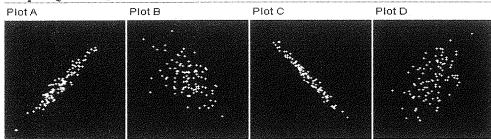
STUDY GUIDE FOR EXAM 2

For each of the topics below look over the relevant problems in your lecture notes and homework.

Chapter 6: Correlation

- Match scatter plots with correlation coefficients. Practice "guessing correlation" game
- Scatter plot has 5 summary statistics: average and SD of the x-values, average and SD of the y-values and the correlation coefficient. Be able to estimate these 5 statistics as well as the SD and the regression line from looking at a scatter plot.
- Compute the correlation coefficient.
- Correlation coefficient is not affected by: adding a constant to all values of one variable, multiplying all values of one variable by a positive constant, interchanging all values of x and y, or changing units (i.e. from inches to centimeters).
- Ecological Correlations are based on averages and tend to be higher than those based on individuals.
- Correlation is NOT causation

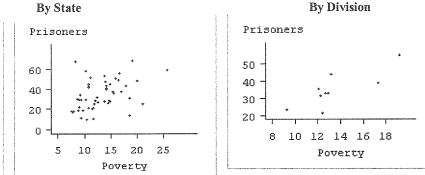
Sample Question on Correlation



1. Write the letter of the plot next to the correlation coefficient that is closest to it.

$$r = 0.52$$
 $r = 0.96$ $r = -0.99$

2. The following scatter plots show the relation between poverty level (percentage of people living below the poverty line) and number of prisoners (per 100,000 people) by state and by geographical region. The graph on the left has 50 points, one for each **individual** state's poverty and prisoner level. The graph on the right has the same information condensed into 9 points, one for each of the 9 geographical regions. (In other words, the 50 states were divided into 9 geographical regions. The average poverty and prisoner level was computed for each region.)



- a)The correlation coefficient for the graph on the left is 0.4. The correlation for the graph on the right is i) less than 0.4 ii) equal to 0.4 iii) greater than 0.4
- b) The scatter plots above are an illustration of
 i) The Regression Effect ii) Simpson's Paradox iii) Ecological Correlation iv) Negative Correlation

3. Compute the correlation coefficient between X and Y by filling in the table below. The average of X = 4 and the SD of X = 2 and the average of Y = 4 and the SD of Y = 2.

X	Y	X in Standard Units	Y in Standard Units	Products
	2			
1	3		The state of the s	
3	1			
4	5			
5	4			
7	7			
,	, ,			

a) The correlation coe	fficient =					
b) If all the y values a i)stay the same	re increased by ii)increase	3 the correlation coeffii)decrease	ficient would			
c) If all the y values a i)stay the same	re doubled the ii)double	correlation coefficient ii)decrease	would			
d) If BOTH the x and y values are all multiplied by -1 then the correlation coefficient would i) stay the same ii) change sign						
e) If all the X and Y values were switched the correlation coefficient would i)stay the same ii)increase ii)decrease						
f) If the top and botto same. Would the corr			ed, the average and the YES	SD of x would stay the NO		

Question 4 pertains to the scatter plot below which shows the exam and final scores for 107 students in a previous Stat 100 class. X-Variable Final Gender 100 HW Labs InClass Exams Final Total Y-Variable 50 Gender HW Labs InClass Exams Final 70 80 90 100 Total 85 a) The average exam score is around 74 b) The average final score is around 85 90 74 Line 1 c) Which is the regression line? Line 2 d) If a student was exactly average on both the exam and the final which line would he fall on? Only the SD Line Only the Regression Line Neither e) If a student was exactly 1 SD above average on both the exam and the final which line would he fall on? Only the Regression Line Both Neither Only the SD Line f) The correlation between exam and final score is closest to -0.20.6 g) The prediction error for Obs 3 is closest to -5 -15 15 -20 h) If a new scatter plot was drawn with 10 pts. added to everyone's final score then the correlation between exam and i) increase ii) decrease iii) stay the same final scores would_ i) If a new scatter plot was drawn with 10 % added to everyone's final score then the correlation between exam and final scores would i) stay the same ii) decrease iii) increase j) The following 3 numbers: 0, 10.27 and 8.25 are, in scrambled order, the SD of the final, the average of the prediction errors and the SD of the errors (when predicting final from exam.) Write the number next to its description. i) average of the errors_ ii) SD of the final iii) SD of the errors k) If Obs 3 was removed, the correlation coefficient would i) stay the same ii) decrease iii) increase

Chapter 7: Regression

- Know which is the regression line and which is the SD line. (The regression line is always less steep.)
- Computing the regression estimate given the 5 summary statistics by converting independent variable to Standard Units, multiplying by r and then converting back to the units of the dependent variable
- Computing the regression estimate for percentiles
- The regression effect and the regression fallacy.

Sample Questions on Regression

- 1. A large group of high school students took the ACT twice. The averages and the SDs of both the first and the second sets of ACT scores were the same: Ave = 20 SD= 5 and the The scatter plot was foot-ball shaped. correlation was r = 0.8
 - a) Predict the 2nd ACT score of someone who got a 15 on the first ACT. (Use the 3 step procedure. Show work.)
 - b) A student got a 15 on his first ACT and an 18 on his second ACT. What is the prediction error (when predicting 2nd ACT from 1st ACT)?_____
 - c) A group of students all got 30on their first ACT. Estimate what their average 2nd ACT score would be. (You may use either the 3 step procedure or the regression equation. Show work)

d) Of course, they won't all get exactly the score you predicted them to get in your answ to (c). But about 2/3 of those who scored 30 on their first ACT will get between	wer
andon their second ACT.	
(Show work)	

- 2. For a past Stat 100 class the correlation between Exam 1 and Exam 2 was r=0.6 and the scatter plot was football-shaped.
- a) If a student scored in the 95th percentile on Exam 1, estimate his Exam 2 percentile. (Draw a picture. Show work You may round z scores to fit the closest line on the table and you may round percents on the table to the nearest whole number.)

- b) If there was NO correlation between Exam 1 and Exam 2 scores then what would be your estimate for the Exam 2 percentile of someone who was in the 95th percentile on Exam 1?
- c) If there was a perfect correlation (r=1) between Exam 1 and Exam 2 scores then what would be your best estimate for the Exam 2 percentile of someone who in the 95th percentile on Exam 1?

_percentile

- d) If a student scored below the 50^{th} percentile on Exam 1 and r = 0.6, then the best estimate for his Exam 2 percentile is
- i) Above 50^{th}
- ii) 50^{th}
- iii) Below his Exam 1 percentile
- iv) Above his Exam 1 percentile but below 50th
- e) Students who did the best on Exam 1 did somewhat worse on Exam 2 and students who did the worst on Exam1 did somewhat better on Exam 2. This is an example of
 - i) Ecological correlations
 - ii) The Regression effect
 - iii) Negative correlation
 - iv) Simpson's paradox

Chapter 8: Prediction Errors

- Prediction Error = Actual Y value- Predicted Y value
- Average of the Prediction Errors is ALWAYS 0
- SD of the Prediction Errors gives the size of the typical error and is calculated by SD of errors= $\sqrt{1-r^2}$ SD of y
- If the scatter plot is roughly elliptical about 2/3 of the predictions will be within 1 SD arror, and 95% will be within 2 SD errors.

Chapter 9: Equation of the Regression Line

- Know how to calculate the slope and the intercept of the regression line. p.207 #3
- Slope of the regression line for predicting y from x is r (SD of y)/(SD of x).
- Intercept may be solved for, since you know the point of averages is always on the line.
- Make predictions using the equation for the regression equation. P.207 #1,2

Sampl

le questions on Predicti	on Errors an	nd the Equation	n of the Reg	ression Line			
			es were recorded	d. Here are the 5 summary statistics:			
Average Age of Husband Average Age of Wives = 4		The scatter p	lot was foot-ball shaped.				
a) The slope of the regression equation for predicting a husband's age from his wife's age is							
i) 0.9	ii)2/3	iii) 3/2	iv) .6	v) 1.35			
b) The y-intercept of the regression equation for predicting a husband's age from his wife's age is							
i) -13	ii) 21	iii) - 9	iv) 4	v) 0			
 c) In the study, husbands of year old men have an average of the regression equation. d) The regression equation. Wife's Age = (0. 	age age of 60? for predicting :	YES a wife's age from	NO	ears. Can you conclude that wives of 72			
One wife in the study has a	husband who is	35 years old. He	ow old would yo	ou estimate her to be?			
e) There's about a 2/3 chance that your estimate in (d), give or takeyears is right.							
i) $\sqrt{1-0.9^2} * 10$	ii) √1-	-0.9 ² * 15	iii) 10	iv) 15			
f) Suppose you don't know the husband's age, what is your best guess for the age of a wife you've never seen?							
g) There's about a 2/3 charmi) $\sqrt{1-0.9^2} * 10$							

Chapter 10: Chance

- Chance of an outcome = # of that outcome/total # of possibilities
- Chance of something = 100% Chance of the opposite
- Multiplication Rule- The chance that 2 events will both happen = (Chance that the first will happen) x (Chance that the second will happen, given that the first has happened)
- If a situation involves 2 or more conditions (e.g. diagnostic tests) a table is helpful

Sample Questions:

- 1. What is the chance of getting no heads on 4 tosses of a fair coin?
- 2. What is the chance of getting at least 1 head?
- 3. A die is rolled 3 times. What is the chance of getting no 4's?
- 4. What is the chance of getting at least one 4?
- Independence/Dependence- 2 events are independent if the chance of one event does not change if the other event happens. They're dependent if the chance of one changes depending on whether the other happened or not.

Sample Questions (Independence):

- 5. What is the chance that the first 10 flips of a fair coin are all heads?
- 6. What is the chance that the 11th flip is a head?_____ What is the chance that the 11th flip is a tail?_____
- 7. A box contains 5 tickets--2 reds, 2 blues and 1 white. Two draws will be made with replacement from the box.
- a. Suppose the first draw is a red ticket. What is the chance of getting a blue ticket on the second draw?
- b. Suppose the first draw is a blue ticket. What is the chance of getting a blue ticket on the second draw?
- c. Are the draws independent?

Sample Questions (Dependence):

8. Do #7a-c again, this time drawing without replacement.

Chap 10 cont.

- 9. Shuffle a deck of 52 cards. What is the chance that the first 2 cards are hearts?
- 10. A drawer contains 4 red socks and 6 white socks. If 2 socks are chosen at random without replacement, what is the chance that both will be white?
- 11. Two draws are made at random from a box containing the numbers 1, 2, and 3. What is the chance of getting a 1 at least once?

C.

- a) with replacement
- b) without replacement
- 12. Randomly choose one card from a deck of 52.
- a. What is the chance that the card is a heart?
- b. What is the chance that the card is a heart given that it is an ace?
- c. Is getting a heart independent of getting an ace?
- 13. If you draw 2 cards what is the chance that both are hearts?
- a. with replacement
- b. without replacement

Problems with 2 or more conditions—It's useful to draw a table.

- 14. There are 10 cans of Coke and 10 cans of Pepsi in a cooler.
- 2 of the Cokes are diet and 5 of the Pepsis are diet.

- a. You draw 1 can at random from the cooler. What is the chance that it is diet?
- b. You draw 2 cans at random without replacement, what is the chance that both are diet?
- c. You draw 1 can, what is the chance that it is diet given that it is Coke?
- d. You draw 1 can, what is the chance that it is Coke given that it is Diet?

Chap 10 cont.

15. Suppose 10% of men aged 70 in routine screening have prostate cancer. Further suppose that a diagnostic test is 95% accurate in correctly giving a positive result for those who have cancer and also 95% accurate in correctly giving a negative result to those who do *not* have cancer.

- a) What's the chance that a 70 year old man who gets a positive result truly has cancer?
- b) Suppose 50% of 90 year old men have cancer. What's the chance that a 90 year old man who gets a positive result truly has cancer?

Chapter 11: More on Chance, the Addition Rule

- Be able to figure the chance by counting all possible way a chance process can turn out. Then figure the chance of an event by (# of that event)/(# of total possibilities).
- Addition Rule- used to figure the chance that **either** of 2 events occurs. If the 2 events are mutually exclusive, simply **add** the chances. If the 2 events are not mutually exclusive, add the chances and then subtract the chance that both occur.
- To figure the chance that at least one of several events happen, it is often easier to calculate the opposite and subtract from 100%.

Sample Questions:

- 1. What's the chance of rolling 2 dice and getting doubles? (Doubles means having both dice show the same number of spots.
- 2. What's the chance of drawing 1 card from a fair deck and getting either a face card or a 7?
- 3. What's the chance of rolling 2 dice and getting either doubles of a sum of 8?
- 4. What's the chance of rolling 2 dice and getting either doubles or a sum of 9?