

Programming Lab #8a

Arithmetic with Reals

Topics: Alternative representations of real numbers; floating-point hardware and emulation, Q16 fixed-point, posit emulation. Comparing relative performance.

Prerequisite Reading: Chapters 1-11

Revised: March 22, 2020

Background: Real numbers may be represented in floating-point¹, fixed-point², or posit³ format. Arithmetic using these representations may be implemented in hardware, or in software written in either a high-level language or assembly. This lab explores the relative performance of these alternatives by evaluating Taylor series approximations of the sine function – i.e., polynomials with coefficient (a_0, a_1, a_2, \cdots) chosen to produce $\sin(x)$:

$$poly(x) = a_0 + a_1 x^1 + a_2 x^2 + \dots + a_{n-1} x^{n-1}$$

The polynomial is most efficiently evaluated using Horner's method⁴, working backwards from a_{n-1} to a_0 :

$$poly(x) = (((0)x + a_{n-1})x + a_{n-2})x + \dots + a_0$$

Assignment: Create a single assembly language file containing five functions that each evaluate the polynomial

Function Min Avg Max
FPH Poly 5 40 60
Q16 Poly 5 50 76
FPA Poly 16 290 471
POS Poly 23 706 1237
FPC Poly 16 670 1116

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shown above. The five function prototypes share a common format, but the *function-name* and *data-type* vary. (*Note: The code for each of the last three functions should be almost identical.*)

data-type function-name(data-type x, data-type a[], int32_t n);

function-name	data-type	same as	Implement this function in assembly using
FPH_Poly	float	float	floating-point addition & multiply instructions
Q16_Poly	Q16	int32_t	integer addition & multiply instructions
FPA_Poly	float32_t	int32_t	ASM library functions qfp_fadd & qfp_fmul
FPC_Poly	float32_t	int32_t	C library functions AddFloats & MulFloats
POS_Poly	posit32_t	int32_t	C library functions AddPosits & MulPosits

The *library functions* are in real-libs.zip on the textbook <u>website</u>. Inside the zip are files lib1-float.s, lib2-float.c, and lib3-posit.c to be extracted into your src directory together with the C main program found <u>here</u>. The program calls each of your polynomial functions with an array of n coefficients chosen to approximate the *sine* function at an angle x expressed in radians. Since the approximation of the sine function requires fewer terms near x = 0 for the same accuracy, the main program varies n from 0 to 8 to reduce average execution time. The values returned by your polynomial functions are used to display moving sine waves. If your code is correct, the display should look like the image above although with possibly different cycle counts. Error messages (if any) will appear as white text on a red background.

¹ https://en.wikipedia.org/wiki/Floating-point arithmetic

² https://en.wikipedia.org/wiki/Fixed-point arithmetic

³ https://en.wikipedia.org/wiki/Unum (number format)

⁴ https://en.wikipedia.org/wiki/Horner%27s method