

Tutorial I <Hints>

Date: / /

1) Here,

$$\text{Area of coil (A)} = (15 \times 17) \text{ mm}^2$$

$$\text{Flux density (B)} = 1.8 \times 10^{-3} \text{ wb/m}^2$$

$$\text{Spring constant (K)} = 0.14 \times 10^{-6} \text{ Nm/rad}$$

$$\text{Angular deflection (}\theta\text{)} = 90^\circ = \pi/2 \text{ rad}$$

$$\text{No. of turns (N)} = ?$$

At balance condition,

$$T_d = T_c$$

$$BINA = K\theta$$

$$\Rightarrow N = \frac{K\theta}{BIA}$$

2) Here,

$$\text{Resistance of meter (R)} = 20 \Omega$$

$$\text{Full scale deflection (}\theta\text{)} = 120^\circ$$

$$\text{Potential difference (V)} = 100 \text{ mV}$$

$$\text{Dimension of coil (A)} = 30 \text{ mm} \times 25 \text{ mm}$$

$$\text{No. of turns (N)} = 100$$

$$\text{Spring constant (K)} = 0.375 \times 10^{-6} \text{ Nm/deg.}$$

$$\text{Flux density (B)} = ?$$

$$\text{Diameter of copper wire (d)} = ?$$

Current in instrument for full scale deflection,

$$I = \frac{V}{R} = \frac{100 \times 10^{-3}}{20}$$

for steady (balance) condition,

$$T_d = T_c$$

$$\text{or, } BINA = K\theta$$

$$\Rightarrow B = \frac{K\theta}{INA} = \frac{0.375 \times 10^{-6} \times 120}{5 \times 10^{-3} \times 100 \times 30 \times 25 \times 10^{-6}}$$

Resistance of coil,

$$R_c = 0.3 \times 20 =$$

(Since resistance of coil is 30% of resistance of instrument)

Length of meanturn, $L_{mt} = 2(l+d)$
 $= 2(30+25)$
 $= 110 \text{ mm}$

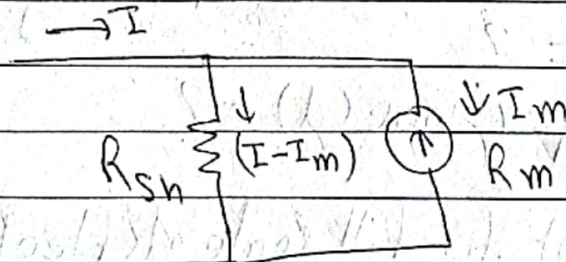
If 'A' be the cross-sectional area of wire, then,

Resistance of coil (R) = $\frac{\rho L_{mt}}{A} \times N$

or, $R = \frac{\rho L_{mt} N}{\frac{\pi d^2}{4}} = \frac{4\rho L_{mt} N}{\pi d^2}$ ← l →
|coil| ↓ d

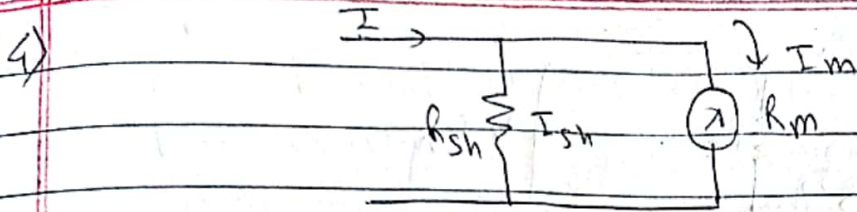
diameter of coil (d) = $\sqrt{\frac{4\rho L_{mt} N}{R\pi}}$

3)



$$I_m R_m = (I - I_m) R_{sh}$$

$$\Rightarrow R_{sh} = \frac{I_m R_m}{I - I_m}$$



$$i) I_m = \frac{V}{R_m} =$$

$$I_{sh} R_{sh} = I_m R_m$$

$$I_{sh} =$$

$$ii) \text{ Given, } I_{sh} = 10A$$

$$I_{sh} R_{sh} = I_m R_m$$

$$\Rightarrow R_m = \frac{I_m}{I_{sh} R_{sh}} =$$

$$iii) \text{ For 40\% deflection,}$$

$$I'_m = 0.4 \times 0.5 \times 10^{-3} =$$

Now,

$$I_{sh} = 100A \text{ (Given)}$$

$$I_{sh} R_{sh} = R'_m I'_m$$

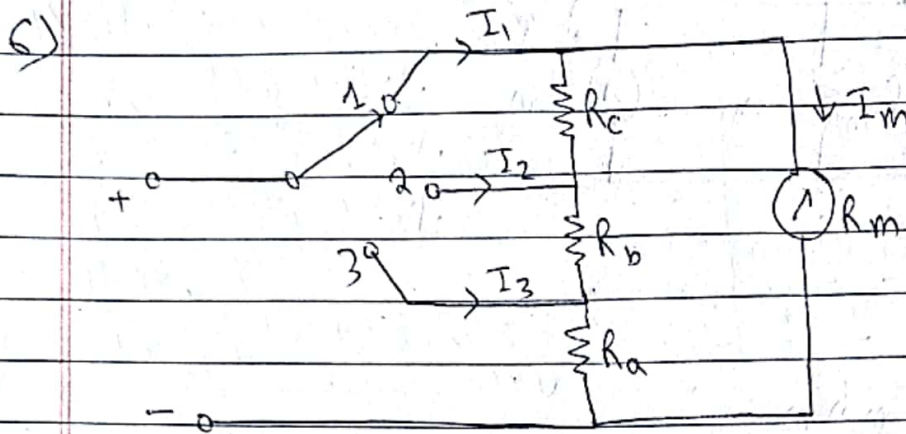
$$R'_m = \frac{I_{sh} R_{sh}}{I'_m} =$$

$$5) i) 0 - 10mA \Rightarrow I = 10mA$$

$$R_{sh1} = \frac{I_m R_m}{I - I_m}$$

$$= \frac{1 \times 50}{10 - 1} = \frac{50}{9} =$$

Similar for others



Here,

$$I_m = 1 \text{ mA}, R_m = 50 \Omega$$

$$I_1 = 1 \text{ A}, I_2 = 5 \text{ A}, I_3 = 10 \text{ A}$$

when switch is at position 1,

$$R_a + R_b + R_c = \frac{R_m}{m_1 - 1} \quad \text{--- i)}; m_1 = \frac{I_1}{I_m}$$

when switch is at position 2,

$$R_a + R_b = \frac{R_c + R_m}{m_2 - 1} \quad \text{--- ii)}; m_2 = \frac{I_2}{I_m}$$

when switch is at position 3,

$$R_a = \frac{R_b + R_c + R_m}{m_3 - 1} \quad \text{--- iii)}; m_3 = \frac{I_3}{I_m}$$

Solve eqⁿ i), ii) & iii) & obtain values of R_a , R_b & R_c .

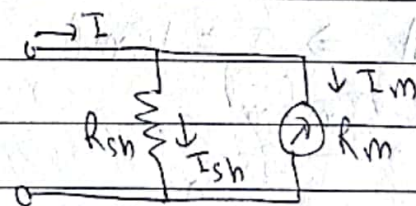
7) a) $I = 100 \text{ A}$

$$I_m = 10 \text{ mA}$$

$$V = 100 \text{ mV}$$

$$I_{sh} R_{sh} = I_m R_m$$

$$R_{sh} = \frac{I_m R_m}{(I - I_m)} = \frac{V}{I - I_m}$$



Power dissipation = $V I =$

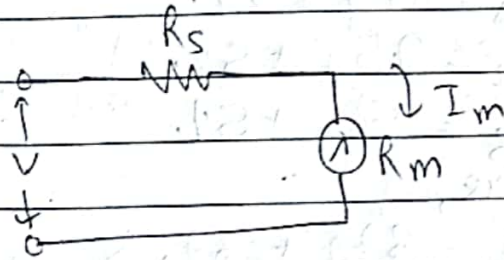
b) $V = 1000 \text{ V}$

$$V - I_m (R_s + R_m) = 0$$

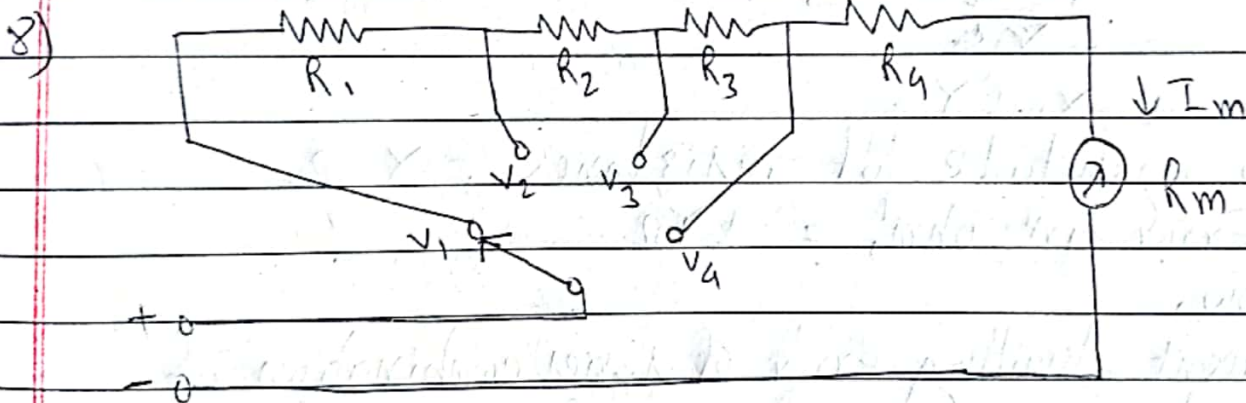
$$\text{or, } R_s = \frac{V}{I_m} - R_m$$

$$= \frac{1000}{10 \times 10^{-3}} - R_m \rightarrow 10 \text{ m}\Omega$$

$$=$$



Power dissipation = $V I_m =$



$$R_1 = R_m (m_1 - m_2)$$

$$m_1 = \frac{V_1}{V_m}$$

$$R_2 = R_m (m_2 - m_3)$$

$$m_2 = \frac{V_2}{V_m}$$

$$R_3 = R_m (m_3 - m_4)$$

$$m_3 = \frac{V_3}{V_m}$$

$$R_4 = R_m (m_4 - 1)$$

$$m_4 = \frac{V_4}{V_m}$$

9) Question correction

$$R_1 = 37\Omega \pm 5\%$$

$$R_2 = 75\Omega \pm 5\%$$

$$R_3 = 50\Omega \pm 5\%$$

Here,

$$R_1 = 37\Omega \pm 37 \times \frac{5}{100} = \underline{\hspace{2cm}}$$

$$R_2 = 75\Omega \pm 75 \times \frac{5}{100} = \underline{\hspace{2cm}}$$

$$R_3 = 50 \pm 50 \times \frac{5}{100} = \underline{\hspace{2cm}}$$

\therefore The limiting value of resultant resistance,

$$R = R_1 + R_2 + R_3$$

$$= \underline{\hspace{2cm}}$$

$$= X \pm Y$$

So, magnitude of resistance = $X \Omega$

Error in ohm, = $\pm Y \Omega$

Now,

Percent limiting error of series combination of resistance,

$$= \pm \frac{Y}{X} \times 100\% = \underline{\hspace{2cm}} \%$$

10) Here,

$$\text{Resistance}(R) = \frac{\text{Power}}{(\text{current})^2} = \frac{P}{I^2} = P I^{-2}$$

\therefore Relative limiting error in measurement of resistance is,

$$\frac{\partial R}{R} = \pm \left(\frac{\partial P}{P} + 2 \frac{\partial I}{I} \right)$$

$$= \pm (1.5 + 2 \times 1)\% = \pm 3.5\%$$

$$11) R_x = \frac{R_2 R_3}{R_1} =$$

Relative limiting error of unknown resistance,

$$\frac{\Delta R_x}{R_x} = \pm \left(\frac{\Delta R_2}{R_2} + \frac{\Delta R_3}{R_3} + \frac{\Delta R_1}{R_1} \right)$$

$$= \pm (1 + 0.5 + 1)$$

$$= \pm 2.5\%$$

Limiting error in ohm = $\pm \frac{2.5}{100} \times R_x \Rightarrow E$

Guaranteed value of resistance,

$$R_x - E =$$

$$\& R_x + E =$$

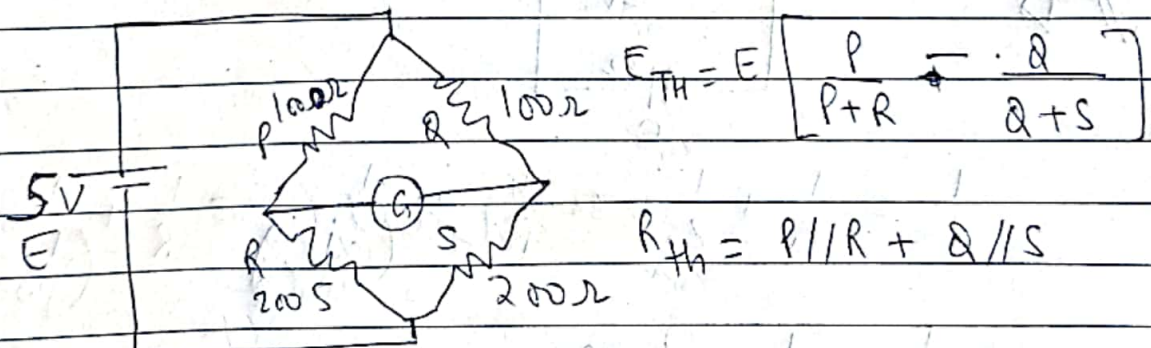
12) See class notes

13) } Same as 12

14)

15) See class notes

16)



$$I_g = \frac{E_{TH}}{R_{TH} + R_g} =$$

Deflection in galvanometer = Sensitivity $\times I_g$

Notes :-

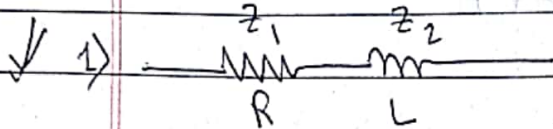
$$Z_c = \frac{1}{j\omega c} = \frac{-j}{\omega c}$$

$$Z_L = j\omega L$$

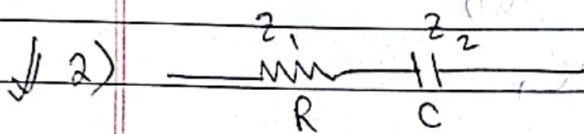
$$Y = \frac{1}{Z}$$

Y → Admittance

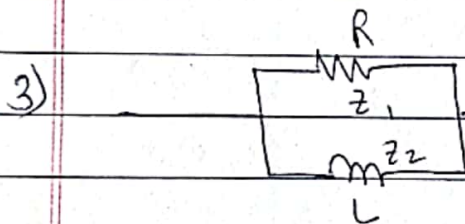
Z → Impedance



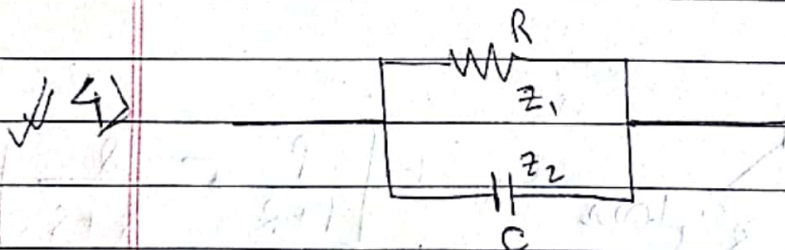
$$Z = Z_1 + Z_2 = R + j\omega L$$



$$Z = Z_1 + Z_2 = R - \frac{j}{\omega c}$$



$$\frac{1}{Z} = \frac{1}{Z_1} + \frac{1}{Z_2} = \frac{1}{R} + \frac{1}{j\omega L}$$



$$\frac{1}{Z} = \frac{1}{Z_1} + \frac{1}{Z_2} = \frac{1}{R} + \frac{1}{\left(\frac{1}{j\omega c}\right)}$$

$$\text{or, } \frac{1}{Z} = \frac{1}{R} + j\omega c$$

$$\text{or, } Y = \frac{1}{R} + j\omega c$$