

**POKHARA UNIVERSITY**

Level: Bachelor

Programme: BE

Course: Engineering Mathematics III

Semester: Fall

Year : 2015

Full Marks: 100

Pass Marks: 45

Time : 3hrs.

*Candidates are required to give their answers in their own words as far as practicable.*

*The figures in the margin indicate full marks.*

*Attempt all the questions.*

- a) Find eigen values and corresponding eigen vector of the matrix

$$\begin{bmatrix} 3 & 1 & 4 \\ 0 & 2 & 6 \\ 0 & 0 & 5 \end{bmatrix}$$

- b) Investigate for what values of p and q, the system of the equations  $x + y + z = 6, x + 2y + 3z = 10, x + 2y + pz = q$  has

- i. No solution.
- ii. A unique solution
- iii. An infinite number of solutions.

- a) Show that the series:

$$\sum (-1)^n \cdot \frac{1}{n+3}$$
 is conditionally convergent.

- b) Find the radius of convergence and interval of convergence of the

$$\text{series } \sum_{n=0}^{\infty} \frac{(x-2)^n}{10^n}$$

8

7

8

**OR**

Find Maclaurin's series of the function  $f(x) = e^x \sec x$ .

Find Fourier series of the function  $f(x) = \pi \sin \pi x$  ( $0 < x < 1$ ),  $p = 2L = 1$

7

Find Fourier expansion of

$$f(x) = 0 \text{ for } -\pi \leq x \leq 0 \\ = 1 \text{ for } 0 \leq x \leq \pi$$

8

and show that  $1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots = \frac{\pi}{4}$

4. a) A particle moves on the curve  $x = 2t^2, y = t^2 - 4t, z = 3t - 5$ , where  $t$  is the time. Find the component of velocity and acceleration at time  $t = 1$  in the direction  $\vec{i} - 3\vec{j} + 2\vec{k}$ .

7

- b) Define directional derivative. If  $\Phi = \log(x^2 + y^2 + z^2)$ . Find:
- $\text{div}(\text{grad } \Phi)$
  - $\text{Curl}(\text{grad } \Phi)$
5. a) State Gauss divergence theorem and use it to evaluate
- $$\iint_S \vec{F} \cdot \vec{n} dA \text{ where } \vec{F} = (e^x, e^y, -e^z), S \text{ is the surface of the cube } |x| \leq 1, |y| \leq 1, |z| \leq 1$$
- OR**
- Find  $\oint_C \vec{F} \cdot d\vec{r}$ , where  $\vec{F} = (y^2, z^2, x^2)$  and  $S$  is the portion of the sphere  $x^2 + y^2 + (z-1)^2 = 1, y \geq 0, z \leq 1$ .
- b) Evaluate  $\int_C \vec{F} \cdot d\vec{r}$  where  $\vec{F} = y^2 \vec{i} + 2x \vec{j} + 5y \vec{k}$  and  $S$  is the hemisphere  $x^2 + y^2 + z^2 = 4$  by using stokes theorem.
6. a) Apply simplex method to solve:
- Maximize  $Z = 40x_1 + 88x_2$   
 Subject to  $2x_1 + 8x_2 \leq 60$   
 $5x_1 + 2x_2 \leq 60$   
 $x_1 \geq 0, x_2 \geq 0$
- b) Find the dual of given lpp and solve by using simplex method  
 minimize  $Z = x_1 + 8x_2 + 5x_3$  subject to  
 $x_1 + x_2 + x_3 \geq 8, -x_1 + 2x_2 + x_3 \geq 2, x_1 \geq 0, x_2 \geq 0, x_3 \geq 0$
7. Do the followings:
- Prove that product of an even function and an odd function is odd function.
  - Let  $T: R^2 \rightarrow R^2$  be a transformation which is defined by  $T(x, y) = (x+y, x-y)$ , check the linearity of  $T$ .
  - Show that  $\begin{vmatrix} 1+x & 2 & 3 \\ 1 & 2+x & 3 \\ 1 & 2 & 3+x \end{vmatrix} = x^2(6+x)$
  - Test the convergence and divergence of  $1 + \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{3}} + \frac{1}{\sqrt{4}} + \dots$

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*Attempt all the questions.*

1. a) Define consistency of the system of linear equations. Check consistency of :  $x + y + z = 8$ ,  $x - y + z = 6$ ,  $2x - y + z = 8$ . If it is consistence, find its solution by Gauss Elimination method. 8
- b) Define Eigen values and vectors of a square matrix with its characteristics equation. If the eigen values and the corresponding eigenvector of the matrix  $\begin{pmatrix} 2 & 1 & 1 \\ 1 & 2 & 1 \\ 0 & 0 & 1 \end{pmatrix}$ . 7
2. a) Show that the infinite series  $\sum_{n=1}^{\infty} \frac{1}{n^p}$  is convergent if  $p > 1$  and divergent if  $0 < p \leq 1$ . 8
- b) Find the centre, radius of convergence and interval of convergence of the power series  $\sum_{n=0}^{\infty} \frac{(x-5)^n}{n5^n}$ . 7
3. a) Using Simplex method, maximize  $z = 150x_1 + 300x_2$  subject to the constant  $2x_1 + x_2 \leq 16$ ,  $x_1 + x_2 \leq 8$ ,  $x_2 \leq 3.5$ ;  $x_1 \geq 0$ ,  $x_2 \geq 0$  8
- b) Define periodic function. Find the fourier series representation of the periodic function  $f(x) = \frac{x^2}{2}$  for  $-\pi \leq x \leq \pi$  and then show that  $1 + \frac{1}{4} + \frac{1}{9} + \frac{1}{16} + \dots = \frac{\pi^2}{6}$  7
4. a) Prove that the necessary and sufficient condition for the vector 8

- function  $\vec{a}$  of scalar variable  $t$  to have constant direction is  $\vec{a} \times \frac{d\vec{a}}{dt}$ .
- b) Define gradient of scalar function. If  $\phi = x^3 + y^3 + z^3 - 3xyz$ , find  $\operatorname{div}(\operatorname{grad}\phi)$  and  $\operatorname{curl}(\operatorname{grad}\phi)$  7
5. a) Evaluate  $\iint_S \vec{F} \cdot \vec{n} dA$  if  $\vec{F} = [x^2, e^y, 1]$  8
- S:  $x + y + z = 1; x \geq 0, y \geq 0, z \geq 0.$
- b) State Stokes theorem. Evaluate  $\oint_C \vec{F} \cdot d\vec{r}$ , where  $\vec{F} = (z, x, y)$ , S : the 7  
hemisphere  $z = (a^2 - x^2 - y^2)^{\frac{1}{2}}$ .
6. a) Construct the dual problem corresponding to optimum problem 8  
minimize:  $Z = 8x_1 + 9x_2$  subject to  $x_1 + x_2 \geq 5, 3x_1 + x_2 \geq 21, x_1 \geq 0$   
 $x_2 \geq 0$  and solve it by simplex method.
- b) Find Fourier sine as well as cosine series representation of the half 7  
range function  $f(x) = e^x$  for  $0 < x < L$ .
7. Write short notes on: (Any two) 2×5
- a) Find the directional derivative of the scalar valued function  
 $f(x) = x^2 + y^2$ , at  $(1, 2)$  in the direction  $\vec{a} = 2\vec{i} - \vec{j}$ .
- b) Prove,  $1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \dots$  is convergent
- c) Let  $T: \mathbb{R}^2 \rightarrow \mathbb{R}$  be defined by  $T(x, y) = |x + y|$ , check  $T$  is linear or not.
- d) Show that the alternating series  $\sum_{n=1}^{\infty} (-1)^n \frac{1}{n}$ , is conditionally convergent series.

## POKHARA UNIVERSITY

Level: Bachelor

Semester: Fall

Year : 2016

Programme: BE

Full Marks: 100

Course: Engineering Mathematics III

Pass Marks: 45

Time : 3hrs.

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*Attempt all the questions.*

1. a) Define basis of vector space. Check the following vectors form a basis of  $\mathbb{R}^3$  or not. 7  
 $(1, 2, 1), (2, 1, 0), (1, -1, 2)$

**OR**

Check whether the system of linear equations is consistent or not, if consistent solve it by using Gauss elimination method.

$$x + 6y + 2z = 0$$

$$7x + 3y + z = 13$$

$$x + 2y + 3z = 20$$

- b) Find Eigen value and Eigen vector of the following matrix: 8

$$\begin{bmatrix} 3 & 0 & 0 \\ 0 & 4 & 0 \\ 0 & 0 & 5 \end{bmatrix}$$

- a) Show that the series  $1 - \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{3}} - \frac{1}{\sqrt{4}} + \dots$  is conditionally convergent. 7

- b) Find the center radius of convergence and interval of convergence of the power series  $\sum_{n=0}^{\infty} \frac{(x-5)^n}{n 5^n}$ . 8

**OR**

Find expansion of  $\log(1 + \sin x)$  as far as the term in  $x^4$ , by using Maclaurin expansion.

- a) Find the Fourier series representation of the periodic function  $f(x) = |x|$  for  $-\pi < x < \pi$ . Using it show that 8

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Candidates are required to  
 as practicable.  
 The figures in the margin  
 Attempt all the questions

$$\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots = \frac{\pi^2}{8}$$

- b) Find Fourier sine as well as cosine series of the function  $f(x) = x$  for  $0 < x < L$
4. a) Define directional derivative of  $\phi$  in the direction of  $\vec{a}$ . Find the directional derivative of  $\phi = x^2 + 3y^2 + 4z^2$  in the direction  $\vec{a} = -\vec{i} - \vec{j} + \vec{k}$  at P(1, 0, 0).
- b) If  $\vec{v} = x^2yz\vec{i} + xy^2z\vec{j} + xyz^2\vec{k}$ , find  $\operatorname{div}(\operatorname{curl}\vec{v})$  and

$\operatorname{curl}(\operatorname{curl}\vec{v})$

5. a) Using Green's theorem, calculate  $\int [(x^2 + y^2)\vec{i} - 2xy\vec{j}] \cdot d\vec{r}$  along the rectangle bounded by  $y=0, y=b, x=0, x=a$
- b) State Gauss Divergence Theorem and hence find  $\iint \vec{F} \cdot \vec{n} dA$ , where  $\vec{F} = (2x^2, \frac{y^2}{2}, -\cos \pi z)$  and S is the surface of the tetrahedron with vertices  $(0, 0, 0), (1, 0, 0), (0, 1, 0), (0, 0, 1)$

OR

State Stokes Theorem and using the theorem evaluate  $\oint \vec{F} \cdot d\vec{r}$  if  $\vec{F} = (y^3, 0, x^3)$ , along the boundary of the triangle  $(1, 0, 0), (0, 1, 0), (0, 0, 1)$

6. a) Maximize  $Z = 4x_1 + x_2 + 2x_3$  subject to the constraints  $x_1 + x_2 + x_3 \leq 1, x_1 + x_2 - x_3 \leq 0, x_1, x_2, x_3 \geq 0$
- b) Minimize  $z = 4x_1 + 3x_2$ , subject to  $2x_1 + 3x_2 \geq 1, 3x_1 + x_2 \geq 4, x_1 \geq 0, x_2 \geq 0$ , by using dual simplex method.

7. Attempt all

- a) Show that vectors  $(1, 0, 0), (0, 1, 0)$  and  $(0, 0, 1)$  are linearly independent
- b) Find the rank of  $A = \begin{bmatrix} 1 & 4 & 5 \\ 2 & 0 & 3 \\ 0 & 8 & 7 \end{bmatrix}$
- c) Check the following transformation is linear or not  $T: \mathbb{R}^2 \rightarrow \mathbb{R}^2$  be defined by  $T(x, y) = (x+3, y)$
- d) Test for convergence of the series  $\sum \frac{n+1}{2n+3}$

4x2.5

1. a) Define Eigen values  
 characteristics equation  
 eigenvectors of the m
- b) Define consistency  
 consistency of:  $x +$   
 consistence, find its
2. a) Prove the necessary  
 $\Sigma u_n$  is  $n \rightarrow \infty$   $u_n$
- b) Find the interval, c  
 $\sum_{n=1}^{\infty} \frac{2^n(x+4)^n}{n}$ .

Find the Maclau  
 terms.

3. a) Find fourier serie  
 b) Define periodic f  
 of the periodic

4. a) Prove that f  
 function

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1. a) Define Eigen values and vectors of a square matrix with its characteristics equation. Find the Eigen values and the corresponding eigenvectors of the matrix  $\begin{pmatrix} 2 & 1 & 1 \\ 1 & 2 & 1 \\ 0 & 0 & 1 \end{pmatrix}$ . 8
- b) Define consistency of the system of the linear equations. Check consistency of:  $x + y + z = 8$ ,  $x - y + z = 6$ ,  $2x - y + z = 8$ . If it is consistence, find its solution by Gauss Elimination method. 7
2. a) Prove the necessary condition for the convergence of an infinite series  $\sum u_n$  is  $n \rightarrow \infty u_n = 0$  but this not sufficient. 8
- b) Find the interval, center and radius of convergence of an infinite series  $\sum_{n=1}^{\infty} \frac{2^n(x+4)^n}{n}$ . 7

**OR**

Find the Maclaurin series representation of  $y = e^{\sin^{-1}x}$ , up to  $x^4$  terms.

Find fourier series of  $f(x) = x + |x|$  for  $-\pi < x < \pi$ .

Define periodic function with suitable example. Find the fourier series of the periodic function  $f(x) = \frac{x^2}{2}$  for  $-\pi < x < \pi$ . Using it show that

$$\frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \frac{1}{4^2} + \dots = \frac{\pi^2}{6}$$

4. a) Prove that the necessary and sufficient condition for a vector valued function  $\vec{r}$  of scalar variable  $t$  to have a constant magnitude is 8

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$$\vec{r} \cdot \frac{d\vec{r}}{dt} = 0.$$

- b) Define gradient of a scalar valued function. Find the directional derivative of the surface  $f = xy^2 + yz^3$  at P (2, -1, 1) along the direction of normal to the surface  $x \log z - y^2 + 4 = 0$  at the point (1, 1, 1).
5. a) Evaluate the line integral  $\oint_C [(x^3 - 3y)dx + (x + \sin y)dy]$ , where C : the boundary of a triangle with vertices (0,0), (1,0), (0,2) along anticlockwise direction.
- b) Evaluate  $\iint_S (\vec{F} \cdot \vec{n})dA$ , where  $\vec{F} = 4x\vec{i} - 2y^2\vec{j} + z^2\vec{k}$  and S is the surface of the region bounded by  $x^2 + y^2 = 4$ ,  $z = 0$ ,  $z = 3$ .

OR

State Stokes theorem. Evaluate  $\oint_C \vec{F} \cdot d\vec{r}$ ,

where  $\vec{F} = 4z\vec{i} - 2x\vec{j} + 2x\vec{k}$ , C is the circle  $x^2 + y^2 = 1$ ,  $z = y + 1$ .

6. a) Maximize  $z = x_1 + x_2 + x_3$  subjected to the constraints  
 $4x_1 + 5x_2 + 8x_3 \leq 12; 8x_1 + 5x_2 + 4x_3 \leq 12; x_1 \geq 0; x_2 \geq 0$ .
- b) Minimize  $z = 4x_1 + 3x_2$  such that  
 $2x_1 + 3x_2 \geq 1; 3x_1 + x_2 \geq 4; x_1 \geq 0; x_2 \geq 0$ , by constructing duality

7. Attempt all

4×2.5

- a) Test the convergence and divergence of series  $\frac{2}{9} + \frac{3}{16} + \frac{4}{25} + \dots$
- b) Let  $T: \mathbb{R}^2 \rightarrow \mathbb{R}$  be defined by  $T(x,y) = |x+y|$ , Check T is linear or not.

c) Find the rank of the matrix: 
$$\begin{bmatrix} 1 & 0 & 0 \\ 2 & 2 & 0 \\ -3 & -2 & 1 \end{bmatrix}$$

- d) If  $\vec{r} = \vec{a}e^{m\theta} + \vec{b}e^{-m\theta}$  where  $\vec{a}$  and  $\vec{b}$  are constant vectors. Show that  $\frac{d^2\vec{r}}{dt^2} - m^2\vec{r} = 0$ .

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Attempt all the que

a) When a set of si  
for consistency  
 $-x+3y-2z = 7, 3x$

b) Find eigen value  
 $A = \begin{pmatrix} 2 & 0 \\ 0 & 1 \end{pmatrix}$

a) Test the conv  
 $\sum [\sqrt{n^3 + 1} -$   
b) Find the int  
 $\sum_{n=0}^{\infty} \frac{x^{2n+1}}{n!}$

Find expansion  
expansion

a) Find the F  
value of  $\frac{1}{1-x}$

b) Find the  
 $f(x) = x$

a) Maxim  
 $x_1 +$   
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b) Co

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1. a) When a set of simultaneous equations is said to be inconsistent? Test for consistency and solve using Gauss elimination method. 8  
 $-x+3y-2z = 7, 3x+3z = -3, 2x+y+2z = -1$
- b) Find eigen values and eigen vector of the Matrix: 7  

$$A = \begin{pmatrix} 2 & 0 & 1 \\ 0 & 2 & 0 \\ 1 & 0 & 2 \end{pmatrix}$$
2. a) Test the convergence and divergence of the infinite series 8  
 $\sum [\sqrt{n^3 + 1} - \sqrt{n^3 - 1}]$
- b) Find the interval and radius of convergence of the power series 7  

$$\sum_{n=0}^{\infty} \frac{x^{2n+1}}{n!}$$

**OR**

Find expansion of  $e^{\sin^{-1} x}$  as far as the term in  $x^4$ , by using Maclaurin expansion.

3. a) Find the Fourier series of  $f(x)=x^2$  for  $-\pi < x < \pi$  and hence find the value of  $\frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots$  8
- b) Find the Fourier sine and cosine series of the function  $f(x) = x$  for  $0 < x < \pi$ . 7
4. a) Maximize  $z = 4x_1 + x_2 + 2x_3$ , subject to  $x_1 + x_2 + x_3 \leq 1$ ,  
 $x_1 + x_2 - x_3 \leq 0, x_1 \geq 0, x_2 \geq 0$  and  $x_3 \geq 0$  by using simplex method. 8
- b) Construct the dual problem corresponding to the optimum problem : 7

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- Minimize  $z = 4x_1 + 3x_2$  subject to  
 $4x_1 + 5x_2 \geq 1$ ;  $3x_1 + x_2 \geq 4$ ;  $x_1 \geq 0, x_2 \geq 0$  and solve it by using simplex method.
5. a) A particle moves on the curve  $x = t^3 + 1, y = t^2, z = 2t + 5$  where  $t$  is the time. Find the component of velocity and acceleration at  $t = 1$  in the direction of  $\vec{i} - \vec{j} + 3\vec{k}$ .  
 b) Define Divergence and Curl of a vector. If  $\phi = \log(x^2 + y^2 + z^2)$  find  $\operatorname{div}(\operatorname{grad} \phi)$  and  $\operatorname{curl}(\operatorname{grad} \phi)$ .
6. a) State Greens theorem in plane. Evaluate  $\oint [5xydx + x^3dy]$ , where C is the closed curve consisting of the graph of  $y = x^2$  and  $y = 2x$  between the points  $(0, 0)$  and  $(2, 4)$ .

OR

State Stoke's theorem. Using the theorem evaluate  $\oint \vec{F} \cdot d\vec{r}$ , where  $\vec{F} = [-5y, 4x, z], C: \text{circle } x^2 + y^2 = 25, z = 1$ .

- b) Evaluate  $\iint_S \vec{F} \cdot \vec{n} dA$  if  $\vec{F} = [x^2, e^y, 1]$   
 S:  $x + y + z = 1, x \geq 0, y \geq 0, z \geq 0$

7. Attempt all

- a) Find the rank of  $A = \begin{bmatrix} 1 & 2 & 4 \\ 3 & 1 & 5 \\ 2 & 4 & 8 \end{bmatrix}$   
 b) Find the inverse of  $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$   
 c) Check the following transformation is linear or not?  
 $T: \mathbb{R}^2 \rightarrow \mathbb{R}^2$  be defined by  $T(x, y) = (x + 3, y)$   
 d) Test the convergence and divergence of infinite series  

$$\frac{2}{9} + \frac{3}{16} + \frac{4}{25} + \dots$$

8

7

8

7

4x2.5

1. a) Find the direction of z-axis at P(2, -1, 0)

b) Show that the vector field

2. a) Find the flux of the portion of

b) State Stoke's theorem

$$\vec{F} = yz\vec{i} + z\vec{j} + x\vec{k}$$

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*Attempt all the questions.*

1. a) State the condition for a set of simultaneous equations to be consistent? Show that the set of simultaneous equations is consistent and solve it using Gauss elimination method. 7  

$$3x-y+z=2, x+5y+2z=6, 2x+3y+z=0$$
1. b) Find the eigen values and eigen vectors of the matrix 8  

$$\begin{bmatrix} 3 & 1 & 0 \\ 1 & 3 & 0 \\ 0 & 0 & 2 \end{bmatrix}$$
2. a) Find the directional derivative of  $f = 4xz^3 - 3x^2yz^2$  in the direction of z-axis at P (2, -1, 2). 7
2. b) Show that the vector  $\vec{F} = (yz)\vec{i} + (xz)\vec{j} + (xy)\vec{k}$  is conservative vector field and find the function  $\phi$  such that  $\vec{F} = \nabla\phi$ . 8
3. a) Find the flux integral of  $\vec{F} = (x, y, z)$  through the surface S, where S is the portion of the plane  $2x + 3y + z = 6$  in first octant. 7
3. b) State Stoke's Theorem and apply it to evaluate  $\oint_C \vec{F} \cdot d\vec{r}$  where  $\vec{F} = yz\vec{i} + xy\vec{j} + xz\vec{k}$  8

**OR**

Using divergence theorem find  $\iint_S \vec{F} \cdot \hat{n} ds$  where  $\vec{F} = y^2e^{xz}\vec{i} - xy\vec{j} + x\tan^{-1}y\vec{k}$  and S is the surface of the region bounded by the coordinate planes and the plane  $x + y + z = 1$ .

4. a) State and prove P-test for hyperharmonic series. 7
4. b) Find the radius of convergence and interval of convergence of the infinite series: 8

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as practicable.  
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Attempt all the questions.

$$\sum_{n=0}^{\infty} \frac{(x-4)^n (n+1)}{10^n}$$

OR

Find expansion of  $e^{\sin x}$  upto the forth power of  $x$  by using Maclaurin expansion.

5. a) Find the fourier series of the periodic function

$$F(x) = x - x^2 \text{ for } (-\pi < x < \pi)$$

- b) Find Fourier sine as well as cosine series of the function  $f(x) = \pi - x$  for  $0 < x < \pi$ .

6. a) Maximize the total output  $z = x_1 + x_2 + x_3$  subject to input constraints  $4x_1 + 5x_2 + 8x_3 \leq 12$ ,  $8x_1 + 5x_2 + 4x_3 \leq 12$

- b) Construct the dual problem corresponding to the optimum problem:

Minimize  $z = 20x_1 + 30x_2$  subject to

$$x_1 + 4x_2 \geq 8; x_1 + x_2 \geq 5; 2x_1 + x_2 \geq 7, x_1 \geq 0, x_2 \geq 0$$

and solve it by using simplex method

7. Attempt all questions

- a) Prove that product of two odd functions is an even function  
 b) Check the following transformation is linear or not?  $T: \mathbb{R}^2 \rightarrow \mathbb{R}^2$  be defined by  $T(x, y) = (x, -2y)$   
 c) If  $f(x, y, z) = xyz$ , show that  $\nabla \cdot (\nabla f) = 0$   
 d) Test the convergence of the series  $1 - \frac{1}{2\sqrt{2}} + \frac{1}{3\sqrt{3}} - \frac{1}{4\sqrt{4}} + \dots$

4x2.5

$$\begin{bmatrix} 3 & 1 & 4 \\ 0 & 2 & 6 \\ 0 & 0 & 5 \end{bmatrix}$$

1. a) Define basis of vector space  $\{(1, 1, 1), (1, 2, 1), (2, 1, 1)\}$

- b) Apply simplex method to solve the following LPP constraints:  $-2x_1 + 10 \geq 0$

3. a) Prove that if an infinite sequence of real numbers  $\{u_n\}_{n=1}^{\infty}$  satisfies  $\lim_{n \rightarrow \infty} u_n = 0$ .

- b) Find the center radius and interval of convergence of the power series  $\sum_{n=0}^{\infty} a_n x^n$

## POKHARA UNIVERSITY

Level: Bachelor  
 Programme: BE  
 Course: Engineering Mathematics III

Semester: Fall

Year : 2018  
 Full Marks: 100  
 Pass Marks: 45  
 Time : 3 hrs.

*Candidates are required to give their answers in their own words as far as practicable.*

*The figures in the margin indicate full marks.*

*Attempt all the questions.*

1. a) Check the consistency of the system of the equations and solve 7

$$2x + 5y + 6z = 13$$

$$3x + y - 4z = 0$$

$$x - 3y - 8z = -10$$

- b) Define Eigen values and vectors of a square matrix with its characteristics equation. Find the Eigen values and the corresponding eigenvectors of the matrix 8

$$\begin{bmatrix} 3 & 1 & 4 \\ 0 & 2 & 6 \\ 0 & 0 & 5 \end{bmatrix}$$

2. a) Define basis of vector space over a given field F. Show that 7  
 $\{(1, 1, 1), (1, 2, 1), (2, 3, 3)\}$  forms a basis for  $R^3$ .

- b) Apply simplex method to Minimize  $Z = 5x_1 - 20x_2$  subjected to the constraints;  $-2x_1 + 10x_2 \leq 5, 2x_1 + 5x_2 \leq 10, x_1, x_2 \geq 0$  8

3. a) Prove that if an infinite series  $\sum u_n$  is convergent then  $\lim_{n \rightarrow \infty} u_n = 0$ . 7  
 By taking suitable example show that  $\sum u_n$  is not convergent even if  $\lim_{n \rightarrow \infty} u_n = 0$ .

- b) Find the center radius of convergence and interval of convergence of 8  
 the power series  $\sum_{n=1}^{\infty} \frac{(-1)^n (2x-1)^n}{n 6^n}$

### OR

Use Maclaurin's theorem to expand  $f(x) = e^{\sin x}$  in powers of x upto four terms.

- a) Find fourier series of  $f(x) = x + |x|$  for  $-\pi < x < \pi$ . 7  
 b) Find the fourier cosine series as well as sine series of the function 8  
 $f(x) = x^2$  for  $0 < x < L$

5. a) Find the dual of given LPP and solve by using simplex method  
 Minimize  $z = x_1 + 8x_2 + 5x_3$  subject to  $x_1 + x_2 + x_3 \geq 8$ ,  $-x_1 + 2x_2 + x_3 \geq 2$ ,  
 $x_1 \geq 0, x_2 \geq 0, x_3 \geq 0$ .  
 b) Find the directional derivative of  $f = xy^2 + yz^3$  at  $(2, -1, 1)$  along the direction of the normal to the surface  $x \log z - y^2 + 4 = 0$  at  $(-1, 2, 1)$ .
6. a) Evaluate  $\iint_S \vec{F} \cdot \vec{n} dA$  where  $\vec{F} = (x^2, e^y, 1)$  where S is the portion of the plane  $x + y + z = 1$  lying in the first octant.

OR

Using Stokes Theorem evaluate  $\oint_C \vec{F} \cdot d\vec{r}$  where  $\vec{F} = (y, \frac{z}{2}, \frac{3y}{2})$  and C is the circle  $x^2 + y^2 + z^2 = 6z$ ,  $z = x + 3$ .

- b) Show that the value under integral sign  $\int_{(1,0,2)}^{(-2,1,3)} (6xy^3 + 2z^2) dx + 9x^2y^2 dy + (4xz + 1)dz$  is exact and evaluate it.

7. Attempt all questions.

8

7

8

7

2.5x4

- a) State condition for a set of vectors to be linearly independent. Show that the set of the vectors  $\{1, x, x^2, x^3\}$  is linearly independent by using elimination method.  $3x-y+2z=0$
- b) State Cayley -Hamilton Theorem. If  $A = \begin{pmatrix} 3 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$

- a) By using Simplex method, solve the following LPP:  
 $x_1 + 3x_2 \leq 15$ ,  $3x_1 + x_2 \leq 10$ ,  $x_1, x_2 \geq 0$ .

- b) Construct the dual problem of the above LPP. Minimize  $Z = 8x_1 + 9x_2$ , solve it by using simplex method.

- a) Show that the alternative numerical methods for solving LPP are numerically less than the simplex method. And using graphical method, find the radius of convergence of the series  $\sum_{n=0}^{\infty} (-1)^n \frac{x^n}{n!}$ .

**POKHARA UNIVERSITY**

Level: Bachelor  
 Programme: BE  
 Course: Engineering Mathematics III

Semester: Spring

Year : 2018  
 Full Marks: 100  
 Pass Marks: 45  
 Time : 3 hrs.

*Candidates are required to give their answers in their own words as far as practicable.*

*The figures in the margin indicate full marks.*

*Attempt all the questions.*

- 3)  $(6xy^3 + 2z^2) dx +$  7  
 t.  $z^3$  at  $(2, -1, 1)$  along the 7  
 $y^2 + 4 = 0$  at  $(-1, 2, 1)$ .  
 where S is the portion 8  
 nt.
- re  $\bar{F} = (y, \frac{z}{2}, \frac{3y}{2})$  and
- 3)  $(6xy^3 + 2z^2) dx +$  7  
 t.  $z^3$  at  $t=1$ .  
 odd or even 2.5x4
- $- \frac{3}{16} + \frac{4}{25} + \dots$
- at  $t=1$ .  
 odd or even
- a) State condition for a set of simultaneous equations to be consistent? 7  
 b) Show that the set of the equations are consistent and solve by Gauss Elimination method.  $3x-y+z=0$ ,  $x+5y+2z=6$ ,  $2x+3y+z=0$ .
- b) State Cayley -Hemilton Theorem Find  $A^{-1}$  by using it. 8

$$A = \begin{pmatrix} 3 & 1 & 4 \\ 0 & 2 & 6 \\ 0 & 0 & 5 \end{pmatrix}$$

2. a) By using Simplex method, Maximize  $z = 20x_1 + 20x_2$  subject to  $-x_1 + x_2 \leq 1$ ,  $x_1 + 3x_2 \leq 15$ ,  $3x_1 + x_2 \leq 21$ ,  $x_1 \geq 0$ ,  $x_2 \geq 0$ . 7  
 b) Construct the dual problem corresponding to the optimum problem:  
 Minimize  $Z = 8x_1 + 9x_2$ , subject to  $x_1 + x_2 \geq 5$ ,  $3x_1 + x_2 \geq 21$ ,  $x_1, x_2 \geq 0$ . Also solve it by using simplex method. 8
3. a) Show that the alternating series  $u_1 - u_2 + u_3 - u_4 + \dots$  in which each term is numerically less than the preceding term and  $\lim_{n \rightarrow \infty} u_n = 0$ , is convergent. And using it show that the series  $1 - \frac{1}{2} + \frac{1}{3} - \frac{1}{4} + \dots$  is convergent. 7  
 b) Find the radius of convergence and interval of convergence of the infinite series: 8

$$\sum_0^{\infty} \frac{10^{n+1}}{3^{2n}} x^n$$

**POKHARA UNIVERSITY**

Level: Bachelor  
Programme: BE  
Course: Engineering Mathematics III

Semester: Fall

Year : 2019  
Full Marks: 100  
Pass Marks: 45  
Time : 3 hrs.

*Candidates are required to give their answers in their own words as far as practicable.*

*The figures in the margin indicate full marks.*

*Attempt all the questions.*

1. a) Check whether the system of linear equations is consistent or not, if consistent solve it by using Gauss elimination method 8  

$$\begin{aligned}x+6y+2z &= 0 \\7x+3y+z &= 13 \\X+2y+3z &= 20\end{aligned}$$
1. b) Define eigen value and eigen vector. Find eigen values and eigen vectors of the matrix. 
$$\begin{bmatrix} 3 & 1 & 4 \\ 0 & 2 & 0 \\ 0 & 0 & 5 \end{bmatrix}$$
 7
2. a) Show that if the infinite series  $\sum u_n$  is convergent then  $\lim_{n \rightarrow \infty} u_n = 0$ . With a suitable example, prove that the converse may not be true. Find the interval of convergence of the power series  $\sum_{n=0}^{\infty} \frac{10^{n+1} x^n}{3^{2n}}$ . 7  
OR  
Find the expansion of  $e^{\sin x}$  upto the fourth power of  $x$  by using Maclaurin Expansion. 8
3. a) If a particle is moving with acceleration  $12 \cos 2t \vec{i} - 8 \sin 2t \vec{j} + 16t \vec{k}$  at time  $t$ , find its velocity  $\vec{v}$  and displacement  $\vec{r}$  at time  $t$ . Given that  $\vec{v} = \vec{0}$  and  $\vec{r} = \vec{0}$  when  $t = 0$ . 7  
b) Define Divergence and Curl of a vector. If  $\phi = \log(x^2 + y^2 + z^2)$  find  $\operatorname{div}(\operatorname{grad} \phi)$  and  $\operatorname{curl}(\operatorname{grad} \phi)$ . 8

Candidates are required to give the answers as practicable.  
The figures in the margin indicate the marks allocated to each question.  
Attempt all the questions.

4. a) Define surface integral of  $\vec{F}$  on the surface S. Evaluate  $\iint_S \vec{F} \cdot \hat{n} ds$   
 where  $\vec{F} = (x^2, e^x, 1)$ , where S is the surface  $x + y + z = 1$ ,  
 $x \geq 0, y \geq 0, z \geq 0$ .
- b) Find  $\iint_S \vec{F} \cdot \hat{n} da$  where  $\vec{F} = (4x, x^2y, -x^2z)$ , S is the surface of the tetrahedron with vertices  $(0,0,0), (1,0,0), (0,1,0), (0,0,1)$
5. a) Find Fourier series of the function  $f(x) = x^2$  for  $-\pi < x < \pi$  and hence deduce  $\frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \frac{1}{4^2} + \dots = \frac{\pi^2}{6}$
- b) Find the Fourier sine as well as cosine series representation of the half range function  $f(x) = x^2$  for  $0 < x < 1$ .
6. a) Using simplex method, Maximize  $z = 5x_1 + 3x_2$  subject to  $x_1 + x_2 \leq 2$ ,  $5x_1 + 2x_2 \leq 10$ ,  $3x_1 + 8x_2 \leq 12$ ,  $x_1 \geq 0$ ,  $x_2 \geq 0$ .
- b) Construct the dual problem corresponding to the optimum problem: Minimize  $z = 8x_1 + 9x_2$  subject to  $x_1 + x_2 \geq 5$ ,  $3x_1 + x_2 \geq 21$ ,  $x_1 \geq 0$ ,  $x_2 \geq 0$ , and solve it by using simplex method.

## 7. Attempt all questions:

a) Find the rank of  $A = \begin{pmatrix} 1 & 4 \\ 2 & 0 \end{pmatrix}$ .

b) Test the convergence and divergence of series  $\frac{2}{9} + \frac{3}{16} + \frac{4}{25} + \dots$

c) Check odd, even or neither of the function:

$$f(x) = \begin{cases} \frac{1}{7} + x & \text{for } -\frac{1}{2} < x < 0 \\ \frac{1}{7} - x & \text{for } 0 < x < \frac{1}{2} \end{cases}$$

d) Evaluate  $\int_{(-1,2)}^{(3,1)} [(y^2 + 2xy)dx + (x^2 + 2xy)dy]$

10

Define Maclaurin series of function of three terms and hence obtain the first three terms.

a) A function  $f(x)$  defined by the series.

b) Find  $F(x)$  as we

4. a) Find the de

3) in t

**POKHARA UNIVERSITY**

Level: Bachelor	Semester: Spring	Year : 2019
Programme: BE		Full Marks: 100
Course: Engineering Mathematics III		Pass Marks: 45
		Time : 3 hrs.

*Candidates are required to give their answers in their own words as far as practicable.*

*The figures in the margin indicate full marks.*

*Attempt all the questions.*

1. a) Solve by using Gauss elimination method  

$$4x - 8y + 3z = 16, -x + 2y - 5z = -21, 3x - 6y + z = 7$$
  1. b) Using Cayley Hamilton Theorem find the inverse of  

$$A = \begin{bmatrix} 7 & -1 & 3 \\ 6 & 1 & 4 \\ 2 & 4 & 8 \end{bmatrix}$$
  2. a) State and prove the Leibnitz's theorem for alternating series and hence test the convergence of the series  $\sum_{n=1}^{\infty} (-1)^{n+1} \frac{n}{n^2+1}$
  2. b) Find the centre, radius and interval of convergence :
- $$\sum_{n=1}^{\infty} \frac{(-1)^n (2x-1)^n}{n^6}$$
- OR**
- Maclaurin series of function  $f(x)$  and find the expansion of  $\tan x$  upto three terms and hence obtain the expansion of  $\sec^2 x$ .
3. a) A function  $f(x)$  defined by  $f(x) = x^2$  for  $0 \leq x \leq L$ . Find the Fourier cosine series.
  3. b) Find Fourier sine as well as cosine series of the function  $f(x) = x$  for  $0 < x < 1$ .
  4. a) Find the directional derivative of the function  $f = x^2 - y^2 + 2z^2$  at the point  $P(1, 2, 3)$  in the direction of line  $PQ$  where  $Q$  is the point  $(5, 0, 4)$ .
  4. b) If  $\theta$  is the acute angle between the surfaces  $xy^2z = 3x + z^2$  and

Candidates are required to answer  
 as practicable.  
 The figures in the margin  
 Attempt all the questions.

3.  $3x^2 - y^2 + 2z = 1$  at the point  $(1, -2, 1)$ . Show that  $\cos \theta = \frac{3}{7\sqrt{6}}$
5. a) Evaluate the line integral  $\oint_C \vec{F} \cdot d\vec{r}$ , where  $\vec{F} = (1, xy, yz)$  and  $S$  is the surface  $x^2 + y^2 \leq z$ ,  $y \geq 0$ ,  $z \leq 4$   
 b) State Gauss divergence theorem and using it, evaluate  $\iint_S \vec{F} \cdot \hat{n} ds$ , where  $\vec{F} = 2x^2 \vec{i} - y^2 \vec{j} + 4xz^2 \vec{k}$  and  $S$  is the region bounded by the cylinder  $y^2 + z^2 = 3$  and  $0 \leq x \leq 2$ ,  $y \geq 0$  and  $z \geq 0$ .
6. a) Solve the following Linear programming problem using the simplex method.
- Maximize  $z = 30x_1 + 20x_2$  subject to:  
 $-x_1 + x_2 \leq 5$   
 $2x_1 + x_2 \leq 10$   
 $x_1, x_2 \geq 0$
- b) Solve the linear programming problem by Simplex method constructing its duality: Minimize  $z = 20x_1 + 30x_2$  Subject to  $x_1 + 4x_2 \geq 8$ ,  $x_1 + x_2 \geq 5$ ,  $2x_1 + x_2 \geq 7$ ,  $x_1 \geq 0$ ,  $x_2 \geq 0$
7. Attempt all the questions.
- a) Check the following transformation is linear or not ?  
 $T: \mathbb{R}^2 \rightarrow \mathbb{R}^2$  be defined by  $T(u, v) = (u, v+3)$
- b) Find the unit tangent vector to the curve  $\vec{r} = (t, t^2, t^3)$  at  $t = 1$
- c) Test the convergence of the series:  $1 + \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{3}} + \frac{1}{\sqrt{4}} + \dots \dots \dots$
- d) Evaluate the integral  
 $\int_{(-1,2)}^{(3,1)} [(y^2 + 2xy)dx + (x^2 + 2xy)dy]$

POKHARA UNIVERSITY

Level: Bachelor  
 Programme: BE  
 Course: Engineering Mathematics III

Semester: Fall

Year : 2020

Full Marks: 100

Pass Marks: 45

Time : 3 hrs.

Candidates are required to give their answers in their own words as far as practicable.

The figures in the margin indicate full marks.

Attempt all the questions.

- What do you mean by consistency of system of linear equations? Is a system of linear equations  $x + 3y + 6z = 2$ ,  $3x - y + 4z = 9$ ,  $x - 4y + 2z = 7$  consistent? If it is consistent system, find its solution.
- State Cayley – Hamilton theorem. Find  $A^{-1}$  by using it.
- Prove that the necessary and sufficient condition for a vector valued function  $\vec{r}$  of scalar variable  $t$  to have a constant magnitude is  $\vec{r} \cdot \frac{d\vec{r}}{dt} = 0$ . A particle moves on the curve  $\vec{r} = 2t^2\vec{i} + (t^2 - 4t)\vec{j} + (3t - 5)\vec{k}$ , where  $t$  is the time. Find the component of velocity and acceleration at time  $t = 1$  in the direction of  $\vec{i} - 3\vec{j} + 2\vec{k}$ .
- Define gradient of a scalar valued function. Find the directional derivative of the surface  $f = xy^2 + yz^3$  at P (2, -1, 1) along the direction of normal to the surface  $x \log z - y^2 + 4 = 0$  at the point (1, 1, 1).
- a) State Green's Theorem in plane. Evaluate  $\oint [5xydx + x^3dy]$ , where C is the closed curve consisting of the graph of  $y = x^2$  and  $y = 2x$  between the points (0, 0) and (2, 4).

$$A = \begin{pmatrix} 2 & 5 & 3 \\ 3 & 1 & 2 \\ 1 & 2 & 1 \end{pmatrix}$$

- b) Evaluate the line integral  $\int_C \vec{F} \cdot d\vec{r}$  by using Stoke's theorem, where  
 $\vec{F} = 4y\vec{i} - 2z\vec{j} + 6y\vec{k}$  and C is the circle  $x^2 + y^2 + z^2 = 6z$ ,  $z = x + 3$   
 OR

Evaluate the surface integral  $\iint_S \vec{F} \cdot \vec{n} dA$  where

$$\vec{F}(x, y, z) = [x^2, y^2, z^2], \text{ and } S \text{ is the surface given by}\\ \vec{r}(u, v) = (u \cos v, u \sin v, 3v), \quad 0 \leq u \leq 1, \quad 0 \leq v \leq 2\pi$$

4. a) State and prove D'Alembert's ratio test. Test the convergence and divergence of the infinite series

$$\sum_{n=1}^{\infty} [\sqrt{n^2 + 1} - n]$$

- b) Find the centre, radius and interval of convergence :

$$\sum_{n=1}^{\infty} \frac{(-1)^n (2x-1)^n}{n^{6^n}}$$

OR

Expand the function  $e^{ax} \cos bx$  upto the third power of x in Maclaurin series by assuming the validity of expansion.

5. a) Solve the linear programming problem: Maximize  $z = 300x_1 + 500x_2$   
 subject to  $2x_1 + 8x_2 \leq 60$ ,  $2x_1 + x_2 \leq 30$ ,  $x_1 + x_2 \leq 15$ ,  $x_1 \geq 0$ ,  $x_2 \geq 0$ .

- b) Solve the linear programing problem, Minimize  $z = 8x_1 + 9x_2$  subject to  $x_1 + x_2 \geq 5$ ,  $3x_1 + x_2 \geq 21$ ,  $x_2 \geq 0$ ,  $x_1 \geq 0$ , using simplex method, by constructing the duality.

6. a) Write the Fourier coefficients of a function f(x). Find the fourier

series representation of the periodic function  $f(x) = \frac{x^2}{2}$  for

$$-\pi \leq x \leq \pi \text{ and hence show that } 1 + \frac{1}{4} + \frac{1}{9} + \frac{1}{16} + \dots = \frac{\pi^2}{6} \text{ and}$$

$$1 - \frac{1}{4} + \frac{1}{9} - \frac{1}{16} + \dots = \frac{\pi^2}{12}.$$

- b) Find Fourier series of  $f(x) = x - x^2$  for  $-\pi < x < \pi$ .

Attempt all questions:  
 a) Check the following  
 $T: \mathbb{R}^2 \rightarrow \mathbb{R}^2$  be defined  
 b) Show that the matrix

$$\begin{vmatrix} 1 & a & a \\ 1 & b & b \\ 1 & c & c \end{vmatrix}$$

c) Evaluate

$$\begin{vmatrix} 1 & a & a \\ 1 & b & b \\ 1 & c & c \end{vmatrix}$$

d) Test the converge

's theorem, where  
 $z^2 = 6z, z = x + iy$

4x2.5

1. Attempt all questions:

a) Check the following transformation is linear or not?

$T: R^2 \rightarrow R^2$  be defined by  $T(m, n) = (m, n+3)$

b) Show that the matrix  $\begin{bmatrix} i & 2+i & 3-i \\ -2+i & 2i & 2 \\ -3-i & -2 & -i \end{bmatrix}$  is skew Hermitian.

c) Evaluate  $\begin{vmatrix} 1 & a & a^2 \\ 1 & b & b^2 \\ 1 & c & c^2 \end{vmatrix}$

d) Test the convergence of series  $\sum \frac{n+1}{2n+3}$

**POKHARA UNIVERSITY**

Level: Bachelor  
 Program: BE  
 Course: Engineering Mathematics III

Semester – Spring

Year: 2020  
 Full Marks: 70  
 Pass Marks: 31.5  
 Time: 2 hrs.

*Candidates are required to answer in their own words as far as practicable. The figures in the margin indicate full marks.*

**Group - A: Attempt all questions (5×10=50)**

Q. N. 1 Let  $2x+3y+5z = 9$ ,  $7x+3y-2z = 8$  and  $2x+3y+az = b$  be the system of equations. 1.5+1.5+6+1

- (i) What is consistency and how is consistency determined?
- (ii) What is the difference between rank of a vector and matrix?
- (iii) In above case, what can be the values of  $a$  and  $b$  so that the system has unique solution, infinite solution and no solution?
- (iv) How infinite solution is geometrically interpreted?

OR

Given the matrix  $A = \begin{pmatrix} 8 & -6 & 2 \\ -6 & -7 & -4 \\ 2 & -4 & 3 \end{pmatrix}$  1+2+3+4

- (i) State Cayley Hamilton theorem
- (ii) Find the characteristics equation and the eigenvalues for  $A$
- (iii) Verify Cayley-Hamilton theorem
- (iv) Also find an inverse of  $A$  using Cayley-Hamilton theorem

Q. N. 2 Let the infinite series be  $f(x) = \frac{1}{2}x + x^2 + \frac{9}{8}x^3 + x^4 + \frac{25}{32}x^5 + \dots$  2+1+3+4

- (i) What is convergence and divergence in a series? What will be its application in engineering?
- (ii) State P test in testing the convergence and divergence for a series?
- (iii) Use appropriate method with its statement to test the convergence of the given series  $f(x)$
- (iv) Find the interval, center and radius of convergence of the power series  $\sum_0^{\infty} \frac{(n+1)(k-2)^n}{10^n}$

Q. N. 3 Let  $f(x) = \begin{cases} \frac{1}{2} + x; & -\frac{1}{2} < x \leq 0 \\ \frac{1}{2} - x; & 0 < x < \frac{1}{2} \end{cases}$  3+2+5

- (i) What is periodicity and how is it determined? Explain with an example. What is the periodicity of above function?
- (ii) Test whether the given function is odd or even or neither.
- (iii) Find the Fourier series expansion of the given function  $f(x)$

Q. N. 4 Let  $x_1 + x_2 + x_3 \geq 100$ ,  $2x_1 + 3x_2 + 10x_3 \geq 100$ ,  $x_1 \geq 0$ ;  $x_2 \geq 0$ ;  $x_3 \geq 0$ , be the set of linear inequalities 2+3+5

- (i) What is the literal meaning of constructing a dual in simplex problems?

- (ii) If the minimizing function is  $C = 10x_1 + 50x_2 + 20x_3$ , What will be its dual?  
 (iii) Solve the dual problem and obtain the value of C.

Q. N. 5

Given the vector  $\vec{r} = x\vec{i} + y\vec{j} + z\vec{k}$ ,

3+3+4

- (i) Determine the angle between the tangents of the curve  $\vec{r}$  if  $x = t^2$ ,  $y = 3t^2$  and  $z = -(t^2 + 1)$  at  $t = \pm 1$ .  
 (ii) Find the velocity and acceleration if  $x = 3t^2$ ,  $y = t^2 - 4t$  and  $z = 3t + 4$ .  
 (iii) What will be the velocity and acceleration at  $t = 3$  in the direction of  $\vec{t} = 2\vec{j} + 2\vec{k}$

**Group - B: (1×20=20)**

Q. N. 6

i) Define surface integral of  $\vec{F}$  on the surface S. Evaluate  $\iint_S \vec{F} \cdot \hat{n} dA$  where

2+6

$\vec{F} = (x, 2y, 4z)$  and S is the surface of the cone  $\sqrt{x^2 + y^2} \leq z, 0 \leq z \leq 2$

ii) Evaluate  $\oint_C \vec{F} \cdot d\vec{r}$  where  $\vec{F} = \left( y, \frac{z}{2}, \frac{3y}{2} \right)$ , C is the circle of  $x^2 + y^2 + z^2 = 4z$ ,  $z = x + 2$ .

6

iii) If  $F = (2x^2 - 4z)\vec{i} - 2xy\vec{j} - 8x^2\vec{k}$ , then evaluate  $\iiint_V \nabla \cdot F dV$  where V is bounded by the planes  $x = 0, y = 0, x = 0, x + y + z = 1$

6

*Best of Luck!*

POKHARA UNIVERSITY

Level: Bachelor Semester  
Programme: BE  
Course: Engineering Mathematics III

Year : 2021  
Full Marks: 100  
Pass Marks: 45  
Time : 3 hrs.

*Candidates are required to give their answers in their own words as far as practicable.*

The figures in the margin indicate full marks.

*The figures in the margin  
attempt all the questions.*

1. a) Define consistence and inconsistence of a system of linear equations. Check consistence of a system of linear equations,  $5x+3y+7z = 4$ ,  $3x+26y+2z = 9$  and  $7x+2y+10z = 5$  and solve it if possible.

b) Find inverse of A with the help of Cayley Hamilton theorem.

$$A = \begin{pmatrix} 0 & 0 & 1 \\ 3 & 1 & 0 \\ -2 & 1 & 4 \end{pmatrix}$$

2. a) State and Prove hyper-harmonic series (p-Test).  
 b) Find the interval, center and radius of convergence of an infinite series

$$A = \begin{pmatrix} 0 & 0 & 1 \\ 3 & 1 & 0 \\ -2 & 1 & 4 \end{pmatrix}$$

OR

Find the Maclaurian Series representation of  $y = e^{\sin^{-1}x}$  upto  $x^4$  terms.

3. a) Find the Fourier series of the following:

$$f(x) = \begin{cases} x & \text{if } -\frac{\pi}{2} < x < \frac{\pi}{2} \\ \pi - x & \text{if } \frac{\pi}{2} < x < \frac{3\pi}{2} \end{cases}$$

b) Find the Fourier cosine as well as sine series of  
 $f(x) = L - x$  for  $0 < x < L$

4. a) Maximize  $Z = x_1 + x_2 + x_3$ , Subjected to the Constraints  $4x_1 + 5x_2 + 8x_3 \leq 12$ ,  $8x_1 + 5x_2 + 4x_3 \leq 12$ ,  $x_1 \geq 0$ ,  $x_2 \geq 0$ ,  $x_3 \geq 0$   
b) Construct the dual problem.  
Minimize  $Z = 4x_1 + 7x_2$  Subject to  $4x_1 + 4x_2 \geq 20$ ,  $3x_1 + x_2 \geq 21$ ,  $x_1 \geq 0$ ,  $x_2 \geq 0$ , and solve by simplex method.

**POKHARA UNIVERSITY**

Level: Bachelor      Semester: Spring  
 Programme: BE  
 Course: Engineering Mathematics III

Year : 2021  
 Full Marks: 100  
 Pass Marks: 45  
 Time : 3hrs.

*Candidates are required to give their answers in their own words as far as practicable.*

*The figures in the margin indicate full marks.*

*Attempt all the questions.*

1. a) What is the condition of systems of linear equation to have unique solution? Check the consistency and solve

$$x + 3y + 6z = 2, 3x - y + 4z = 9, x - 4y + 2z = 7.$$

- b) State Cayley-Hamilton theorem .Find  $A^{-1}$  by using it if

$$A = \begin{bmatrix} 7 & -1 & 3 \\ 6 & 1 & 4 \\ 2 & 4 & 8 \end{bmatrix}$$

OR

Define Eigen value and vector of a square matrix. Find the Eigen value and corresponding Eigen vector of the matrix

$$A = \begin{bmatrix} 2 & 1 & 1 \\ 1 & 2 & 1 \\ 0 & 0 & 1 \end{bmatrix}$$

- a) The necessary condition for the convergence of an infinite series  $\sum u_n$  is ,  $\lim_{n \rightarrow \infty} u_n = 0$ , but this is not sufficient. Test the absolute convergence of the series  $\sum_1^{\infty} (-1)^{n+1} \frac{n}{n^3 + 1}$ .

- b) Find the center, radius, and interval of convergence of  $\sum_1^{\infty} (-1)^n (2x-1)^n$ .

OR

Find expansion of  $\log(1 + \tan x)$  by using Maclaurins expansion.

3. a) Find the Fourier series of the periodic functions  $f(x) = |x|$  for  $-\pi < x < \pi$  also show that

$$\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots = \frac{\pi^2}{8}.$$

Level: Bachelor  
Programme: BE  
Course: Applied Mech

Candidates are req  
as practicable.  
The figures in the  
Attempt all the qu

1. b) Find Fourier sine as well as cosine series of the function  $f(x) = \pi - x$  for  $0 < x < \pi$ . 8
4. a) Maximize:  $Z = 5x_1 + 4x_2$  Subjected to constraints :  $x_1 + x_2 \leq 20$ ,  
 $2x_1 + x_2 \leq 35$ ,  $-3x_1 + x_2 \leq 12$ . by regular simplex method. 7
- b) Minimize  $Z = x_1 + 8x_2 + 5x_3$  subject to  $x_1 + x_2 + x_3 \geq 8$ ,  
 $-x_1 + 2x_2 + x_3 \geq 2$ .  $x_1 \geq 0, x_2 \geq 0, x_3 \geq 0$  by  
constructing duality method. 8
5. a) Define directional derivative of  $f$  in the direction of  $\vec{a}$ . Find the  
directional derivative of  $f = 4xz^3 - 3x^2yz^2$  in the direction of z-axis at  
 $P(2, -1, 2)$ . 7
- b) State Greens theorem in a plane. By using it evaluate  $\int_C \vec{F} \cdot d\vec{r}$ ,  
where  $\vec{F} = \sin y \vec{i} + \cos x \vec{j}$  and  $C$  is the positively oriented  
triangle with vertices  $(0, 0), (\pi, 0), (\pi, 1)$ . 8
6. a) Evaluate  $\iint_S \vec{F} \cdot n dA$  where  $F = (x^2, e^y, 1)$ ,  $S: x+y+z=1, x \geq 0, y \geq 0,$   
 $z \geq 0$ . 7
- b) State Stokes Theorem, Evaluate  $\oint_C \vec{F} \cdot d\vec{r}$   
Where,  $\vec{F} = (y, \frac{z}{2}, \frac{3y}{2})$ ,  $C$  is circle,  $x^2 + y^2 + z^2 = 6z$  and  
 $z = x+3$ . 8
7. Attempt all questions:
- a) Check the following transformation is linear or not ?  
 $T: R^2 \rightarrow R^2$  be defined by  $T(m, n) = (m, n+3)$  2.5
- b) Test the convergence of series  $\sum \frac{n+1}{2n+3}$ . 2.5
- c) Find the rank of  $A = \begin{pmatrix} 1 & 2 & 4 \\ 3 & 1 & 5 \\ 2 & 4 & 8 \end{pmatrix}$  2.5
- d) If  $\phi = \log(x^2 + y^2 + z^2)$  Find  $\operatorname{div}(\operatorname{grad}\phi)$  2.5

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figure1. Th  
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position 2