

## Problem Q

### Longest V-Shape Subsequence

Time limit: 3 seconds

Memory limit: 256 megabytes

#### Problem Description

Suppose you are given a sequence  $S$  of integers  $s_1, \dots, s_n$ .  $s_{i_1}, \dots, s_{i_k}$  is a V-shape subsequence of  $S$  if the following conditions.

- $i_1 < i_2 < \dots < i_k$ .
- $k > 2$ .
- There exists  $c$  such that  $1 < c < k$ ,  $s_{i_1} > s_{i_2} > \dots > s_{i_c}$  and  $s_{i_c} < s_{i_{c+1}} < \dots < s_{i_k}$ .

Write a program to compute the length of the longest V-shape subsequence of  $S$ .

#### Input Format

The first line of the input contains an integer  $t$  ( $t \leq 25$ ) indicating the number of test cases. Each test case consists of two lines. The first line contains an integer  $n$  which is the length of the sequence  $S$ . The second line contains  $n$  32-bit integers  $s_1, \dots, s_n$  separated by blanks. You may assume  $n \leq 10^5$ .

#### Output Format

For each test case, output the length of the longest V-shape subsequence of  $S$ . If there does not exist such subsequence, output 0.

#### Sample Input

```
3
3
1 0 1
5
0 1 0 1 0
7
1 2 3 4 5 6 7
```

#### Sample Output

```
3
3
0
```