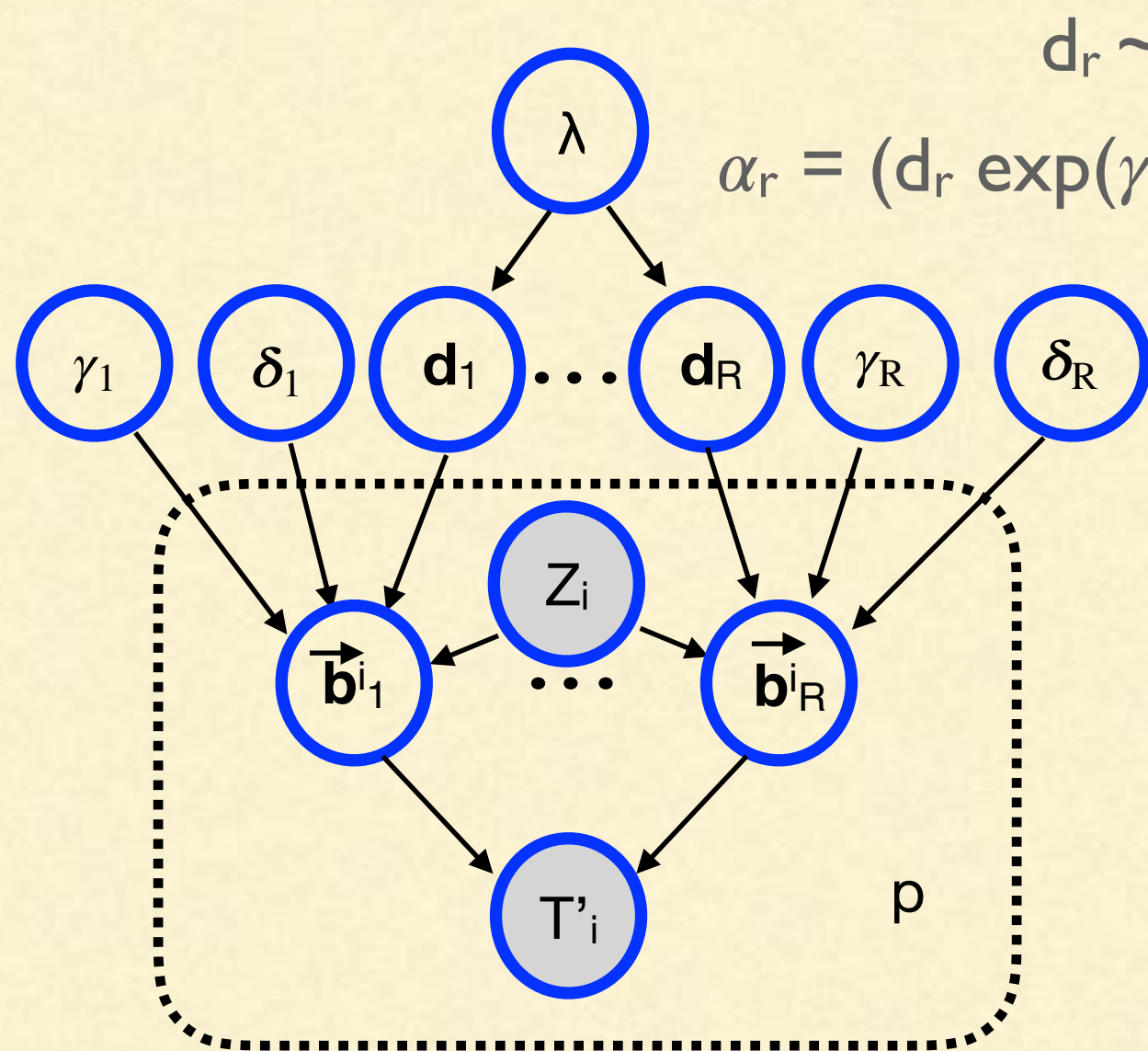


# WITH MORE CATEGORIES AND COVARIATES



$$d_r \sim \text{Exponential}(\lambda) \text{ i.i.d. } r = 1 \dots R$$

$$\alpha_r = (d_r \exp(\gamma_{r1} + \delta_{r1} Z_i), \dots, d_r \exp(\gamma_{rC-1} + \delta_{rC-1} Z_i), d_r)$$

$$r = 1, \dots, R$$

$$\mathbf{b}_r^i | \alpha_r \sim \text{Dirichlet}(\alpha_r) \text{ i.i.d.}$$

$$r = 1, \dots, R$$

$$\theta_{ic} = X_{i1}^i b_{1c}^{i_1} + X_{iR}^i b_{Rc}^{i_R}$$

$$c = 1, \dots, C$$

$$T'_{ic} \sim \text{Multinomial}(N_i, \theta_i)$$

Note:  $\log \mathbb{E}(b_{rc}^i) / (1 - (b_{rc}^i)) = \gamma_{rc} + \delta_{rc} Z_i$

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# A HIERARCHICAL BAYESIAN APPROACH - SIMULATION STUDY

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[demo modeling and fitting with pymc3]

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