A New Approach to Understanding Age–Related Memory Impairments

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We test three influential theories of age—related changes in memory function: the Associative Deficit Hypothesis, the Inhibitory Deficit Hypothesis, and the Cognitive Slowing Hypothesis. By translating these verbal theories into a quantitative model we test their ability to account for the complex pattern of preserved and impaired episodic memory shown by older adults on the free recall task. We do this within the framework of the context maintenance and retrieval model of memory search, which accounts for many detailed aspects of memory performance in younger adults. Simulations show that the theories have difficulty simultaneously accounting for the key age effects. We develop a novel theory that does account for the data and implicates four factors: 1) the ability to sustain attention across an encoding episode, 2) the ability to retrieve contextual representations for use as retrieval cues, 3) the ability to monitor retrievals and reject intrusions, and 4) the level of noise in retrieval competitions.

As we grow older many aspects of our cognitive functioning change. Some aspects like verbal ability (Verhaeghen, 2003), social skills (Carstensen, Isaacowitz, & Charles, 1999) and possibly wisdom (Baltes & Staudinger, 2000) show welcome increases. Unfortunately, most aspects of cognition show age-related declines rather than improvements (Baltes & Lindenberger, 1997; MacDonald, Dixon, Cohen, & Hazlitt, 2004; Park et al., 2002; Zelinski & Burnight, 1997). Perhaps the most salient of these declines occur in episodic memory, as revealed both by selfreports (Newson & Kemps, 2006; Zacks, Hasher, & Li, 2000) and laboratory studies (Craik & Jennings, 1992; Kausler, 1994; Light, 1991; Moscovitch & Winocur, 1992; Provyn, Sliwinski, & Howard, 2007; Salthouse, 1991). The central role played by episodic memory in aspects of cognition ranging from autobiographical recall (Levine, Svoboda, Hay, Winocur, & Moscovitch, 2002) to abstract reasoning (Healey, Crutchley, & Kahana, submitted; Mogle, Lovett, Stawski, & Sliwinski, 2008; Unsworth, 2009) make agerelated declines particularly disturbing. Therefore, as the av-

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phone: (215) 746–3500 Version of October 1, 2013 21975 Words (Approximate due to use of LATEX) erage life span lengthens, developing interventions to prevent, slow, or reverse age-related memory decline has become one of the most important challenges facing cognitive science.

Success in developing such interventions will require a detailed understanding of how and why memory changes with age. Over the last several decades the field of cognitive aging has provided a detailed description of *how* memory changes with age by comparing older and younger adults on a wide variety of memory tasks, as detailed in multiple thorough reviews (Craik, 1977; Craik & Rose, in press; Kausler, 1994; Light, 1991; Lindenberger & Ghisletta, 2009; Salthouse, 1991; Zacks et al., 2000). The field, however, has not yet converged on a common theoretical account of *why* these changes occur.

The dominant approach to theory development has been to propose a cognitive process that may deteriorate with age and then develop a set of paradigms to test and refine that proposal. This approach has led to many candidate mechanisms being considered (for very different contemporary accounts see Bender, Naveh-Benjamin, & Raz, 2010; Benjamin, 2010; Craik, Luo, & Sakuta, 2010; Hasher, Lustig, & Zacks, 2007; Lindenberger & Ghisletta, 2009; Werkle-Bergner, Freunberger, Sander, Lindenberger, & Klimesch, 2012; West, 1996; Yassa, Mattfeld, Stark, & Stark, 2011). Such research programs naturally tend to examine those aspects of task performance most relevant to the proposed memory mechanism, thereby developing a set of benchmark empirical effects against which to test the theory.

Developing a set of specialized experimental paradigms is necessary to determine if a particular mechanism is a plausible locus of cognitive decline. A side effect, however, is that different theoretical perspectives gradually became focused on explaining different sets of benchmark findings, making it difficult to compare the various theoretical perspectives to determine which cognitive mechanisms are critical in accounting for the broader pattern of age—related change. That is, it is unclear if any of the proposed impairments provide a complete account of why memory changes with age.

We take the complementary approach of focusing on detailed measures of performance in a single paradigm, free recall. As reviewed in detail below, the free recall task reveals a complicated pattern of both preserved and impaired aspects of episodic memory performance. Older adults show a deficit in the overall number of items retrieved. But show no deficit in initiating recall and continue to exhibit primacy and recency effects. Older adults do, however, show a deficit in using new temporally—defined (i.e., episodic) associations to guide recalls. Older adults also produce many more intrusions than younger adults, both of words from prior lists and of words never presented in the experiment. The ability of most existing aging theories to account for this detailed pattern has not been extensively tested, making free recall an ideal paradigm with which to compare the theories.

The complexity of the pattern of age differences revealed by free recall makes it difficult to determine if a given theory can fully account for the pattern. To make this complexity tractable, we use a computationally explicit theory of healthy episodic memory as a starting point and test aging theories by "lesioning" this healthy model memory system. We can then compare simulated data from the lesioned model with data from older adults, to determine which memory processes are critical in producing age effects.

Aging and Memory Change: The Data and The Theories

Much of the early work on cognitive aging compared the performance of older and younger adults on the major laboratory paradigms that had been developed in the broader memory literature (Craik, 1977). This work revealed a hierarchy of impairment: recognition tasks showed minimal age deficits (Erber, 1974; Schonfield & Robertson, 1966), cued recall tasks showed moderate deficits (Smith, 1977), and free recall showed large and robust deficits (Craik, 1968; Hultsch, 1969; Schonfield & Robertson, 1966). This basic pattern has been well supported over the decades (Verhaeghen, Marcoen, & Goossens, 1993).

The gradient of age impairments across recognition, cued recall, and free recall led to one of the most influential early frameworks for thinking about age—related memory impairments: the environmental support framework of Craik and colleagues (Craik, 1977; Craik et al., 2010). The environmental support framework begins with the assumption that the processes underlying encoding and retrieval require cognitive resources. Absent external cues, participants must "self-initiate" processing to generate retrieval cues, or to refine vague cues. Self-initiated processes are assumed to be highly resource demanding. Tasks that provide strong ex-

ternal cues, such as recognition, reduce the load placed on self-initiated processes and thus make the task less resource demanding. If a task requires more self-initiated processing than can be accommodated by a participant's available resources, performance decrements will be seen, a claim that has been supported in young adults by imposing a secondary task during retrieval (N. Anderson, Craik, & Naveh-Benjamin, 1998). If one assumes that cognitive aging reduces the available resources, this framework elegantly accounts for the hierarchy of impairments older adults show on recognition, cued recall, and free recall.

The finding that the sizes of age effects track the specificity of retrieval cues is perhaps the broadest and best supported generalization one can make about aging and memory and is consistent with data from a variety of memory tasks. For example, semantic memory, when measured using vocabulary tests such as the Shipley (1946) test or the WAIS-R, is generally unimpaired (Verhaeghen, 2003). These tests, however, provide very strong and direct retrieval cues. Fluency tasks also measure semantic memory, but do so using a less–focused retrieval cue. For example, in category fluency tests a participant may be given 60 seconds to generate members of the category "animals". Fluency tasks generally show small but consistent age decrements (Loonstra, Tarlow, & Sellers, 2001; Troyer, Moscovitch, & Winocur, 1997).

Priming shows a similar pattern of cue-dependent age effects. Older adults tend to show intact priming, especially when the possibility for explicit retrieval attempts is minimized (Mitchell & Bruss, 2003). Notice that priming tasks generally provide an unambiguous cue; a particular recently presented item (e.g., bread) provides a clear cue for the primed item (e.g., butter). If, instead, several primes cue the target, older adults begin to show deficits. For example, Ikier, Yang, and Hasher (2008) had participants count the vowels in a list of words that included orthographically similar pairs (e.g., ALLERGY and ANALOGY). A later task required participants to complete word fragments that resembled both words but could actually be completed by only one (e.g., a _ l _ _ gy). Both older and younger adults showed priming in a control condition in which only the correct solution had appeared in the vowel counting task, allowing it to provide an unambiguous cue for the fragment. When both words are presented, however, there is an ambiguous cue and older adults now show reduced priming relative to younger adults.

One of the main weakness of the environmental support framework is that the notion of "resources" is very vague. Therefore, a major focus of the cognitive aging literature over the past 30 years has been to identify specific cognitive processes that become dysfunctional with age.

The processes that have been advanced as the locus of age decrements range from basic perceptual processes (Baltes & Lindenberger, 1997; Lindenberger & Ghisletta, 2009;

Pichora-Fuller, Schneider, & Daneman, 1995), to representational fidelity (Benjamin, 2010), to processes subserved by the frontal lobes (e.g. the frontal theory of aging, West, 1996), to the ability to conduct pattern separation in the hippocampus (Stark, Yassa, & Stark, 2010; Yassa et al., 2011). Several of these theories have gained considerable support and led to groups of researchers working on issues related to that perspective. To illustrate, we will focus on three of the most prominent aging theories: the Associative Deficit Hypothesis (Naveh-Benjamin, 2000), the Inhibitory Deficit Hypothesis (Hasher & Zacks, 1988), and the Cognitive Slowing Hypothesis (Salthouse, 1996). We choose to focus on these three theories for two key reasons. First, they are well established and widely viewed as foundational. Second, each makes clear claims about the locus of age deficits (cf. other theories that are more descriptive).

We review each of these literatures next. Our aim is to show that starting from the basic environmental support observation, the field of cognitive aging has diverged along a number of empirical paths, each guided by a different theoretical perspective. Although there have been some attempts to use ideas from one theoretical perspective to account for findings from another (e.g., Campbell, Hasher, & Thomas, 2010; Craik et al., 2010), for the most part the theoretical perspectives have come to focus on explaining largely non-overlapping empirical benchmarks. Our suggestion is that the field will benefit from exploring the extent to which the different theories can explain a neutral set of benchmark findings.

Associative Deficit Hypothesis (ADH). Naveh-Benjamin (2000) suggested that older adults are selectively impaired in the ability to form (or use) new associations. This hypothesis was based on a body of evidence from the 1980's and 1990's that revealed the broad generalization that recognition memory remains intact with age to be an oversimplification. Standard recognition tasks require a simple decision of whether a probe item was among a study set. Researchers in the broader memory literature began devising recognition tests that required more subtle distinctions, such as whether a given item was presented in a particular location in the display array or whether two items were paired together at study. Compared to younger adults, older adults showed a disproportionally large drop in performance on these associative tasks (Chalfonte & Johnson, 1996).

Naveh-Benjamin (2000) solidified this evidence with a series of novel experiments designed to decouple memory for items and memory for associations. For example, in one experiment participants had to study word–nonword pairs followed by an associative recognition test that required responding "old" to intact pairs (pairs in which the word and nonword had been paired at study) but not to rearranged pairs (i.e., pairs in which both the word and nonword had been

studied but in different pairs). Compared to control conditions in which items but not associations had to be recognized, older adults showed a disproportionate associative deficit.

Support for a selective deficit in associations has come from a variety of tasks that contrast memory for items with memory for associations. These include contrasting tasks that require memory only for the identity of an item with tasks that require memory both for the item and perceptual characteristics of the item (e.g., was this item presented in this particular font) or for face/name pairs (Naveh-Benjamin, Guez, Kilb, & Reedy, 2004). Other work has examined the selective effects of various manipulations on item versus associative memory, such as repetition (Kilb & Naveh-Benjamin, 2011; Overman & Becker, 2009) and the use of strategies (Naveh-Benjamin, Bray, & Levy, 2007).

Many different types of associations have been found to be impaired with age. A meta-analysis by Old and Naveh-Benjamin (2008) identified 6 types of associations: memory source (e.g., which of several voices presented an item), item-feature bindings (e.g., the font of the item), temporal order (e.g., which item was presented first), location (e.g., which part of the display the item appeared in), item-item pairings (e.g., intact versus rearranged word pairs), and presentation modality (e.g., visual versus auditory presentation). All but presentation modality were found to show a selective associative deficit.

Inhibitory Deficit Hypothesis (IDH). Hasher and Zacks (1988) reviewed evidence that across a diverse set of tasks and materials, age deficits tend to be disproportionately large in situations that require overcoming interference. In many cases the interference is proactive interference from earlier in the task, but there is also evidence that older adults have difficulty dealing with distraction that is perceptually present (Gazzaley et al., 2008; Lustig, Hasher, & Tonev, 2006). Early formulations of the theory suggested that inhibition was an attentional mechanism that regulated the flow of information into and out of working memory. More recent formulations do not assume a dual–store model of memory (Healey, Campbell, Hasher, & Ossher, 2010; Healey, Hasher, & Campbell, in press; Healey, Ngo, & Hasher, in press).

Early work validating the theory focused on finding evidence that reducing the amount of interference on a memory task reduced or eliminated age differences (May, Hasher, & Kane, 1999). More recently, researchers have been pursuing evidence that distraction can actually have a beneficial impact on some tasks, such as creativity tasks in which the distracting information can aid in arriving at novel solutions (for a review see Healey, Campbell, & Hasher, 2008). This work has even been extended to show that under certain circumstances exposure to distraction can benefit older adults on memory tasks (Biss, Ngo, Hasher, Campbell, & Rowe, 2013; Campbell et al., 2010; Campbell, Zimerman, Healey,

Lee, & Hasher, 2012).

Research on the IDH has resulted in an extensive toolbox of paradigms specifically tailored to detecting signs of vulnerability to interference. Complex span tasks (Daneman & Carpenter, 1980; Turner & Engle, 1989) have been used to determine how proactive interference influences age differences in memory span (May et al., 1999; Rowe, Hasher, & Turcotte, 2008). Garden path sentences, in which the initial part of the sentence suggests an ending (e.g., "She ladled the soup into her _____"), have been used to show that older adults are less able than young adults to suppress disconfirmed endings. For example, when given the unexpected ending of "lap", older, but not younger, adults retain access to the disconfirmed ending (Hamm & Hasher, 1992; May & Hasher, 1998). Fragment completion tasks have been used to show that older adults suffer from interference in priming tasks (Ikier et al., 2008) and fail to suppress competitors during interference resolution (Healey, Hasher, & Campbell, in press). Situation modeling tasks (e.g., remembering a series of object-location pairings) have been used to investigate the role of fan size in age differences (Copeland & Radvansky, 2007). In neuroimaging work selective remembering tasks which require participants to attend to only certain sections of a display or certain items in a series have been used to study neural signatures of the suppression of irrelevant stimuli (Gazzaley et al., 2008; Werkle-Bergner et al., 2012).

Note that the interference and transfer tasks developed to test the IDH differ considerably from the complex recognition tasks developed to test the ADH. Although there have been some attempts to devise paradigms that pit the two theories against each other (e.g., Campbell et al., 2010), the ecosystems of tasks that have grown around each theory are so different that it is almost impossible to rigorously assess the ability of one theory to account for the empirical base of the other.

Cognitive Slowing Hypothesis (CSH). Salthouse (1996) laid out a detailed case that aging is associated with a general reduction in the speed with which cognitive processing occurs. Unlike the IDH and the ADH, which arose from experiments showing interactions between a manipulation and age group (e.g., that age differences grow disproportionally with the level of interference), the CSH arose from large-scale psychometric studies that correlated age with performance on a wide range of tasks. studies generally find that most cognitive abilities, with the exception of those measuring crystalized intelligence (e.g., vocabulary tests) decline with age (Darowski, Helder, Zacks, Hasher, & Hambrick, 2008; Park et al., 2002, 1996). Among the tasks that show declines are those that require carrying out some simple operation; generally, some sort of perceptual task that requires little use of memory or reasoning, as quickly as possible (Hertzog, Dixon, Hultsch, & MacDonald, 2003; Park et al., 1996; Salthouse, 1993). For

example, the digit symbol substitution test (a component of the WAIS IQ test) shows participants a table of digit-symbol pairs. They are then shown a list of digits and must write the corresponding symbol for each as quickly as possible (the coding table is always available to them).

Salthouse (1996) proposed two primary mechanisms by which slowed processing could lead to deficits on tasks like recall. The first is the limited time principle: If a task limits the amount of time a participant has to make a response, slowed cognitive processing makes it less likely that the required processing can be completed before the time limit. The second mechanism is the simultaneity principle: Slowed processing can be devastating in a system that depends on information from different subsystems being available at precisely the same time. An assumption here is that many tasks require the products of early processing stages to be available at the same time so that a later processing stage can operate on both simultaneously.

The primary evidence that reductions in processing speed underlie age differences on memory tasks comes from statistically controlling for age—related declines in these speed tasks and then determining whether any age—related differences remain on memory tasks. Across many studies it has been found that controlling for speed reduces the correlation between age and memory. For example, in a meta—analysis Verhaeghen (2011) found that processing speed explained almost 70% of the variance shared between age and episodic memory performance.

This overview of cognitive aging theories is far from comprehensive. Among much else, we have omitted important work on the motivational factors that influence age difference (Carstensen et al., 1999; May, Rahhal, Berry, & Leighton, 2005), task conditions that can mitigate age differences (Castel, 2005), age differences in strategy generation and implementation (Dunlosky & Hertzog, 1998), and age differences in meta-memory (Hertzog & Dunlosky, 2011). Our overview does, however, capture the major thrust of theory development in the cognitive aging literature.

A Fragmented Empirical Landscape

In addition to implicating very different cognitive mechanisms, the literatures surrounding each of the major aging theories focus on a particular set of paradigms and analytical methods. For example, the ADH literature makes extensive use of various modifications of associative recognition tasks as they allow for teasing apart subtle distinctions between item and associative memory. The IDH literature relies heavily on transfer paradigms as they allow tests of the conditions under which older and younger adults consider irrelevant information from previous tasks during the current task. The CSH literature uses large sample size studies and sophisticated analytical procedures to detect statistical factor structures that would be impossible to detect with experimental

methods.

The great advantage of this methodological specialization is that it has allowed researchers to efficiently test their theory's key predictions, discover boundary conditions, and refine the theory. A side effect, however, is that the set of methodological tools employed within each of these literatures has shaped the empirical landscape within which theorists operate. Thus, there is a risk that the literatures surrounding different theories will slowly drift apart and their explanatory scope (i.e., the body of benchmark findings they attempt to account for) will grow increasingly nonoverlapping. Were this sort of drift to occur, it would compromise the broader goal of cognitive aging research, which is to discover which cognitive processes account for the overall pattern of age effects across memory tasks. In other words, whereas methodological specialization is well-suited to determining if a particular cognitive process is necessary to account for a particular finding, it is not well suited to determining if that process is sufficient to explain the broader

Therefore we suggest a complementary approach, which we hope can bring the theories into close contact. Specifically we propose to put the theories on a level playing field by testing their ability to account for the details of a common task. A task chosen for this purpose should meet several criteria. First, it should not be a task that has been a major focus of any of the theories, so that no theory has an advantage. Second, the task should provide rich data on age differences—that is, the more complex the pattern of age differences revealed by the task, the more easily the theories can be distinguished from each other. The free recall task is a good choice on both criteria. Although free recall has received relatively little attention from aging theorists, it has been the subject of extensive empirical investigation that has revealed a complex pattern of age effects with both impaired and spared aspects of performance.

Aging and Free Recall

One of the earliest and clearest findings in cognitive aging research was that older adults are impaired on the free recall task (Ceci & Tabor, 1981; Craik, 1968; Hultsch, 1969; Laurence, 1967; Schonfield & Robertson, 1966).

Examination of the dynamics of free recall reveals a detailed picture of episodic retrieval and a complex pattern of age effects. Serial position curves are shown in Figure 1A. The older and younger and older adult SPC are qualitatively similar, with both groups showing clear primacy and recency effects (Kahana, Howard, Zaromb, & Wingfield, 2002). But older adults have lower recall levels across the SPC (Capitani, Della Sala, Logie, & Spinnler, 1992; Foos, Sabol, Corral, & Mobley, 1987; Parkinson, Lindholm, & Inman, 1982; Poitrenaud, Moy, Girousse, Wolmark, & Piette, 1989; Rissenberg & Glanzer, 1987).

More subtle age differences are revealed by decomposing the retrieval sequence into measures of how recall is initiated and measures of how transitions are made among items after initiation (Kahana et al., 2002). Probability of first recall (PFR) curves (Hogan, 1975; Howard & Kahana, 1999; D. Laming, 1999) show the probability of initiating recall at each serial position. Older and younger adults' PFR curves are virtually identical (Figure 1B), with both groups tending to initiate recall with the final item. After initiation, recalls are driven by associations between the just-recalled word and other words in the lexicon.

Temporal associations exert a powerful influence on transitions for younger adults (Kahana, 1996). Given that the item from position i has just been recalled, conditional response probability (lag-CRP) indicates the probability that item i + lag will be recalled next. Lag-CRPs show the *conti*guity effect, a tendency to successively recall neighboring list items, and the asymmetry effect, a tendency to recall items in forward order, regardless of variables such as presentation modality or encoding task. The idea of temporal contiguity captures the core of episodic memory—the ability to reconstruct the sequence of past events and thereby place them on an autobiographical timeline. There is also evidence that the ability to reproduce temporal order is a key element, not just in memory tasks, but complex cognition more broadly. As the extent to which young adults show temporal contiguity is correlated with general cognitive ability, as measured by WAIS IQ (Healey et al., submitted).

Older adults show reduced contiguity (Figure 1C), indicating that they are less influenced by temporal associations (Kahana et al., 2002). Note that age differences are especially pronounced for lags of +1 and -1, with older adults being less likely to make these close temporal transitions. This reduced ability to use temporal information could make it difficult for older adults situate events in time and impair autobiographical recall. If so, a temporal contiguity deficit is likely a large part of what makes memory difficulties so troubling for older adults. As we will see, it is this temporal contiguity deficit that poses the greatest challenge to aging theories.

Intrusion errors refer to recall of items that were not on the target list. Prior-list intrusions (PLIs) come from a previous study list in the session whereas extra-list intrusions (ELIs) were not studied on an earlier list. Older adults show increased rates of both types (Figure 1D). When PLIs occur, they tend to be words from recent lists—a PLI recency effect. Figure 1E shows that both older and younger adults show this effect, mirroring the finding that older adults have preserved recency as measured by PFR curves.

Our Approach to Theory Building

Figure 1 provides a set of benchmark free recall age effects that a complete theory of cognitive aging must account for.

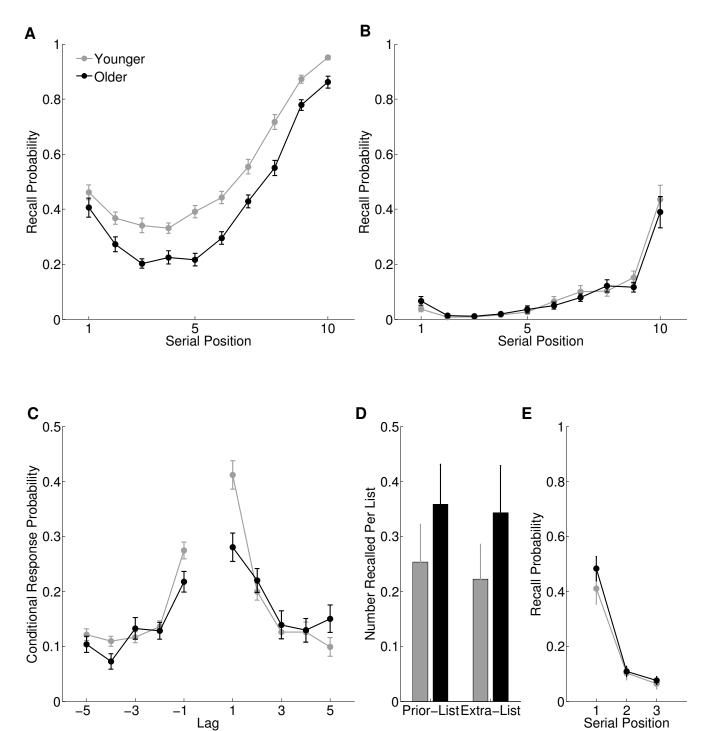


Figure 1. The Free Recall Aging Pattern: Serial position curve (A), probability first recall function (B), lag-conditional response probability function (C), Prior–list and Extra–list intrusions (D), and Prior–list intrusion recency effect. Error bars represent one standard error of the mean. Data from Kahana et al. (2002).

The complexity of the pattern makes it an ideal benchmark against which to test the sufficiency of the leading single–factor theories. That is, because the free recall pattern includes multiple effects that show both impairments and sta-

bility across age groups that are not obviously generated by a common mechanism, it provides a strong test of a theory's ability to account for a diversity of findings.

While necessary to provide a reasonable test of the the-

ories, this level of complexity makes it difficult to evaluate the theories' ability to account for the pattern. When considering univariate measures of performance such as overall accuracy (e.g., percent recall) it is relatively easy to check a theory's predictions against the data with simple thought experiments. For example, one can easily intuit that failing to inhibit words from previous lists will make it hard to selectively retrieve items from the current list, lowering overall recall. However, the multivariate nature of the measures in Figure 1 makes such thought experiments more difficult—it is difficult to intuit if or how the effect of reduced inhibition would vary with serial position. Thought experiments become intractable when trying to consider several multivariate effects at once (e.g., how can reduced inhibition simultaneously lower non-recency portions of the SPC while leaving recall initiation intact but making near temporal transitions less likely). The difficulty is magnified if we are interested in testing the ability of a theory to capture the quantitative level of the effects (e.g., not just predicting that older adults' SPCs are lower than younger adults', but predicting precisely how much lower they are).

A similar problem faced the researchers working on episodic memory in younger adults—the complex pattern revealed by recall dynamics functions was difficult to convincingly account for with verbal theorizing. To a large extent this problem was solved by developing formal models of benchmark effects in a small number of laboratory paradigms. This modeling work has led to a broad consensus about many fundamental aspects of memory such as the importance of context-based cues in retrieval (e.g., Bower, 1967; Davelaar, Goshen-Gottstein, Ashkenazi, Haarmann, & Usher, 2005; Estes, 1955; Farrell, 2012; Howard & Kahana, 2002; Lohnas, Polyn, & Kahana, submitted; Mensink & Raaijmakers, 1988; Murdock, 1997; Polyn, Norman, & Kahana, 2009; Sederberg, Howard, & Kahana, 2008). We can leverage this existing computational framework to help make the complexity of the free recall aging pattern tractable.

Moving to a formal modeling framework aids our goal of pitting the theories against each other in another way. A theory of age-related impairments must be embedded within a broader theory of healthy memory. The task of comparing the explanatory power of different theories will be much easier if the theories are embedded in a common theory of healthy memory. That is, to make a fair comparison among aging theories we must evaluate them within the same theoretical framework.

Theorizing in cognitive aging generally follows a disease model in which it is assumed that the cognitive systems of older adults can be characterized as a version of the younger adult cognitive system in which one or more mechanisms are dysfunctional (for a somewhat different approach see Carstensen et al., 1999; Zimmerman, Hasher, & Goldstein, 2011). This view of aging is particularly well suited to testing

within a computational model of younger adults' episodic memory. We can begin with a model that accurately simulates the performance of younger adults. Then, for a given aging theory we can identify which memory mechanisms are implicated by the theory and then "lesion" the corresponding model mechanisms, and use the lesioned model to generate simulated data: If the theory is accurate the simulated data should resemble that of older adults.

The IDH, ADH, and CSH have not made strong commitments about the nature of the underlying memory system at the computational level, which leaves us with a choice about how to develop computational implementations of the theories. Although some aging work has used models, this work has generally either developed novel models designed specifically to account for age effects (Benjamin, 2010; Li, Naveh-Benjamin, & Lindenberger, 2005) rather than using extensively tested and validated models of the tasks in question or used existing models (e.g. Ratcliff, Thapar, & McKoon, 2004; Surprenant, Neath, & Brown, 2006) to develop unique theories of aging rather than to test existing theories. Therefore, we take the approach of implementing each of the theories within the retrieved context framework. The retrieved context framework has been extensively used to model the free recall effects outlined above in young adult samples (Howard & Kahana, 2002; Lohnas et al., submitted; Polyn et al., 2009; Sederberg et al., 2008). The retrieved context framework provides a good test bed for at least two reasons. First, most contemporary models of episodic memory share the core features of the retrieved context framework (i.e., that associations between items and a drifting context representation are critical in accounting for recall dynamics, e.g., Davelaar et al., 2005; Farrell, 2012). Second, the retrieved context framework accounts for many findings that cannot be accounted for by competing models (e.g., Lohnas & Kahana, in press).

The Retrieved Context Framework

The notion that memory for an item is intimately tied to the context in which it occurred has a very long history in the science of memory (Bower, 1967; Estes, 1955; Howard & Kahana, 1999, 2002; McGeoch, 1932; Mensink & Raaijmakers, 1988; Murdock, 1997; Tulving, 1972; Underwood, 1945). Yet, exactly what is meant by "context" can be difficult to define. Therefore, we start with an example to provide an intuition of the retrieved context framework (the appendix provides a full formal description).

Imagine you have just been presented with a picture of your childhood home. Perceptual processes will create a very clear representation of the physical details of the picture. This representation will in turn trigger a cascade of episodic and semantic associations. You may recall details of the neighborhood; you may recall specific episodes that took place at the house; you may remember friends you had while

you lived there, and all of these semantic and episodic memories will be colored by various emotions. This rich ensemble of activated representations is what we call context—a milieu of brain activity that is not identical with the representation of the picture itself.

The power of the retrieved context framework lies in the dynamics of how item and context representations interact as events occur in the environment. To continue with our example, imagine I present a new picture: One of your Psych 101 professor. Just as the "childhood house" picture did, this new picture will trigger a cascade of associations; you may remember where you sat in class; the cover art of the course textbook; your favorite study place. But this new cascade does not completely erase the activated representations that formed the "childhood home" context, rather it builds upon it; resulting in a new ensemble of activated representations that is neither purely "childhood home" nor purely "Psych 101", but a blend of the two. Because the professor representation is active alongside the "childhood house" representation, new associations will form between the two representations. That is, aspects of the professor representation will become linked to the house context, and, reciprocally, aspects of the house context will become associated with the professor representation. These reciprocal associations between items and contexts allow for the formation of new episodic memories (Gallistel, 2008; Howard & Kahana, 1999, 2002).

If I continued showing you pictures, they would continue to initiate cascades of associations, with each new picture adding to the ensemble of activated representations. Of course, these representations do not stay active indefinitely; rather mental context continually drifts as new events activate new representations, with representations associated with the most recent events being strongly active and those associated with more distant events fading into the background. Context is thus a recency—weighted history of past events.

Moreover, you would continue associating each newly presented item with the state of context that prevailed when it was presented (and forming reciprocal associations between contexts and items). The strength of these newly formed associations is unlikely to be uniform across the list, however. Instead, associations formed early in the list are likely to be stronger than those formed later in the list. That is, there is a primacy gradient. This primacy gradient reflects stronger encoding of early—list items, due either to more frequent rehearsals (D. L. Laming, 2006, 2008; Marshall & Werder, 1972; Modigliani & Hedges, 1987; Rundus, 1980; Tan & Ward, 2000; Ward, 2002) or to more efficient encoding during the item's initial presentation (Atkinson & Shiffrin, 1968; Neath & Crowder, 1990; Sederberg et al., 2006).

Now imagine that I ask you to recall all of the pictures you have seen (i.e., to do the free recall task). How do you begin recalling the items? The retrieved context framework proposes that you do so by using the current state of the con-

text representation as a retrieval cue. Such cuing happens by allowing the context representation to activate those item representations to which it is associated. The last picture you saw is likely to be strongly activated because its contextual state is still strongly represented in the contextual ensemble. Therefore, consistent with the PFR data (Figure 1B), you are likely to recall the last item first.

The act of recalling an item is very similar to being presented with the item, in that it triggers a cascade of associative retrieval, leading its contextual state to be reinstated and incorporated into the context layer. This new contextual state is then used to cue the next recall. A key difference is that because learning occurred during the list, recalling an item activates a somewhat different contextual representation than did studying it for the first time—a context that is a blend of the context that prevailed when it was presented and its original context. The first component of this reinstated context (i.e., the state of context that prevailed when the item was first presented) provides a good cue for items that were presented either before or after the just-recalled item. It is this similarity of contexts that gives rise to the contiguity effect (Figure 1C). The second component of the retrieved context representation, the pre-experimental component, is the context the item activated when it was originally presented. During the original list presentation, this pre-experimental context only became active when the item was presented, and therefore it formed associations only with those items that came later in the list. Thus, the pre-experimental component of reinstated context is a good cue for items that were presented after the just-recalled item, but is a poor cue for items presented before the just-recalled item. The fact that one component of the context reinstated by retrieved items provides a cue to both earlier and later list items, but the other component provides a cue only to later list items means that forward transitions are more likely than backward transitions, giving rise to the asymmetry in the lag-CRP.

This intuitive example captures the spirit of the retrieved context framework and the core mechanisms that produce the free recall patterns shown in Figure 1. The retrieved context framework has been implemented in several neural models that represent items and contextual states as nodes and represent associations as the connections between nodes (Howard & Kahana, 2002; Lohnas et al., submitted; Polyn et al., 2009; Sederberg et al., 2008). For the simulations in this paper we use the context maintenance and retrieval model version 2 (CMR2; Lohnas et al., submitted), an implementation that can simulate an entire session of free recall trials within a common associative network. By contrast, most previous free recall models have reset their associative networks after each simulated trial, a simplification that prevents them from modeling PLIs in a natural way. Here we provide an overview of the model with a focus on key mechanisms that will be used to implement the aging theories. The Appendix provides a full formal description of CMR2 (see also Lohnas et al., submitted).

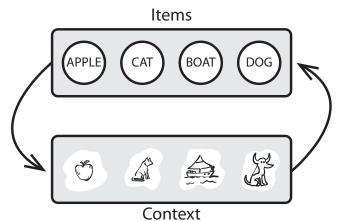


Figure 2. Schematic of CMR2. The item layer represents the identity of list items, with one node for each item. The context layer represents the ensemble of contextual associates that are activated when an item is presented; each item has a corresponding context node. The two layers are connected by two associative matrices; one encoding item—to—context associations and one encoding context—to—item associations.

For illustration we will use a scaled-down version of the model that simulates a single free recall trial with the 4-item list apple, cat, boat, dog. Figure 2 shows the basic structure of the model: items are represented as nodes on an item layer and context is represented as nodes on a context layer. Each word has a corresponding node on both the item layer and the context layer. A word's item node stands for the low-level representation of the item triggered by its presentation. In contrast, the corresponding context node represents the ensemble of activated semantic and episodic associates we defined as context. Each item node has a directional connection to each context node. Each of these connections has a value that encodes the strength of the association between the item and a context. In the model these associations are stored in associative matrices. Each item has a strong connection to its corresponding context node and very weak connections to the remaining context nodes. Just as each item is connected to each context, there are reciprocal connections from context nodes to item nodes, which are stored in a separate associative matrix.

Figure 3 shows how the network responds as items are presented during the encoding phase. In the first panel *apple* has just been presented, which causes its node to become active on the item layer (represented by the shading of the node). Activation flows through the network via the item-to-context associations. Because the *apple* item node is strongly associated with the *apple* context node, but weakly associated with all other context nodes, only the *apple* context is activated.

The second panel shows what happens when the next item, cat, is presented; first note that the cat item node has been activated and the apple item node is now completely deactivated, reflecting the fact that activation on the item layer lasts only while the stimuli is perceptually present. In contrast, both the *cat* and *apple* nodes are active on the context layer: activating cat on the item layer causes its context node to activate via the item-to-context associations, and this new activation is added to the existing activation of the *apple* node. Allowing multiple context nodes to be active at the same time is the critical feature that allows the context layer to simulate the blending the contextual states of recently presented items. But the two nodes are not equally active; instead, the node associated with the most recently presented item is strongly activated and the activity of the apple node has decayed somewhat (represented by the size of the icons in the context layer). This strong activation of recently presented items and progressively decaying activation of more distant items allows the layer to serve as a recency-weighted history of past events. The amount by which activated nodes decay with each new item presentation is governed by a model parameter, β_{enc} . When β_{enc} is set to one, each new item completely erases existing activation and when it is set to zero, new items have no effect on the context layer. Thus, β_{enc} controls the degree of recency weighting in the context layer.

The second panel also illustrates how episodic memories are formed in the model. The model uses a Hebbian learning rule so that associations form between item nodes and context nodes that are active at the same time. Because the activation of the *apple* context node persists when *cat* is presented the *cat* item node and the *apple* context node become associated via Hebbian learning. This new association is represented by the shading of the corresponding cell in the associative matrix in the second panel of Figure 3.

The efficiency with which new associations are formed is governed by several factors. First, two parameters, γ_{FC} and γ_{CF} control the strength of new feature-to-context and context-to-feature associations, respectively. When the value of γ_{FC} is low, weak associations are formed; when it is high, strong associations are formed. The second factor governing association formation is attention. Consistent with the notion that primacy results from changes in the efficiency of encoding across the list (Serruya, Sederberg, & Kahana, in press; Tulving & Rosenbaum, 2006), there is a primacy gradient such that early items are encoded more strongly than later items. Two model parameters govern the primacy gradient. ϕ_s controls the size of the initial primacy boost, and ϕ_d controls the rate at which it fades across the list. As described in the Appendix, the values of ϕ_d , ϕ_s , and γ_{FC} scale the strength of new feature-to-context associations.

The third and fourth panels of Figure 3 show the evolution of both the context layer and the associative matrix as the remaining list items are presented. As each successive item is

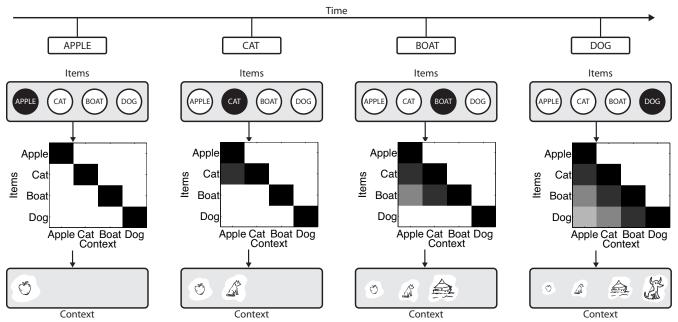


Figure 3. Sequence of events during the encoding period. When the first item, apple, is presented its item node is activated, which in turn activates its context representation by projecting through the item-to-context associative weight matrix. When the next item, cat, is presented, its context representation is activated, and added to the existing context representation so that both apple and cat are active on the context layer. As each item is presented Hebbian learning creates links between co-active items and context nodes. At the end of the trial the context layer provides a recency—weighted history of item presentation and the associative matrices encode newly formed associations between items and contexts that were co-active.

presented its context node becomes strongly activated and the activation of the context nodes of more distantly presented items decays. When each new item is presented, its item node becomes associated with all active context nodes, with the strength of the association being determined both by how active the context node is (items become strongly associated with highly active nodes and weakly associated with weakly activated nodes) and the value of the primacy parameters and γ_{FC} . Notice that item nodes are only associated with the context nodes of items that preceded them in the list; *apple* is not associated with any new context, whereas *dog* has been associated with all of the context nodes. This fact helps explain the asymmetry of the contiguity effect.

Figure 4 illustrates the retrieval process. Once all items have been presented, recall begins by using the current contextual state to cue retrieval via context-to-feature associations. Each context node sends activation to each item node via the context-to-item associative matrix. The specific amount of activation sent from a given context node to a given item node is determined by the activation level of the context node multiplied by the strength of the context-to-item association between the nodes. The total amount of activation received by a given item node is simply the sum of all activations arriving from all context nodes.

These activation levels on the item layer are used as the

starting points for a retrieval competition in which all items race to cross a threshold, following the dynamics of the competitive accumulator model of Usher and McClelland (2001). The retrieval competition includes noise, so that although the item with the strongest initial activation has the best chance of winning, items with lower activation can sometimes win. As we will see, the amount of noise in the process, which is governed by a model parameter, turns out to be an important factor in capturing age differences.

Before the winning item is actually output by the model, it undergoes a post–retrieval editing phase to screen for possible intrusions. Items that were actually studied on the list should be associated with states of context that are very similar to the state of context that prevailed during the recall period. By contrast, intrusions will tend to be associated with contexts less similar to the test context. Therefore, CMR2 screens for intrusions by allowing each potential retrieval to reinstate its context, and comparing that reactivated context to the existing context. If the similarity of the two exceeds a threshold, the item is recalled.

Once an item is recalled it retrieves its context state, which is incorporated into the context layer. Just as during encoding, new states of context do not completely erase old ones, but blend with them. A parameter, β_{rec} , controls how rapidly context drifts during retrieval. The rate at which context

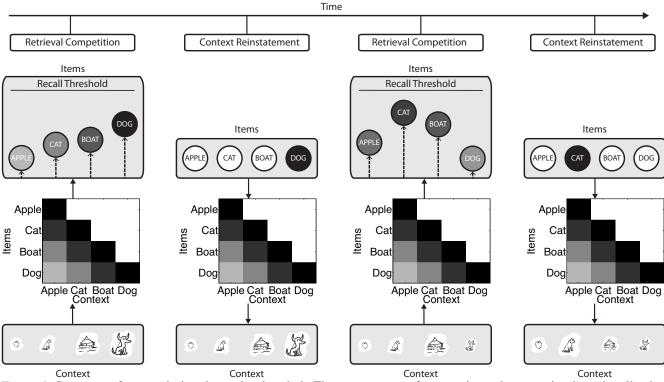


Figure 4. Sequence of events during the retrieval period. The current state of context is used as a retrieval cue by allowing it to project through the context—to—item associative matrix, activating nodes on the item layer. This activation is used as the starting point for an noisy diffusion process in which the first item to cross an activation threshold is recalled. The recalled item is reactivated on the item layer and activates its associated context representation, which is then added to the previous state of context. This updated context is used as a cue to initiate a second retrieval competition. Retrieval competitions continue until the recall period ends.

drifts has a powerful influence on the size of the contiguity effect. The updated context representation is used to drive another recall competition. Note that once an item is recalled it is still allowed to compete in subsequent retrieval competitions (i.e., like participants, the model can recall the same item more than once), but is handicapped by having to pass a higher threshold than never-recalled items (see the appendix for full details). The cycle of context cuing, retrieval competition, editing, and context reinstatement continues until the end of the recall period (30 seconds in the study considered here) is reached, at which point the next trial begins. The number of cycles that can take place during the retrieval period is determined by how long each retrieval competition takes: The accumulator proceeds in a series of iterations and a model parameter governs how many seconds each iteration takes.

It is thought that the transition from one trial to the next is accompanied by a change in mental context (Sahakyan & Kelley, 2002). CMR2 simulates this context shift by activating a unique "disruption" item on the item layer and allowing this item to update context. One effect of this interlist

context shift, which will become important later, is to reduce the accessibility of items presented before the shift, as the activation of contexts associated with prior–list items is significantly reduced. That is, the shift serves to contextually isolate successive lists.

Under CMR2, the free recall effects shown in Figure 1 derive from the dynamics of context drift, in particular the ability of presented and recalled items to reinstate contexts with which they have been associated. Recency occurs because the context at the end of the list, which is used as a retrieval cue, most closely matches items presented near the end of the list. Primacy occurs because the effectiveness of encoding processes changes across a trial. At the start of a trial they are highly efficient but become less effective with each successive word, following an exponential decay to a baseline level. As a consequence, early list items form stronger associations with the context that prevails when they are presented than do items presented later in the list. Temporal contiguity occurs because each recalled item retrieves a new context that is similar to the contexts associated with its near neighbors in the list and less similar to its more distant

neighbors. Intrusions occur because the context retrieved by a current list item is similar to a context associated with previous list items (existing semantic associations produce ELIs and new episodic associations produce PLIs).

For simplicity, our description of the model omitted several details. Although a full description of the model is available in the appendix, we highlight a few important details here. In our four-item example, item-to-context associations and context-to-item associations had the same strengths; however, this need not be the case in the full model. Similarly, in our example we assumed that associative matrices begin the simulated trial with each item being associated to its context node, but no other context nodes (and vise versa for context-to-item associations). In the actual model the matrices encode pre-experimental semantic associations among items (e.g., the dog item node is most strongly associated with the dog context node, but also has a weaker association with the cat node, reflecting the fact that the two words are semantically related). The strengths of these semantic associations were determined by Latent Semantic Analysis (LSA; Landauer & Dumais, 1997). LSA allows one to measure the semantic relationship between two words as the cosine of the angle between the words' representations in a multidimensional model of semantic space. The raw LSA values are then scaled by two model parameters (one for item-to-context associations and one for context-to-item associations) that control the strength of pre-experimental semantic associations. Finally, in the simulations presented below the actual layers and associative matrices are much larger than those in the 4-item example; they include nodes for each item presented (30 lists \times 10-items per list = 300 items) plus nodes for an equal number of items that were not presented. These un-presented items simulate the fact that participants must distinguish list items from a much larger lexicon of words that includes close semantic associates of the list items, which often occur as intrusions (Zaromb et al., 2006).

Implementing the Theories

The ADH, IDH, and CSH each implicate certain cognitive processes as the locus of age—related memory impairments. Our goal is to determine if deficits in these processes can account for the effects in Figure 1. To do so we will identify mechanisms in the CMR2 model that correspond to the cognitive processes implicated by the theories. We will then âĂIJlesionâĂİ those model mechanisms and determine if the lesioned model produces simulated data that duplicates the pattern of spared and impaired performance shown by older adults.

This approach assumes that the memory mechanisms that comprise CMR2 *can* be impaired in a way that captures the age effects. To ensure that the CMR2 framework can simulate the age effects, we began by fitting the model indepen-

dently to both the older and younger adult data, allowing all parameters to vary. As illustrated in Figure 5, the model provided accurate fits to both the older and younger adult data.

We can now use the parameter values that produced the simulated younger adult data as our model of healthy memory. We will test if we can make this healthy model simulate older adult data by lesioning the mechanisms implicated by the aging theories. We begin by describing how we implement each theory within the retrieved context framework.

Implementing a theory that was originally specified at a verbal level within a formal model requires making many choices. For example, does an associative deficit occur due to a failure to encode new associations or due to difficulty retrieving them (or both)? Some of these issues have been discussed in the aging literature (Naveh-Benjamin, 2000; Wingfield, Lindfield, & Kahana, 1998), but generally not at the level of detail required to implement a formal model. The result is that the modeler has a great degree of flexibility in how to implement the theories, and it is impractical to explore all possible implementations.

Rather than pick a single arbitrary implementation, we have chosen to implement each of the theories in three different ways that are straightforwardly consistent with existing descriptions of the theories. Our decision to explore only a subset of possible implementations offers an obvious way of defending a theory, should it fail to account for the data: It may have worked if some alternative implementation was used. In our view, this situation actually points to a hidden reason why the field has failed to converge on a common theoretical account: The verbal nature of existing theories provides them with a large degree of flexibility, which makes it easy to modify the theory to accommodate new data.

Associative Deficit Hypothesis. The associative deficit hypothesis (ADH) attributes older adults' memory impairment to a reduced ability to form associations (Naveh-Benjamin, 2000). In CMR, the formation of new episodic associations is governed by two parameters, γ_{FC} and γ_{CF} , that respectively control the extent to which the strength of item-to-context and context-to-item associations change with learning. If these parameters are set to zero, no new associations are formed and recall is dominated by pre-existing semantic associations. As the values of these parameters are increased above zero, the influence of new associations learned during list presentation increases. Therefore, a natural way to implement an associative deficit is to reduce the value of γ_{FC} or γ_{CF} . Impairing the ability of the model to form feature-context associations would lead to smaller changes in the association between list items and the state of context that prevailed when they were presented. During retrieval these weak associations would prevent the model from using each recalled item to retrieve a new context that serves as a good cue for neighboring list items. In contrast, impaired context-feature associations would prevent the model

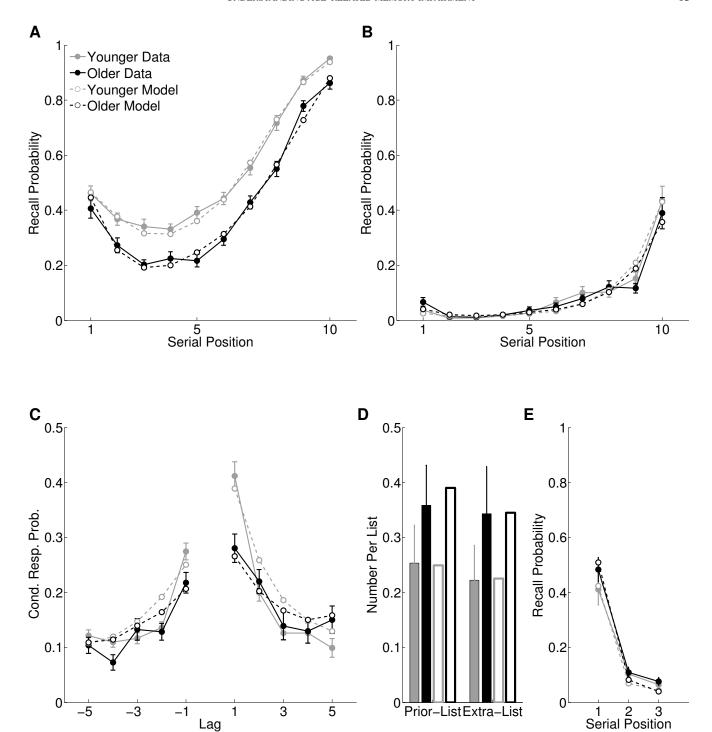


Figure 5. CMR2 simulations: Serial position curve (A), probability first recall function (B), lag-conditional response probability function (C), Prior–list and Extra–list intrusions (D), and Prior–list intrusion recency effect. The model was fit independently to the younger and older adult data and all model parameters were allowed to vary. Black lines or bars are used for older adults. Grey lines or bars are used for younger adults. Solid lines with filled symbols or filled bars are used for participant data. Broken lines with open symbols or unfilled bars are used for model simulations. Error bars represent one standard error of the mean. Data from Kahana et al. (2002).

from using current contextual states as retrieval cues. The fact that there are separate parameters controlling feature-to-context and context-to-feature associations raises the question of whether only one or both types of associations are affected by aging (and if both, whether they are equally affected). To give this implementation of the ADH the greatest chance of simulating the age effects, we allow both γ_{FC} and γ_{CF} to vary independently. Concretely, we implemented this version of the ADH by taking the best–fitting *younger* adult parameters (i.e., our model of healthy memory in Figure 5 and attempted to fit the older adult data while holding all parameters at the younger adult values except γ_{FC} and γ_{CF} , which were allowed to vary.

An associative deficit could arise if newly formed associations are weak relative to pre-existing associations. But it could also arise from noisy association formation. In the standard version of CMR2, association formation is noisefree in that when an item is presented its item node becomes associated with only those context nodes that are currently active. That is, the associations encode a noise-free representation of which feature and context nodes were co-active and the degree to which they were co-active. We can introduce noise into the association formation process by adding a random vector to the contextual states that retrieved items reinstate during retrieval so that items are no longer retrieving a noise free representation of the contexts to which they were associated. Specifically, $\mathbf{c}^{\mathbf{IN}}_{i} = M^{FC}\mathbf{f}_{i} + \zeta\mathbf{n}_{r}$, where \mathbf{n}_{r} is a normal random vector and ζ is a parameter controlling the weighting of the noise vector. To test this version of the ADH we allowed ζ , which controls the amount of associative noise, to vary.

Of course, weak and noisy associations are not mutually exclusive. Therefore we included a third implementation of the ADH in which we allow both the parameters controlling association strength (γ_{FC} and γ_{CF}) and the parameter controlling associative noise (ζ) to vary.

Inhibitory Deficit Hypothesis. Under the inhibitory deficit hypothesis (IDH) older adults have difficulty preventing irrelevant information from interfering with retrieval of relevant information (Hasher & Zacks, 1988). Several mechanisms in CMR2 control the extent to which information not directly relevant to the current list is activated during encoding and retrieval.

First, access to memories may be regulated by using contextual drift to isolate irrelevant information. In the case of free recall such contextual isolation could be accomplished by allowing the internal context representation to drift by a large amount during the period between successive lists. Such drift will decrease the similarity between the context that prevailed during the previous list and the context of the current list. As a consequence, items in successive lists will be associated to largely uncorrelated contextual states. Thus, during retrieval prior list items will be relatively less acces-

sible because context cues that provide a good match to the current list will be a poor match to previous lists. Perhaps older adults do not allow context to drift enough to form such contextual boundaries. To test this possibility we allowed the β_{post}^{recall} parameter, which governs the rate of context drift between lists, to vary.

Alternatively, an inhibitory deficit may take the form of difficultly rejecting intrusions when they come to mind. Such a deficit maps directly onto the post-retrieval decision mechanism in CMR2 and can be implemented by lowering the threshold, c_{thresh} , of similarity between an item's retrieved context and the current state of context needed for an item to be recalled. We tested this version by allowing c_{thresh} to vary.

Another interpretation of the IDH implicates the rate at which mental context drifts during encoding and retrieval. When a item is presented for encoding it triggers a cascade of associated thoughts and memories, many of which are not relevant to the task at hand. Younger adults may use inhibition to prune this cascade (Healey, Hasher, & Campbell, in press). For older adults, an inhibitory deficit may allow these irrelevant thoughts and memories to remain active and become bound to relevant information in memory (e.g., Hamm & Hasher, 1992). As a result, older adults' memories may be densely interconnected, setting the stage for massive interference at retrieval (G. Radvansky, Zacks, & Hasher, 2005). Moreover, if during retrieval each recalled item triggers retrieval of many associated, but irrelevant, memories it may hamper the ability to target list items. Such deficits can be simulated in CMR2 by varying how rapidly mental context drifts. For both younger and older adults, when an item is presented it will activate its pre-experimental context—its semantic associates. Older adults may integrate too much of this newly retrieved context into their context representations (but see Howard, Kahana, & Wingfield, 2006). Such rapid drift can be simulated with the β_{enc} parameter, which controls the extent to which newly retrieved context replaces existing context in the context layer. Similarly, rapid context drift during retrieval can be simulated with a higher value of β_{rec} . Therefore, we implemented this version of the IDH by allowing both β_{enc} and β_{rec} to vary freely.

The Cognitive Slowing Hypothesis. The cognitive slowing hypothesis (Salthouse, 1996) suggests that older adults suffer a general slowing of cognitive processes. During encoding, slowed processing would result in weaker associations being formed per unit of processing time. For example, older adults may not have time to finish processing the current word before the next appears. Therefore, we can simulate slowed encoding processes by simply downweighting the influence of newly learned episodic associations in the same way we did for the ADH.

Slowed retrieval can also be readily simulated in CMR2. The recall period is limited in time (30 seconds in the data considered here), and any slowing of retrieval processes will

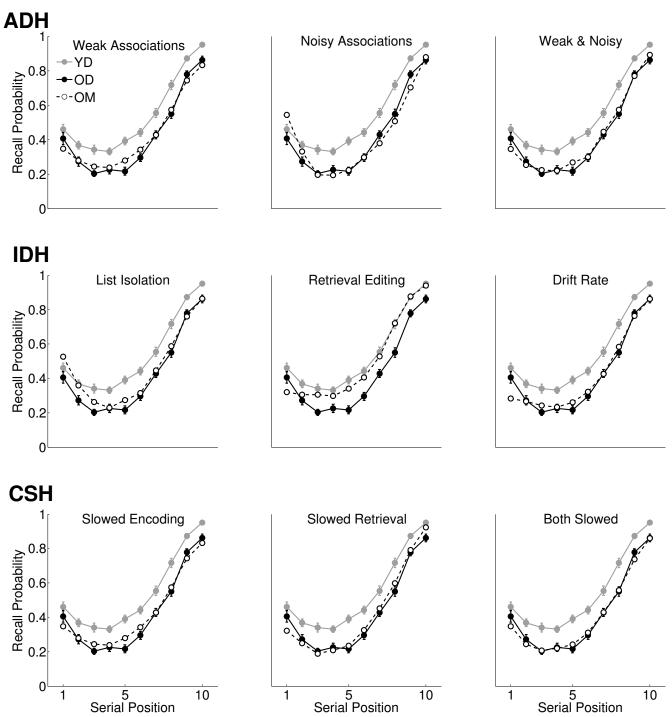


Figure 6. The lesioned models' simulations of the serial position curve. Each panel represents one version of the model and shows the best–fitting simulated data along with the actual data from both older and younger adults. Black lines are used for older adults. Grey lines are used for younger adults. Solid lines with filled symbols are used for participant data. Broken lines with open symbols are used for model simulations. YD = Younger Data; OD = Older Data; OM = Older Model.

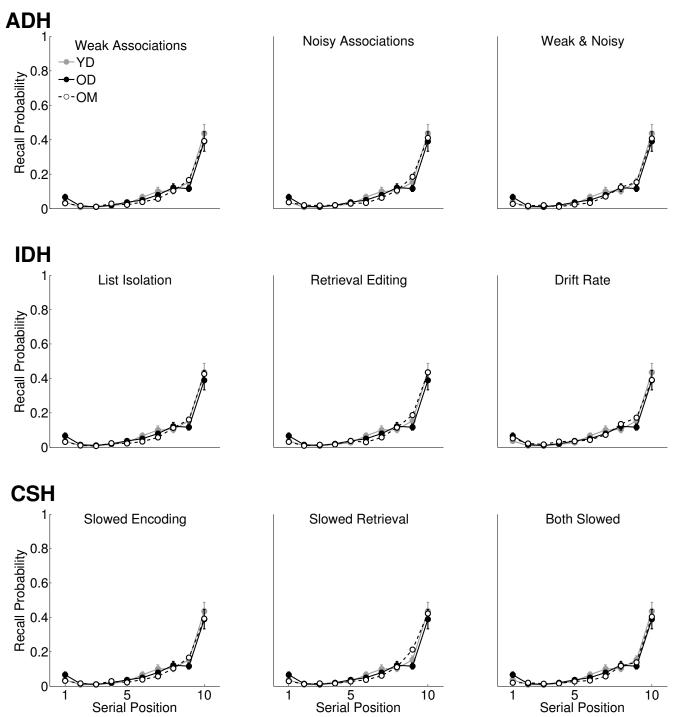


Figure 7. The lesioned models' simulations of the probability of first recall function. Each panel represents one version of the model and shows the best–fitting simulated data along with the actual data from both older and younger adults. Black lines are used for older adults. Grey lines are used for younger adults. Solid lines with filled symbols are used for participant data. Broken lines with open symbols are used for model simulations. YD = Younger Data; OD = Older Data; OM = Older Model.

reduce the maximum number of items that can be recalled in that time. Each retrieval attempt takes a finite amount of time, and that time is governed by a model parameter. By varying that parameter we can simulate slowed retrieval—the consequence of which is to reduce the number of retrieval attempts that can be made within the recall period time limit.

As a final implementation of the CSH, we can assume that older adults suffer from both slowed encoding and slowed retrieval processes. To do so we simply allow the parameters governing both association formation and the speed of retrieval to vary.

Testing the Theories

Ultimately, we want to arrive at a set of lesioned mechanisms that can simulate all of the age effects simultaneously using a the set of parameter values. Simulating the effects simultaneously, however, involves complex tradeoffs, which make it difficult to understand why a particular mechanism fails or succeeds in capturing the age effects. We therefore start by considering the ability of each lesioned mechanism to capture the effects in isolation. We did this by taking the SPC, PFR, lag-CRP, intrusion rates, and the PLI-Recency data one at a time and determining if each of the theory implementations was able to fit that aspect of the data while ignoring the other aspects.

As described above, each theory implementation consists of a set of parameters that may differ from the optimal younger adult values, thereby simulating a deficit in the mechanisms governed by those parameters. To determine if a theory can describe older adults' behavior for a particular effect we must systematically vary the implicated parameters, and for each variation run the model to produce simulated data. We can measure how well each of these simulations fits the older adult data by computing the root-mean-square deviation (RMSD) between the model simulations and the older adult data. The goal is then to find the parameter set that minimizes the RMSD. If we want to claim that a given theory cannot account for an effect, it is critical that we have first thoroughly explored the parameter space to ensure that there is no set of parameter values that would allow the model to simulate the effect. Thus, to search for the best parameter set for each theory we began by simulating 100 parameter sets evenly distributed across the parameter space.

We then conducted a focused grid search centered on the best–fitting of those initial 100 parameter sets. Specifically, we created a multi–dimensional grid by selecting 20 evenly spaced values for each parameter and evaluating the parameter sets defined by the intersections of the grid, for a total of 20^p parameter sets where p is the number of parameters in the theory implementation. Take, for example, CSH implemented as slowed encoding and retrieval processes, which implicates 3 parameters (the two association formation parameters and the parameter governing how long a retrieval

attempts takes). For this theory, the grid search would encompass $20^3 = 8000$ parameter sets. The best–fitting parameter values for all simulations are reported in the appendix.

Serial Position Curve. Figure 6 shows the simulated serial position curves produced by the best–fitting version of each model. Rows one to three show the ADH, IDH, and CSH respectively. Each column corresponds to a different implementation. Each panel shows both the younger and older adult data along with simulated data from best–fitting parameter sets for the older adult data. Simulations from the healthy young adult model are shown in Figure 5 and are not reproduced here to improve the readability of the graphs.

The ADH, as implemented by weak associations, provides a very good fit to the data. Noisy associations provide a good fit to most of the curve, but under–predict the age deficit on primacy items. The combination of weak *and* noisy associations provides a very good fit.

The IDH as implemented by reduced contextual drift between lists fits the age deficit for most of the serial position curve but underestimates the deficit on the primacy portion. Changing the post-retrieval editing threshold impairs primacy items but has little impact of rest of the SPC. Finally, allowing the contextual drift parameters to vary was able to fit all aspects of the SPC with the exception of overestimating the age deficit at serial position 1.

For the CSH, the slowed encoding implementation provides a good fit to older adults' SCPs. The slowed retrieval implementation also provides a good fit, though it does overestimate the age difference at the first serial position. When combined, slowed encoding and slowed retrieval provide a very good fit at all serial positions.

Probability of First Recall. Figure 7 shows the results of fitting the lesioned models to PFR curves, ignoring all other effects. A quick examination of the simulations speaks for itself: all of the models provided excellent fits to older adults' performance and are indistinguishable from the actual data. This is not surprising given that the PFR exhibits no age differences. This lack of an age difference essentially guarantees that the lesioned models will be able to simulate the older adult data.

Lag Conditional Response Probability. Figure 8 shows simulated Lag-CRP curves generated by the best-fitting lesioned models. The weak association implementation of the ADH underestimated older adults' deficit on +1 transitions. Adding noise to new associations does allow the model to fit the older adult data. The combination of weak and noisy associations provides a very good fit to the older adult data.

For the IDH, both the list isolation and the retrieval editing implementations were unable to capture older adults' deficit. The unregulated contextual drift implementation, however, provides good fit to the lag-CRP data. To understand how the model achieves this fit, we can compare the values of

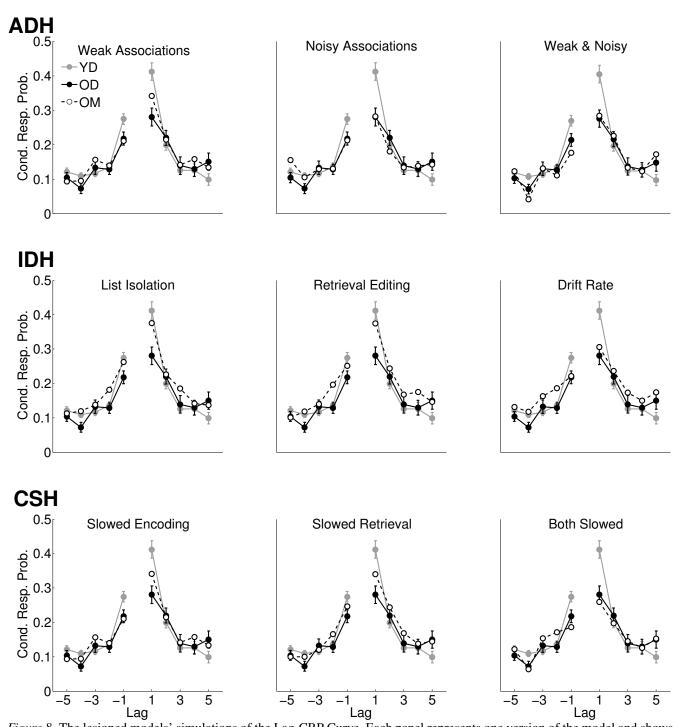


Figure 8. The lesioned models' simulations of the Lag-CRP Curve. Each panel represents one version of the model and shows the best–fitting simulated data along with the actual data from both older and younger adults. Black lines are used for older adults. Grey lines are used for younger adults. Solid lines with filled symbols are used for participant data. Broken lines with open symbols are used for model simulations. YD = Younger Data; OD = Older Data; OM = Older Model.

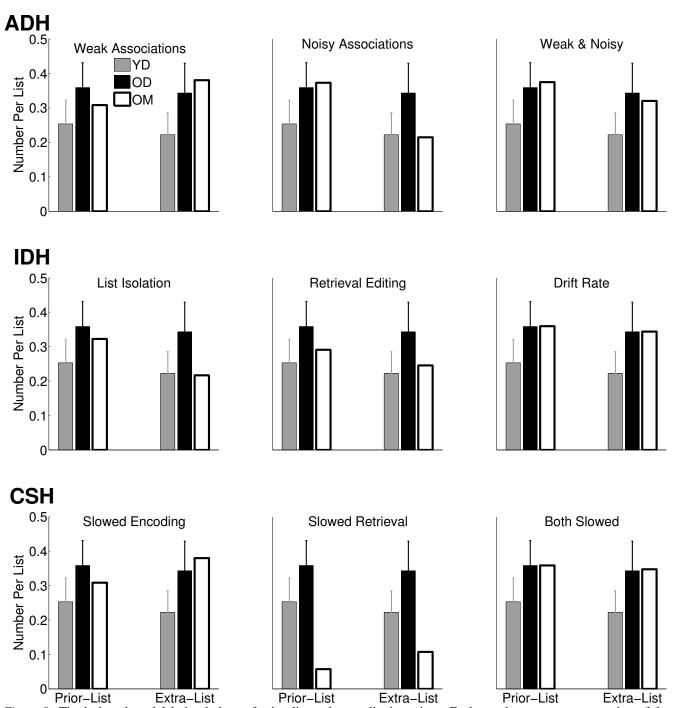


Figure 9. The lesioned models' simulations of prior–list and extra–list intrusions. Each panel represents one version of the model and shows the best–fitting simulated data along with the actual data from both older and younger adults. Black bars are used for older adults. Grey bars are used for younger adults. Filled bars are used for participant data. Unfilled bars are used for model simulations. YD = Younger Data; OD = Older Data; OM = Older Model.

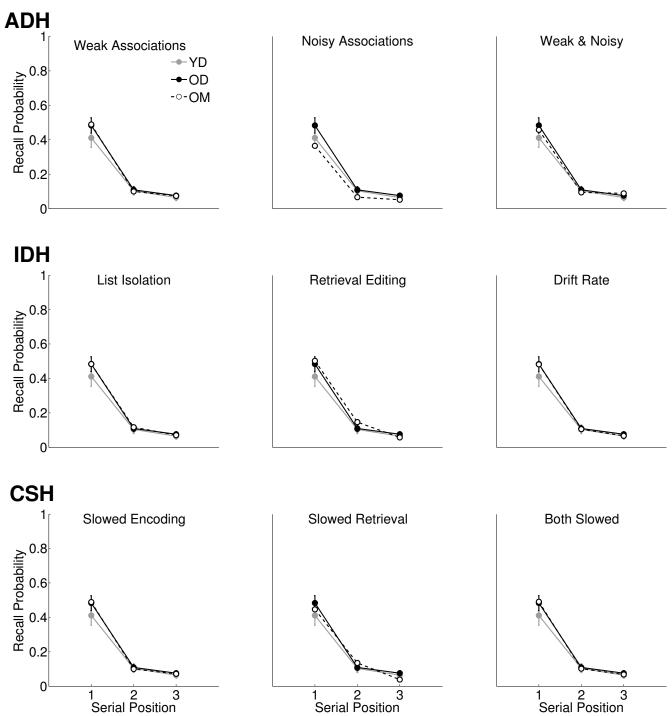


Figure 10. The lesioned model's simulations of the prior-list recency effect. Each panel represents one version of the model and shows the best-fitting simulated data along with the actual data from both older and younger adults. Black lines are used for older adults. Grey lines are used for younger adults. Solid lines with filled symbols are used for participant data. Broken lines with open symbols are used for model simulations. YD = Younger Data; OD = Older Data; OM = Older Model.

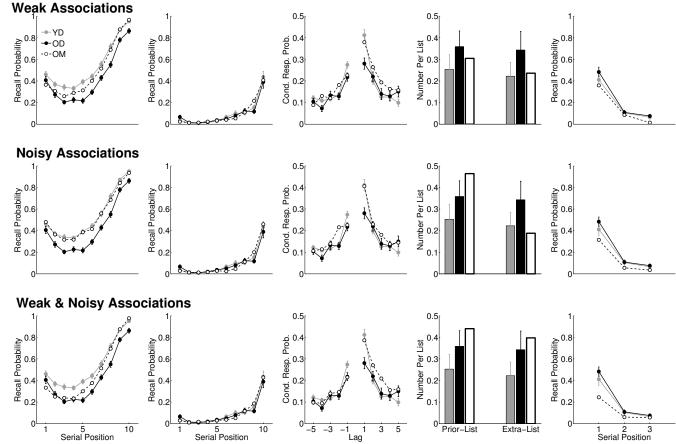


Figure 11. The Associative Deficit Hypothesis simulating all effects simultaneously. Each row represents one implementation of the theory and shows the best–fitting simulated data from that model along with the actual data from both older and younger adults. See the text for full details on each implementation. Black lines and bars are used for older adults. Grey lines and bars are used for younger adults. Solid lines with filled symbols and filled bars are used for participant data. Broken lines with open symbols and unfilled bars are used for model simulations. YD = Younger Data; OD = Older Data; OM = Older Model.

drift rate parameters that produced the simulated data with the corresponding values in the younger adult model (See Table A1 and A2 for all parameter values). This comparison reveals that the drift rate during encoding was somewhat lower than for the healthy model ($\beta_{enc}^{younger} = 0.561$ and $\beta_{rec}^{lesioned} = 0.532$). The drift rate during retrieval was substantially lower in the lesioned model ($\beta_{rec}^{younger} = 0.375$ and $\beta_{enc}^{lesioned} = 0.252$). A lower value of β_{rec} means that each newly retrieved item injects less of its associated context into the context layer, and therefore has less of an influence on the state of context that will be used to cue the next recall. As a consequence, the updated context representation will be a weaker cue for items that were presented in temporal proximity to the just-recalled item than it would be with higher values of β_{rec} . Note, however, that this is actually the opposite of the intuition that drove this implementation of the IDH. IDH seems to suggest that older adults should integrate more contextual information into mental context than younger adults, not less as the simulation suggests. We note

that explicitly specifying the IDH in this way and using a model to test it has allowed us to essentially eliminate this version of the IDH.

For the CSH, slowed encoding processes underestimated the extent of the age effect. Similarly, slowed retrieval processes over–predict older adults' performance on the critical +1 lag. The combination of slowed encoding and retrieval, however, provides a near perfect fit.

Prior-List and Extra-List Intrusions. Figure 9 shows the simulated PLI and ELI data for each lesioned model. For the ADH, the weak association implementation provided a reasonable fit. The noisy association implementation was able to capture older adults' PLI rate but not their ELI rate. However, the combination of both weak and noisy associations allowed the model to capture PLIs and ELIs.

For the IDH, both the list isolation and the retrieval editing implementations failed to capture the older adult ELI rate. The context drift implementation of the IDH—the version that allowed older and younger adults to have different rates

of context drift both during encoding and during retrieval was able to capture both the PLI and the ELI rates.

For the CSH, the slowed encoding implementation provided a reasonable fit. The slowed retrieval implementation failed to fit either the PLI or the ELI rates. Slowing both encoding and retrieval process provided a very good fit to both the PLI and ELI data.

Prior-List Intrusion Recency. The results of simulating the PLI Recency effect are shown in Figure 10. As with the PFR, there were no behavioral age differences in PLI Recency, and as such, all of the lesioned models provided excellent fits to the data.

Simulating All Effects

Examining the effects in isolation has demonstrated that all three theories have at least one implementation that can capture each age effect. That is, each of the theories is able to pass the first hurdle of accounting for the individual effects with a reasonable level of quantitative precision. This finding represents an important step in building aging theories as most previous treatments of these theories have accounted for broad patterns at a qualitative level, and those that have used models to test quantitative predictions have mainly considered effects that the theory was specifically designed to account for (e.g., Li et al., 2005).

Before any of the theories can be considered to provide an adequate description of age differences in free recall, a second, more challenging hurdle must be crossed. Specifically, the theories must be able to account for the above effects simultaneously rather than in isolation. Meeting this challenge is critical because a complete aging theory must account for all of the effects with a common set of parameter values. In other words, because the aging brain uses the same configuration to produce SPCs, PFRs, lag-CRPs, and intrusion effects, a model of aging must also use a single configuration (i.e., the same parameter values) to produce all of the effects. It is, however, possible that the parameter values that allow a theory to fit one effect provide a very poor fit to another effect. Therefore, we tested the ability of each lesioned model to simulate all effects with a single set of parameters. To find the best-fitting parameter set for each theory we used the same grid search approach employed with the isolated effects.

Figure 11 shows the performance of the various ADH implementations. Weak associations (top row) capture the age effect in the primacy portion of the SPC, but not the recency portion. Unsurprisingly the model does capture both the PFR and the PLI recency effect, which show no age differences. However, it fails to account for the CRP and for PLIs and ELIs. The noisy association implementation also performs poorly, failing to capture any effects save the lack of age differences on PFR and PLI recency. The combined weak and noisy associations implementation is able to capture the PLI

Table 1

BIC values for simulation of all effects simultaneously

Theory	Figure	BIC
Full Model	5	-251
ADH Weak Associations	11A	-185
ADH Noisy Associations	11B	-172
ADH Weak & Noisy	11C	-176
IDH List Isolation	12A	-182
IDH Retrieval Editing	12B	-180
IDH Drift Rate	12C	-185
CSH Slowed Encoding	13A	-185
CSH Slowed Retrieval	13B	-183
CSH Both Slowed	13C	-201
All Theories Combined	14	-223
Four Factor Model	16	-230

The figure column gives the figure in which the simulations are shown.

and ELI data but does so at the cost of severely mispredicting the SPC, lag-CRP and PLI recency data.

Figure 12 shows the IDH simulations. Unlike when each effect was considered in isolation, none of the three implementations were able to capture all of the effects simultaneously. The top row of Figure 12 reveals that the impaired list-isolation editing model was able to simulate older adults' PLI rate, but was unable to capture either the SPC, lag-CRP, or ELI deficits. Similarly, the impaired post-retrieval editing model (Figure 12 middle row), fails to capture either the SPC, the lag-CRP, or the intrusion effects. Finally, allowing context drift rates during encoding and during retrieval to differ between older and younger adults (Figure 12 bottom row) fails to capture several effects. For the SPC, it accurately captures the age deficit in the recency portion but overestimates the effect in the primacy portion. It is also unable to simulate older adults impaired temporal contiguity. The model does, however, accurately simulate older adults' PFR, intrusion, and PLI recency data.

The performance of the CSH (Figure 13) is better. Slowed encoding processes (top row) fail to account for the SPC, lag-CRP and intrusion data, as does slowed retrieval processes. Slowing both encoding and retrieval provides a better fit, especially to the SPC, but still misses several key aspects of the data. The model accurately simulates older adults' temporal contiguity deficit for positive lags, but at the cost of underestimating their deficit at negative lags. The slowed encoding and retrieval implementation also fails to account for the PLI data. Surprisingly, this implementation also distorts older adults' PLI recency data, predicting a non–monotonic function (the dip at serial position 2).

In summary, while each theory is able to accurately simulate some aspects of the full pattern of age effects, in the process of doing so it severely mispredicts other aspects.

The quality of each implementation's fit to the full set of

effects is summarized in Table 1, which shows Bayesian Information Criterion (BIC; Kahana, Zhou, Geller, & Sekuler, 2007; Schwarz, 1978) values for each model. Lower BIC values indicate a better fit and take in to account the number of free parameters in a model. Table 1 reveals that none of the models performs as well as the full model, even though the full model is heavily penalized for having many parameters. When viewed in light of the fact that CMR2 can easily capture the age pattern when all parameters are allowed to vary (Figure 5), the failure of single–factor theories to capture the effects suggests that age-related changes in multiple memory processes underlie the age pattern. The challenge is to determine which processes are key.

Multi-Factor Theories

A sensible starting point is to ask if some combination of the IDH, ADH, and CSH theories can account for the full pattern of age effects. We explored this possibility by allowing all of the parameters implicated by the theories to vary freely. Specifically, γ_{FC} , γ_{CF} , ζ , β_{enc} , β_{rec} , c_{thresh} , β_{post}^{recall} , and au were allowed to vary. The multi-factor model includes 8 free parameters, which makes the parameter space too large to efficiently explore with a grid search. We therefore used a genetic algorithm, which past work has shown to be quite effective at finding optimal parameter sets for the CMR family of models (Healey & Kahana, in press; Lohnas et al., submitted; Polyn et al., 2009; Sederberg et al., 2008). The genetic algorithm started by simulating 1000 parameter sets evenly distributed across the parameter space. The algorithm was then allowed to run for 10 generations, with each simulating 500 parameter sets. A further 10 generations each simulated 100 sets but with each simulation producing 5 times the true number of trials, allowing the algorithm to distinguish subtle differences between parameter sets. Figure 14 shows the simulated data from the best-fitting parameter set.

This combined model provided a very good fit to the SPC, the PFR, both PLIs and ELIs, and PLI-recency. However, the model was unable to simultaneously simulate older adults contiguity deficit, over-predicting the extent of their contiguity deficit for +1 lags. Older adult's temporal contiguity deficit is perhaps the single most important aspect of the pattern of age effects on free recall for several reasons. First, as we have argued above, the ability to reproduce temporal order represents a key feature of episodic memory—the ability to place events on an autobiographical timeline. A reduced ability to situate events in their temporal context, a blurring of the autobiographical timeline, is likely a large part of what makes memory difficulties so troubling for older adults. Second, among younger adults, the extent to which an individual shows temporal contiguity is correlated with general cognitive ability, as measured by WAIS IQ (Healey et al., submitted). Therefore, a reduced temporal contiguity effect may be closely related to deficits on various non-memory tasks. In

this light, the failure to accurately predict older adults' temporal contiguity deficit poses a serious challenge to a theory of aging.

Given that even when combined, the lesioned models were unable to fit the age effects as accurately as the full model, it is important to understand which mechanisms are critical in the full model simulations. A simple approach to this problem would be to examine the parameter values used to fit the younger versus older adult data shown in Figure 5, and determine which parameters differ substantially between age groups. A major difficulty with such an approach is that there is no way to test if the parameters are significantly different between age groups. We can overcome this challenge by moving from fitting average data to fitting the data of each individual participant. Doing so provides us with a estimate of each of the model parameters from each participant. We can use these individual parameter estimates to form a distribution of values for each parameter, which can be broken down by age group. We can then determine for which parameters the older and younger adult distributions differ significantly.

We fit individual participant data using the same genetic algorithm procedure described for average data. To ensure stable parameter estimates, we repeated the fitting procedure 3 times for each participant and averaged the estimates for each parameter and then used these average estimates to generate simulated data.

To visualize age differences on the parameter distributions, we placed all of the parameters on a common scale by converting them to z-score units (ignoring age group). Then for each parameter we calculated a young minus older adult difference score. These difference scores are plotted in Figure 15 along with 95% confidence intervals on the age differences (see the Appendix for the raw parameter values). The figure reveals age differences on the magnitude and decay rate of the primacy effect (ϕ_s and ϕ_d), on the context drift rate during retrieval (β_{rec}), the editing threshold (c_{thresh}), and the lateral inhibition and noise parameters (λ and η) in the decision accumulator.

To confirm that these 6 parameters are indeed capable of accounting for the pattern of age differences, we used the same lesioning procedure we used to test the aging theories. Specifically, we took the same younger adult model we lesioned when testing the verbal theories and attempted to simulate the older adult data allowing only these 6 parameters to vary. As can be seen in Figure 16, we achieved an excellent fit to the older adult data. The BIC values in Table 1 reveal that this 6–parameter model outperformed all of the aging theories. That is, a reduced model consisting of only 6 parameters provided a better fit than the 8 parameter combined aging theory model. Although promising, we must be aware of several potential pitfalls.

First, we need to ensure that the correlations between parameter values are not overly high. If particular parameters

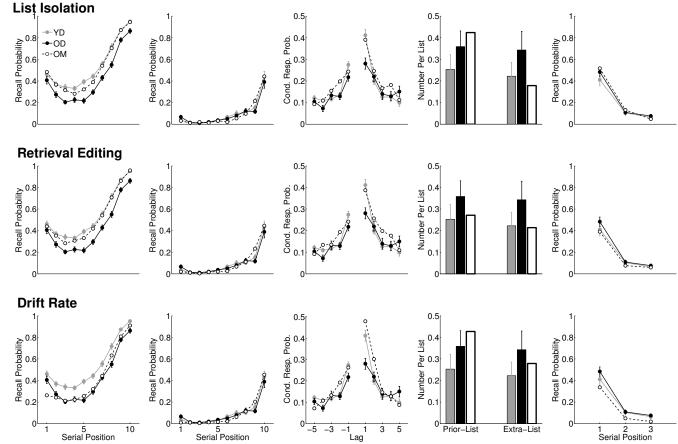


Figure 12. The Inhibitory Deficit Hypothesis simulating all effects simultaneously. Each row represents one implementation of the theory and shows the best–fitting simulated data from that model along with the actual data from both older and younger adults. See the text for full details on each implementation. Black lines and bars are used for older adults. Grey lines and bars are used for younger adults. Solid lines with filled symbols and filled bars are used for participant data. Broken lines with open symbols and unfilled bars are used for model simulations. YD = Younger Data; OD = Older Data; OM = Older Model.

were highly intercorrelated (i.e., a participant's estimate for one parameter predicted their estimate for another), it would suggest that the two parameters do not represent independent processes and should be considered as a single parameter. Two parameters, lateral inhibition and the standard deviation of noise in the decision accumulator, were correlated at r > .9 in both the older and younger adult groups. Therefore, in the rest of the paper we treat these two parameters as reflecting a joint parameter. No other parameters were highly correlated.

A second potential pitfall we must avoid is the possibility that the reduced 6-parameter model we have found is but one of many reduced models that are capable of fitting the data. If it were the case that many different reduced models provided simulations of roughly equivalent accuracy (i.e., the model is underdetermined), then it would simply be telling us that there is not enough data to distinguish between different reduced models. We took three steps to test the validity of the 6-parameter model.

First, we attempted to determine if the 6 parameters we

identified are necessary to simulate the age pattern. We did this by attempting to fit the pattern using all of the model parameters *except* those in the reduced model. This model consisted of 9 parameters and failed to fit the data (BIC = -163), suggesting that at least some of the parameters in the reduced model are critical.

Second, to determine if any of the 6 parameters are unnecessary, we ran a step—wise leave-one-out procedure. Starting with the 6 parameters we tested whether any of those parameters could be removed by testing the ability of all possible 5 parameter models to fit the data (i.e., allowing 5 of the original 6 to vary and fixing the 6^{th} to the younger adult value). We compared the 6–parameter model with each of the 5–parameter models: The best–fitting 5–parameter model excluded the editing threshold parameter (i.e., c_{thresh} was held at the younger adult value). However, this model had a lower BIC value than the 6–parameter model (BIC = -230 for the 6–parameter model and BIC = -219 for the 5–parameter model). The remaining 5–parameter models had BIC values

ranging from -157 to -173. That is, the parameters excluded from the 6-parameter model are unable to simulate the older adult data and excluding any of the 6 parameters from the reduced model degrades the quality of its fit.

Finally, we tested if we could substantially improve the fit of the 6-parameter model by allowing a 7^{th} parameter to vary. We tested this possibility by fitting all possible 7-parameter models (i.e., those in which the parameters from the original 6-parameter model, plus one on the remaining parameters were allowed to vary). The best-fitting 7-parameter model allowed ζ , which controls the amount of associative noise, to vary and resulted in only a small improvement in fit (BIC = -230 for the 6-parameter model and BIC = -231 for the 7-parameter model). We now turn to interpreting the 6-parameter model.

The parameters in the reduced model map directly on to psychological constructs. The age differences in the primacy parameters, ϕ_s and ϕ_d , suggest that older adults give a strong attentional boost to early items but that their attention drops off more rapidly than younger adults. This pattern is evident in Figure 17, which plots the age difference in the primacy gradient (i.e., the initial boost and how it decays across items) derived from the model parameters. The figure shows that older adults have a stronger initial boost than younger adults (due to a higher value of ϕ_s), but their decay rate (ϕ_d) is so high that by the second item younger adults are receiving a greater primacy boost. One interpretation of this pattern is that older adults initially allocate too much attention to encoding and then suffer from rapid camatosis (i.e., decreasing efficiency of encoding processes across a trial; Serruya et al., in press; Tulving & Rosenbaum, 2006). The idea that older adults have difficulty allocating attention is consistent with evidence that older adults have difficulty with attention tasks (Darowski et al., 2008), and also with the idea that frontal executive processes are impaired with age (West, 1996). We note that the fact that the IDH, ADH, and CSH do not suggest any age differences in the allocation of attention across time may explain part of their difficulty in fitting all of the effects.

The next mechanism showing an age deficit is the rate of context drift during retrieval. This drift rate, β_{rec} , governs the extent to which the just–recalled item reinstates its associated contextual states and was lower for older adults. Contextual reinstatement lies at the core of the retrieved context framework, and is a key factor in producing the contiguity effect: Because nearby list items become associated with similar contexts during encoding, if a retrieved item reactivates its context, it will provide a strong cue for its list neighbors. In contrast, if a retrieved item reactivates little of its associated context, it will provide a relatively weak cue to its neighbors, thus reducing the temporal contiguity effect. The fact that context drift differs between older and younger adults only at retrieval helps explain the fact that there are no age differences on the PFR—if older adults had lower context

drift rates during encoding, CMR2 would predict they would have shallower PFR curves than younger adults, as the end of list context would provide a strong match to a wider range of items. Insofar as contextual reinstatement during retrieval represents a deliberate attempt by participants to create an effective retrieval cue, age differences in this drift rate are consistent with the view that older adults suffer at self–initiated processing (Craik, 1977) or the ability to use well–specified cues to constrain retrieval (Jacoby, Bishara, Hessels, & Toth, 2005). It is also consistent with the suggestion that regulation of contextual representation allows for the selective retrieval of relevant memories which we have termed contextual gating (Healey et al., submitted).

The age difference in the post-retrieval editing threshold suggests that older adults are more willing to accept intrusions as true list items. This interpretation is consistent with the finding that older adults tend to endorse more intrusions in externalized free recall (in which participants say all words that come to mind, and reject those that they know are errors; Kahana, Dolan, Sauder, & Wingfield, 2005). An impaired ability to monitor for intrusions is consistent with evidence that older adults have difficulty monitoring retrievals in other tasks such as autobiographical recall (McDonough & Gallo, 2013). An age difference in retrieval editing may seem inconsistent with our simulation of the retrieval editing implementation of the IDH, which showed that the editing threshold parameter, by itself, was not able to simulate older adults' intrusion rates (Figure 6). However, for intrusions to reach the editing stage, they must win a retrieval competition, and evidence from externalized free recall suggests that older adults produce more potential intrusions than do younger adults (Kahana et al., 2005). The retrieval editing mechanism has no influence on how many non-list items win retrieval competitions; some other deficit must provide the editing mechanism with a supply of potential intrusions. The next impaired mechanism does just that.

Older adults had higher estimates of the lateral inhibition and noise parameters of the decision accumulator process (λ and η). We stress that these two parameters are so highly correlated that they cannot be treated as separate entities. Instead the fact that older adults had high values for both parameters suggests that the evidence accumulation process is noisy for older adults. A noisy accumulation process would allow items that would seldom win a retrieval competition in the younger adult model to occasionally accumulate enough evidence to win. The likelihood of an item accumulating enough evidence to be retrieved is codetermined by the strength of genuine evidence for the item (given by the match between the context cue and the item) and the noise. Therefore, a higher variance in the noise parameter means that an item with little genuine support will occasionally have enough spurious support from noise to win the retrieval competition. Conversely, given that the noise parameter can take

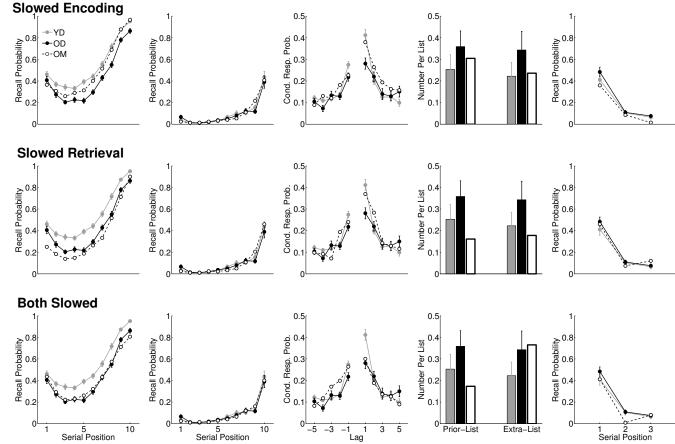


Figure 13. The Cognitive Slowing Hypothesis simulating all effects simultaneously. Each row represents one implementation of the theory and shows the best–fitting simulated data from that model along with the actual data from both older and younger adults. See the text for full details on each implementation. Black lines and bars are used for older adults. Grey lines and bars are used for younger adults. Solid lines with filled symbols and filled bars are used for participant data. Broken lines with open symbols and unfilled bars are used for model simulations. YD = Younger Data; OD = Older Data; OM = Older Model.

on negative values, items with high genuine support will occasionally lose due to noise. Thus, a higher value of the noise parameter will lead to fewer accurate recalls and more false recalls being passed on to the post–retrieval editing phase. Moreover, noise will tend to disrupt retrieval dynamics. Normally items that were near the just–recalled item in the presentation list will receive the most support in the retrieval competition (because the are associated to similar states of context). With a high degree of noise, however, distant items will more often accumulate sufficient evidence to be recalled, which will tend to lower the extent of temporal contiguity.

Together, the age differences in the CMR2 parameter estimates suggest four distinct age-related impairments: Rapid waning of attention across the list; difficulty retrieving contextual representations during the recall period; a lower threshold for endorsing candidate retrievals; and a noisy evidence accumulation process.

Discussion

Developing a detailed understanding of why episodic memory changes with age is amongst the most important tasks facing cognitive aging researchers. This understanding will form the foundation for interventions designed to prevent, slow, or remediate age-related memory declines. Many theories have been proposed to account for age differences in memory. Here we evaluated three major theories of cognitive aging against the complex pattern of age differences in free recall by implementing the theories as lesions within a computational model of healthy episodic memory. Simulations revealed that whereas each theory was able to precisely account for certain aspects of the pattern of agerelated differences, no theory was able to account for the full pattern simultaneously. Moreover, even when the theories were combined into a multi-factor theory, they failed to provide an adequate account of the full pattern. Simulating the performance of individual older and younger adults revealed

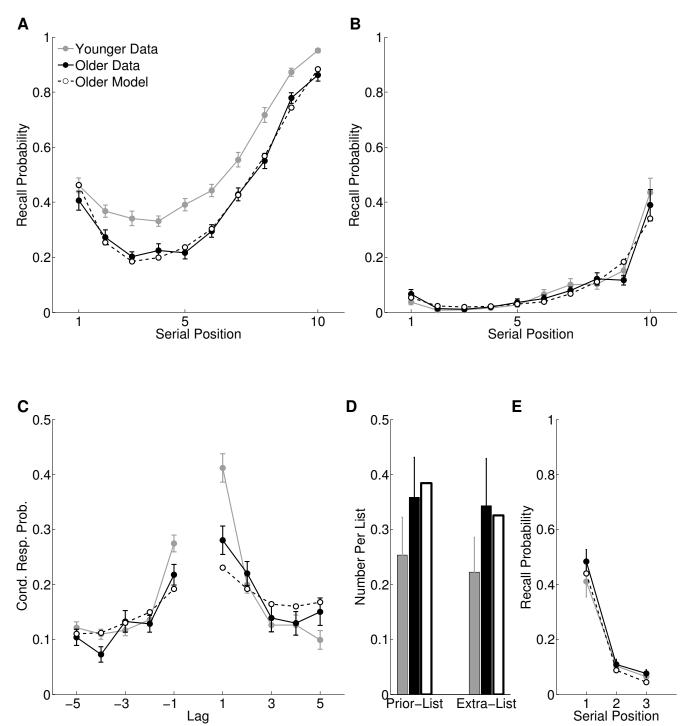


Figure 14. Fit of the of the combined aging theories. All parameters implicated by the ADH, IDH, and CSH were allowed to vary. The best–fitting simulated data is shown along with the actual data from both older and younger adults. See the text for full details on how each model was implemented. Black lines or bars are used for older adults. Grey lines or bars are used for younger adults. Solid lines with filled symbols or filled bars are used for participant data. Broken lines with open symbols or unfilled bars are used for model simulations.

four critical cognitive mechanisms that allowed the model to capture the full pattern of age differences: 1) the ability to

sustain attention across an encoding episode, 2) the ability to retrieve contextual representations for use as retrieval cues,

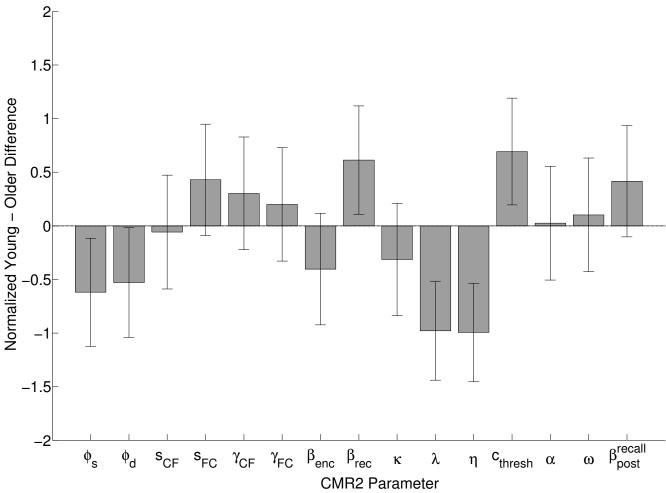


Figure 15. Age differences in CMR2 parameters. To put each parameter on the same scale, the individual participant estimates for each parameter were z-scored (ignoring age), and then averaged within age group. The bars represent differences in the mean z-scored parameter estimates for younger versus older adults; error bars are 95% confidence intervals on that difference. Parameters for which the confidence interval does not include zero differed significantly between age groups.

3) the ability to monitor retrievals and reject intrusions, and 4) the level of noise in retrieval competitions.

Testing theories of cognitive aging

A common, and reasonable, assumption in developing theories of age—related memory change is that the changes result from deterioration in some critical memory process. Theory development, therefore, typically takes the form of proposing a particular process as the locus of age—related deficits and developing a set of paradigms to test and refine that proposal (for recent examples see, Bastin et al., 2013; Werkle-Bergner et al., 2012; Yassa et al., 2011). This approach has yielded many theories (for reviews see Craik, 1977; Craik & Rose, in press; Kausler, 1994; Light, 1991; Lindenberger & Ghisletta, 2009; Salthouse, 1991; Zacks et al., 2000). The most successful of these theories have ex-

panded the boundaries of our knowledge of cognitive aging as scholars devise experimental paradigms to test the theories. An unintended consequence of this success is that the empirical and theoretical landscapes of cognitive aging have become somewhat fragmented, as theories become increasingly specialized and begin to focus on explaining nonoverlapping sets of empirical findings. Unless remedied this trend could undermine the goal of providing a general theory of age—related decline. We suggest that the most effective remedy is to occasionally take a step back and evaluate the various candidate theories against a common, independent dataset. Here we have attempted to evaluate three major aging theories against the complex pattern of age differences in free recall.

Specifically we evaluated the Associative Deficit Hypothesis (ADH; Naveh-Benjamin, 2000), The Inhibitory Deficit Hypothesis (IDH; Hasher & Zacks, 1988), and the Cogni-

tive Slowing Hypothesis (CSH; Salthouse, 1996). The ADH implicates impaired associative processes as a locus of agerelated memory changes; episodic memory depends on efficiently forming new associations and using existing ones. Thus, if older adults have difficulty with the processes that underlie the formation and use of associations, they will show memory deficits. Evidence for a specific associative deficit has come from comparing performance on tasks that depend on memory for associations with those that rely more heavily on memory for items (Old & Naveh-Benjamin, 2008). The IDH, suggests that inefficient inhibitory processes are the locus of age-related memory changes; because interference from competing memories is one of the biggest obstacles to successful retrieval (J. R. Anderson & Bower, 1974; Postman & Underwood, 1973; G. A. Radvansky, 1999a, 1999b; Underwood, 1957; Underwood & Postman, 1960), a reduced ability to inhibit competitors will produce memory impairments. Evidence for a specific inhibitory deficit comes from comparing tasks that vary in the need to keep irrelevant information from interfering with performance (for a review see Healey et al., 2008). The CSH suggests that a general slowing of cognitive processing underlies age-related declines in memory (and other cognitive abilities); because memory tasks provide limited time for encoding and retrieval and require precise temporal coordination of many memory processes, slowed processing will disrupt the memory system and cause deficits. Evidence that age-related memory deficits are attributable to slowed processing comes from large-scale individual difference studies that show a reduced correlation between age and memory ability when statistically controlling for variation in processing speed (Verhaeghen, 2011).

These theories have been widely influential because they make clear claims about the causes of age deficits that have been strongly supported by many years of research. We tested the ability of the three theories to account for a common set of findings: age differences on the free recall task. This task is well–suited to comparing theories because it shows large and reliable age differences, including spared recall initiation, impaired post–initiation transitions, and increased intrusions but a spared prior–list intrusion recency effect. Figure 1 summarizes this pattern of age differences. To test the theories against the data, we implemented each theory as a lesion within a model of healthy episodic memory: The Context Maintenance and Retrieval model version 2 (CMR2; Lohnas et al., submitted).

In an initial set of simulations we considered each of the age effects in isolation and tested whether the theories, implemented as lesions to the healthy younger adult model, were able to simulate older adults' deficit on that effect (or lack of deficit in the case of recall initiation and the prior—list intrusion recency effect). We found that all of the theories were able to account for each of the effects.

But accounting for the effects in isolation is not sufficient to establish the validity of a theory, because considering the effects in isolation allows the model to use different sets of parameter values when fitting each effect. The aging brain produces each of the effects with the same configuration, and we must expect a truly adequate theory of cognitive aging to do the same. For example, it may be that the set of parameter values that allows the model to simulate older adults' SPCs provides a very poor fit to their lag-CRPs. Therefore we tested the ability of the theories to simultaneously fit all five sets of age effects with a single set of parameter values. No theory was able to account for the full pattern simultaneously. Both the ADH and the IDH were unable to capture the SPC and lag-CRP data simultaneously. Examining Table A2 shows why: The parameter values that allowed these models to capture the effects when considered in isolation varied considerably from effect to effect and were in general quite different than the parameter values that allowed the model to make the best compromise when fit to the effects simultaneously. In other words, there was no single model configuration that was able to simulate all aspects of older adults' performance. The CSH, implemented as slowed encoding and retrieval processes, faired somewhat better, and was able to accurately simulate older adults SPCs. It was, however, unable to fully capture their temporal contiguity deficit, predicting an age deficit only for forward, but not backward, transitions. It also failed to account for older adults' PLI rates.

Toward a multi-factor theory of cognitive aging

The ADH, IDH, and CSH each implicate a specific memory process as the locus of age differences. The fact that none of these theories were able to simultaneously account for the full pattern of age differences suggests that a multi-factor theory is needed. A logical first step in developing such a theory is to combine single-factor theories. Surprisingly, even when all of the parameters implicated by the ADH, IDH, and CSH were allowed to vary, we were unable to achieve a satisfactory simulation of the age differences. In particular, the combined theories were unable to capture older adults' temporal contiguity deficit. Again, the reason for this is apparent from inspecting the parameter values in Table A1: The values for the combined theories model all differ substantially from the parameter values that allowed individual implementations to simulate the temporal contiguity deficit when considered in isolation, which are in turn quite different than the values required to allow the implementations to fit the other age effects. Put simply, the model mechanisms implicated by the theories do not provide the model with enough flexibility to mimic older adults' behavior.

It is noteworthy that simulating older adults' temporal contiguity deficit posed the greatest challenge to the theories. As we have argued above, temporal contiguity reflects

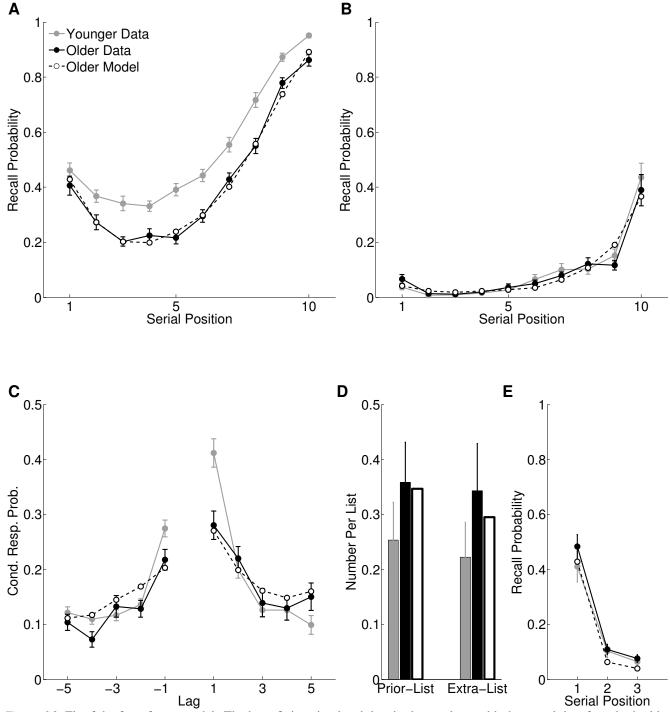


Figure 16. Fit of the four–factor model. The best–fitting simulated data is shown along with the actual data from both older and younger adults. Black lines or bars are used for older adults. Grey lines or bars are used for younger adults. Solid lines with filled symbols or filled bars are used for participant data. Broken lines with open symbols or unfilled bars are used for model simulations.

the ability to place events in their temporal context, and a deficit in this ability may blur the autobiographical timeline. Moreover, in light of the fact that strong temporal contiguity effects predict recall success (Healey et al., submitted; Sederberg, Miller, Howard, & Kahana, 2010; Spillers & Unsworth, 2011) and higher IQ (Healey et al., submitted), a deficit in

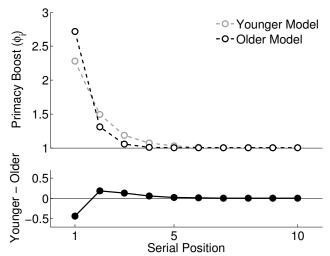


Figure 17. Age differences in primacy gradients implied by the four–factor model. The top panel shows the primacy gradients for older and younger adults. For each serial position, i, the gradients give the value of ϕ_i by which the strengths of newly formed context–to–feature associations are multiplied. The bottom panel shows the younger–older difference scores. The gradients were derived by entering the ϕ_s and ϕ_d parameter values form the younger adult model and the four–factor older adult model in to Equation 6 (Appendix).

temporal contiguity may be related to age deficits on nonmemory tasks. Therefore, the temporal contiguity deficit is perhaps the single most important aspect of the pattern of age effects.

How do we go about developing a theory that can account for all of the effects, including the critical temporal contiguity deficit? Our model–based approach to theory development allows the data to speak for themselves and tell us which model mechanisms are essential in capturing the aging pattern. We used the model to simulate each individual participant's data, which allowed us to determine which model parameters showed significant age differences. This procedure identified 6 critical parameters that allowed the model to capture the full pattern of age differences. This reduced 6–parameter model involves two fewer free parameters than did the combined ADH, IDH, and CSH model (8 total parameters). Thus, the fact that our model provided a superior fit is not simply a consequence of more parameters granting more flexibility.

The 6 parameters in our model of aging correspond to 4 distinct memory processes: 1) the ability to sustain attention across an encoding episode, 2) the ability to retrieve contextual representations for use as retrieval cues, 3) the ability to monitor retrievals and reject intrusions, and 4) the level of noise in retrieval competitions.

The first factor needed to simulate the age differences was

the primacy gradient. Two parameters (ϕ_s and ϕ_d) control extent of the primacy boost and how rapidly it decays. Older adults tended to show a somewhat stronger initial primacy boost than young adults, but one that decays rapidly (Figure 17). This pattern suggests that older adults have difficulty sustaining attention over the course of a trial. The notion that older adults have difficulty sustaining the efficiency of encoding processes across a trial is broadly consistent with theories that implicate age differences in attentional (Craik, 1977; Hasher & Zacks, 1988) or frontal executive processes (West, 1996). Our simulations allow a refinement of the general claim that older adults have impaired attentional processes by suggesting that the attentional deficit is specifically related to the ability to *sustain* attention.

The next factor was an impaired ability to reinstate contextual states during recall. One parameter, (β_{rec}) , governs the extent to which contextual representations are reactivated during retrieval of items. The ability to reactivate contextual states is at the heart of CMR2's ability to simulate retrieval dynamics as each item reactivates its associated context, which in turn serves as a retrieval cue for items near it in the presentation list. A reduced ability to retrieve contextual states that provide effective cues suggests a mechanistic basis for the self-initiated processing deficits from which Craik and colleagues have suggested older adults suffer (Craik, 1977; Craik et al., 2010). As noted by Howard et al. (2006), an impaired ability to retrieve contextual states, provides an elegant account of the fact that older adults show no impairment in initiating recall but do show a deficit in subsequent temporally-mediated transitions: Under the retrieved context framework, when the recall period begins, the existing state of mental context is used to cue recall with no need to reactivate previous states, only subsequent recalls depend on context reinstatement. Here we build on work of Howard et al. (2006) by showing that although impaired contextual retrieval is critical, is not the full story—other mechanisms are necessary to account for the full aging pattern.

The next factor needed to simulate older adults' performance was a lower threshold for accepting intrusions (the c_{thresh} parameter). In CMR2, intrusions are controlled (in part) during a post-retrieval editing phase in which the context representation associated with candidate retrievals is compared to the current context to ensure that retrieved items are associated with context similar to that which prevailed during list presentation. The higher the threshold on this similarity comparison, the less likely an intrusion will be made. Older adults had a lower threshold, indicating they were more likely to endorse intrusions (for behavioral evidence from externalized free recall tasks see Kahana et al., 2005). This finding is consistent with the spirit of the IDH (indeed, lowering the editing threshold was one way we implemented the IDH), and suggests older adults do have a specific deficit in the ability to reject intrusions of non-relevant items. Although this finding provides support for the IDH, the true value of our simulations is in showing that such a deficit is not sufficient to account for the full pattern—it forms one leg of a multi–factor set of deficits. The notion that older adults have difficulty monitoring the output of retrieval processes and editing out those that come from inappropriate sources has a long history in the study of aging (Hashtroudi, Johnson, & Chrosniak, 1989; McDonough & Gallo, 2013). CMR2's mechanism of computing the similarity of retrieved context to the current state of context suggests a computational basis of impaired source monitoring.

In addition to difficulties sustaining attention, impaired context retrieval, and lower editing thresholds, we found that it is necessary to assume an additional deficit to fully account for the aging pattern. Specifically, older adults also tended to have higher values for the parameters controlling noise in the retrieval-phase decision accumulators (λ and η). A consequence of noisy retrieval competitions is that items that would ordinarily stand little chance of being recalled will occasionally accumulate enough spurious evidence in the form of noise to win the competition. Such noise-induced recalls will have multiple consequences. First, they reduce the probability that true list items will be recalled, lowering recall accuracy. Second, they increase the likelihood of distant temporal transitions and may contribute to older adults' reduced temporal contiguity. Finally, they will allow more non-list items to win retrieval competitions and be passed on to the post-retrieval editing phase which, in combination with a reduced editing threshold, paves the way for PLIs and ELIs. In essence, noisy retrieval competitions make it difficult to distinguish target memories (list items) from competitors. This difficulty may help explain recent findings that whereas young adults suppress competitors during the process of interference resolution (Healey et al., 2010; Healey, Ngo, & Hasher, in press), older adults do not (Healey, Hasher, & Campbell, in press; Healey, Ngo, & Hasher, in press). Effectively applying suppression may require a signal-to-noise ratio that is high enough to allow target items to gain an initial advantage that can then be amplified by suppressing competitors; without that initial advantage it would be difficult for the memory system to "know" which items are likely to be competitors and therefore should be suppressed.

In summary, our multi–factor model of age differences in free recall suggests that age deficits cannot be localized to a particular process or even to a particular stage of processing. Instead, older adults suffer deficits at multiple stages: attentional deficits during encoding, difficulty generating cues during retrieval, difficulty selecting among competitors during retrieval competition, and difficulty monitoring and editing responses. The need for multiple deficits is consistent the finding that aging has broad influences on the brain (Raz, 2005).

It is important to note that although our results suggest

memory deficits cannot be attributed to a single deficient memory process, they leave open the possibility that a single underlying cause produces deficits in multiple processes. For example, some biological cause, such as accumulation of plaques or loss of white matter, may impair multiple brain networks, and thus multiple memory processes. Moreover, the rate and degree of change need not be the same in different networks, leaving room for divergent trajectories of impairments in different processes. Such a common cause may help explain the apparent tension between our finding that impairments in multiple processes are needed to capture the aging pattern and correlational studies that seem to suggest a single statistical factor accounts for age—related variation (Baltes & Lindenberger, 1997; Salthouse, 1996).

Relation to other paradigms and theories

For most of the paper we have focused on detailed measures of episodic memory derived from the dynamics of memory search in free recall. Our four-factor model provides a full account of these age differences. We began the paper, however, by discussing the broader empirical landscape of the aging and memory literature. We suggested that the broadest generalization that one can make about how memory changes with age is that the size of age deficits tracks the specificity of retrieval cues. Tasks that provide extremely strong cues, such as repetition priming in which the cue is the item itself show essentially no deficit (Mitchell & Bruss, 2003). As retrieval cues become less specific, age deficits increase, ranging from moderate on priming tasks with ambiguous cues Ikier et al. (2008) to large on tasks like free recall that provide only weak cues (Craik, 1968; Hultsch, 1969; Schonfield & Robertson, 1966).

Our results suggest a refinement and a caveat to this generalization. First, the refinement: the key dimension along which tasks vary may not be cue specificity but the extent to which they require the reinstatement of past contextual states. Simple tasks like priming do not require any reinstatement of context but simply rely on existing states of context. More complex tasks like free recall are critically dependent on reinstating contexts. Highly complex tasks such as reasoning may rely on the ability, not just to reinstate contextual states, but to control which states are reinstated and thereby provide access to task relevant memories. The caveat is that this generalization is a serious oversimplification in that it ignores the fact that differences in attention, evidence accumulation, and retrieval editing are also critical in determining whether a task will show age deficits and the exact nature of those deficits. Nonetheless it may prove to be a useful framework for thinking about age differences across many different types of tasks. Next we apply these ideas to age differences on a variety of tasks, and discuss how our four-factor model relates to existing theoretical accounts.

Priming. Repetition priming in tasks such as word naming or lexical decision involves a more rapid response to a stimuli the second time it is presented. The first time an item is presented it is likely to automatically activate its associated context representation as in the encoding phase of free recall. Therefore, when the item is presented a second time the context representation will be in a state that makes it easy to recognize the item. One way to think of this, is that in a naming task the context layer continually feeds activation to the item layer via context-to-item associations. Because the context layer tracks the history of recent events, the item representations of recently presented items will have more activation than the representations of items that were not presented recently. Therefore, when an item is presented a second time its item representation will already be partially active, reducing the amount of time required for it to fully activate and trigger a response. Note that this process does not require the reinstatement of any newly learned associations as in the retrieval phase of free recall. Moreover, priming effects are thought to arise, in part, from an automatic process (Balota, Black, & Cheney, 1992) and therefore older adults' difficulty with sustained attention would not be a detriment. Similarly, there is little need to edit out intrusions and the cues are so strong that evidence for the correct response is likely to accumulate rapidly even in the presence of noise.

The situation is more complex, however, with associative priming in which an initial item primes a related item. As discussed in the introduction, older adults do show deficits if a cue elicits several potential responses. For example, Ikier et al. (2008) had participants count the vowels in a list of words that included orthographically similar pairs.

When a word fragment (e.g., a _ l_ gy) resembled several words that had been seen in an earlier task but only one of which was a correct solution (e.g., ALLERGY and ANALOGY), older adults tended to show less priming for the correct solution than did younger adults. Several of the mechanisms in our four-factor theory could contribute to such an effect. For example, younger adults may be able to reject the competitor because the contextual retrieval allows them to determine it seems familiar because it appeared on an earlier task and not because it is a correct solution. For older adults, an inability to reinstate contextual states may make it difficult to determine that a candidate response was seen earlier in the task (we return to this idea when discussing source memory below). Noisy retrieval competitions may also contribute, increasing the chance that competitors will accumulate enough evidence to win. Finally, reduced editing thresholds would prevent older adults from editing such intrusions.

implicit transfer. Implicit transfer tasks are those on which older adults use information from a previous, ostensibly irrelevant task, on the current task (for a review see Healey et al., 2008). For example, Biss et al. (2013) had par-

ticipants study a list of words for free recall but gave them a surprise second recall test 15min after the first. During the 15min delay, participants completed an unrelated task in which some of the words from the free recall list were presented as distractors. The representation of these list items had little influence on the performance of younger adults, but older adults showed better recall for the repeated words than the non–repeated words.

Findings such as this have been interpreted within the framework of the IDH as evidence that older adults fail to inhibit information from previous tasks. Our four–factor theory suggests a somewhat different explanation: When context is used to cue retrievals in these tasks, items from the prior task receive equal degrees of evidence for both younger and older adults, but because the evidence accumulation process is noisier for older adults than for younger adults, the prior–task items win the competition more often for older adults. Older adults' lower threshold for endorsing candidate retrievals would amplify this effect. Adjudicating between the inhibitory and noisy competition accounts would require detailed simulations.

Recognition. Standard recognition tasks in which a list of items are presented after which the participant must indicate if a probe item was, or was not, a member of the list, typically show only a small age deficit, which can be difficult to detect in studies with modest sample sizes (Verhaeghen et al., 1993). They do however show robust differences in reaction times. These differences have been modeled by Ratcliff, Thapar, and McKoon (2004) using the diffusion model. They found that the differences in reaction time were largely accounted for by differences in non-decision time rather than by differences in the rate of evidence accumulation. The lack of age differences in the rate of evidence accumulation during recognition may seem at odds with our finding of a noisy evidence accumulation process in free recall. But differences between recognition and free recall make it difficult to interpret this discrepancy. A possible explanation, for example, is that evidence accumulation in recognition is driven by the match between the probe and memory (the probe will tend to be a very strong and specific cue for a particular item) whereas in free recall it is driven between a match between a contextual state and memory (any given contextual state will provide a relatively weak and non-specific cue for many list, and non-list items). Consistent with this interpretation, (Spaniol, Madden, & Voss, 2006) did find lower diffusion model drift rates on a version of the recognition task that placed greater demands on episodic retrieval (e.g., longer retention intervals).

Because of the modest age—related deficits in accuracy, most recent empirical and theoretical work on age differences in recognition memory has focused on more complex versions of the recognition task. As we have reviewed above, Naveh-Benjamin and colleagues have extensively in-

vestigated tasks that require memory for associations among items or items and aspects of the presentation event (Old & Naveh-Benjamin, 2008). Older adults' difficulty with such associative recognition tasks has been attributed to difficulty forming or retrieving new associations (Naveh-Benjamin, 2000). We have shown that such a deficit is not sufficient to account for age differences in free recall, but can our fourfactor theory account for differences in associative recognition? Under the retrieved context framework, associations between items are not direct but mediated by mental context. For example, while studying the item pair *cat*–*table* both words would form associations to very similar sates of mental context. Recognizing the pair at test could be, for example, modeled by allowing both words to retrieve their associated contexts and then computing their similarity, which could then be compared to some response threshold. A reduced ability to reactivate past contextual sates (i.e., the reduced β_{rec} parameter in our four–factor model) would clearly impair such a process.

Closely related to the associative deficit view is the notion of source memory: the ability to remember both that a particular item was seen and to remember specific details of the episode in which it occurred (Johnson, Hashtroudi, & Lindsay, 1993). There is considerable evidence that older adults are selectively impaired in the ability to recall the sources of memories (Spencer & Raz, 1995). A related view, deriving from dual process theories of recognition (Yonelinas, 2002), is that older adults have impaired recollection processes but intact familiarity processes (Jacoby, 1999). Although the retrieved context framework has not been used to formally model recognition tasks, such an implementation of the framework could be developed. Familiarity is essentially a signal that varies with how recently a probe item was presented; it will be stronger for probes that were presented recently and very low for probes that were not part of the list (i.e., lures). If the current state of context provides a history of past events, one could extract a familiarity signal by simply comparing the probe's item representation to the current state of context ($\mathbf{f}_{probe} \cdot \mathbf{c}_i$). The idea of recollection corresponds closely with context reinstatement, such that successful recollection would require not just that a probe have a strong similarity to items in memory, but that it successfully reactivates a context representation that is similar to the current state of context $(M^{FC}\mathbf{f}_{probe} \cdot \mathbf{c}_i)$. Our four-factor model suggests that it is precisely this reactivation on which older adults should show deficits. Therefore, our four-factor theory seems consistent with a selective recollection deficit.

Although our four-factor theory seems consistent with deficits in associative memory, source memory, and recollection, it would not necessarily predict that deficits would be specifically localized to recognition tasks that require of contextual details, because the other deficits implicated in our four-factor model (such as rapidly waning attention,

and noisy retrieval competitions) would be likely to cause deficits, perhaps only subtle ones, even on tasks that require memory only for items. Consistent with this suggestion, recent evidence shows that such subtle deficits in noncontext-dependent recognition tasks can be observed (Benjamin, 2010).

Recall tasks. Age related–deficits on cued recall tasks tend to be larger than those on recognition but not as large as those for free recall. This pattern makes a great deal of sense in light of our four-factor theory. Under the retrieved context framework, producing the associate of a probe item would require allowing the probe item to reinstate its context and then using that context to cue recall of the associate. This need for context reinstatement suggests older adults would have difficulty with the task and will often fail to reinstate the required context. The consequence of a single failure to reinstate context is quite different in cued and free recall, however. In cued recall, if one probe fails to reinstate its context, the failure is unlikely to have much of an impact on the probability that the next item will reinstate its context. By contrast, in free recall there are no probe items, rather the stream of recalls depends on each item reinstating a context that provides an effective cue for the next recall. Therefore, a failure of a single item to reinstate its context could halt the entire recall process. The dependence of sequential recalls in free recall may be a large part of the reason it shows larger age deficits than cued recall.

The influence of emotionally valenced stimuli on the magnitude of age-related memory impairments has recently become a topic of much interest. There is evidence that age deficits are smaller for positively valenced material (Mather & Knight, 2005; Thomas & Hasher, 2006). It is possible that emotional stimuli capture attention (Mather & Knight, 2005), which helps to offset older adults' difficulty with sustained attention. It may also be that emotional stimuli introduce large shifts in mental context by injecting "more" of their context into the context layer than do non-emotional stimuli (i.e., emotional stimuli may temporarily increase the drift rate parameter). Such large context shifts may serve to make them particularly accessible: All else being equal if emotional stimuli cause their associated contextual states to be strongly represented in the context vector, the change will take a long time to dissipate (i.e., to be erased due to drift), and therefore many subsequent events will be linked to the emotional stimuli, providing many cues, essentially producing a encoding variability effect (Lohnas & Kahana, Submitted).

Moving away from laboratory tasks, there is evidence that older adults have difficulty retrieving the details of their autobiographical memories (St Jacques, Rubin, & Cabeza, 2012). When asked to recall specific life episodes, younger adults tend to provide many details. For example, if asked to recall a birthday party, they may report which people attended, what

kind of cake they had, what presents they received. By contrast, older adults tend to provide "gist" level summaries that rely on semantic details rather than episodic details tied to a specific spatio—temporal context (Levine et al., 2002). Under the retrieved context framework, recalling specific details of an episode in response to a question about birthday parties would require using the question as a probe to reinstate a particular contextual sate. If older adults have difficulty with such reinstatement, as our simulations suggest, one would expect that they would have impaired access to the details of the episode.

Non-memory tasks. Older adults show deficits even on tasks that do not directly test memory (Baltes & Lindenberger, 1997; MacDonald et al., 2004; Park et al., 2002; Zelinski & Burnight, 1997). Although we certainly make no claim that our four–factor theory provides a comprehensive account of all of these differences, it is worth considering a few examples of how it could be extended beyond memory tasks.

Tasks that measure processing speed have arguably been the most influential non-memory tasks in the cognitive aging literature. We suggest that noisy accumulation of evidence could lead to slowing on many different tasks. For example, string comparison tasks are often used to measure processing speed. In these tasks participants must compare two strings of numbers or letters and determine if the two are identical or not. Older adults are slower than younger adults to make such comparisons (Lustig et al., 2006). Their slow responding may be due to a general slowing of processing, or it may be due to a specific slowing of the evidence accumulation processes caused by increased noise. Because studies that measure processing speed tend not to include tasks specifically designed to measure the evidence accumulation process, it is conceivable that many of the findings that have been attributed to age differences in speed of processing are, on a computational level, due to age differences in selecting among competing response alternatives. Indirect support for this notion comes from the finding that older adults deficit in processing speed is reduced in comparison tasks that present a single item on screen at a time, rather than a full page of items as more typical (Lustig et al., 2006). Although this finding has been interpreted as evidence that older adults have trouble inhibiting interference from items they are not currently working on, it may be that these items add noise to the accumulation process.

Processing speed tasks are quite simple. At the other end of the spectrum older adults show deficits on complex cognitive activities such as reasoning tasks. We have suggested that an ability to regulate the drift of the mental context representation so that it provides effective cues to memories relevant to the current tasks is a critical component in general intelligence. In support of this claim we have shown that, among young adults, those individuals who's recall dynam-

ics is biased toward the use of newly formed temporal associations (rather than long-standing semantic associations) show higher IQ scores than those who show a weaker influence of temporal associations (Healey et al., submitted). It may be that older adults' reduced ability to reinstate contextual states at retrieval contributes both to their memory deficits and to impairments on complex cognitive tasks such as IQ tests.

A New Approach to Theory Development

The above is merely a sketch of how one could begin to apply the four–factor theory beyond the free recall task; a first–approximation verbal fit of the theory to the data. In the spirit of the approach we have taken to analyzing the free recall task we want to stress that this sort of verbal theory fitting is insufficient. Much more work will be needed to rigorously assess the limits of the explanatory power of our theory. Indeed, rather than endorsing the specifics of the four–factor model as a complete theory of aging, our main goal is to advocate for a new approach to theory development in the study of aging and memory. Specifically, theories of aging should be specified in sufficient detail that model–based quantitative predictions can be derived and validated against a large volume of data.

Model-based predictions are necessary because, as illustrated in our simulations, it can be quite difficult to predict how an impairment in a particular cognitive process will alter the behavior of the memory system. These difficulties are only compounded when the goal is to adjudicate between competing theories. An even more fundamental limitation in verbal theories lies in the flexibility of their predictions. We implemented each theory in three different ways by allowing different model parameters to vary. These parameters grant each implementation a certain amount of flexibility that allowed it to produce different patterns of predicted behavior. If a theory has too much flexibility-if it can contort itself to fit many different data patterns—it runs the risk of being unfalsifiable. As it turned out, the flexibility of our implementations was not enough to allow the theories to fit the older adults' data. But one could imagine many other ways to implement these theories, each with its own degree of flexibility. That is, because it admits of being specified and implemented in many different ways, a verbal theory has a tremendous amount of "latent flexibility". Because a model reflects one out of many ways a given verbal theory could be implemented the model has, almost by necessity, less flexibility than the verbal theory that it implements. In our view, the latent flexibility of verbal theories is a hidden reason that the aging literature has not converged toward a common theoretical account.

Model-based predictions are not, by themselves, sufficient. Theories must also be evaluated against a large volume of data because, as our simulations show, even when translated into models, single effects were not sufficient to distinguish among theories. However, by considering a complex, multi-variate pattern we were able to show that none of the theories, not even the combination of the theories, can fully account for the pattern of age differences. To put it more starkly, if we had attempted to validate the theories at a verbal level against isolated effects, we would have concluded that each of the theories provided a viable account, but quantitatively validating them against multiple effects simultaneously, revealed all of the theories to be inadequate.

Therefore, we suggest that a profitable avenue for future work is to document and model the details of age differences on paradigms that have been foundational in the young adult episodic memory literature. This will include serial recall, free recall, and recognition tasks. These tasks are ideal because detailed measures of task performance are welldocumented with younger adults, allowing for easy age comparisons. Moreover, there are existing well-specified and validated models of these tasks (e.g., Farrell, 2012; Kahana & Sekuler, 2002; Murdock, 1993; Nosofsky, Little, Donkin, & Fific, 2011; Ratcliff, Thapar, & McKoon, 2004; Shiffrin & Steyvers, 1997), which will admit quite easily of the same approach we used here—use the models as a healthy memory system and lesion various processes to see which are critical in producing age deficits. Researchers have already made much progress applying drift diffusion models to recognition data (Ratcliff, Thapar, & McKoon, 2004; Spaniol et al., 2006) and various forced alternative choice tasks like lexical decision and brightness discrimination (Ratcliff, Gomez, & McKoon, 2004; Starns & Ratcliff, 2010). Surprenant et al. (2006) have used the SIMPLE model to show the influence of stimuli similarity on age differences in serial recall. Modeling efforts should also focus on key tasks that have been used to test existing aging theories such as those used to assess associative deficits, inhibitory deficits, and speed deficits. Researchers working on the associative deficits (Li et al., 2005) and source memory deficits (Benjamin, 2010) have already begun pursuing this path.

A potential complication of our proposal is that different researchers will use different models. For example, we have used the CMR2 model, Ratcliff, Thapar, and McKoon (2004) and Spaniol et al. (2006) have used the diffusion model, Surprenant et al. (2006) have used the SIMPLE model, and both Benjamin (2010) and Li et al. (2005) have used novel models specifically designed to address age differences. The use of so many different models creates the danger that the land-scape of this emerging modeling literature will become as fragmented as the current landscape of verbal theories. It will therefore be critical to directly pit model–based theories against each other within a common framework, much as we have done here for verbal theories.

Conclusions

Theory development in cognitive aging has reached a level of sophistication at which it is no longer possible to fully evaluate a given theory against univariate measures because a theory that accounts for multiple single effects, when considered in isolation, may fail to account for the same effects when considered simultaneously. Instead theories must be evaluated against the details of multivariate data sets such as the one presented here. Such evaluations will require implementing aging theories within computationally explicit models of healthy memory.

Using this model—based approach, we developed a four–factor model of age differences on the free recall task. By insisting that candidate theories account for multiple data points *simultaneously* we were able to quickly eliminate in-adequate theories and develop a novel theory that implicates four factors: 1) the ability to sustain attention across an encoding episode, 2) the ability to retrieve contextual representations for use as retrieval cues, 3) the ability to monitor retrievals and reject intrusions, and 4) the level of noise in retrieval competitions. This approach can be extended to develop a model of age differences on a broad range of tasks. A tight coupling between experimentation and model—based theory evaluation promises rapid progress in building a comprehensive theory of the aging memory system.

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Appendix Model Details

In CMR2 (Lohnas et al., submitted) two types of cognitive representations interact: (a) the feature representation (F), in which the features of the current list item are activated, and (b) the context representation (C), in which the current state of context is activated. Each of these representational layers is defined as a vector. Hebbian associative matrices connect these representations, one connecting features to context (M^{FC}) , and one connecting context to features (M^{CF}) .

Each association matrix is a weighted sum of a pre-experimental component (M_{pre}^{FC} and M_{pre}^{CF}) that reflects long-standing semantic relationships and an experimental component (M_{exp}^{FC} and M_{exp}^{CF}) that reflects new learning that occurs during the experiment. The semantic associations in M_{pre}^{FC} and M_{pre}^{CF} are defined using Latent Semantic Analysis (LSA; Landauer & Dumais, 1997). LSA measures the semantic relationship between two words as the cosine of the angle between the words' representations in a multidimensional model of semantic space.

Studying an item activates the corresponding features, \mathbf{f}_i , which in turn retrieve the context states to which those features have previously been associated:

$$\mathbf{c}_i^{\mathbf{IN}} = M^{FC} \mathbf{f}_i \tag{1}$$

This retrieved context, $\mathbf{c}_i^{\mathbf{IN}}$, is incorporated into the context representation by adding it to the current context vector \mathbf{c}_{i-1} . The context vector is continuously maintained at unit length. Therefore, when a new state of context is added to the existing sate, the two vectors, \mathbf{c}_{i-1} and $\mathbf{c}_i^{\mathbf{IN}}$ must be scaled so their sum has a length of one:

$$\mathbf{c}_i = \rho_i \mathbf{c}_{i-1} + \beta \mathbf{c}_i^{\mathbf{IN}} \tag{2}$$

Where β is a model parameter governing how quickly context changes, and ρ_i is chosen such that $\|\mathbf{c}_i\| = 1$:

$$\rho_i = \sqrt{1 + \beta^2 [(\mathbf{c}_{i-1} \cdot \mathbf{c}_i^{\mathbf{IN}})^2 - 1]} - \beta (\mathbf{c}_{i-1} \cdot \mathbf{c}_i^{\mathbf{IN}}).$$
 (3)

More intuitively, because context is always of unit length it can be thought of as point on the surface of a (hyper) sphere, with β determining how far along the surface of the sphere it travels with each newly presented item.

At the start of an experimental session, the experimental associations are initialized to zero. As each new item is presented, new experimental associations are formed, both between the item's representation and the current state of context (represented in M_{exp}^{FC}) and between the current state of context and the item (represented in M_{exp}^{CF}). These associations are formed according to a Hebbian outer-product learning rule:

$$\Delta M_{exp}^{FC} = \mathbf{c}_{i-1} \mathbf{f}_i^{\top}$$

$$\Delta M_{exp}^{CF} = \mathbf{f}_i \mathbf{c}_{i-1}^{\top}$$
(4)

These newly formed experimental associations are incorporated with pre-experimental semantic associations. The balance between new and existing associations is controlled by parameters γ_{FC} and γ_{CF} :

$$\begin{split} M^{FC} &= (1 - \gamma_{FC})(I + s_{FC}M_{pre}^{FC}) + \gamma_{FC}M_{exp}^{FC} \\ M^{CF} &= (1 - \gamma_{CF})(I + s_{CF}M_{pre}^{CF}) + \gamma_{CF}\phi_{i}M_{exp}^{CF} \end{split} \tag{5}$$

 s_{FC} and s_{CF} are scaling parameters that control the influence of pre-experimental semantic associations. Note that the Lohnas et al. (submitted) implementation of CMR2 used only s_{CF} , effectively setting s_{FC} to zero and preventing features from activating the contexts of semantically associated features. In line with the observation that most extra-list intrusions are semantically related to list items (Zaromb et al., 2006), we found that simulating the extra-list Intrusion rates of older adults required allowing features to activate semantically related contexts. I is an identity matrix the same size as M_{pre}^{CF} and M_{pre}^{FC} (The two associative matrices are of the same size for all simulations in this paper). Effectively this means that the on-diagonal terms are not multiplied by the s parameter. This allows the s parameter to scale semantic relations between pairs of different items while having no effect on auto-associations.

 ϕ_i simulates increased attention to beginning-of-list items, producing a primacy effect, by scaling the magnitude of context-to-feature associations across the list:

$$\phi_i = \phi_s e^{-\phi_d(i-1)} + 1, \tag{6}$$

where ϕ_s and ϕ_d are model parameters. See Sederberg et al. (2008) for a more complete discussion.

In previous implementations of the retrieved context framework the experimental component of the associative matrices were re-initialized for each simulated list, erasing the learning that occurred on previous lists. By contrast, in CMR2 the matrices are initialized once at the beginning of the simulated experiment and allowed to accumulate associations across all lists. This development allows CMR2 to simulate prior list intrusions. In a departure from the Lohnas et al. (submitted) implementation of CMR2, we include an extended vocabulary that includes a strong associate of each presented item. These items are included on the assumption that ELIs are driven by strong semantic associations, and can be most naturally modeled by providing the model with a set of rich semantic associates.

During recall, the current contextual state is used to cue retrieval via the M^{CF} associations:

$$\mathbf{f}_{t}^{\mathbf{IN}} = M^{CF} \mathbf{c}_{t},\tag{7}$$

The resulting \mathbf{f}_t^{IN} gives the degree of support, or activation, for each item in the model's vocabulary. Items with low activation values are unlikely to be recalled by the retrieval process described below and considering them as candidates for

retrieval is extremely computationally expensive. Therefore, only the 40 items with the highest activation values are assigned to a vector **a** of retrieval candidates. The values in **a** are then used as the starting point for a set of competitive accumulators, one for each candidates, according to the leaky competitive accumulator model of Usher and McClelland (2001):

$$\mathbf{x}_{n} = (1 - \tau \kappa - \tau \lambda \mathbf{N}) \mathbf{x}_{n-1} + \tau \mathbf{a} + \epsilon,$$

$$\mathbf{x}_{n} \rightarrow max(\mathbf{x}_{n}, \mathbf{0})$$
(8)

 \mathbf{x}_n is a vector with one element for each retrieval candidate in \mathbf{a} . When the retrieval competition starts, all elements are set to zero (i.e., $\mathbf{x}_0 = \mathbf{0}$) and the activation for each item given in \mathbf{a} is used as its starting line in the race to threshold. τ is a fixed time constant, κ is a parameter that determines the decay rate for item activations, and λ is the lateral inhibition parameter, scaling the strength of an inhibitory matrix \mathbf{N} that subtracts each item's activations from all of the others except itself. ϵ is a random vector whose elements are drawn from a random normal distribution with mean zero and standard deviation η . The second line of Equation 8 means that the accumulating elements cannot take on negative values. \mathbf{x}_n continues to be updated until one of the activation values exceeds its threshold or until the recall period ends.

CMR2 dynamically sets the retrieval threshold of each item as the recall period progresses to allow items that were recalled earlier in the period to participate in, but not dominate, current retrieval competitions. Specifically, at the beginning of the recall period, each item, i, has a threshold of $\Theta_i = 1$. If item i is retrieved, its threshold is incremented by a value ω and then gradually returns to 1 with subsequent recalls:

$$\Theta_i = 1 + \omega \alpha^j \tag{9}$$

Where α is a parameter between 0 and 1; the larger the value of α , the more intervening retrievals needed before and item is likely to be retrieved again.

The first word to accumulate enough activation to cross its threshold wins the retrieval competition. The winner's representation is reactivated on F, allowing the model to retrieve the contextual state associated with the item. Context is updated using the same mechanism used during the study period (separate parameters, β_{enc} and β_{rec} control the rate of context drift during encoding and retrieval). Before the item is actually output by the model, however, it undergoes a post-retrieval editing phase, consistent with the observation that people often report thinking of items that they do not overtly recall during free recall experiments (Keppel, 1968; Wixted & Rohrer, 1994). Editing is accomplished by comparing the context representation retrieved by the candidate item with the currently active context representation (J. R. Anderson & Bower, 1972; Dennis & Humphreys, 2001):

$$\mathbf{c}_{t+1}^{\mathbf{IN}} \cdot \mathbf{c}_t. \tag{10}$$

Because associations are formed between items and the context that prevailed when they were originally presented, true list items will tend to retrieve a context that is similar to the context that prevails during retrieval. The match between retrieved context and the current context will depend on how much contextual drift has occurred between original presentation and the recall event. Relatively little drift will have occurred for items that were genuinely presented on the current list, whereas considerable drift will have occurred for items that were presented on earlier lists. Thus, on average, accurate recalls will produce a higher value than either PLIs or ELIs. If the comparison returns a value that is beneath a threshold parameter, c_{thresh} , the item is rejected as an intrusion.

Once an item is either recalled or rejected, another recall competition begins. This series of competitions continues until the end of the recall period is reached, at which point the next trial begins. It is thought that the transition from one trial to the next is accompanied by a change in temporal context Sahakyan and Kelley (2002). CMR2 simulates this shift in temporal context by activating a unique

"disruption" item on the feature layer and allowing this item to update context using Equation 2, with a post-recall drift rate parameter, β_{post}^{recall} .

Details of Simulations

The model parameters obtained by fitting the model independently to the average younger adult and average older adult data are shown in Table A1. These are the parameters used to generate the model simulations shown in Figure 5. Table A1 also shows the average younger and older adult parameter values obtained by fitting the model to individual participant's data.

Table A2 shows the parameter values obtained by fitting each of the verbal theory implementations, both independently to each effect (i.e., the values used to generate Figures 6—10) and simultaneously to all the effects (i.e., the values used to generate Figures 11—13). The table also shows the Root Mean Squared Deviation (RMSD) values for each model.

Table A1

The optimized parameter values for simulations of average data and individual participant data.

			<u> </u>		
Parameter	Younger	Older	Younger	Older	
	(average data)	(average data)	(individual data)	(individual data)	
ϕ_s	1.283	1.553	1.483	1.655	
ϕ_d	0.960	1.145	0.884	1.034	
S_{cf}	6.147	3.398	2.109	2.177	
S_{fc}	0.006	0.005	0.004	0.001	
γ_{cf}	0.984	0.969	0.918	0.898	
γ_{fc}	0.540	0.583	0.411	0.403	
eta_{enc}	0.561	0.552	0.514	0.522	
eta_{rec}	0.375	0.266	0.421	0.329	
К	0.108	0.104	0.274	0.289	
λ	0.178	0.275	0.187	0.263	
η	0.427	0.492	0.431	0.496	
C_{thresh}	0.000	0.000	0.052	0.009	
α	0.617	0.591	0.810	0.809	
ω	13.658	4.726	12.515	12.201	
eta^{recall}_{post}	0.961	0.922	0.924	0.905	
au	10.000	10.000	10.000	10.000	
ϵ	0.000	0.000	0.000	0.000	

Table A2

The optimized parameter values for each verbal theory implementation's simulation of all data simultaneously and each effect independently.

Theory	Implementation	Parameter	All Data	SPC	PFR	Lag-CRP	Intrusions	PLI-Recency
ADH	Weak Associations	γ_{CF}	0.986	0.926	0.956	0.899	0.964	0.983
		$_{ m RMSD}^{\gamma_{FC}}$	0.436	0.510	0.614	0.477	0.966	0.874
	3.T. 1 4 1		0.065	0.038	0.023	0.025	0.044	0.007
	Noisy Associations	€ DMCD	0.001	0.061	0.186	0.052	0.000	0.000
	Weak & Noisy	RMSD	0.082 0.977	0.058 0.943	0.026 0.961	0.023 0.895	0.091 0.982	0.074 0.982
	weak & Noisy	γ_{CF}	0.389	0.389	0.316	0.893	0.982	0.982
		γ_{FC}	0.369	0.369	0.002	0.007	0.000	0.000
		RMSD	0.004	0.030	0.002	0.020	0.020	0.000
IDH	List Isolation		0.807	0.362	0.025	0.711	0.923	0.746
Юп	List isolation	$eta_{post}^{recall} \ ext{RMSD}$	0.807	0.362	0.093	0.711	0.923	0.006
	Retrieval Editing		0.071	0.036	0.024	0.043	0.093	0.006
	Retileval Editing	$c_{thresh} \\ ext{RMSD}$	0.000	0.204	0.001	0.045	0.084	0.019
	Drift Rate	β_{enc}	0.610	0.596	0.489	0.532	0.630	0.458
	Dint Rate	eta_{rec}	0.551	0.846	0.887	0.252	0.514	0.823
		RMSD	0.065	0.046	0.019	0.032	0.001	0.006
CSH	Slowed Encoding	γ_{CF}	0.986	0.926	0.956	0.899	0.964	0.983
	· ·		0.436	0.510	0.614	0.477	0.966	0.874
		$_{ m RMSD}^{\gamma_{FC}}$	0.065	0.038	0.023	0.025	0.044	0.007
	Slowed Retrieval	au	18.286	14.524	9.190	18.524	39.619	9.857
	D 1 61 1	RMSD	0.069	0.040	0.035	0.029	0.271	0.034
	Both Slowed	τ	17.818	14.545	53.182	37.727	9.182	11.818
		γ_{CF}	0.959 0.877	0.943	0.975	0.927	0.986	0.973 0.789
		$_{ m RMSD}^{\gamma_{FC}}$	0.877	0.552 0.026	0.318 0.020	0.761 0.022	0.320 0.003	0.789
All Theories Combined			0.049	0.020	0.020	0.022	0.003	0.008
All Theories Combined	_	γ_{CF} γ_{FC}	0.595					
		γ F C €	0.002					
		β_{enc}	0.519					
		β_{rec}	0.181					
		β_{post}^{recall}	0.749					
			0.006					
		c_{thresh}	18.339					
		RMSD	0.028					
Four Factor Model	_	β_{rec}	0.251					
		ϕ_s	1.716					
		ϕ_d	1.011					
		C_{thresh}	0.009					
		λ	0.273					
		η	0.493					
RMSD = Root Mean Square Do		ŔMSD	0.028					

RMSD = Root Mean Square Deiviation, which was minimized by the genetic algorithm.