7524 - Teoría de la programación
TP Individual

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Ejercicio 1) - Procesamiento de listas

1. Length
   a. Código Oz

```
% Length function
declare fun {Length Xs}
        case Xs of nil then 0
        [] H|T then 1 + {Length T}
        end
    end
```

   b. Ejemplos de ejecución

2. Take
   a. Código Oz

```
% Take function
declare fun {Take Xs N}
        if N == 0 then nil
        else
            case Xs of nil then nil
            [] H|T then H|{Take T N-1}
            end
        end
    end
```

b. Ejemplos de ejecución

3. Drop

a. Código Oz

```
% Drop function
declare fun {Drop Xs N}
        if N == 0 then Xs
        else
            case Xs of nil then nil
            [] H|T then {Drop T N-1}
            end
        end
    end
```

b. Ejemplos de ejecución

4. Append

a. Código Oz

```
% Append function
declare fun {Append Xs Ys}
        if Ys == nil then Xs
        else
            case Xs of nil then Ys
            [] H|T then H|{Append T Ys}
            end
        end
    end
```

b. Ejemplos de ejecución

5. Member

a. Código Oz

```
% Member function
declare fun {Member Xs Y}
        case Xs of nil then false
        [] H|T then
            if H == Y then true
            else
             {Member T Y}
            end
        end
   end
```

b. Ejemplos de ejecución

Oz Programming Interface (emacs@KARINA-VAIO)

File Edit Options Buffers Tools Oz Help

```
% Member function
declare fun {Member Xs Y}
          case Xs of nil then false
          [] H|T then
              if H == Y then true
              else
                  {Member T Y}
              end
          end
      end
% invocation examples Member
{Show 'Member examples'}
{Show {Member [1 2 10 15] 2}}
{Show {Member [1 2 10 15] 1}}
{Show {Member [1 2 10 15] 10}}
{Show {Member [1 2 10 a 15] 15}}
{Show {Member [1 2 10 a 15] a}}
{Show {Member [1 2 10 15] b}}
{Show {Member [1 2 10 15] 3}}
{Show {Member [1 2 10 15] 5}}
{Show {Member [1 2 10 15] nil}}
{Show {Member nil a}}
```

1**- Oz   All L11   (Oz)

```
'Member examples'
true
true
true
true
true
false
false
false
false
false
```

1**- *Oz Emulator*   All L11   (Comint:run)

6. Position

a. Código Oz

```
% Position function
declare fun {Position Xs Y}
        case Xs of nil then 0
        [] H|T then
            if H == Y then 0
            else 1 + {Position T Y}
            end
        end
    end
```

b. Ejemplos de ejecución

Ejercicio 2) - Referencias externas

1. proc {P X Y} local Z in {Q Z U} end end

    Referencias externas: Q, U

2. proc {P X Y} local Z in {Q Z Y} end end

    Referencias externas: Q

3. proc {P X Y} local Z in {P Z Y} end end

    Referencias externas: ninguna

Ejercicio 3) - Ejemplo de ejecución

Programa 1

Estado inicial

Stack	Store	E

local B in
      if B then
           Skip
      else
           skip
      end
end
	-	-

=> Ejecución de declaración de variable

Stack	Store	E

if B then
      skip
else
      skip
end
	b1	**B-> b1**

=> **Ejecución de condicional. Como E(B) no está determinado, el programa se suspende, a la espera que b1 tome algun valor.**

Programa 2

Estado inicial

Stack	Store	E

local B in
    B = false
    if B then
        skip
    else
        skip
    end
end
	-	**-**

=> **Ejecución de declaración de variable y composición**

Stack	Store	E

B = false
if B then
    skip
else
    skip
end
	b1	**B-> b1**

=> **Ejecución de binding de variables**

Stack	Store	E

if B then
    skip
else
    skip
end
	b1 = **false**	B-> b1

=> **Ejecución de condicional, como B = false entonces se agrega en el stack la sentencia dentro del else**

Stack	Store	E
skip	b1 = false	B-> b1

=> Ejecución del skip (St6), no hay cambios en el store y se quita la sentencia.

Stack	Store	E
-	b1 = false	B-> b1

No hay nada mas en el stack, entonces el programa finaliza.

Programa 3

Estado inicial

Stack	Store	E

local X Z A B P in
      proc {P X Y}
          Y = X+Z
      end
      Z=7
      X=4
      {P X A}
      {P A B}
end
	-	-

=> Ejecución de declaración de variables

Stack	Store	E
proc {P X Y} Y = X+Z end Z=7 X=4 {P X A} {P A B}	**x1** **z1** **a1** **b1** **p1**	**X -> x1** **Z-> z1** **A -> a1** **B -> b1** **P-> p1**

=> Ejecución de procedure value

Stack	Store	E
Z=7 X=4 {P X A} {P A B}	x1 z1 a1 b1 p1 = **proc {P X Y}** **Y = X+Z** **end, CE = {Z -> z1}**	X -> x1 Z-> z1 A -> a1 B -> b1 P-> p1

=> **Ejecución de binding de variable**

Stack	Store	E
X=4 {P X A} {P A B}	x1 z1 = **7** a1 b1 p1 = proc {P X Y} Y = X+Z end, CE = {Z -> z1}	X -> x1 Z-> z1 A -> a1 B -> b1 P-> p1

=> **Ejecución de binding de variable**

Stack	Store	E
{P X A} {P A B}	x1 = **4** z1 = 7 a1 b1 p1 = proc {P X Y} Y = X+Z end, CE = {Z -> z1}	X -> x1 Z-> z1 A -> a1 B -> b1 P-> p1

=> **Ejecución de procedure value**

Stack	Store	E
A = **X + Z** {P A B}	x1 = 4 z1 = 7 a1 b1 p1 = proc {$ X Y} Y = X+Z end, CE = {Z -> z1}	X -> x1 Z-> z1 A -> a1 B -> b1 P-> p1

=> **Asignacion de variable mas suma en base al store**

Stack	Store	E
{P A B}	x1 = 4 z1 = 7 a1 = **11** b1 p1 = proc {$ X Y} Y = X+Z end, CE = {Z -> z1}	X -> x1 Z-> z1 A -> a1 B -> b1 P-> p1

=> **Ejecución de procedure value**

Stack	Store	E
B = A + Z	x1 = 4 z1 = 7 a1 = 11 b1 p1 = proc {$ X Y} Y = X+Z end, CE = {Z -> z1}	X -> x1 Z-> z1 A -> a1 B -> b1 P-> p1

=> **Asignacion de variable mas suma en base al store**

Stack	Store	E
-	x1 = 4 z1 = 7 a1 = 11 b1 = **18** p1 = proc {$ X Y} Y = X+Z end, CE = {Z -> z1}	X -> x1 Z-> z1 A -> a1 B -> b1 P-> p1

Programa 4

Estado inicial

Stack	Store	E

local X Z A B P in
     proc {P X Y}
         Y = X+Z
     end
     Z=10
     local Z in
         Z = 2
         X=4
         {P X A}
         {P A B}
     end
end
	-	-

=> **Ejecución de declaración de variables**

Stack	Store	E

proc {P X Y}
      Y = X+Z
end
Z=10
local Z in
      Z = 2
      X=4
      {P X A}
      {P A B}
end
	x1
	z1
	a1
	b1
	p1
		X - > x1
		Z -> z1
		A -> a1
		B -> b1
		P -> p1

=> **Ejecución de declaración de procedure value**

Stack	Store	E

Z=10
local Z in
      Z = 2
      X=4
      {P X A}
      {P A B}
end
	x1
	z1
	a1
	b1
	p1 = **proc {$ X Y}**
	           Y = X+Z
	end, CE = {Z -> z1}
		X - > x1
		Z -> z1
		A -> a1
		B -> b1
		P -> p1

=> **Ejecución de asignación de variable**

Stack	Store	E

local Z in
      Z = 2
      X=4
      {P X A}
      {P A B}
end
	x1
	z1 = **10**
	a1
	b1
	p1 = proc {$ X Y}
	           Y = X+Z
	end, CE = {Z -> z1}
		X - > x1
		Z -> z1
		A -> a1
		B -> b1
		P -> p1

=> **Ejecución de declaración de variable Z**

Stack	Store	E
Z = 2 X=4 {P X A} {P A B}	x1 z1 = 10 **z2** a1 b1 p1 = proc {$ X Y}	X - > x1 Z -> **z2** A -> a1 B -> b1 P -> p1

	Y = X+Z end, CE = {Z -> z1}	

=> **Ejecución de asignación de variable Z (en el nuevo entorno)**

Stack	Store	E
X=4 {P X A} {P A B}	x1 z1 = 10 z2 = **2** a1 b1 p1 = proc {$ X Y} Y = X+Z end, CE = {Z -> z1}	X - > x1 Z -> z2 A -> a1 B -> b1 P -> p1

=> **Ejecución de asignación de variable X (en el nuevo entorno)**

Stack	Store	E
{P X A} {P A B}	x1 = **4** z1 = 10 z2 = 2 a1 b1 p1 = proc {$ X Y} Y = X+Z end, CE = {Z -> z1}	X - > x1 Z -> z2 A -> a1 B -> b1 P -> p1

=> **Ejecución de procedure value (en el nuevo entorno usando su entorno contextual)**

Stack	Store	E
A = X + Z {P A B}	x1 = 4 z1 = 10 z2 = 2 a1 b1 p1 = proc {$ X Y} Y = X+Z end, CE = {Z -> z1}	X - > x1 Z -> z2 A -> a1 B -> b1 P -> p1

=> **Ejecución de la única sentencia del procedure (en el nuevo entorno usando su entorno contextual)**

Stack	Store	E

| {P A B} | x1 = 4
z1 = 10
z2 = 2
a1 = **14 (Z -> z1 = 10)**
b1
p1 = proc {$ X Y}
      Y = X+Z
end, CE = {Z -> z1} | X - > x1
Z -> z2
A -> a1
B -> b1
P -> p1 |

=> **Ejecución del procedure value(en el nuevo entorno usando su entorno contextual)**

Stack	Store	E
B = A + Z	x1 = 4 z1 = 10 z2 = 2 a1 = 14 b1 p1 = proc {$ X Y} Y = X+Z end, CE = {Z -> z1}	X - > x1 Z -> z2 A -> a1 B -> b1 P -> p1

=> **Ejecución de la única sentencia del procedure (en el nuevo entorno usando su entorno contextual)**

Stack	Store	E
-	x1 = 4 z1 = 10 z2 = 2 a1 = 14 b1 = **24 (a1:14 +z1:10)** p1 = proc {$ X Y} Y = X+Z end, CE = {Z -> z1}	X - > x1 Z -> z2 A -> a1 B -> b1 P -> p1

Fin del programa

Programa 5

Estado inicial

Stack	Store	E

local X Y Z P Q in
      X=6
      Y=4
      proc {P A B}
            proc {B U V}
                  local F in
                          F=A+1
                          V=U+F
                  end
            end
      end
      {P X Q}
      {Q Y Z}
end
	-	-

=> **Declaracion de variables**

Stack	Store	E

X=6
Y=4
proc {P A B}
      proc {B U V}
            local F in
                 F=A+1
                 V=U+F
            end
      end
end
{P X Q}
{Q Y Z}
	x1
	y1
	z1
	p1
	q1
		X -> x1
		Y -> y1
		Z -> z1
		P -> p1
		Q -> q1

=> **Asignación de variable**

Stack	Store	E

Y=4
proc {P A B}
      proc {B U V}
            local F in
	x1 = **6**
	y1
	z1
	p1
		X -> x1
		Y -> y1
		Z -> z1
		P -> p1

F=A+1 V=U+F end end end {P X Q} {Q Y Z}	q1	Q -> q1

=> **Asignación de variable**

Stack	Store	E
proc {P A B} proc {B U V} local F in F=A+1 V=U+F end end end {P X Q} {Q Y Z}	x1 = 6 y1 = **4** z1 p1 q1	X -> x1 Y -> y1 Z -> z1 P -> p1 Q -> q1

=> **Declaración procedure value**

Stack	Store	E
{P X Q} {Q Y Z}	x1 = 6 y1 = 4 z1 p1 = **proc {$ A B}** **proc {B U V}** **local F in** **F=A+1** **V=U+F** **end** **end** **end, CE** = {} q1	X -> x1 Y -> y1 Z -> z1 P -> p1 Q -> q1

=> **Ejecución procedure value**

Stack	Store	E

proc {Q U V}
          local F in
                    F = X + 1
                    V = U + F
          end
end
{Q Y Z}
	x1 = 6
	y1 = 4
	z1
	p1 = proc {$ A B}
	          proc {B U V}
	                    local F in
	                              F=A+1
	                              V=U+F
	                    end
	          end
	end, CE = {}
	q1
		X -> x1
		Y -> y1
		Z -> z1
		P -> p1
		Q -> q1

=> **Declaración procedure value**

Stack	Store	E

{Q Y Z}	x1 = 6
	y1 = 4
	z1
	p1 = proc {$ A B}
	          proc {B U V}
	                    local F in
	                              F=A+1
	                              V=U+F
	                    end
	          end
	end, CE = {}
	q1 = **proc {$ U V}**
	          local F in
	                    F = X + 1
	                    V = U + F
	          end
	End, CE = **{X-> x1}**
		X -> x1
		Y -> y1
		Z -> z1
		P -> p1
		Q -> q1

=> Ejecución procedure value

Stack	Store	E

local F in
      F = X + 1
      Z = Y + F
end
	x1 = 6
	y1 = 4
	z1
	p1 = proc {$ A B}
	        proc {B U V}
	            local F in
	                  F=A+1
	                  V=U+F
	            end
	        end
	end, CE = {}
	q1 = proc {$ U V}
	      local F in
	         F = X + 1
	         V = U + F
	      end
	End, CE = {X-> x1}
		X -> x1
		Y -> y1
		Z -> z1
		P -> p1
		Q -> q1

=> declaración de variable

Stack	Store	E

F = X + 1
Z = Y + F
	x1 = 6
	y1 = 4
	z1
	f1
	p1 = proc {$ A B}
	        proc {B U V}
	            local F in
	                   F=A+1
	                   V=U+F
	            end
	        end
	end, CE = {}
	q1 = proc {$ U V}
	      local F in
	         F = X + 1
	         V = U + F
	      end
	End, CE = {X-> x1, **F -> f1**}
		X -> x1
		Y -> y1
		Z -> z1
		P -> p1
		Q -> q1

=> **Asignación y suma de variables**

Stack	Store	E
Z = Y + F	x1 = 6 y1 = 4 z1 f1 = **7** p1 = proc {$ A B} proc {B U V} local F in F=A+1 V=U+F end end end, CE = {} q1 = proc {$ U V} local F in F = X + 1 V = U + F end End, CE = {X-> x1, F -> f1}	X -> x1 Y -> y1 Z -> z1 P -> p1 Q -> q1

=> **Asignación y suma de variables**

Stack	Store	E
-	x1 = 6 y1 = 4 z1 = **7(f1) + 4(y1) = 11** f1 = 7 p1 = proc {$ A B} proc {B U V} local F in F=A+1 V=U+F end end end, CE = {} q1 = proc {$ U V} local F in F = X + 1 V = U + F end End, CE = {X-> x1, F -> f1}	X -> x1 Y -> y1 Z -> z1 P -> p1 Q -> q1

Programa 6

Estado inicial

Stack	Store	E

local X Y Z in
    X = Y
    try
        X = 1 Y = 2 Z = 3
    catch Exception then
        skip
    end
    {Browse X#Y#Z}
end
	-	-

=> **Declaración de variables**

Stack	Store	E

X = Y
try
    X = 1 Y = 2 Z = 3
catch Exception then
    skip
end
{Browse X#Y#Z}
	x1
	y1
	z1
		X -> x1
		Y -> y1
		Z -> z1

=> **Asignación de variables**

Stack	Store	E

try
    X = 1
    Y = 2
    Z = 3
catch Exception then
    skip
end
{Browse X#Y#Z}
	x1
	y1
	z1
		X -> y1
		Y -> y1
		Z -> z1

=> **Ejecución de try**

Stack	Store	E
X = 1 Y = 2	x1 y1	X -> y1 Y -> y1

Z = 3 catch Exception then skip end {Browse X#Y#Z}	z1	Z -> z1

=> Ejecución de asignación de variable (dentro del catch)

Stack	Store	E
Y = 2 Z = 3 catch Exception then skip end {Browse X#Y#Z}	x1 y1 = **1** z1	X -> y1 Y -> y1 Z -> z1

=> Ejecución de asignación de variable (dentro del catch)

Stack	Store	E
Y = 2 Z = 3 catch Exception then skip end {Browse X#Y#Z}	x1 y1 = 1 z1	X -> y1 Y -> y1 Z -> z1

Acá se intenta asignar a y1 el valor 2, pero esta variable ya tiene valor porque X = Y, entonces dispara la Exception y se quitan todas las operaciones hasta la del catch

=> Ejecución Exception

Stack	Store	E
skip {Browse X#Y#Z}	x1 y1 = 1 z1	X -> y1 Y -> y1 Z -> z1

=> Ejecución Skip

Stack	Store	E
{Browse X#Y#Z}	x1 y1 = 1 z1	X -> y1 Y -> y1 Z -> z1

Stack	Store	E
	x1 y1 = 1 z1	X -> y1 Y -> y1 Z -> z1

Como el valor de Z no esta determinado el browse mostrará un '_' indicando que aun no se definió, en otras operaciones podría suspenderse la ejecución, pero no ocurre con Browse. La ejecución mostrará:

1#1#_

Ejercicio 4) - Case

{Test [b c a]}

Predicción: 'case'(4)

Ejecución: 'case'(4)

La lista no empieza con a como primer elemento, ni es un record, es una lista pero el primer y elemento no son iguales, luego es una lista, entonces case 4.

{Test f(b(3))}

Predicción: 'case'(5)

Ejecución: 'case'(5)

No es lista que empiece con a, si bien es un tupla llamada f, su valor no es a sino b(3), tampoco es una lista, con lo cual saltamos al caso 5 que cumple, dado que es un tupla llamada f y Y tomará el valor b(3)

{Test f(a)}

Predicción: 'case'(2)

Ejecución: 'case'(2)

No es lista, entonces analiza el case 2 donde coincide el nombre de la tupla y el elemento que contiene.

{Test f(a(3))}

Predicción: 'case'(5)

Ejecución: 'case'(5)

No es lista, luego es una tupla llamada f pero el elemento no es a, luego caso 3 y 4 no cumple por no ser una lista, en el caso 5 satisface la condición porque se llama f y el valor de la variable Y será a(3)

{Test f(d)}

Predicción: 'case'(5)

Ejecución: 'case'(5)

No es lista, luego es una tupla llamada f pero el elemento no es a, luego caso 3 y 4 no cumple por no ser una lista, en el caso 5 satisface la condición porque se llama f y el valor de la variable Y será d

{Test [a b c]}

Predición: 'case'(1)

Ejecución: 'case'(1)

Es una lista que empieza con el valor a, cumple la primer condición.

{Test [c a b]}

Prediccion: 'case'(4)

Ejecución:'case'(4)

No es una lista que comience con el valor a, luego no es una tupla, luego no es una lista con los primeros dos elementos iguales. Finalmente es una lista por lo que entra en el caso 4.

{Test a|a}

Predicción: 'case'(1)

Ejecución: 'case'(1)

Es una lista que comienza con el valor a.

{Test 'l'(v b)}

Predicción: 'case'(6)

Ejecución: 'case'(4)

No es una lista que comience con a, tampoco es tupla, no es una lista con dos elementos iguales al inicio, pero si es una lista donde el valor de Zes b. El motivo por el cual mi predicción fue incorrecta es que pensé que el formato aceptado era una cabeza con una cola, o sea que debía ser 'l'(v [b]), pero es incorrecto.

{Test 'l'(a a)}

Predicción: 'case'(6)

Ejecución: 'case'(1)

Es una lista que comienza con a, por el mismo motivo que el punto anterior me equivoqué en la predicción.

{Test 'l'(b b)}

Predicción 'case'(6)

Ejecución: 'case'(3)

No es una lista que comienza con a, luego tampoco es tupla, luego si es una lista con ambos elementos primero y segundo iguales.

{Test 'l'(a b c)}

Predicción 'case'(6)

Ejecución: 'case'(6)

Al tener 3 elementos no coincide con una lista iniciando con a, luego no es tupla ni lista con ambos elementos iguales, tampoco es lista en la 4ta opcion, tampoco tupla llamada f, y queda como única opción el caso 6.

{Test 'l'(a [b c]}

Predicción: 'case'(1)

Ejecución: 'case'(1)

En este caso si crea con la cabeza y la cola la lista con 3 elementos que empiezan con a, por lo tanto coincide la primer condición.

Ejercicio 5) - Recursividad

1. Traducción al lenguaje Kernel

```
local Length in
    Length =  proc {$ Xs N}
            case Xs of nil then
                N = 0
            else
                case Xs of _|T then
                    local U in
                            {Length T U}
                            N = U + 1
                    end
                else
                    skip
                end
            end
          end
end
local K in
    {Length [1 2 3 4] K}
    {Show K}
end
```

2. "Tail Recursive"

```
local Length in
    Length = proc {$ Xs A N}
            case Xs of nil then
             N = A
            else
             case Xs of _|T then
                 local X in
                  X = A + 1
                  {Length T X N}

                 end
            else
                skip
```

```
              end
            end

          end
 end

local K in
    {Length [1 2 3 4] 0 K}
    {Show K}
end
```

En el primer caso no es la llamada recursiva lo último que se ejecuta, entonces voy a tener las operaciones que siguen acumuladas en el stack y hasta que no se termine la invocación de la última llamada recursiva no voy a poder liberar el stack. Al hacerlo tail recursive no tengo en el stack operaciones pendientes, el cual me queda claramente más pequeño. Este es el motivo por el cual siempre debemos tratar de hacer la invocación a la recursividad al final. Esto se verá claramente en el punto 3.

3. Ejecución en la máquina abstracta

Implementación básica

Estado inicial

Stack	Store	E

<pre>local Length in
    Length = proc {$ Xs N}
            case Xs of nil then
                N = 0
            else
                case Xs of _|T then
                    local U in
                        {Length T U}
                        N = U + 1
                    end
                else
                    skip
                end
            end
        end
end
local K in
    {Length [1 2 3 4] K}
    {Show K}</pre>
	-	-

end		

=> **Declaración de variable**

Stack	Store	E
| ```
Length =  proc {$ Xs N}
     case Xs of nil then
         N = 0
     else
         case Xs of _|T then
             local U in
                    {Length T U}
                    N = U + 1
             end
         else
             skip
         end
     end
end
local K in
    {Length [1 2 3 4] K}
    {Show K}
end
``` | length | **length -> Length** |

=> **Asignación de procedure value**

Stack	Store	E
| ```
local K in
    {Length [1 2 3 4]
K}
    {Show K}
end
``` | length = (proc {$ Xs N}<br>    case Xs of nil then<br>      N = 0<br>    else<br>      case Xs of _|T then<br>        local U in<br>              {Length T U}<br>              N = U + 1<br>        end<br>      else<br>        skip<br>      end<br>    end<br>end, CE = {}) | length -> Length |

=> **Declaración variable K**

Stack	Store	E
| ```
{Length [1 2 3 4] K}
{Show K}
``` | length = (proc {$ Xs N}<br>    case Xs of nil then<br>      N = 0 | **k-> K** |

| | ```
            else
                case Xs of _|T then
                    local U in
                                {Length T U}
                                N = U + 1
                        end
                    else
                        skip
                    end
                end
end, CE = {})
``` **k** | |

=> **Ejecución de procedure**

Stack	Store	E

case Xs of nil then
          N = 0
else
    case Xs of _|T then
        local U in
            {Length T U}
            N = U + 1
        end
    else
        skip
    end
end
{Show K}
	length = (proc {$ Xs N}
	    case Xs of nil then
	      N = 0
	    else
	      case Xs of _|T then
	        local U in
	            {Length T U}
	            N = U + 1
	        end
	      else
	        skip
	      end
	    end
	end, *)
	k
	
	    Store* / **CE***
	    xs = [1 2 3 4] / xs -> Xs
	    n = / n -> K
		k-> K

=> **Ejecución de case**

Stack	Store	E

case Xs of _|T then
    local U in
        {Length T U}
        N = U + 1
    end
else
    skip
end
{Show K}
	length = (proc {$ Xs N}
	    case Xs of nil then
	      N = 0
	    else
	      case Xs of _|T then
	        local U in
	            {Length T U}
	            N = U + 1
	        end
	      else
	        skip
	      end
	    end
	end, *)
		k-> K

	k	
		Store*	CE*
	xs = [1 2 3 4] n =	xs -> Xs n -> K

=> Ejecución de case

Stack	Store	E

local U in
    {Length T U}
    N = U + 1
end
{Show K}
	length = (proc {$ Xs N}
	        case Xs of nil then
	            N = 0
	        else
	            case Xs of _|T then
	                local U in
	                        {Length T U}
	                        N = U + 1
	                end
	            else
	                skip
	            end
	        end
	end, *)
	k
		k-> K

En el Store aparece la tabla:

Store*	CE*
xs = [1 2 3 4] n = **t = [2 3 4]**	xs -> Xs n -> K t -> T

=> Declaración de U

Stack	Store	E

{Length T U}
N = U + 1
{Show K}
	length = (proc {$ Xs N}
	        case Xs of nil then
	            N = 0
	        else
	            case Xs of _|T then
	                local U in
	                        {Length T U}
	                        N = U + 1
	                end
	            else
	                skip
	            end
	        end
	end, *)
	k
		k-> K

	Store*	CE*
	xs = [1 2 3 4] n = t = [2 3 4] **u =**	n -> K t -> T **u->U**

=> **Ejecución de Length**

Stack	Store	E
| ```
case Xs of nil then
        N = 0
    else
        case Xs of _|T then
            local U in
                {Length T U}
                N = U + 1
            end
        else
            skip
        end
    end
N = U + 1
{Show K}
``` | length = (proc {$ Xs N}<br>    case Xs of nil then<br>      N = 0<br>    else<br>      case Xs of _\|T then<br>        local U in<br>          {Length T U}<br>          N = U + 1<br>        end<br>      else<br>        skip<br>      end<br>    end<br>end, *)<br>k<br><br>**Store\*** / **CE\*\***:<br>xs = [1 2 3 4] — **xs' -> Xs**<br>n = — **n' -> N**<br>t = [2 3 4] — t -> T<br>u = — u->U<br>**xs'=[2 3 4]**<br>**n'=** | k-> K |

Store table inside:

Store*	CE**
xs = [1 2 3 4] n = t = [2 3 4] u = **xs'=[2 3 4]** **n'=**	**xs' -> Xs** **n' -> N** t -> T u->U

=> **Ejecución de case**

Stack	Store	E
| ```
case Xs of _|T then
     local U in
            {Length T U}
            N = U + 1
     end
else
     skip
end
``` | length = (proc {$ Xs N}<br>    case Xs of nil then<br>      N = 0<br>    else<br>      case Xs of _\|T then<br>        local U in<br>          {Length T U}<br>          N = U + 1<br>        end<br>      else<br>        skip | k-> K |

N = U + 1 {Show K}	end 　　　end end, *) k | Store*	CE** | |---|---|
xs = [1 2 3 4] n = t = [2 3 4] u = **xs'=[2 3 4]** **n'=**	**xs' -> Xs** **n' -> N** t -> T u->U		

=> **Ejecución de case**

Stack	Store	E
local U in 　　　**{Length T U}** 　　　**N = U + 1** **end** N = U + 1 {Show K}	length = (proc {$ Xs N} 　　　case Xs of nil then 　　　　　N = 0 　　　else 　　　　　case Xs of _|T then 　　　　　　　local U in 　　　　　　　　　　{Length T U} 　　　　　　　　　　　N = U + 1 　　　　　　　end 　　　　　else 　　　　　　　skip 　　　　　end 　　　end end, *) k | Store*	CE** | |---|---|
xs = [1 2 3 4] n = t = [2 3 4] u = xs'=[2 3 4] n'= **t'=[3 4]**	xs' -> Xs n' -> N **t' -> T** u->U		k-> K

=> **Declaración de U**

Stack	Store	E
{Length T U} **N = U + 1**	length = (proc {$ Xs N} 　　　case Xs of nil then 　　　　　N = 0	k-> K

N = U + 1
{Show K}
	``
	        else
	            case Xs of _|T then
	                local U in
	                        {Length T U}
	                        N = U + 1
	                end
	            else
	                skip
	            end
	        end
	end, *)
	k```	

Store*	CE**
xs = [1 2 3 4] n = t = [2 3 4] u = xs'=[2 3 4] n'= t'=[3 4] **u'=**	xs' -> Xs n' -> N t' -> T **u'->U**

=> **Ejecución de Length**

Stack	Store	E

case Xs of nil then
**   N = 0**
else
**   case Xs of _|T then**
**   local U in**
**   {Length T U}**
**   N = U + 1**
**   end**
**   else**
**   skip**
**   end**
end
N = U + 1
N = U + 1
{Show K}
	length = (proc {$ Xs N}
	``
	        case Xs of nil then
	            N = 0
	        else
	            case Xs of _|T then
	                local U in
	                        {Length T U}
	                        N = U + 1
	                end
	            else
	                skip
	            end
	        end
	end, *)
	k```
		k-> K

Store*	CE***
xs = [1 2 3 4] n = t = [2 3 4] u = xs'=[2 3 4] n'= t'=[3 4]	**xs" -> Xs** **n" -> N** t' -> T u'->U

	u'= **xs" = [3 4]** **n" =**	

=> Ejecución de case

Stack	Store	E
| ```
case Xs of _|T then
      local U in
            {Length T U}
            N = U + 1
      end
else
      skip
end
N = U + 1
N = U + 1
{Show K}
``` | length = (proc {$ Xs N} <br>       case Xs of nil then <br>          N = 0 <br>       else <br>          case Xs of _\|T then <br>            local U in <br>                {Length T U} <br>                N = U + 1 <br>            end <br>          else <br>            skip <br>          end <br>       end <br> end, *) <br> k <br><br> | <table><tr><td>Store*</td><td>CE***</td></tr><tr><td>xs = [1 2 3 4]<br>n =<br>t = [2 3 4]<br>u =<br>xs'=[2 3 4]<br>n'=<br>t'=[3 4]<br>u'=<br>**xs" = [3 4]**<br>**n" =**</td><td>**xs" -> Xs**<br>**n" -> N**<br>t' -> T<br>u'->U</td></tr></table> | k-> K |

=> Ejecución de case

Stack	Store	E
| ```
local U in
      {Length T U}
      N = U + 1
end
N = U + 1
N = U + 1
{Show K}
``` | length = (proc {$ Xs N} <br>       case Xs of nil then <br>          N = 0 <br>       else <br>          case Xs of _\|T then <br>            local U in <br>                {Length T U} <br>                N = U + 1 <br>             end <br>          else | k-> K |

<table>
<tr><td></td><td colspan="2">

```
           skip
        end
      end
end, *)
k
```

</td><td></td></tr>
<tr><td></td><td colspan="2">

Store*	CE***
xs = [1 2 3 4] n = t = [2 3 4] u = xs'=[2 3 4] n'= t'=[3 4] u'= xs'' = [3 4] n'' = **t'' = [4]**	xs'' -> Xs n'' -> N **t'' -> T** u'->U

</td><td></td></tr>
</table>

=> **Declaración de variable U**

<table>
<tr><th>Stack</th><th>Store</th><th>E</th></tr>
<tr>
<td>

{Length T U}
N = U + 1
N = U + 1
N = U + 1
{Show K}

</td>
<td>

```
length = (proc {$ Xs N}
          case Xs of nil then
              N = 0
          else
              case Xs of _|T then
                  local U in
                          {Length T U}
                          N = U + 1
                  end
              else
                  skip
              end
          end
end, *)
k
```

Store*	CE***
xs = [1 2 3 4] n = t = [2 3 4] u = xs'=[2 3 4] n'= t'=[3 4] u'= xs'' = [3 4]	xs'' -> Xs n'' -> N t'' -> T **u''->U**

</td>
<td>

k-> K

</td>
</tr>
</table>

	n'' = t'' = [4] **u'' =**	

=> **Ejecución de Length**

Stack	Store	E
| ```
case Xs of nil then
        N = 0
else
    case Xs of _|T then
        local U in
            {Length T U}
            N = U + 1
        end
    else
        skip
    end
end
N = U + 1
N = U + 1
N = U + 1
{Show K}
``` | length = (proc {$ Xs N}<br>　　case Xs of nil then<br>　　　N = 0<br>　　else<br>　　　case Xs of _\|T then<br>　　　　local U in<br>　　　　　　{Length T U}<br>　　　　　　N = U + 1<br>　　　　end<br>　　　else<br>　　　　skip<br>　　　end<br>　　end<br>end, *)<br>k<br><br>| Store* | CE**** |<br>\|---\|---\|<br>| xs = [1 2 3 4]<br>n =<br>t = [2 3 4]<br>u =<br>xs'=[2 3 4]<br>n'=<br>t'=[3 4]<br>u'=<br>xs'' = [3 4]<br>n'' =<br>t'' = [4]<br>u'' =<br>**xs'''= [4]**<br>**n'''=** | **xs'''-> Xs**<br>**n''' -> N**<br>t'' -> T<br>u''->U | | k-> K |

=> **Ejecución de case**

Stack	Store	E
| ```
case Xs of _|T then
    local U in
        {Length T U}
``` | length = (proc {$ Xs N}<br>　　case Xs of nil then<br>　　　N = 0<br>　　else | k-> K |

``
        N = U + 1
      end
else
      skip
end
N = U + 1
N = U + 1
N = U + 1
{Show K}
``
	``
	        case Xs of _|T then
	            local U in
	                    {Length T U}
	                    N = U + 1
	            end
	        else
	            skip
	        end
	    end
	end, *)
	k
	``	

Store*	CE****
xs = [1 2 3 4] n = t = [2 3 4] u = xs'=[2 3 4] n'= t'=[3 4] u'= xs'' = [3 4] n'' = t'' = [4] u'' = xs'''= [4] n'''=	xs'''-> Xs n''' -> N t'' -> T u''->U

=> **Ejecución de case**

Stack	Store	E

``
local U in
      {Length T U}
      N = U + 1
end
N = U + 1
N = U + 1
N = U + 1
{Show K}
``
	length = (proc {$ Xs N}
	       case Xs of nil then
	          N = 0
	       else
	          case Xs of _|T then
	             local U in
	                 {Length T U}
	                 N = U + 1
	             end
	          else
	            skip
	          end
	       end
	end, *)
	k
		k-> K

Store*	CE****
xs = [1 2 3 4]	xs'''-> Xs

n = t = [2 3 4] u = xs'=[2 3 4] n'= t'=[3 4] u'= xs'' = [3 4] n'' = t'' = [4] u'' = xs'''= [4] n'''= t''' = nil	n''' -> N **t''' -> T** u''->U

=> **Declaración variable U**

Stack	Store	E

{Length T U}
N = U + 1
N = U + 1
N = U + 1
N = U + 1
{Show K}
	length = (proc {$ Xs N}
	    case Xs of nil then
	      N = 0
	    else
	      case Xs of _|T then
	        local U in
	          {Length T U}
	          N = U + 1
	        end
	      else
	        skip
	      end
	    end
	end, *)
	k
	
	Store* / **CE******
	xs = [1 2 3 4] — xs'''-> Xs
	n = — n''' -> N
	t = [2 3 4] — **t''' -> T**
	u = — **u'''->U**
	xs'=[2 3 4]
	n'=
	t'=[3 4]
	u'=
	xs'' = [3 4]
	n'' =
	t'' = [4]
		k-> K

	u'' = xs'''= [4] n'''= t''' = nil u''' =	

=> Ejecución Length

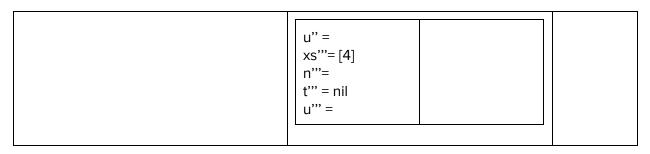| Stack	Store	E

case Xs of nil then
      N = 0
else
  case Xs of _|T then
     local U in
        {Length T U}
        N = U + 1
     end
  else
     skip
  end
end
N = U + 1
N = U + 1
N = U + 1
N = U + 1
{Show K}
	length = (proc {$ Xs N}
	    case Xs of nil then
	      N = 0
	    else
	      case Xs of _|T then
	        local U in
	          {Length T U}
	          N = U + 1
	        end
	      else
	        skip
	      end
	    end
	end, *)
	k
	
	Store* — **CE******
	xs = [1 2 3 4] — **xs''''-> Xs**
	n = — **n'''' -> N**
	t = [2 3 4] — t''' -> T
	u = — u'''->U
	xs'=[2 3 4]
	n'=
	t'=[3 4]
	u'=
	xs'' = [3 4]
	n'' =
	t'' = [4]
	u'' =
	xs'''= [4]
	n'''=
	t''' = nil
	u''' =
	xs''''= nil
	n''''=
		k-> K

=> Ejecución case

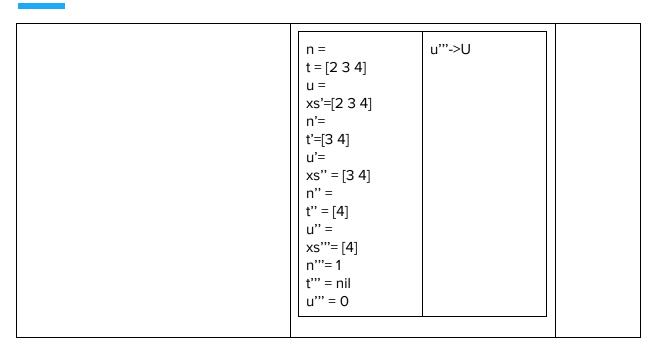| Stack	Store	E

N = 0
N = U + 1
N = U + 1
N = U + 1
N = U + 1
{Show K}
	length = (proc {$ Xs N}
	    case Xs of nil then
	      N = 0
	    else
	      case Xs of _|T then
	        local U in
	          {Length T U}
	          N = U + 1
	        end
	      else
	        skip
	      end
	    end
	end, *)
	k
	
	Store* · CE**** (see sub-table below)
		k-> K

Store*	CE****
xs = [1 2 3 4] n = t = [2 3 4] u = xs'=[2 3 4] n'= t'=[3 4] u'= xs'' = [3 4] n'' = t'' = [4] u'' = xs'''= [4] n'''= t''' = nil u''' = xs''''= nil n''''=	xs''''-> Xs n'''' -> N t''' -> T u'''->U

=> **Ejecución asignación valor**

Stack	Store	E

N = U + 1
N = U + 1
N = U + 1
N = U + 1
{Show K}
	length = (proc {$ Xs N}
	    case Xs of nil then
	      N = 0
	    else
	      case Xs of _|T then
	        local U in
	          {Length T U}
	          N = U + 1
	        end
		k-> K

<table>
<tr><td></td><td>

```
        else
            skip
        end
    end
end, *)
k
```
</td><td></td></tr>
</table>

Store*	CE****
xs = [1 2 3 4] n = t = [2 3 4] u = xs'=[2 3 4] n'= t'=[3 4] u'= xs'' = [3 4] n'' = t'' = [4] u'' = xs'''= [4] n'''= t''' = nil u''' = xs''''= nil **n''''= 0**	xs''''-> Xs n'''' -> N t''' -> T u'''->U

=> **Ejecución asignación valor**

Stack	Store	E
| ```
N = U + 1
N = U + 1
N = U + 1
{Show K}
``` | ```
length = (proc {$ Xs N}
        case Xs of nil then
            N = 0
        else
            case Xs of _|T then
                local U in
                        {Length T U}
                        N = U + 1
                end
            else
                skip
            end
        end
end, *)
k
``` | k-> K |

Store*	CE***
xs = [1 2 3 4]	n''' -> N

Stack	Store	E
	n = t = [2 3 4] u = xs'=[2 3 4] n'= t'=[3 4] u'= xs'' = [3 4] n'' = t'' = [4] u'' = xs'''= [4] n'''= 1 t''' = nil u''' = 0	u'''->U

=> **Ejecución asignación valor**

Stack	Store	E

N = U + 1
 N = U + 1
 {Show K}
	length = (proc {$ Xs N}
	      case Xs of nil then
	        N = 0
	      else
	        case Xs of _|T then
	          local U in
	              {Length T U}
	              N = U + 1
	          end
	        else
	          skip
	        end
	      end
	end, *)
	k
	
	 Store* / **CE**** table:
	 xs = [1 2 3 4] n'' -> N
	 n = u''->U
	 t = [2 3 4]
	 u =
	 xs'=[2 3 4]
	 n'=
	 t'=[3 4]
	 u'=
	 xs'' = [3 4]
	 n'' = 2
		k-> K

	t'' = [4] u'' = 1		

=> Ejecución asignación valor

Stack	Store	E

N = U + 1
{Show K}
	length = (proc {$ Xs N}
	    case Xs of nil then
	      N = 0
	    else
	      case Xs of _|T then
	        local U in
	            {Length T U}
	            N = U + 1
	        end
	      else
	        skip
	      end
	    end
	end, *)
	k
	
	Store* / _CE*_:
	xs = [1 2 3 4] n' -> N
	n = u'->U
	t = [2 3 4]
	u =
	xs'=[2 3 4]
	n'= 3
	t'=[3 4]
	u'= 2
		k-> K

=> Ejecución asignación valor

Stack	Store	E

{Show K}	length = (proc {$ Xs N}
	    case Xs of nil then
	      N = 0
	    else
	      case Xs of _|T then
	        local U in
	            {Length T U}
	            N = U + 1
	        end
	      else
	        skip
	      end
	    end
	end, *)
		k-> K

	k = 4		
	Store*	CE	
	xs = [1 2 3 4] n = 4 t = [2 3 4] u = 3	n -> N u->U	

=> **Ejecución de show, muestra un 4**

Stack	Store	E

	length = (proc {$ Xs N}
	      case Xs of nil then
	        N = 0
	      else
	        case Xs of _|T then
	          local U in
	                {Length T U}
	                N = U + 1
	          end
	        else
	          skip
	        end
	      end
	end, *)
	k = 4
		k-> K

Implementación Tail Recursive

Estado inicial

Stack	Store	E
| ```
local Length in
    Length = proc {$ Xs A N}
            case Xs of nil then
             N = A
            else
             case Xs of _|T then
                local X in
                 X = A + 1
                 {Length T X N}

                end
             else
                skip
             end
            end
``` | - | - |

| ```
        end
end

local K in
    {Length [1 2 3 4] 0 K}
    {Show K}
end
``` | | |

=> **Declaración de variable**

Stack	Store	E
| ```
Length = proc {$ Xs A N}
      case Xs of nil then
            N = A
      else
            case Xs of _|T then
                 local X in
                       X = A + 1
                       {Length T X N}
                 end
            else
                 skip
            end
      end
end

local K in
    {Length [1 2 3 4] 0 K}
    {Show K}
end
``` | **length =** | **Length ->length** |

=> **Asignación procedure value**

Stack	Store	E
| ```
local K in
    {Length [1 2 3 4] 0
K}
    {Show K}
end
``` | length =**{proc {$ Xs A N}**<br>**case Xs of nil then**<br>**N = A**<br>**else**<br>**case Xs of _\|T then**<br>**local X in**<br>**X = A + 1**<br>**{Length T X N}**<br>**end**<br>**else**<br>**skip**<br>**end**<br>**end, CE={}}** | Length ->length |

=> **Declaración variable K**

Stack	Store	E

{Length [1 2 3 4] 0 K}
{Show K}
	length =_{{proc {$ Xs A N}}
	 case Xs of nil then
	      N = A
	 else
	      case Xs of _|T then
	          local X in
	             X = A + 1
	             {Length T X N}
	          end
	      else
	         skip
	      end
	 end, CE={}}
	K=
		Length ->length
		K -> k

=> **Ejecución de Length**

Stack	Store	E

case Xs of nil then
      N = A
else
      case Xs of _|T then
          local X in
             X = A + 1
             {Length T X N}
        end
      else
        skip
      end
 end
{Show K}
	length =_{{proc {$ Xs A N}}
	 case Xs of nil then
	      N = A
	 else
	      case Xs of _|T then
	          local X in
	             X = A + 1
	             {Length T X N}
	        end
	      else
	        skip
	      end
	 end, *}
	K=
	
	| Store*
		CE |
		|---|---|

xs=[1 2 3 4] a =0 n= k =	Xs -> xs A -> a N->n K->k		Length ->length K -> k

=> **Ejecución de case**

Stack	Store	E

case Xs of _|T then
      local X in
          X = A + 1
          {Length T X N}
	length =_{{proc {$ Xs A N}}
	 case Xs of nil then
	      N = A
	 else
		Length ->length
		K -> k

| ```
     end
else
       skip
end
{Show K}
``` | ```
       case Xs of _|T then
               local X in
                       X = A + 1
                       {Length T X N}
              end
        else
               skip
        end
 end, *}
K=
``` <br><br> | Store\* | CE |<br>|---|---|<br>| xs=[1 2 3 4]<br>a =0<br>n=<br>k = | Xs -> xs<br>A -> a<br>N->n<br>K->k | | |

=> **Ejecución de case**

Stack	Store	E
| ```
local X in
       X = A + 1
       {Length T X N}
end
{Show K}
``` | length =(proc {$ Xs A N} <br>```
 case Xs of nil then
        N = A
 else
        case Xs of _|T then
                local X in
                        X = A + 1
                        {Length T X N}
               end
        else
                skip
        end
 end, *}
K=
``` <br><br> | Store\* | CE |<br>|---|---|<br>| xs=[1 2 3 4]<br>a =0<br>n=<br>k =<br>**t=[2 3 4]** | Xs -> xs<br>A -> a<br>N->n<br>K->k<br>**T->t** | Length ->length<br>K -> k |

=> **Declaración de variable local X**

Stack	Store	E

`X = A + 1`
`{Length T X N}`
{Show K}
	length =`{proc {$ Xs A N}`
	` case Xs of nil then`
	`        N = A`
	` else`
	`        case Xs of _|T then`
	`                local X in`
	`                      X = A + 1`
	`                      {Length T X N}`
	`              end`
	`        else`
	`                skip`
	`        end`
	` end, *}`
	K=
		Length ->length
		K -> k

Store*	CE
xs=[1 2 3 4] a =0 n= k = t=[2 3 4] **x=**	Xs -> xs A -> a N->n K->k T->t **X->x**

=> **Asignación de valor**

Stack	Store	E

`{Length T X N}`
{Show K}
	length =`{proc {$ Xs A N}`
	` case Xs of nil then`
	`        N = A`
	` else`
	`        case Xs of _|T then`
	`                local X in`
	`                      X = A + 1`
	`                      {Length T X N}`
	`              end`
	`        else`
	`                skip`
	`        end`
	` end, *}`
	K=
		Length ->length
		K -> k

Store*	CE
xs=[1 2 3 4] a =0 n= k = t=[2 3 4]	Xs -> xs A -> a N->n K->k T->t

	x=1	X->x	

=> Ejecución de Length

Stack	Store	E
| ```
case Xs of nil then
        N = A
else
        case Xs of _|T then
                local X in
                        X = A + 1
                        {Length T X N}
                end
        else
                skip
        end
 end
{Show K}
``` | length =<sub>{proc {$ Xs A N}</sub><br>```
 case Xs of nil then
        N = A
 else
        case Xs of _|T then
                local X in
                        X = A + 1
                        {Length T X N}
                end
        else
                skip
        end
 end, *}
``` K= | Length ->length<br>K -> k |

length ={proc {$ Xs A N}
```
 case Xs of nil then
        N = A
 else
        case Xs of _|T then
                local X in
                        X = A + 1
                        {Length T X N}
                end
        else
                skip
        end
 end, *}
```
K=

Store*	CE*
xs=[1 2 3 4] a =0 n= k = t=[2 3 4] x=1 **xs'=[2 3 4]** **a'=1** **n'=**	**Xs -> xs'** **A -> a'** **N->n'** K->k T->t X->x

=> Ejecución de case

Stack	Store	E
| ```
case Xs of _|T then
        local X in
                X = A + 1
                {Length T X N}
        end
else
        skip
end
Show K}
``` | length =<sub>{proc {$ Xs A N}</sub><br>```
 case Xs of nil then
        N = A
 else
        case Xs of _|T then
                local X in
                        X = A + 1
                        {Length T X N}
                end
        else
                skip
        end
 end, *}
``` | Length ->length<br>K -> k |

	K=	

Store*	CE*
xs=[1 2 3 4] a =0 n= k = t=[2 3 4] x=1 **xs'=[2 3 4]** **a'=1** **n'=**	**Xs -> xs'** **A -> a'** **N->n'** K->k T->t X->x

=> Ejecución de case

Stack	Store	E
| ```
local X in
      X = A + 1
      {Length T X N}
end
``` <br>{Show K} | length =₍proc {$ Xs A N}<br> case Xs of nil then<br>        N = A<br> else<br>        case Xs of _\|T then<br>                local X in<br>                        X = A + 1<br>                        {Length T X N}<br>                end<br>        else<br>                skip<br>        end<br> end, *}<br>K= | Length ->length<br>K -> k |

Store*	CE*
xs=[1 2 3 4] a =0 n= k = t=[2 3 4] x=1 xs'=[2 3 4] a'=1 n'= **t'=[3 4]**	Xs -> xs' A -> a' N->n' K->k **T->t'** X->x

=> **Declaración de X**

Stack	Store	E

`X = A + 1`
`{Length T X N}`
{Show K}
	length =`{proc {$ Xs A N}`
	` case Xs of nil then`
	`        N = A`
	` else`
	`        case Xs of _|T then`
	`                local X in`
	`                        X = A + 1`
	`                        {Length T X N}`
	`            end`
	`        else`
	`                skip`
	`        end`
	` end, *}`
	K= <table><tr><td>Store*</td><td>CE*</td></tr><tr><td>xs=[1 2 3 4]
	a =0
	n=
	k =
	t=[2 3 4]
	x=1
	xs'=[2 3 4]
	a'=1
	n'=
	t'=[3 4]
	x'=</td><td>Xs -> xs'
	A -> a'
	N->n'
	K->k
	T->t'
	X->x'</td></tr></table>
		Length ->length
		K -> k

=> **Asignación de valor**

Stack	Store	E

`{Length T X N}`
{Show K}
	length =`{proc {$ Xs A N}`
	` case Xs of nil then`
	`        N = A`
	` else`
	`        case Xs of _|T then`
	`                local X in`
	`                        X = A + 1`
	`                        {Length T X N}`
	`            end`
	`        else`
	`                skip`
	`        end`
	` end, *}`
	K=
		Length ->length
		K -> k

Store*	CE*
xs=[1 2 3 4] a =0 n= k = t=[2 3 4] x=1 xs'=[2 3 4] a'=1 n'= t'=[3 4] **x'= 2**	Xs -> xs' A -> a' N->n' K->k T->t' X->x'

=> **Ejecución de Length**

Stack	Store	E
| ```
case Xs of nil then
        N = A
else
        case Xs of _|T then
                local X in
                        X = A + 1
                        {Length T X N}
            end
        else
                skip
        end
 end
{Show K}
``` | `length =`{proc {$ Xs A N}<br>`case Xs of nil then`<br>`        N = A`<br>` else`<br>`        case Xs of _|T then`<br>`                local X in`<br>`                        X = A + 1`<br>`                        {Length T X N}`<br>`                end`<br>`        else`<br>`                skip`<br>`        end`<br>` end, *}`<br>`K=` | Length ->length<br>K -> k |

Store*	CE**
xs=[1 2 3 4] a =0 n= k = t=[2 3 4] x=1 xs'=[2 3 4] a'=1 n'= t'=[3 4] x'= 2	**Xs -> xs"** **A -> a"** **N->n"** K->k T->t' X->x'

	xs"=[3 4] **a"=2** **n"=**		

=> **Ejecución de case**

Stack	Store	E
| ```
case Xs of _|T then
        local X in
                X = A + 1
                {Length T X N}
        end
else
        skip
end
{Show K}
``` | length ={proc {$ Xs A N}<br> case Xs of nil then<br>　　　N = A<br> else<br>　　　case Xs of _\|T then<br>　　　　　local X in<br>　　　　　　　X = A + 1<br>　　　　　　　{Length T X N}<br>　　　　　end<br>　　　else<br>　　　　　skip<br>　　　end<br> end, *}<br>K=<br><br>Store* / CE** table below | Length ->length<br>K -> k |

Store*	CE**
xs=[1 2 3 4] a =0 n= k = t=[2 3 4] x=1 xs'=[2 3 4] a'=1 n'= t'=[3 4] x'= 2 xs''=[3 4] a''=2 n''=	Xs -> xs'' A -> a'' N->n'' K->k T->t' X->x'

=> **Ejecución de case**

Stack	Store	E

| ```
local X in
        X = A + 1
        {Length T X N}
end
``` <br> {Show K} | length =<sub>{proc {$ Xs A N}</sub> <br> ```
 case Xs of nil then
        N = A
 else
        case Xs of _|T then
                local X in
                        X = A + 1
                        {Length T X N}
                end
        else
                skip
        end
 end, *}
``` <br> K= | Length ->length <br> K -> k |

length =_{{proc {$ Xs A N}}

```
 case Xs of nil then
        N = A
 else
        case Xs of _|T then
                local X in
                        X = A + 1
                        {Length T X N}
                end
        else
                skip
        end
 end, *}
```
K=

Store*	CE**
xs=[1 2 3 4] a =0 n= k = t=[2 3 4] x=1 xs'=[2 3 4] a'=1 n'= t'=[3 4] x'= 2 xs''=[3 4] a''=2 n''= **t''=[4**]	Xs -> xs'' A -> a'' N->n'' K->k **T->t''** X->x'

=> **Declaración de variable X**

Stack	Store	E
| ```
X = A + 1
{Length T X N}
``` <br> {Show K} | length =<sub>{proc {$ Xs A N}</sub> <br> ```
 case Xs of nil then
        N = A
 else
        case Xs of _|T then
                local X in
                        X = A + 1
                        {Length T X N}
                end
        else
                skip
        end
 end, *}
``` <br> K= | Length ->length <br> K -> k |

	Store*	**CE****
	xs=[1 2 3 4] a =0 n= k = t=[2 3 4] x=1 xs'=[2 3 4] a'=1 n'= t'=[3 4] x'= 2 xs''=[3 4] a''=2 n''= t''=[4] x''=	Xs -> xs'' A -> a'' N->n'' K->k T->t'' X->x''

=> **Asignación de valor**

Stack	Store	E

`{Length T X N}`
{Show K}
	length ={proc {$ Xs A N}
	 case Xs of nil then
	      N = A
	 else
	      case Xs of _|T then
	          local X in
	              X = A + 1
	              {Length T X N}
	          end
	      else
	          skip
	      end
	 end, *}
	K=
	
	Store* / **CE****
	xs=[1 2 3 4] / Xs -> xs''
	a =0 / A -> a''
	n= / N->n''
	k = / K->k
	t=[2 3 4] / T->t''
	x=1 / X->x''
		Length ->length
		K -> k

	xs'=[2 3 4] a'=1 n'= t'=[3 4] x'= 2 xs''=[3 4] a''=2 n''= t''=[4] **x''= 3**		

=> **Ejecución de Length**

Stack	Store	E
| ```
case Xs of nil then
        N = A
else
        case Xs of _|T then
                local X in
                        X = A + 1
                        {Length T X N}
                end
        else
                skip
        end
 end
{Show K}
``` | length =<sub>{proc {$ Xs A N}</sub><br> case Xs of nil then<br>　　　N = A<br> else<br>　　　case Xs of _\|T then<br>　　　　　local X in<br>　　　　　　　X = A + 1<br>　　　　　　　{Length T X N}<br>　　　　　end<br>　　　else<br>　　　　　skip<br>　　　end<br> end, *}<br>K= <br><br>| Store* | CE*** |<br>| --- | --- |<br>| xs=[1 2 3 4]<br>a =0<br>n=<br>k =<br>t=[2 3 4]<br>x=1<br>xs'=[2 3 4]<br>a'=1<br>n'=<br>t'=[3 4]<br>x'= 2<br>xs''=[3 4]<br>a''=2<br>n''=<br>t''=[4] | **Xs -> xs'''**<br>**A -> a'''**<br>**N->n'''**<br>K->k<br>T->t''<br>X->x'' | | Length ->length<br>K -> k |

	x"= 3 **xs'''=[4]** **a'''=3** **n'''=**	

=> Ejecución de Case

Stack	Store	E
| ```
case Xs of _|T then
        local X in
                X = A + 1
                {Length T X N}
      end
else
       skip
end
{Show K}
``` | length ={proc {$ Xs A N}<br> case Xs of nil then<br>        N = A<br> else<br>        case Xs of _\|T then<br>                local X in<br>                        X = A + 1<br>                        {Length T X N}<br>                end<br>        else<br>                skip<br>        end<br> end, *}<br>K=<br><br>| Store* | CE*** |<br>|---|---|<br>| xs=[1 2 3 4]<br>a =0<br>n=<br>k =<br>t=[2 3 4]<br>x=1<br>xs'=[2 3 4]<br>a'=1<br>n'=<br>t'=[3 4]<br>x'= 2<br>xs"=[3 4]<br>a"=2<br>n"=<br>t"=[4]<br>x"= 3<br>xs'''=[4]<br>a'''=3<br>n'''= | Xs -> xs'''<br>A -> a'''<br>N->n'''<br>K->k<br>T->t"<br>X->x" | | Length ->length<br>K -> k |

=> Ejecución de Case

Stack	Store	E
| ```
local X in
        X = A + 1
        {Length T X N}
end
{Show K}
``` | length =₍proc {$ Xs A N}<br> case Xs of nil then<br>          N = A<br> else<br>          case Xs of _\|T then<br>                  local X in<br>                          X = A + 1<br>                          {Length T X N}<br>                  end<br>          else<br>                  skip<br>          end<br> end, *₎<br>K=<br><br>\| Store* \| CE*** \|<br>\|---\|---\|<br>\| xs=[1 2 3 4]<br>a =0<br>n=<br>k =<br>t=[2 3 4]<br>x=1<br>xs'=[2 3 4]<br>a'=1<br>n'=<br>t'=[3 4]<br>x'= 2<br>xs''=[3 4]<br>a''=2<br>n''=<br>t''=[4]<br>x''= 3<br>xs'''=[4]<br>a'''=3<br>n'''=<br>**t'''=nil** \| Xs -> xs'''<br>A -> a'''<br>N->n'''<br>K->k<br>**T->t'''**<br>X->x''' \| | Length ->length<br>K -> k |

=> Declaración de variable X

Stack	Store	E
| ```
X = A + 1
{Length T X N}
{Show K}
``` | length =₍proc {$ Xs A N}<br> case Xs of nil then<br>          N = A | Length ->length<br>K -> k |

```
 else
        case Xs of _|T then
                local X in
                        X = A + 1
                        {Length T X N}
                end
        else
                skip
        end
 end, *}
K=
```

Store*	CE***
xs=[1 2 3 4] a =0 n= k = t=[2 3 4] x=1 xs'=[2 3 4] a'=1 n'= t'=[3 4] x'= 2 xs''=[3 4] a''=2 n''= t''=[4] x''= 3 xs'''=[4] a'''=3 n'''= t'''=nil x'''=	Xs -> xs''' A -> a''' N->n''' K->k T->t''' **X->x'''**

=> **Asignación de valor**

Stack	Store	E

`{Length T X N}`
{Show K}
	length =`{proc {$ Xs A N}`
	` case Xs of nil then`
	`        N = A`
	` else`
	`        case Xs of _|T then`
	`                local X in`
	`                        X = A + 1`
	`                        {Length T X N}`
	`                end`
	`        else`
		Length ->length
		K -> k

| | ```
              skip
          end
 end, *}
K=
``` | |
| | | |

K=

Store*	CE***
xs=[1 2 3 4] a =0 n= k = t=[2 3 4] x=1 xs'=[2 3 4] a'=1 n'= t'=[3 4] x'= 2 xs''=[3 4] a''=2 n''= t''=[4] x''= 3 xs'''=[4] a'''=3 n'''= t'''=nil **x'''=4**	Xs -> xs''' A -> a''' N->n''' K->k T->t''' X->x'''

=> **Ejecución de Length**

Stack	Store	E
| ```
 case Xs of nil then
        N = A
 else
        case Xs of _|T then
                local X in
                        X = A + 1
                        {Length T X N}
            end
        else
                skip
        end
 end
{Show K}
``` | ```
length ={proc {$ Xs A N}
 case Xs of nil then
        N = A
 else
        case Xs of _|T then
                local X in
                        X = A + 1
                        {Length T X N}
            end
        else
                skip
        end
 end, *}
K=
``` | Length ->length<br>K -> k |

	Store*	CE****	
	xs=[1 2 3 4] a =0 n= k = t=[2 3 4] x=1 xs'=[2 3 4] a'=1 n'= t'=[3 4] x'= 2 xs''=[3 4] a''=2 n''= t''=[4] x''= 3 xs'''=[4] a'''=3 n'''= t'''=nil x'''=4 **xs''''=nil** **a''''=4** **n''''=**	**Xs -> xs''''** **A -> a''''** **N->n''''** K->k T->t''' X->x'''	

=> **Ejecución de case**

Stack	Store	E

```N = A```
```{Show K}```
	length =_{{proc {$ Xs A N}}
	``` case Xs of nil then```
	``` N = A```
	``` else```
	``` case Xs of _|T then```
	``` local X in```
	``` X = A + 1```
	``` {Length T X N}```
	``` end```
	``` else```
	``` skip```
	``` end```
	``` end, *}```
	K=
		Length ->length
		K -> k

	Store*	CE****	

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| | xs=[1 2 3 4]
 a =0 <br> n=
 k =
 t=[2 3 4]
 x=1 <br> xs'=[2 3 4]
 a'=1 <br> n'=
 t'=[3 4]
 x'= 2 <br> xs''=[3 4]
 a''=2 <br> n''=
 t''=[4]
 x''= 3 <br> xs'''=[4]
 a'''=3 <br> n'''=
 t'''=nil <br> x'''=4 <br> xs''''=nil <br> a''''=4 <br> n''''= | Xs -> xs''''
 A -> a''''
 N->n''''
 K->k
 T->t'''
 X->x''' | |

=> **Asignación de valor**

Stack	Store	E

{Show K}	length =_{{proc {$ Xs A N}}
	 ` case Xs of nil then`
	 `        N = A`
	 ` else`
	 `        case Xs of _|T then`
	 `                local X in`
	 `                        X = A + 1`
	 `                        {Length T X N}`
	 `                end`
	 `        else`
	 `                skip`
	 `        end`
	 ` end, *}`
	 K=4
	
	 <table><tr><td>Store*</td><td>CE****</td></tr><tr><td>xs=[1 2 3 4]</td><td>Xs -> xs''''</td></tr></table>
		Length ->length
		 K -> k

	a =0 n= **k =4** t=[2 3 4] x=1 xs'=[2 3 4] a'=1 **n'=4** t'=[3 4] x'= 2 xs''=[3 4] a''=2 **n''=4** t''=[4] x''= 3 xs'''=[4] a'''=3 **n'''=4** t'''=nil x'''=4 xs''''=nil a''''=4 **n''''=4**	A -> a'''' N->n'''' K->k T->t''' X->x'''

=> Ejecución de show, muestra un K=4 y finaliza la ejecución

Stack	Store	E

--	length ={proc {\$ Xs A N}
	 case Xs of nil then
	     N = A
	 else
	     case Xs of _|T then
	        local X in
	           X = A + 1
	           {Length T X N}
	       end
	     else
	       skip
	     end
	 end, *}
	K=4
		Length ->length
		K -> k

Ejercicio 6) - Alto orden con listas

FoldL

    a. Código Oz

```
% FoldL function
declare fun {FoldL L F U}
        case L of nil then U
        [] H|T then {F {FoldL T F U} H}
        end
     end
declare fun {Multiplica X Y}
        X * Y
     end
{Show {FoldL [2 2 3] Multiplica 1}}
```

    b. Ejemplo de ejecución

FoldR

a. Código Oz

```
% FoldR function
declare fun {FoldR L F U}
        case L of nil then U
        [] H|T then {F H {FoldR T F U}}
        end
     end
declare fun {Suma X Y}
        X + Y
     end
{Show {FoldR [1 2 3] Suma 0}}
```

b. Ejemplo de ejecución

Map

a. Código Oz

```
% Map function
declare fun {Map L F }
        case L of nil then nil
        [] H|T then {F H}|{Map T F}
        end
    end
declare fun {Potencia X}
        X * X
    end
{Show {Map [2 1 3 6] Potencia}}
```

b. Ejemplo de ejecución

Filter

a. Código Oz

```
% Filter function
declare fun {Filter L F}
        case L of nil then nil
        [] H|T then
            if {F H} then
             H|{Filter T F}
            else
             {Filter T F}
            end
        end
     end

declare fun {Condicion X}
        X > 2
     end
{Show {Filter [2 1 3 6] Condicion}}
```

b. Ejemplo de ejecución

Ejercicio 7) - Hilos

WaitSome

a. Código Oz

```
local WaitSome in
   WaitSome = proc {$ Xs}
           local Y in
               {ForAll Xs
                proc {$ X}
                 thread {Wait X}
                     Y = true
                     {Show 'Valor Bindeado:'}
                     {Show X}
                 end
```

```
                 end
                }
                {Show 'Esperando por algun valor a bindear'}
                {Wait Y}
                {Show 'Al menos uno fue bindeado'}

            end

          end
   {Show 'Primera lista los 3 valores bindeados'}
   {WaitSome [1 2 3]}
   {Show 'Segunda lista solo uno esta bindeado'}
   {WaitSome [_ 2 _]}
   {Show 'Tercera lista ninguno esta bindeado'}
   {WaitSome [_ _ _]}
end
```

b. Ejemplo de ejecución

Maquina abstracta

a. Código Oz

```
local A B C in
   thread
      if A then
       B=true
       {Show 'thread 1 A is true'}
      else
```

```
        B=false
        {Show 'thread 1 A is false'}
       end
   end
   thread
      if B then
       C=false
       {Show 'thread 2 B is true'}
      else
       C=true
       {Show 'thread 2 B is false'}
      end
   end
   A=false
end
```

b. Ejemplo de ejecución

Le agregué impresiones por pantalla para poder ver claramente el seguimiento del código. Vemos que se lanzan dos threads de ejecución, ambos comienzan con una sentencia if, la cual se suspende porque ni A ni B están definidos, entonces se suspende. En el momento de ejecutar A=false, el thread 1 se libera puesto que tiene asignado el valor de A y ejecuta la sentencia "B = false". En consecuencia, B está definido por lo que la ejecución del thread 2 puede continuar y evaluar el if, para finalmente asignar el valor C=true.

```
local A B C in
    thread
        if A then
            B=true
            {Show 'thread 1 A is true'}
        else
            B=false
            {Show 'thread 1 A is false'}
        end
    end
    thread
        if B then
            C=false
            {Show 'thread 2 B is true'}
        else
            C=true
            {Show 'thread 2 B is false'}
        end
    end
    A=false
```

```
'thread 1 A is false'
'thread 2 B is false'
```

Ejercicio 8) - Evaluación perezosa

8.1 Maquina Abstracta

a. Código Oz

```
local Ints in
    local L in
        local A in
```

```
       local B in
          local C in
             fun lazy {Ints N}
              {Show N}
              N|{Ints N+1}
             end
             {Show 'Comienzo'}
             L = {Ints 1}
             {Show 'Asignacion de L'}
             A = L.2.2.1
             {Show 'Asignacion de A usando L'}
             B = L.1
             {Show 'Asignacion de B usando L'}
             C = A+B
             {Show 'Asignacion de C'}
             {Show C}
          end
       end
      end
    end
end
```

b. Ejemplo de ejecución

8.2 Reverse

- La diferencia en comportamiento es que la función Rev al ser lazy en la segunda implementación, solo va a ser ejecutada, cuando realmente sea necesario y no antes. Lo que ocurre es que como a su vez se encuentra dentro de otra funcion lazy, tambien va a ser ejecutada cuando necesitemos los valores de la lista y eso va a ocurrir al mismo tiempo, la necesidad de ejecución de una, en este caso fuerza a la ejecución de la otra.

- Ambas funciones retornan el mismo resultado, recién se ejecutan la función recursiva al hacer uso de los elementos de la lista. A continuación un ejemplo de ejecución:

Codigo oz

```oz
local Reverse1 Reverse2 A B C in
   fun lazy {Reverse1 S}
      fun {Rev S R}
       case S of nil then
           {Show R}
           R

       [] X|S2 then
           {Show X}
           {Rev S2 X|R}

       end
      end
   in {Rev S nil} end

   fun lazy {Reverse2 S}
      fun lazy {Rev S R}
       case S of nil then
           {Show R}
           R

       [] X|S2 then
           {Show X}
           {Rev S2 X|R}

       end
      end
   in {Rev S nil} end
   {Show 'Comenzamos'}
   A = [a b c]
   {Show 'Antes de llamar reverse1'}
   B = {Reverse1 A}
   {Show 'Antes del Show B'}
 % {Show  {Reverse1 A}}
 % {Show A}
   {Show B}
   {Show 'Antes del case'}
   case B of K|_ then
      {Show K}
   end
   {Show 'Antes de llamar reverse2'}
```
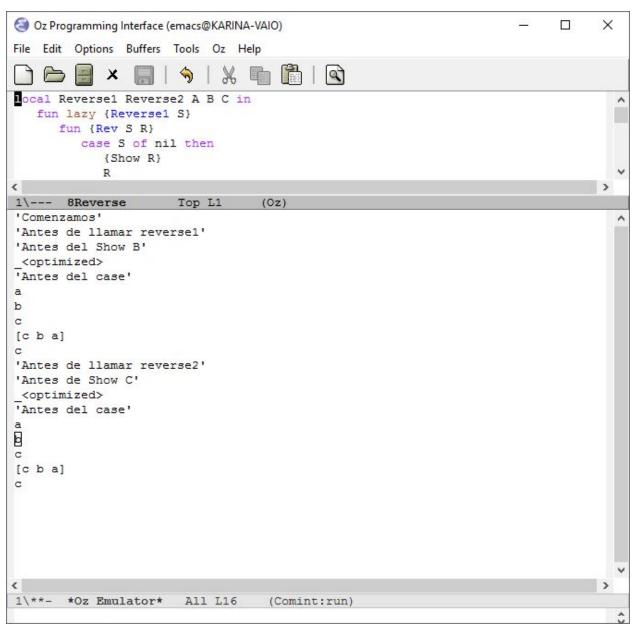
```
    C = {Reverse2 A}
    {Show 'Antes de Show C'}
    %{Show {Reverse2 A}}
    {Show C}
    {Show 'Antes del case'}
    case C of M|_ then
        {Show M}
    end
end
```