Supplementary Table 1:

Equations governing the dynamics of the phosphorelay module

We assume mass conservation for the molecules of the three-component-system during the relevant time span. ATP is considered to be in excess and its concentration is included in the rate constant for phosphorylation of Sln1.

$$\frac{d}{dt}Sln1 = -v_1^{TCS} + v_2^{TCS} - Sln1 \cdot V_{ratio}$$
(1.1)

$$\frac{d}{dt}Sln1P = v_1^{TCS} - v_2^{TCS} - Sln1P \cdot V_{ratio}$$
(1.2)

$$\frac{d}{dt}Ypd1 = v_3^{TCS} - v_2^{TCS} - Ypd1 \cdot V_{ratio}$$
(1.3)

$$\frac{d}{dt}Ypd1P = v_2^{TCS} - v_3^{TCS} - Ypd1P \cdot V_{ratio}$$
(1.4)

$$\frac{d}{dt}Ssk1 = v_4^{TCS} - v_3^{TCS} - Ssk1 \cdot V_{ratio}$$
 (1.5)

$$\frac{d}{dt}Ssk1P = v_3^{TCS} - v_4^{TCS} - Ssk1P \cdot V_{ratio}$$
(1.6)

$$v_1^{TCS} = k_1^{TCS}(t) \cdot Sln1 \tag{1.7}$$

with
$$k_1^{TCS}(t) = k_1^{TCS,0} \cdot \left(\frac{\Pi_t(t)}{\Pi_t^0}\right)^{n_1}$$
 (compare with main text)

$$v_2^{TCS} = k_2^{TCS} \cdot Sln1P \cdot Ypd1 - k_{-2}^{TCS} \cdot Sln1 \cdot Ypd1P$$
 (1.8)

$$v_3^{TCS} = k_3^{TCS} \cdot Ssk1 \cdot Ypd1P \tag{1.9}$$

$$v_4^{TCS} = k_4^{TCS} \cdot Ssk1P \tag{1.10}$$

Conservation relations

$$Sln1_{tot} = Sln1^0 + Sln1P^0 (1.11)$$

$$Ypd1_{tot} = Ypd1^{0} + Ypd1P^{0} (1.12)$$

$$Ssk1_{tot} = Ssk1^{0} + Ssk1P^{0} (1.13)$$

$$k_1^{TCS,0} = 5 \,\mathrm{s}^{-1}$$
 $n_1 = 2$
 $k_2^{TCS} = 50 \,(\mu \mathrm{M} \cdot \mathrm{s})^{-1}$
 $k_{-2}^{TCS} = 50 \,(\mu \mathrm{M} \cdot \mathrm{s})^{-1}$
 $k_3^{TCS} = 50 \,(\mu \mathrm{M} \cdot \mathrm{s})^{-1}$
 $k_4^{TCS} = 0.415 \,\mathrm{s}^{-1}$

 $Sln1_{tot} = 0.016 \mu M$ (656 molecules per cell)¹

 $Ypd1_{tot} = 0.156 \mu M$ (6330 molecules per cell)¹

 $Ssk1_{tot} = 0.029 \mu M$ (1200 molecules per cell)¹

Numbers of molecules per cell are taken from the Yeast Localization Database¹ at http://yeastgfp.ucsf.edu/

Initial concentration values

$$Sln1P^0 = 2.25 \cdot 10^{-3} \, \mu M$$

$$Ypd1P^0 = 36 \cdot 10^{-3} \, \mu M$$

$$Ssk1P^0 = 1.88 \cdot 10^{-3} \, \mu M$$