 2 10 15] 2}}
{Show {Take [1 2 10 15] 8}}
{Show {Take [a b c d] 3}}
{Show {Take [a b c d] 4}}
{Show {Take [a b c d] 1}}
{Show {Take [a b c d] 0}}
1\**- Oz
                      All L16
                                  (Oz)
'Take examples'
[1 2]
[1 2 10 15]
[a b c]
[abcd]
[a]
nil
1\**- *Oz Emulator*
                      All L8
                                 (Comint:run)
Beginning of buffer
```

## 3. Drop

a. Código Oz

```
% Drop function
declare fun {Drop Xs N}
    if N == 0 then Xs
    else
        case Xs of nil then nil
     [] H|T then {Drop T N-1}
        end
    end
    end
end
```

```
Oz Programming Interface (emacs@KARINA-VAIO)
                                                                            X
File Edit Options Buffers Tools Oz Help
% Drop function
declare fun {Drop Xs N}
           if N == 0 then Xs
           else
              case Xs of nil then nil
              [] H|T then {Drop T N-1}
              end
           end
        end
% invocation examples Drop
{Show 'Drop examples'}
{Show {Drop [1 2 10 15] 2}}
{Show {Drop [1 2 10 15] 8}}
{Show {Drop [a b c d] 4}}
{Show {Drop [a b c d] 1}}
{Show {Drop [a b c d] 0}}
1\**- Oz
                       All L10
                                  (Oz)
'Drop examples'
[10 15]
nil
nil
[b c d]
[abcd]
1\**- *Oz Emulator*
                                  (Comint:run)
                      All L7
```

## 4. Append

a. Código Oz

```
% Append function
declare fun {Append Xs Ys}
    if Ys == nil then Xs
    else
        case Xs of nil then Ys
    [] H|T then H|{Append T Ys}
        end
    end
    end
end
```

```
Oz Programming Interface (emacs@KARINA-VAIO)
                                                                             X
File Edit Options Buffers Tools Oz Help
% Append function
declare fun {Append Xs Ys}
           if Ys == nil then Xs
           else
              case Xs of nil then Ys
              [] H|T then H|{Append T Ys}
              end
           end
        end
% invocation examples Append
{Show 'Append examples'}
{Show {Append [1 2 10 15] [a b c d]}}
{Show {Append [1 2 10 15] nil}}
{Show {Append nil [a b]}}
{Show {Append [1 2 10 15] [a]}}
{Show {Append [1] [a b]}}
1\**- Oz
                       All L8
                                   (Oz)
'Append examples'
[1 2 10 15 a b c d]
[1 2 10 15]
[a b]
[1 2 10 15 a]
[1 a b]
1\**- *Oz Emulator*
                       All L7
                                   (Comint:run)
```

## 5. Member

a. Código Oz

```
% Member function
declare fun {Member Xs Y}
    case Xs of nil then false
    [] H|T then
        if H == Y then true
        else
        {Member T Y}
        end
    end
end
```

```
Oz Programming Interface (emacs@KARINA-VAIO)
                                                                           X
File Edit Options Buffers Tools Oz Help
                           * •
% Member function
declare fun {Member Xs Y}
           case Xs of nil then false
           [] H|T then
              if H == Y then true
              else
                 {Member T Y}
              end
           end
        end
s invocation examples Member
{Show 'Member examples'}
{Show {Member [1 2 10 15] 2}}
{Show {Member [1 2 10 15] 1}}
{Show {Member [1 2 10 15] 10}}
{Show {Member [1 2 10 a 15] 15}}
{Show {Member [1 2 10 a 15] a}}
{Show {Member [1 2 10 15] b}}
{Show {Member [1 2 10 15] 3}}
{Show {Member [1 2 10 15] 5}}
{Show {Member [1 2 10 15] nil}}
{Show {Member nil a}}
1\**- Oz
                    All L11
                                  (Oz)
'Member examples'
true
true
true
true
true
false
false
false
false
false
1\**- *Oz Emulator* All L11 (Comint:run)
```

## 6. Position

a. Código Oz

```
Oz Programming Interface (emacs@KARINA-VAIO)
                                                                             X
File Edit Options Buffers Tools Oz Help
% Position function
declare fun {Position Xs Y}
           case Xs of nil then 0
            [] H|T then
              if H == Y then 0
              else 1 + {Position T Y}
              end
           end
        end
% invocation examples Position
{Show 'Position examples'}
{Show {Position [1 2 10 15] 10}}
{Show {Position [1 2 10 a 15] 15}}
{Show {Position [1 2 10 a 15] a}}
{Show {Position [1 2 10 15] 1}}
{Show {Position [1 2 10 15] 3}}
1\**- Oz
                       All L5
                                   (Oz)
'Position examples'
3
0
4
<
1\**- *Oz Emulator*
                        All L7
                                    (Comint:run)
```

# Ejercicio 2) - Referencias externas

1.  $proc \{P X Y\} local Z in \{Q Z U\} end end$ 

Referencias externas: Q, U

2.  $proc \{P X Y\} local Z in \{Q Z Y\} end end$ 

Referencias externas: Q

3.  $proc \{P X Y\} local Z in \{P Z Y\} end end$ 

Referencias externas: ninguna

# Ejercicio 3) - Ejemplo de ejecución

# Programa 1

#### **Estado inicial**

| Stack                          | Store | Е |
|--------------------------------|-------|---|
| local B in if B then Skip else | -     | - |
| skip<br>end<br>end             |       |   |

## => Ejecución de declaración de variable

| Stack          | Store | Е      |
|----------------|-------|--------|
| if B then skip | b1    | B-> b1 |
| else<br>skip   |       |        |
| end            |       |        |

=> Ejecución de condicional. Como E(B) no está determinado, el programa se suspende, a la espera que b1 tome algun valor.

## Programa 2

#### **Estado inicial**

| Stack                                    | Store | Е |
|--|-------|---|
| local B in B = false if B then skip else | -     | - |
| skip<br>end<br>end                       |       |   |

## => Ejecución de declaración de variable y composición

| Stack                                  | Store | Е      |
|--|-------|--------|
| B = false if B then skip else skip end | b1    | B-> b1 |

## => Ejecución de binding de variables

| Stack                        | Store             | Е      |
|------------------------------|-------------------|--------|
| if B then skip else skip end | b1 = <b>false</b> | B-> b1 |

# => Ejecución de condicional, como B = false entonces se agrega en el stack la sentencia dentro del else

| Stack | Store      | Е      |
|-------|------------|--------|
| skip  | b1 = false | B-> b1 |

=> Ejecución del skip (St6), no hay cambios en el store y se quita la sentencia.

| Stack | Store      | Е      |
|-------|------------|--------|
| -     | b1 = false | B-> b1 |

No hay nada mas en el stack, entonces el programa finaliza.

# Programa 3

## **Estado inicial**

| Stack              | Store | E |
|--------------------|-------|---|
| local X Z A B P in | -     | - |
| end                |       |   |

## => Ejecución de declaración de variables

| Stack        | Store                      | E   |
|--------------|----------------------------|---|
| proc {P X Y} | x1<br>z1<br>a1<br>b1<br>p1 | X -> x1<br>Z-> z1<br>A -> a1<br>B -> b1<br>P-> p1 |

## => Ejecución de procedure value

| Stack                            | Store   | E                                       |
|----------------------------------|---|---|
| Z=7<br>X=4<br>{P X A}<br>{P A B} | x1<br>z1<br>a1<br>b1                                | X -> x1<br>Z-> z1<br>A -> a1<br>B -> b1 |
| = j                              | p1 = proc {P X Y}<br>Y = X+Z<br>end, CE = {Z -> z1} | P-> p1                                  |

# => Ejecución de binding de variable

| Stack                     | Store  | E   |
|---------------------------|--|---|
| X=4<br>{P X A}<br>{P A B} | x1<br>z1 = <b>7</b><br>a1<br>b1<br>p1 = proc {P X Y}<br>Y = X+Z<br>end, CE = {Z -> z1} | X -> x1<br>Z-> z1<br>A -> a1<br>B -> b1<br>P-> p1 |

# => Ejecución de binding de variable

| Stack              | Store  | E   |
|--------------------|--|---|
| {P X A}<br>{P A B} | x1 = <b>4</b><br>z1 = 7<br>a1<br>b1<br>p1 = proc {P X Y}<br>Y = X+Z<br>end, CE = {Z -> z1} | X -> x1<br>Z-> z1<br>A -> a1<br>B -> b1<br>P-> p1 |

# => Ejecución de procedure value

| Stack                                  | Store  | E   |
|--|--|---|
| <b>A</b> = <b>X</b> + <b>Z</b> {P A B} | x1 = 4<br>z1 = 7<br>a1<br>b1<br>p1 = proc {\$ X Y} | X -> x1<br>Z-> z1<br>A -> a1<br>B -> b1<br>P-> p1 |

## => Asignacion de variable mas suma en base al store

| Stack   | Store  | Е   |
|---------|--|---|
| {P A B} | x1 = 4<br>z1 = 7<br>a1 = <b>11</b><br>b1<br>p1 = proc {\$ X Y}<br>Y = X+Z<br>end, CE = {Z -> z1} | X -> x1<br>Z-> z1<br>A -> a1<br>B -> b1<br>P-> p1 |

## => Ejecución de procedure value

| Stack     | Store   | E   |
|-----------|---|---|
| B = A + Z | x1 = 4<br>z1 = 7<br>a1 = 11<br>b1<br>p1 = proc {\$ X Y} | X -> x1<br>Z-> z1<br>A -> a1<br>B -> b1<br>P-> p1 |

## => Asignacion de variable mas suma en base al store

| Stack | Store   | Е   |
|-------|---|---|
| -     | x1 = 4<br>z1 = 7<br>a1 = 11<br>b1 = <b>18</b><br>p1 = proc {\$ X Y} | X -> x1<br>Z-> z1<br>A -> a1<br>B -> b1<br>P-> p1 |

# Programa 4

## **Estado inicial**

| Stack   | Store | Е |
|---|-------|---|
| local X Z A B P in<br>proc {P X Y}<br>Y = X+Z | -     | - |
| end   |       |   |
| Z=10  |       |   |
| local Z in                                    |       |   |
| Z = 2   |       |   |
| X=4   |       |   |
| {P X A}                                       |       |   |
| {P A B}                                       |       |   |
| end   |       |   |
| end   |       |   |

# => Ejecución de declaración de variables

| Stack        | Store                      | E  |
|--------------|----------------------------|--|
| proc {P X Y} | x1<br>z1<br>a1<br>b1<br>p1 | X - > x1<br>Z -> z1<br>A -> a1<br>B -> b1<br>P -> p1 |

# => Ejecución de declaración de procedure value

| Stack      | Store                              | Е        |
|------------|------------------------------------|----------|
| Z=10       | x1                                 | X - > x1 |
| local Z in | z1                                 | Z -> z1  |
| Z = 2      | a1                                 | A -> a1  |
| X=4        | b1                                 | B -> b1  |
| {P X A}    | p1 = <b>proc</b> { <b>\$ X Y</b> } | P -> p1  |
| {P A B}    | Y = X+Z                            |          |
| end        | end, CE = {Z -> z1}                |          |

# => Ejecución de asignación de variable

| Stack      | Store                   | Е        |
|------------|-------------------------|----------|
| local Z in | x1                      | X - > x1 |
| Z = 2      | z1 = <b>10</b>          | Z -> z1  |
| X=4        | a1                      | A -> a1  |
| {P X A}    | b1                      | B -> b1  |
| {P A B}    | p1 = proc {\$ X Y}      | P -> p1  |
| end        | Y = X+Z                 | ·        |
|            | end, $CE = \{Z -> z1\}$ |          |

# => Ejecución de declaración de variable Z

| Stack   | Store              | Е              |
|---------|--------------------|----------------|
| Z = 2   | x1                 | X - > x1       |
| X=4     | z1 = 10            | Z -> <b>z2</b> |
| {P X A} | <b>z2</b>          | A -> a1        |
| {P A B} | a1                 | B -> b1        |
|         | b1                 | P -> p1        |
|         | p1 = proc {\$ X Y} |                |

| Y = X+Z<br>end, CE = {Z -> z1} |  |
|--------------------------------|--|
| eria, CL - (Z > Zij            |  |

## => Ejecución de asignación de variable Z (en el nuevo entorno)

| Stack                     | Store  | Е  |
|---------------------------|--|--|
| X=4<br>{P X A}<br>{P A B} | x1<br>z1 = 10<br>z2 = <b>2</b><br>a1<br>b1<br>p1 = proc {\$ X Y} | X - > x1<br>Z -> z2<br>A -> a1<br>B -> b1<br>P -> p1 |

## => Ejecución de asignación de variable X (en el nuevo entorno)

| Stack              | Store  | Е  |
|--------------------|--|--|
| {P X A}<br>{P A B} | x1 = <b>4</b><br>z1 = 10<br>z2 = 2<br>a1<br>b1<br>p1 = proc {\$ X Y} | X - > x1<br>Z -> z2<br>A -> a1<br>B -> b1<br>P -> p1 |

## => Ejecución de procedure value (en el nuevo entorno usando su entorno contextual)

| Stack                | Store   | Е  |
|----------------------|---|--|
| A = X + Z<br>{P A B} | x1 = 4<br>z1 = 10<br>z2 = 2<br>a1<br>b1<br>p1 = proc {\$ X Y} | X - > x1<br>Z -> z2<br>A -> a1<br>B -> b1<br>P -> p1 |

# => Ejecución de la única sentencia del procedure (en el nuevo entorno usando su entorno contextual)

| Stack | Store | E |
|-------|-------|---|
|-------|-------|---|

| {P A B} | x1 = 4                           | X - > x1 |
|---------|----------------------------------|----------|
|         | z1 = 10                          | Z -> z2  |
|         | z2 = 2                           | A -> a1  |
|         | a1 = <b>14 (Z -&gt; z1 = 10)</b> | B -> b1  |
|         | b1                               | P -> p1  |
|         | p1 = proc {\$ X Y}               |          |
|         | Y = X+Z                          |          |
|         | end, CE = {Z -> z1}              |          |

## => Ejecución del procedure value(en el nuevo entorno usando su entorno contextual)

| Stack     | Store  | Е  |
|-----------|--|--|
| B = A + Z | x1 = 4<br>z1 = 10<br>z2 = 2<br>a1 = 14<br>b1<br>p1 = proc {\$ X Y} | X - > x1<br>Z -> z2<br>A -> a1<br>B -> b1<br>P -> p1 |

# => Ejecución de la única sentencia del procedure (en el nuevo entorno usando su entorno contextual)

| Stack | Store   | Е  |
|-------|---|--|
| -     | x1 = 4<br>z1 = 10<br>z2 = 2<br>a1 = 14<br>b1 = <b>24 (a1:14 +z1:10)</b><br>p1 = proc {\$ X Y}<br>Y = X+Z<br>end, CE = {Z -> z1} | X - > x1<br>Z -> z2<br>A -> a1<br>B -> b1<br>P -> p1 |

## Fin del programa

# Programa 5

## **Estado inicial**

| Stack              | Store | E |
|--------------------|-------|---|
| local X Y Z P Q in | -     | • |
| X=6                |       |   |
| Y=4                |       |   |
| proc {P A B}       |       |   |
| proc {B U V}       |       |   |
| local F in         |       |   |
| F=A+1              |       |   |
| V=U+F              |       |   |
| end                |       |   |
| end                |       |   |
| end                |       |   |
| {P X Q}            |       |   |
| {Q Y Z}            |       |   |
| end                |       |   |

## => Declaracion de variables

| Stack        | Store | E       |
|--------------|-------|---------|
| X=6          | x1    | X -> x1 |
| Y=4          | y1    | Y -> y1 |
| proc {P A B} | z1    | Z -> z1 |
| proc {B U V} | p1    | P -> p1 |
| local F in   | q1    | Q -> q1 |
| F=A+1        |       |         |
| V=U+F        |       |         |
| end          |       |         |
| end          |       |         |
| end          |       |         |
| {P X Q}      |       |         |
| {Q Y Z}      |       |         |

# => Asignación de variable

| Stack                                    | Store                           | Е  |
|--|---------------------------------|--|
| Y=4 proc {P A B} proc {B U V} local F in | x1 = <b>6</b><br>y1<br>z1<br>p1 | X -> x1<br>Y -> y1<br>Z -> z1<br>P -> p1 |

| 0.00               | F=A+1<br>V=U+F | q1 | Q -> q1 |
|--------------------|----------------|----|---------|
| end                | a e            |    |         |
| end                |                |    |         |
| end                |                |    |         |
| {P X Q}            |                |    |         |
| {P X Q}<br>{Q Y Z} |                |    |         |

# => Asignación de variable

| Stack                        | Store                   | Е                             |
|------------------------------|-------------------------|-------------------------------|
| proc {P A B}<br>proc {B U V} | x1 = 6<br>y1 = <b>4</b> | X -> x1<br>Y -> y1            |
| local F in<br>F=A+1<br>V=U+F | z1<br>p1<br>q1          | Z -> z1<br>P -> p1<br>Q -> q1 |
| end<br>end<br>end            |                         |                               |
| {P X Q}<br>{Q Y Z}           |                         |                               |

# => Declaración procedure value

| Stack   | Store                              | Е       |
|---------|------------------------------------|---------|
| {P X Q} | x1 = 6                             | X -> x1 |
| {Q Y Z} | y1 = 4                             | Y -> y1 |
|         | z1                                 | Z -> z1 |
|         | p1 = <b>proc</b> { <b>\$ A B</b> } | P -> p1 |
|         | proc {B U V}                       | Q -> q1 |
|         | local F in                         |         |
|         | F=A+1                              |         |
|         | V=U+F                              |         |
|         | end                                |         |
|         | end                                |         |
|         | end, CE = {}                       |         |
|         | q1                                 |         |

# => Ejecución procedure value

| Stack        | Store              | E       |
|--------------|--------------------|---------|
| proc {Q U V} | x1 = 6             | X -> x1 |
| local F in   | y1 = 4             | Y -> y1 |
| F = X + 1    | z1                 | Z -> z1 |
| V = U + F    | p1 = proc {\$ A B} | P -> p1 |
| end          | proc {B U V}       | Q -> q1 |
| end          | local F in         |         |
| {Q Y Z}      | F=A+1              |         |
|              | V=U+F              |         |
|              | end                |         |
|              | end                |         |
|              | end, CE = {}       |         |
|              | q1                 |         |

# => Declaración procedure value

| Stack   | Store  | Е   |
|---------|--|---|
| {Q Y Z} | x1 = 6<br>y1 = 4<br>z1<br>p1 = proc {\$ A B}<br>proc {B U V}<br>local F in<br>F=A+1<br>V=U+F<br>end<br>end, CE = {}<br>q1 = proc {\$ U V}<br>local F in<br>F = X + 1<br>V = U + F<br>end<br>End, CE = {X-> x1} | X -> x1<br>Y -> y1<br>Z -> z1<br>P -> p1<br>Q -> q1 |

# => Ejecución procedure value

| Stack      | Store   | Е  |
|------------|---|--|
| local F in | <pre>x1 = 6 y1 = 4 z1 p1 = proc {\$ A B}     proc {B U V}</pre> | E  X -> x1  Y -> y1  Z -> z1  P -> p1  Q -> q1 |
|            | , ()  |  |

## => declaración de variable

| Stack                  | Store   | Е   |
|------------------------|---|---|
| F = X + 1<br>Z = Y + F | x1 = 6<br>y1 = 4<br>z1<br>f1<br>p1 = proc {\$ A B}<br>proc {B U V}<br>local F in<br>F=A+1<br>V=U+F                | X -> x1<br>Y -> y1<br>Z -> z1<br>P -> p1<br>Q -> q1 |
|                        | end end end, CE = {} q1 = proc {\$ U V} local F in F = X + 1 V = U + F end End, CE = {X-> x1, <b>F -&gt; f1</b> } |   |

# => Asignación y suma de variables

| Stack | Store   | Е   |
|-------|---|---|
| Z=Y+F | x1 = 6<br>y1 = 4<br>z1<br>f1 = <b>7</b><br>p1 = proc {\$ A B}<br>proc {B U V}<br>local F in<br>F=A+1<br>V=U+F<br>end<br>end<br>end, CE = {}<br>q1 = proc {\$ U V}<br>local F in<br>F = X + 1<br>V = U + F<br>end<br>End, CE = {X-> x1, F -> f1} | X -> x1<br>Y -> y1<br>Z -> z1<br>P -> p1<br>Q -> q1 |

# => Asignación y suma de variables

| Stack | Store                          | Е       |
|-------|--------------------------------|---------|
| -     | x1 = 6                         | X -> x1 |
|       | y1 = 4                         | Y -> y1 |
|       | z1 = <b>7(f1) + 4(y1) = 11</b> | Z -> z1 |
|       | f1 = 7                         | P -> p1 |
|       | p1 = proc {\$ A B}             | Q -> q1 |
|       | proc {B U V}                   |         |
|       | local F in                     |         |
|       | F=A+1                          |         |
|       | V=U+F                          |         |
|       | end                            |         |
|       | end                            |         |
|       | end, CE = {}                   |         |
|       | q1 = proc {\$ U V}             |         |
|       | local F in                     |         |
|       | F = X + 1                      |         |
|       | V = U + F                      |         |
|       | end                            |         |
|       | End, CE = {X-> x1, F -> f1}    |         |

# Programa 6

## **Estado inicial**

| Stack  | Store | E |
|--|-------|---|
| local X Y Z in     X = Y     try     X = 1Y = 2 Z = 3     catch Exception then     skip     end     {Browse X#Y#Z} end | -     | - |

## => Declaración de variables

| Stack  | Store          | E                             |
|--|----------------|-------------------------------|
| <pre>X = Y try      X = 1Y = 2 Z = 3 catch Exception then      skip end {Browse X#Y#Z}</pre> | x1<br>y1<br>z1 | X -> x1<br>Y -> y1<br>Z -> z1 |

# => Asignación de variables

| Stack                | Store | Е       |
|----------------------|-------|---------|
| try                  | x1    | X -> y1 |
| X = 1                | y1    | Y -> y1 |
| Y = 2                | z1    | Z -> z1 |
| Z = 3                |       |         |
| catch Exception then |       |         |
| skip                 |       |         |
| end                  |       |         |
| {Browse X#Y#Z}       |       |         |

# => Ejecución de try

| Stack | Store | E       |
|-------|-------|---------|
| X = 1 | x1    | X -> y1 |
| Y = 2 | y1    | Y -> y1 |

| Z = 3                | z1 | Z -> z1 |
|----------------------|----|---------|
| catch Exception then |    |         |
| skip                 |    |         |
| end                  |    |         |
| {Browse X#Y#Z}       |    |         |

## => Ejecución de asignación de variable (dentro del catch)

| Stack  | Store                     | Е                             |
|--|---------------------------|-------------------------------|
| Y = 2 Z = 3 catch Exception then skip end {Browse X#Y#Z} | x1<br>y1 = <b>1</b><br>z1 | X -> y1<br>Y -> y1<br>Z -> z1 |

## => Ejecución de asignación de variable (dentro del catch)

| Stack  | Store              | Е                             |
|--|--------------------|-------------------------------|
| Y = 2 Z = 3 catch Exception then skip end {Browse X#Y#Z} | x1<br>y1 = 1<br>z1 | X -> y1<br>Y -> y1<br>Z -> z1 |

Acá se intenta asignar a y1 el valor 2, pero esta variable ya tiene valor porque X = Y, entonces dispara la Exception y se quitan todas las operaciones hasta la del catch

## => Ejecución Exception

| Stack                  | Store              | E                             |
|------------------------|--------------------|-------------------------------|
| skip<br>{Browse X#Y#Z} | x1<br>y1 = 1<br>z1 | X -> y1<br>Y -> y1<br>Z -> z1 |

## => Ejecución Skip

| Stack          | Store              | Е                             |
|----------------|--------------------|-------------------------------|
| {Browse X#Y#Z} | x1<br>y1 = 1<br>z1 | X -> y1<br>Y -> y1<br>Z -> z1 |

## => Ejecución Browse

| Stack | Store              | E                             |
|-------|--------------------|-------------------------------|
|       | x1<br>y1 = 1<br>z1 | X -> y1<br>Y -> y1<br>Z -> z1 |

Como el valor de Z no esta determinado el browse mostrará un '\_' indicando que aun no se definió, en otras operaciones podría suspenderse la ejecución, pero no ocurre con Browse. La ejecución mostrará:

1#1#\_

# Ejercicio 4) - Case

#### {Test [b c a]}

Predicción: 'case'(4)

Ejecución: 'case'(4)

La lista no empieza con a como primer elemento, ni es un record, es una lista pero el primer y elemento no son iguales, luego es una lista, entonces case 4.

## {Test f(b(3))}

Predicción: 'case'(5)

Ejecución: 'case'(5)

No es lista que empiece con a, si bien es un tupla llamada f, su valor no es a sino b(3), tampoco es una lista, con lo cual saltamos al caso 5 que cumple, dado que es un tupla llamada f y Y tomará el valor b(3)

#### {Test f(a)}

Predicción: 'case'(2)

Ejecución: 'case'(2)

No es lista, entonces analiza el case 2 donde coincide el nombre de la tupla y el elemento que contiene.

# {Test f(a(3))}

Predicción: 'case'(5)

Ejecución: 'case'(5)

No es lista, luego es una tupla llamada f pero el elemento no es a, luego caso 3 y 4 no cumple por no ser una lista, en el caso 5 satisface la condición porque se llama f y el valor de la variable Y será a(3)

#### {Test f(d)}

Predicción: 'case'(5)

Ejecución: 'case'(5)

No es lista, luego es una tupla llamada f pero el elemento no es a, luego caso 3 y 4 no cumple por no ser una lista, en el caso 5 satisface la condición porque se llama f y el valor de la variable Y será d

#### {Test [a b c]}

Predición: 'case'(1)

Ejecución: 'case'(1)

Es una lista que empieza con el valor a, cumple la primer condición.

## {Test [c a b]}

Prediccion: 'case'(4)

Ejecución: case (4)

No es una lista que comience con el valor a, luego no es una tupla, luego no es una lista con los primeros dos elementos iguales. Finalmente es una lista por lo que entra en el caso 4.

#### {Test ala}

Predicción: 'case'(1)

Ejecución: 'case'(1)

Es una lista que comienza con el valor a.

## {Test '|'(v b)}

Predicción: 'case'(6)

Ejecución: 'case'(4)

No es una lista que comience con a, tampoco es tupla, no es una lista con dos elementos iguales al inicio, pero si es una lista donde el valor de Zes b. El motivo por el cual mi predicción fue incorrecta es que pensé que el formato aceptado era una cabeza con una cola, o sea que debía ser 'l'(v [b]), pero es incorrecto.

#### {Test '|'(a a)}

Predicción: 'case'(6)

Ejecución: 'case'(1)

Es una lista que comienza con a, por el mismo motivo que el punto anterior me equivoqué en la predicción.

#### {Test 'l'(b b)}

Predicción 'case'(6)

Ejecución: 'case'(3)

No es una lista que comienza con a, luego tampoco es tupla, luego si es una lista con ambos elementos primero y segundo iguales.

#### {Test '|'(a b c)}

Predicción 'case'(6)

Ejecución: 'case'(6)

Al tener 3 elementos no coincide con una lista iniciando con a, luego no es tupla ni lista con ambos elementos iguales, tampoco es lista en la 4ta opcion, tampoco tupla llamada f, y queda como única opción el caso 6.

#### {Test 'l'(a [b c]}

Predicción: 'case'(1)

Ejecución: 'case'(1)

En este caso si crea con la cabeza y la cola la lista con 3 elementos que empiezan con a, por lo tanto coincide la primer condición.

# Ejercicio 5) - Recursividad

# 1. Traducción al lenguaje Kernel

```
local Length in
   Length = proc {$ Xs N}
            case Xs of nil then
               N = 0
            else
               case Xs of _|T then
                  local U in
                        {Length T U}
                        N = U + 1
                  end
               else
                  skip
               end
            end
           end
end
local K in
   {Length [1 2 3 4] K}
   {Show K}
end
```

## 2. "Tail Recursive"

```
end
end
end
end
local K in
{Length [1 2 3 4] 0 K}
{Show K}
end
```

En el primer caso no es la llamada recursiva lo último que se ejecuta, entonces voy a tener las operaciones que siguen acumuladas en el stack y hasta que no se termine la invocación de la última llamada recursiva no voy a poder liberar el stack. Al hacerlo tail recursive no tengo en el stack operaciones pendientes, el cual me queda claramente más pequeño. Este es el motivo por el cual siempre debemos tratar de hacer la invocación a la recursividad al final. Esto se verá claramente en el punto 3.

## 3. Ejecución en la máquina abstracta

Implementación básica

#### **Estado inicial**

| Stack                            | Store | E |
|----------------------------------|-------|---|
| local Length in                  | -     | - |
| Length = proc {\$ Xs N}          |       |   |
| case Xs of nil then              |       |   |
| N = 0                            |       |   |
| else                             |       |   |
| case Xs of _ T then              |       |   |
| local U in                       |       |   |
| {Length T U}                     |       |   |
| N = U + 1                        |       |   |
| end                              |       |   |
| else                             |       |   |
| skip                             |       |   |
| end                              |       |   |
| local K in                       |       |   |
| {Length [1 2 3 4] K}<br>{Show K} |       |   |

| and |  |
|-----|--|
| ena |  |

## => Declaración de variable

| Stack  | Store  | E                |
|--|--------|------------------|
| <pre>Length = proc {\$ Xs N}     case Xs of nil then        N = 0     else        case Xs of _ T then        local U in        {Length T U}        N = U + 1</pre> | length | length -> Length |
| end  |        |                  |
| else<br>skip   |        |                  |
| end  |        |                  |
| end  |        |                  |
| end  |        |                  |
| <pre>local K in   {Length [1 2 3 4] K}   {Show K} and</pre>  |        |                  |
| end  |        |                  |

# => Asignación de procedure value

| Stack  | Store                               | E                |
|--|-------------------------------------|------------------|
| local K in {Length [1 2 3 4] K} {Show K} end | <pre>length = (proc {\$ Xs N}</pre> | length -> Length |

## => Declaración variable K

| Stack                            | Store   | E     |
|----------------------------------|---|-------|
| {Length [1 2 3 4] K}<br>{Show K} | <pre>length = (proc {\$ Xs N}      case Xs of nil then      N = 0</pre> | k-> K |

# => Ejecución de procedure

| Stack  | Store   | E     |
|--|---|-------|
| case Xs of nil then N = 0  | <pre>length = (proc {\$ Xs N}     case Xs of nil then     N = 0</pre> | k-> K |
| else  case Xs of _ T then  local U in  {Length T U}  N = U + 1  end  else  skip  end | else  |       |
| end<br>{Show K}  | Store* CE*  xs = [1 2 3 4] xs -> Xs n = n -> K                        |       |

## => Ejecución de case

| Stack                          | Store                               | E     |
|--------------------------------|-------------------------------------|-------|
| <pre>case Xs of _ T then</pre> | <pre>length = (proc {\$ Xs N}</pre> | k-> K |

| k                     | _                  |  |
|-----------------------|--------------------|--|
| Store*                | CE*                |  |
| xs = [1 2 3 4]<br>n = | xs -> Xs<br>n -> K |  |
| n =                   | n -> K             |  |

# => Ejecución de case

| {Length T U} N = U + 1 end {Show K}  {Show K}     Case Xs of nil then   N = 0 | Stack                      | E     |
|---|----------------------------|-------|
| Store* CE* xs = [1 2 3 4] xs -> Xs  | {Length T U} N = U + 1 end | k-> K |
| n =   |                            |       |

## => Declaración de U

| Stack                           | Store                               | E     |
|---------------------------------|-------------------------------------|-------|
| {Length T U} N = U + 1 {Show K} | <pre>length = (proc {\$ Xs N}</pre> | k-> K |

| Store*                                      | CE*                                |  |
|---|------------------------------------|--|
| xs = [1 2 3 4]<br>n =<br>t = [2 3 4]<br>u = | n -> K<br>t -> T<br><b>u-&gt;U</b> |  |
|   |                                    |  |

# => Ejecución de Length

| Stack   | Store  |                                      | E     |
|---|--|--------------------------------------|-------|
| <pre>case Xs of nil then     N = 0     else         case Xs of _ T then         local U in         {Length T U}         N = U + 1         end     else         skip     end</pre> | <pre>length = (proc {\$ Xs</pre>                           | il then<br>f _ T then                | k-> K |
| end N = U + 1 {Show K}  | Store*  xs = [1 2 3 4] n = t = [2 3 4] u = xs'=[2 3 4] n'= | CE**  xs' -> Xs n' -> N  t -> T u->U |       |

# => Ejecución de case

| Stack                          | Store   | E     |
|--------------------------------|---|-------|
| <pre>case Xs of _ T then</pre> | <pre>length = (proc {\$ Xs N}     case Xs of nil then     N = 0     else         case Xs of _ T then         local U in</pre> | k-> K |

| N = U + 1<br>{Show K} | end<br>end<br>end, *)<br>k  | end end, *)                            |  |
|-----------------------|---|--|--|
|                       | Store*  | CE**                                   |  |
|                       | xs = [1 2 3 4]<br>n =<br>t = [2 3 4]<br>u =<br>xs'=[2 3 4]<br>n'= | xs' -> Xs<br>n' -> N<br>t -> T<br>u->U |  |

# => Ejecución de case

| Stack  | Store   |                       | E     |
|--|---|-----------------------|-------|
| local U in {Length T U} N = U + 1 end N = U + 1 {Show K} | length = (proc {\$ xs case Xs of n N = 0 else case Xs o local  end else skip end end end, *) k  Store*  xs = [1 2 3 4] n = t = [2 3 4] u = xs'=[2 3 4] n'= t'=[3 4] | il then<br>f _ T then | k-> K |

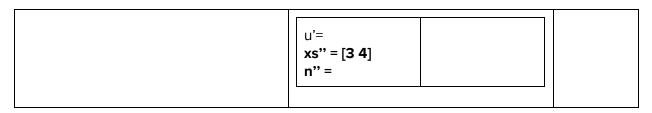
## => Declaración de U

| Stack                  | Store   | E     |
|------------------------|---|-------|
| {Length T U} N = U + 1 | <pre>length = (proc {\$ Xs N}     case Xs of nil then     N = 0</pre> | k-> K |

```
N = U + 1
                                                      else
                                                          case Xs of _|T then local U in
{Show K}
                                                                       {Length T U}
                                                                       N = U + 1
                                                             end
                                                          else
                                                             skip
                                                          end
                                                      end
                                               end, *)
                                                                     CE**
                                                Store*
                                               xs = [1 2 3 4]
                                                                     xs' -> Xs
                                                                     n' -> N
                                                n =
                                                t = [2 \ 3 \ 4]
                                                                     t' -> T
                                                                     u'->U
                                                u =
                                                xs'=[2 3 4]
                                                n'=
                                               t'=[3 4]
                                                u'=
```

# => Ejecución de Length

| Stack                          | Store  | E     |
|--------------------------------|--|-------|
| <pre>case Xs of nil then</pre> | <pre>length = (proc {\$ Xs N}</pre>  | k-> K |
|                                | Store*   CE***   xs = [1 2 3 4]  n =  t = [2 3 4]  u =  xs'' -> Xs  n" -> N  t' -> T  u'-> U  xs'=[2 3 4]  n'=  t'=[3 4] |       |



# => Ejecución de case

| Stack                          | Store   |  | E     |
|--------------------------------|---|--|-------|
| <pre>case Xs of _ T then</pre> | <pre>length = (proc {\$ Xs N}</pre>   |  | k-> K |
|                                | Store*  | CE***                                    |       |
|                                | xs = [1 2 3 4]<br>n =<br>t = [2 3 4]<br>u =<br>xs'=[2 3 4]<br>n'=<br>t'=[3 4]<br>u'=<br>xs" = [3 4]<br>n" = | xs" -> Xs<br>n" -> N<br>t' -> T<br>u'->U |       |

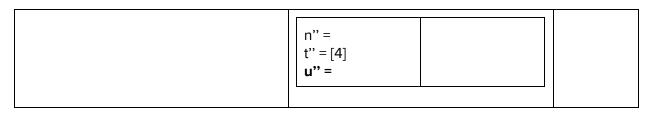
# => Ejecución de case

| Stack   | Store   | E     |
|---|---|-------|
| <pre>local U in      {Length T U}      N = U + 1 end N = U + 1 N = U + 1 {Show K}</pre> | <pre>length = (proc {\$ Xs N}     case Xs of nil then     N = 0     else     case Xs of _ T then         local U in         {Length T U}         N = U + 1         end     else</pre> | k-> K |

| skip<br>end<br>end, *)<br>k  |  |  |
|--|--|--|
| Store*   | CE***  |  |
| xs = [1 2 3 4]<br>n =<br>t = [2 3 4]<br>u =<br>xs'=[2 3 4]<br>n'=<br>t'=[3 4]<br>u'=<br>xs'' = [3 4]<br>n'' =<br>t'' = [4] | xs" -> Xs<br>n" -> N<br><b>t" -&gt; T</b><br>u'->U |  |

### => Declaración de variable U

| Stack   | Store   |  | E  |  |       |
|---|---|--|--|--|-------|
| {Length T U} N = U + 1 N = U + 1 N = U + 1 {Show K} | <pre>length = (proc {\$ Xs N}</pre>   |  | <pre>case Xs of nil then    N = 0 else    case Xs of _ T then    local U in    {Length T U}    N = U + 1    end    else    skip    end end end end end, *)</pre> |  | k-> K |
|   | Store*  | CE***  |  |  |       |
|   | xs = [1 2 3 4]<br>n =<br>t = [2 3 4]<br>u =<br>xs'=[2 3 4]<br>n'=<br>t'=[3 4]<br>u'=<br>xs" = [3 4] | xs" -> Xs<br>n" -> N<br>t" -> T<br><b>u"-&gt;U</b> |  |  |       |



# => Ejecución de Length

| Stack   | Store   |   | E     |
|---|---|---|-------|
| <pre>case Xs of nil then     N = 0 else     case Xs of _ T then         local U in         {Length T U}         N = U + 1         end     else         skip     end end</pre> | <pre>length = (proc {\$ Xs</pre>  | il then  f _ T then                       | k-> K |
| N = U + 1<br>N = U + 1<br>N = U + 1<br>{Show K}   | Store*  xs = [1 2 3 4] n = t = [2 3 4] u = xs'=[2 3 4] n'= t'=[3 4] u'= xs'' = [3 4] n'' = t'' = [4] u'' = xs'''= [4] n'''= | xs'"-> Xs<br>n'" -> N<br>t" -> T<br>u"->U |       |

| Stack  | Store  | E     |
|--|--|-------|
| <pre>case Xs of _ T then   local U in   {Length T U}</pre> | <pre>length = (proc {\$ Xs N}     case Xs of nil then     N = 0     else</pre> | k-> K |

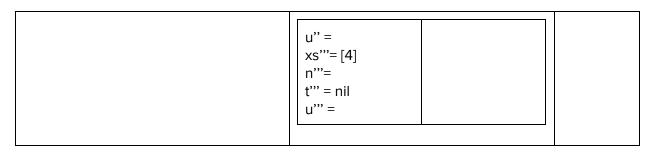
```
case Xs of _|T then
  local U in
               N = U + 1
       end
                                                                    {Length T U}
else
                                                                    N = U + 1
                                                          end
       skip
                                                       else
end
                                                          skip
                                                       end
N = U + 1
                                                    end
N = U + 1
                                            end, *)
N = U + 1
                                             k
{Show K}
                                                                  CE****
                                              Store*
                                                                  xs'"-> Xs
                                              xs = [1234]
                                              n =
                                                                  n''' -> N
                                                                  t'' -> T
                                              t = [2 \ 3 \ 4]
                                                                  u"->U
                                              u =
                                              xs'=[2 3 4]
                                              n'=
                                              t'=[3 4]
                                              u'=
                                              xs'' = [3 4]
                                              n'' =
                                              t'' = [4]
                                              u" =
                                              xs''' = [4]
                                              n""=
```

| Stack  | Store                              |                    | E     |
|--|------------------------------------|--------------------|-------|
| <pre>local U in           {Length T U}           N = U + 1 end N = U + 1 N = U + 1 N = U + 1 Show K}</pre> | <pre>length = (proc {\$ Xs N</pre> | l then<br>_ T then | k-> K |
|  |                                    | xs'"-> Xs          |       |

|  |                                  | 1 |
|--|----------------------------------|---|
| n = t = [2 3 4] u = xs'=[2 3 4] n'= t'=[3 4] u'= xs" = [3 4] n" = t" = [4] u" = xs""= [4] n""= t"" = nil | n''' -> N<br>t''' -> T<br>u''->U |   |

### => Declaración variable U

| Stack  | Store  |   | E     |
|--|--|---|-------|
| {Length T U} N = U + 1 N = U + 1 N = U + 1 N = U + 1 Show K} | <pre>length = (proc {\$ Xs N}</pre>  |   | k-> K |
|  | Store*   | CE****                                    |       |
|  | xs = [1 2 3 4]<br>n =<br>t = [2 3 4]<br>u =<br>xs'=[2 3 4]<br>n'=<br>t'=[3 4]<br>u'=<br>xs'' = [3 4]<br>n'' =<br>t'' = [4] | xs'"-> Xs<br>n'"-> N<br>t'"-> T<br>u"'->U |       |



# => Ejecución Length

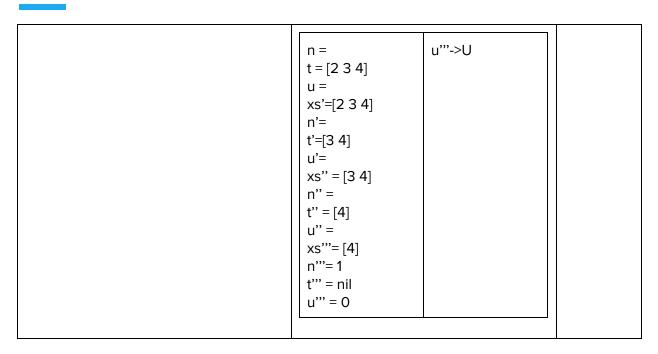
| Stack   | Store  |   | E     |
|---|--|---|-------|
| <pre>case Xs of nil then     N = 0 else     case Xs of _ T then         local U in         {Length T U}         N = U + 1         end     else         skip     end end</pre> | end else skip end end end end k  | il then  f _ T then  J in {Length T U}  N = U + 1 | k-> K |
| N = U + 1<br>N = U + 1<br>N = U + 1<br>{Show K}   | Store*  xs = [1 2 3 4] n = t = [2 3 4] u = xs'=[2 3 4] n'= t'=[3 4] u'= xs" = [3 4] n" = t' = [4] u" = xs"'= [4] n"'= t" = nil u" = xs""= nil n""= | xs'"'-> Xs<br>n'"' -> N<br>t"' -> T<br>u'"->U     |       |

| Stack   | Store   |  | E     |
|---|---|--|-------|
| N = 0<br>N = U + 1<br>N = U + 1<br>N = U + 1<br>N = U + 1<br>{Show K} | <pre>length = (proc {\$ Xs N}</pre>   |  | k-> K |
|   | Store*  | CE****                                 |       |
|   | xs = [1 2 3 4]<br>n =<br>t = [2 3 4]<br>u =<br>xs'=[2 3 4]<br>n'=<br>t'=[3 4]<br>u'=<br>xs'' = [3 4]<br>n'' =<br>t'' = [4]<br>u'' =<br>xs'''= [4]<br>n'''=<br>t''' = nil<br>u''' =<br>xs''''= nil<br>n''''= | xs''''-> Xs<br>n'''' -> N<br>t''''-> U |       |

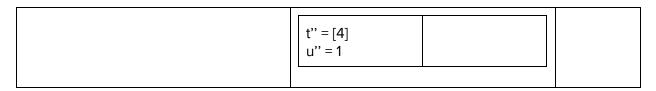
| Stack  | Store                               | E     |
|--|-------------------------------------|-------|
| N = U + 1<br>N = U + 1<br>N = U + 1<br>N = U + 1<br>{Show K} | <pre>length = (proc {\$ Xs N}</pre> | k-> K |

| else<br>skip<br>end<br>end<br>end, *)  |   |  |
|--|---|--|
| Store*   | CE****  |  |
| xs = [1 2 3 4]<br>n =<br>t = [2 3 4]<br>u =<br>xs'=[2 3 4]<br>n'=<br>t'=[3 4]<br>u'=<br>xs" = [3 4]<br>n" =<br>t" = [4]<br>u" =<br>xs"= [4]<br>n""=<br>t'" = nil<br>u"' =<br>xs""= nil | xs''''-> Xs<br>n'''' -> N<br>t''' -> T<br>u'''->U |  |

| Stack   | Store                            |                       | E     |
|---|----------------------------------|-----------------------|-------|
| N = U + 1<br>N = U + 1<br>N = U + 1<br>{Show K} | <pre>length = (proc {\$ Xs</pre> | il then<br>f _ T then | k-> K |
|   | Store*                           | CE***                 |       |
|   | xs = [1 2 3 4]                   | n''' -> N             |       |



| Stack                              | Store   |                  | E     |
|------------------------------------|---|------------------|-------|
| N = U + 1<br>N = U + 1<br>{Show K} | <pre>length = (proc {\$ Xs N}</pre>   |                  | k-> K |
|                                    | Store*  | CE**             |       |
|                                    | xs = [1 2 3 4]<br>n =<br>t = [2 3 4]<br>u =<br>xs'=[2 3 4]<br>n'=<br>t'=[3 4]<br>u'=<br>xs" = [3 4]<br>n" = 2 | n" -> N<br>u"->U |       |



| Stack                 | Store  |                       | E     |
|-----------------------|--|-----------------------|-------|
| N = U + 1<br>{Show K} | <pre>length = (proc {\$ Xs</pre>   | il then<br>f _ T then | k-> K |
|                       | Store*   | CE*                   |       |
|                       | xs = [1 2 3 4]<br>n =<br>t = [2 3 4]<br>u =<br>xs'=[2 3 4]<br>n'= 3<br>t'=[3 4]<br>u'= 2 | n' -> N<br>u'->U      |       |

| Stack    | Store                               | E     |
|----------|-------------------------------------|-------|
| {Show K} | <pre>length = (proc {\$ Xs N}</pre> | k-> K |

| k = 4   |                |  |
|---|----------------|--|
| Store*  | CE             |  |
| xs = [1 2 3 4]<br>n = 4<br>t = [2 3 4]<br>u = 3 | n -> N<br>u->U |  |
|   |                |  |

# => Ejecución de show, muestra un 4

| Stack | Store                               | E     |
|-------|-------------------------------------|-------|
|       | <pre>length = (proc {\$ Xs N}</pre> | k-> K |

# Implementación Tail Recursive

### Estado inicial

| Stack                     | Store | Е |
|---------------------------|-------|---|
| local Length in           | -     | - |
| Length = proc {\$ Xs A N} |       |   |
| case Xs of nil then       |       |   |
| N = A                     |       |   |
| else                      |       |   |
| case Xs of _ T then       |       |   |
| local X in                |       |   |
| X = A + 1                 |       |   |
| {Length T X N}            |       |   |
|                           |       |   |
| end                       |       |   |
| else                      |       |   |
| skip                      |       |   |
| end                       |       |   |
| end                       |       |   |

```
end
end
local K in
{Length [1 2 3 4] 0 K}
{Show K}
end
```

### => Declaración de variable

| Stack   | Store    | E               |
|---|----------|-----------------|
| <pre>Length = proc {\$ Xs A N}   case Xs of nil then       N = A   else</pre> | length = | Length ->length |
| case Xs of _ T then local X in X = A + 1 {Length T X N} end                   |          |                 |
| end<br>else<br>skip<br>end<br>end<br>end                                      |          |                 |
| <pre>local K in   {Length [1 2 3 4] 0 K}   {Show K} end</pre>                 |          |                 |

### => Asignación procedure value

| Stack  | Store   | Е               |
|--|---|-----------------|
| local K in {Length [1 2 3 4] 0 K} {Show K} end | <pre>length ={proc {\$ Xs A N}     case Xs of nil then         N = A     else         case Xs of _ T then</pre> | Length ->length |

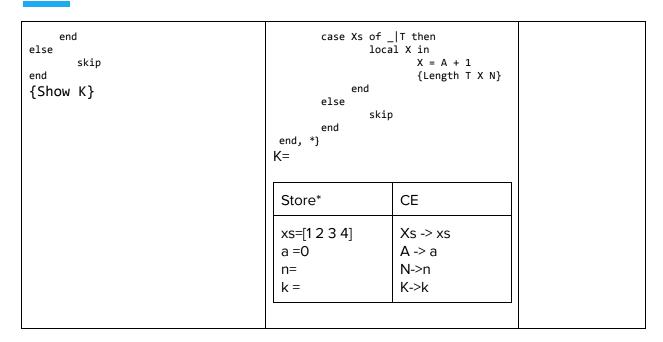
#### => Declaración variable K

| Stack                              | Store  | E                                   |
|------------------------------------|--|-------------------------------------|
| {Length [1 2 3 4] 0 K}<br>{Show K} | <pre>length ={proc {\$ Xs A N}     case Xs of nil then</pre> | Length ->length<br><b>K -&gt; k</b> |

# => Ejecución de Length

| Stack   | Store   |  | E                         |
|---|---|--|---------------------------|
| <pre>case Xs of nil then     N = A else  case Xs of _ T then     local X in     X = A + 1     {Length T X N}     end     else         skip     end end {Show K}</pre> | <pre>length ={proc {\$ Xs A   case Xs of nil then       N = A   else       case Xs of _ T       local</pre> | T then X in X = A + 1 {Length T X N}     | Length ->length<br>K -> k |
|   | xs=[1 2 3 4]  | CE<br>Xs -> xs<br>Δ -> a<br>N->n<br>K->k |                           |

| Stack   | Store  | E                         |
|---|--|---------------------------|
| case Xs of _ T then local X in X = A + 1 {Length T X N} | <pre>length ={proc {\$ Xs A N}   case Xs of nil then      N = A   else</pre> | Length ->length<br>K -> k |



### => Ejecución de case

| Stack  | Store  |   | E                         |
|--|--|---|---------------------------|
| local X in     X = A + 1     {Length T X N} end {Show K} | length ={proc {\$ Xs case Xs of nil then N = A else case Xs of ilocal end else skip end end, *}    Store*   Xs=[1 2 3 4]   a = 0   n =   k =   t=[2 3 4] | n<br>_ T then<br>al X in<br>X = A + 1<br>{Length T X N} | Length ->length<br>K -> k |
|  |  |   |                           |

#### => Declaración de variable local X

| Stack | Store | E |
|-------|-------|---|
|-------|-------|---|

```
X = A + 1
                                                                                      Length ->length
                                          length ={proc {$ Xs A N}
{Length T X N}
                                           case Xs of nil then
                                                                                      K \rightarrow k
{Show K}
                                                  N = A
                                           else
                                                  case Xs of _|T then local X in
                                                                   X = A + 1
                                                                   {Length T X N}
                                                        end
                                                  else
                                                           skip
                                                  end
                                           end, *}
                                          K=
                                           Store*
                                                                CE
                                                                Xs \rightarrow xs
                                           xs=[1 2 3 4]
                                           a =0
                                                                A -> a
                                           n=
                                                                N->n
                                           k =
                                                                K->k
                                           t=[2 3 4]
                                                                T->t
                                           x=
                                                                X->x
```

### => Asignación de valor

| Stack                   | Store   |  | Е                         |
|-------------------------|---|--|---------------------------|
| {Length T X N} {Show K} | <pre>length ={proc {\$ Xs   case Xs of nil then</pre> | T then  I X in  X = A + 1  {Length T X N}  | Length ->length<br>K -> k |
|                         | Store*  | CE   |                           |
|                         | xs=[1 2 3 4]<br>a =0<br>n=<br>k =<br>t=[2 3 4]        | Xs -> xs<br>A -> a<br>N->n<br>K->k<br>T->t |                           |

| x=1 | X->x     |  |
|-----|----------|--|
| -   | <u>.</u> |  |

# => Ejecución de Length

| Stack     |   | Store  |   | E                         |
|-----------|---|--|---|---------------------------|
| end {Show | <pre>of nil then N = A  case Xs of _ T then</pre> | <pre>length ={proc {\$ Xs}   case Xs of nil ther       N = A   else       case Xs of _       loca        end       else       skip     end, *} K=</pre> Store* | T then  I X in  X = A + 1  {Length T X N}             | Length ->length<br>K -> k |
|           |   | xs=[1 2 3 4]<br>a =0<br>n=<br>k =<br>t=[2 3 4]<br>x=1<br>xs'=[2 3 4]<br>a'=1<br>n'=  | Xs -> xs'<br>A -> a'<br>N->n'<br>K->k<br>T->t<br>X->x |                           |

| Stack                          | Store  | E                         |
|--------------------------------|--|---------------------------|
| <pre>case Xs of _ T then</pre> | <pre>length ={proc {\$ Xs A N}     case Xs of nil then</pre> | Length ->length<br>K -> k |

| Store*       CE*         xs=[1 2 3 4]       Xs -> xs'         a = 0       A -> a'         n=       N->n'         k =       K->k         t=[2 3 4]       T->t         y=1       Y->y | K=   |                          |  |
|---|--|--------------------------|--|
| a =0<br>n=<br>k =<br>t=[2 3 4]<br>A -> a'<br>N->n'<br>K->k<br>T->t  | Store*   | CE*                      |  |
| xs'=[2 3 4]<br>a'=1<br>n'=  | a =0<br>n=<br>k =<br>t=[2 3 4]<br>x=1<br>xs'=[2 3 4]<br>a'=1 | A -> a'<br>N->n'<br>K->k |  |

| Stack                 | Store   |  | E                         |
|-----------------------|---|--|---------------------------|
| <pre>local X in</pre> | end<br>else   |  | Length ->length<br>K -> k |
|                       | Store*  | CE*  |                           |
|                       | xs=[1 2 3 4]<br>a =0<br>n=<br>k =<br>t=[2 3 4]<br>x=1<br>xs'=[2 3 4]<br>a'=1<br>n'=<br>t'=[3 4] | Xs -> xs'<br>A -> a'<br>N->n'<br>K->k<br>T->t'<br>X->x |                           |

#### => Declaración de X

| Stack  | Store  |   | E                         |
|--|--|---|---------------------------|
| <pre>X = A + 1 {Length T X N} {Show K}</pre> | <pre>length ={proc {\$ Xs   case Xs of nil then      N = A   else</pre>          | _ T then<br>al X in                           | Length ->length<br>K -> k |
|  | Store*  xs=[1 2 3 4] a =0 n= k = t=[2 3 4] x=1 xs'=[2 3 4] a'=1 n'= t'=[3 4] x'= | CE*  Xs -> xs' A -> a' N->n' K->k T->t' X->x' |                           |

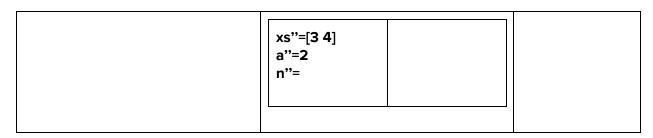
### => Asignación de valor

| Stack    | Store   | E                         |
|----------|---|---------------------------|
| {Show K} | <pre>length ={proc {\$ Xs A N}   case Xs of nil then         N = A   else         case Xs of _ T then</pre> | Length ->length<br>K -> k |

| a =0 |  | k = | K->k |  |
|------|--|-----|------|--|
|------|--|-----|------|--|

### => Ejecución de Length

| Stack   | Store   |        | E                         |
|---|---|--------|---------------------------|
| <pre>case Xs of nil then     N = A else  case Xs of _ T then     local X in     X = A + 1     {Length T X N}     end     else         skip     end end {Show K}</pre> | length ={proc {\$ Xs A case Xs of nil then N = A else case Xs of _ T local loca | Γ then | Length ->length<br>K -> k |
|   | x'= 2   |        |                           |



### => Ejecución de case

| Stack                          | Store  |  | Е                         |
|--------------------------------|--|--|---------------------------|
| <pre>case Xs of _ T then</pre> | <pre>length ={proc {\$ Xs   case Xs of nil then      N = A   else</pre>                                  | T then<br>   X in<br>  X = A + 1<br>  {Length T X N} | Length ->length<br>K -> k |
|                                | Store*  xs=[1 2 3 4] a =0 n= k = t=[2 3 4] x=1 xs'=[2 3 4] a'=1 n'= t'=[3 4] x'= 2 xs''=[3 4] a''=2 n''= | Xs -> xs" A -> a" N->n" K->k T->t' X->x'             |                           |

| Stack | Store | E |  |
|-------|-------|---|--|
|       |       |   |  |

```
local X in
                                                                                  Length ->length
                                        length ={proc {$ Xs A N}
       X = A + 1
                                         case Xs of nil then
                                                                                  K \rightarrow k
       {Length T X N}
                                                N = A
end
                                         else
                                                case Xs of _|T then local X in
{Show K}
                                                                X = A + 1
                                                                {Length T X N}
                                                     end
                                                else
                                                        skip
                                                end
                                         end, *}
                                        K=
                                         Store*
                                                             CE**
                                                             Xs -> xs"
                                         xs=[1 2 3 4]
                                                             A -> a"
                                         a =0
                                                             N->n"
                                         n=
                                                             K->k
                                         k =
                                                             T->t"
                                         t=[2 3 4]
                                         x=1
                                                             X->x'
                                         xs'=[2 3 4]
                                         a'=1
                                         n'=
                                         t'=[3 4]
                                         x'= 2
                                         xs"=[3 4]
                                         a"=2
                                         n"=
                                         t"=[4]
```

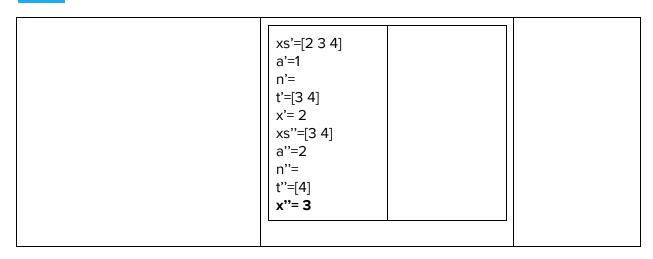
#### => Declaración de variable X

| Stack  | Store  | E                         |
|--|--|---------------------------|
| <pre>X = A + 1 {Length T X N} {Show K}</pre> | <pre>length ={proc {\$ Xs A N}     case Xs of nil then</pre> | Length ->length<br>K -> k |

| Store*  | CE**                                     |  |
|---|--|--|
| xs=[1 2 3 4] a =0 n= k = t=[2 3 4] x=1 xs'=[2 3 4] a'=1 n'= t'=[3 4] x'= 2 xs''=[3 4] a''=2 n''= t''=[4] x''= | Xs -> xs" A -> a" N->n" K->k T->t" X->x" |  |
|   |  |  |

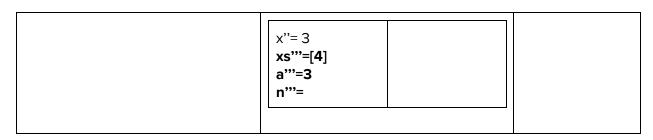
### => Asignación de valor

| Stack                   | Store   |  | E                         |
|-------------------------|---|--|---------------------------|
| {Length T X N} {Show K} | <pre>length ={proc {\$ Xs   case Xs of nil then      N = A   else</pre> | _ T then<br>al X in<br>X = A + 1<br>{Length T X N} | Length ->length<br>K -> k |
|                         | Store*  xs=[1 2 3 4] a =0 n= k = t=[2 3 4] x=1                          | CE**  Xs -> xs" A -> a" N->n" K->k T->t" X->x"     |                           |



# => Ejecución de Length

| Stack  | Store   |   | Е                         |
|--|---|---|---------------------------|
| case Xs of nil then     N = A else  case Xs of _ T then     local X in     X = A + 1     {Length T X N}     end else     skip end end {Show K} | <pre>length ={proc {\$ Xs   case Xs of nil then      N = A   else      case Xs of _</pre> | T then<br>  X in<br>  X = A + 1<br>  {Length T X N} | Length ->length<br>K -> k |
|  | n"=<br>t"=[4]   |   |                           |



| Stack                          | Store  |  | E                        |
|--------------------------------|--|--|--------------------------|
| <pre>case Xs of _ T then</pre> | length ={proc {\$ Xs case Xs of nil the N = A else case Xs of local end else skillend end, *} K=  Store*  Store*  xs=[1 2 3 4] a = 0 n= k = t=[2 3 4] x=1 xs'=[2 3 4] a'=1 | _ T then<br>al X in<br>X = A + 1<br>{Length T X N} | E Length ->length K -> k |
|                                | n'= t'=[3 4] x'= 2 xs''=[3 4] a''=2 n''= t''=[4] x''= 3 xs'''=[4] a'''=3 n'''=   |  |                          |

### => Ejecución de Case

| Stack   | Store   |   | E                        |
|---|---|---|--------------------------|
| Stack  local X in     X = A + 1     {Length T X N} end {Show K} | <pre>length ={proc {\$ Xs   case Xs of nil ther      N = A   else      case Xs of _</pre> | T then  I X in  X = A + 1  {Length T X N} | E Length ->length K -> k |
|   | x"= 3<br>xs""=[4]<br>a""=3<br>n""=<br><b>t""=nil</b>                                      |   |                          |

### => Declaración de variable X

| Stack  | Store  | E                         |
|--|--|---------------------------|
| <pre>X = A + 1 {Length T X N} {Show K}</pre> | <pre>length ={proc {\$ Xs A N}   case Xs of nil then     N = A</pre> | Length ->length<br>K -> k |

```
else
       case Xs of \_|\mathsf{T} then
               local X in
                       X = A + 1
                       {Length T X N}
            end
       else
                skip
       end
end, *}
K=
 Store*
                     CE***
 xs=[1 2 3 4]
                    Xs -> xs'"
                     A -> a'''
 a =0
 n=
                    N->n'''
                     K->k
 k =
                    T->t'''
 t=[2 3 4]
                    X->x'''
 x=1
xs'=[2 3 4]
 a'=1
 n'=
 t'=[3 4]
 x'= 2
xs"=[3 4]
 a"=2
 n"=
t"=[4]
 x"= 3
xs'"=[4]
 a'''=3
 n'''=
 t""=nil
 χ";=
```

### => Asignación de valor

| Stack                      | Store   | E                         |
|----------------------------|---|---------------------------|
| {Length T X N}<br>{Show K} | <pre>length ={proc {\$ Xs A N}   case Xs of nil then       N = A   else       case Xs of _ T then</pre> | Length ->length<br>K -> k |

| Store*  CE***  xs=[1 2 3 4] |
|-----------------------------|
| n'''= t'''=nil x'''=4       |

# => Ejecución de Length

| Stack                          | Store  | E                         |
|--------------------------------|--|---------------------------|
| <pre>case Xs of nil then</pre> | <pre>length ={proc {\$ Xs A N}     case Xs of nil then</pre> | Length ->length<br>K -> k |

| Stack             | Store                                       |   | E                         |
|-------------------|---|---|---------------------------|
| N = A<br>{Show K} | end<br>else<br>skip<br>end<br>end, *}<br>K= | T then  I X in  X = A + 1  {Length T X N} | Length ->length<br>K -> k |
|                   | Store*                                      | CE****                                    |                           |

| xs=[1 2 3 4] a = 0 n= k = t=[2 3 4] x=1 xs'=[2 3 4] a'=1 n'= t'=[3 4] x'= 2 xs''=[3 4] a''=2 n''= t''=[4] x''= 3 xs'''=[4] a'''=3 n'''= t'''=nil x'''=4 xs''''=nil a''''=4 n''''= | Xs -> xs"" A -> a"" N->n"" K->k T->t"" X->x" |  |
|---|--|--|

### => Asignación de valor

| Stack    | Store   |  | E                         |
|----------|---|--|---------------------------|
| {Show K} | <pre>length ={proc {\$ Xs   case Xs of nil ther      N = A   else</pre> | T then I X in X = A + 1 {Length T X N} | Length ->length<br>K -> k |
|          | Store*  | CE****                                 |                           |
|          | xs=[1 2 3 4]  | Xs -> xs''''                           |                           |

# => Ejecución de show, muestra un K=4 y finaliza la ejecución

| Stack | Store  | E                         |
|-------|--|---------------------------|
|       | <pre>length ={proc {\$ Xs A N}     case Xs of nil then</pre> | Length ->length<br>K -> k |

# Ejercicio 6) - Alto orden con listas