## $\begin{array}{c} {\rm Manual~for~Package:~mathematics} \\ {\rm Revision~25M} \end{array}$

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		wavelet_transform
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### 1 calendar

# $1.1 \quad days\_per\_month$

# 1.2 isnight

# 2 mathematics

mathematical functions of various kind

# ${\bf 2.1} \quad cast\_byte\_to\_integer$

cast byte to integer

# 3 complex-analysis

operations on complex numbers

#### 3.1 complex\_exp\_product\_im\_im

### 3.2 complex\_exp\_product\_im\_re

#### 3.3 complex\_exp\_product\_re\_im

### $3.4 \quad complex\_exp\_product\_re\_re$

```
product of the real part of two complex exponentials
re(c1 exp(io1x))*re(c2 exp(io2x)) =
               real(c1*c2*exp(i*(n1+n2)*o*x)) ...
             + real(conj(c1)*c2*exp(i*(n2-n1)*o*x)) )
the product has two frequency components
 input :
       c : complex amplitudes
       o : frequencies
output :
       {\tt cp} : amplitude of the product
       {\tt op} : frequencies of the product
3.5 croots
nth-roots of a complex number
input:
c : complex number
n : order of root
    n must be rational, to obtain n solutions
    otherwise no finite set of solutions exists
r : roots of the complex number
3.6 \quad root\_complex
root of a complex number
```

### 4 derivation

3.7 test\_imroots

derivation of several functions by means of symbolic computation

4.1	derive_acfar1
4.2	$derive\_ar1\_spectral\_density$
4.3	derive_ar2param
4.4	${\it derive\_arc\_length}$
4.5	$derive\_fourier\_power$
4.6	$derive\_fourier\_power\_exp$
4.7	$derive\_laplacian\_curvilinear$
4.8	$derive\_laplacian\_fourier\_piecewise\_linear$
4.9	${\tt derive\_logtripdf}$
4.10	derive_phase_drift_inv

4.11	$ m derive\_smooth1d\_parametric$
4.12	${\tt derive\_spectral\_density\_bandpass\_initial\_condition}$
5	derivation/master
5.1	$derive\_bc\_one\_sided$
5.2	${\bf derive\_convergence}$
5.3	${\tt derive\_error\_fdm}$
5.4	$ m derive\_fdm\_poly$
5.5	$ m derive\_fdm\_power$
5.6	$ m derive\_fdm\_taylor$
5.7	$ m derive\_fdm\_vargrid$

- $5.8 \quad derive\_fem\_2d\_mass$
- 5.9 derive\_fem\_error\_2d
- 5.10 derive\_fem\_error\_3d
- 5.11 derive\_fem\_sym\_2d
- 5.12 derive\_grid\_constants
- 5.13 derive\_interpolation
- 5.14 derive\_laplacian
- 5.15 derive\_limit
- 5.16 derive\_nc\_1d
- 5.17 derive\_nc\_1d\_

5.18	$ m derive\_nc\_2d$
5.19	$derive\_nonuniform\_symmetric$
%	
5.20	${\bf derive\_richardson}$
5.21	$derive\_sum$
5.22	nn
5.23	${ m test\_derive}$
5.24	$test\_derive\_fdm\_poly$
5.25	${ m test\_filter}$

5.26 test\_vargrid

# 6 derivation

derivation of several functions by means of symbolic computation

### $6.1 \quad simplify\_atan$

symbolic simplification of the arcus tangent

### 7 mathematics

mathematical functions of various kind

## 7.1 entropy

### 8 finance

- $8.1 \quad derive\_skewrnd\_walsh\_paramter$
- $8.2~{
  m gbb\_geostd\_entire\_series}$
- 8.3 gbb\_mean
- 8.4 gbb\_simulate
- $8.5 \quad gbb\_std$

8.6	${ m gbm\_bridge}$
8.7	${ m gbm\_cdf}$
8.8	${f gbm\_fit}$
8.9	${f gbm\_fit\_old}$
8.10	${ m gbm\_geomean}$
8.11	${ m gbm\_geostd}$
8.12	${ m gbm\_inv}$
8.13	${ m gbm\_mean}$
8.14	${\tt gbm\_mean\_entire\_series}$

 $8.15 \quad \text{gbm\_median}$ 

8.16	${ m gbm\_moment2par}$
8.17	${\tt gbm\_moment2par\_entire\_series}$
8.18	${ m gbm\_pdf}$
8.19	$gbm\_simulate$
8.20	${ m gbm\_skewness}$
8.21	${f gbm\_std}$
8.22	${\tt gbm\_std\_entire\_series}$
8.23	${\tt gbm\_transform\_time\_step}$
8.24	put_price_black_scholes

 $skewgbm\_simulate$ 

8.25

#### 8.26 skewrnd\_walsh

- 9 finance/test
- $9.1 ext{test\_gbm}$
- 9.2  $test\_gbm\_pdf$
- 9.3 test\_skewrnd\_walsh

# 10 fourier/@STFT

#### 10.1 STFT

class for short time fourier transform

Note: the interval Ti should be set to at leat 2\*max(T), as
 otherwise coefficients
 tend to oscillate in the presence of noise
Note: for convenience, the independent variable is labeled as time
 (t),
 but the independent variable is arbitrary, so it works
 likewise in space

#### 10.2 itransform

inverse of the short time fourier transform

10.3 stft\_

static wrapper for  ${\tt STFT}$ 

#### 10.4 stftmat

transformation matrix for the short time fourier transform

#### 10.5 transform

short time fourier transform

#### 11 fourier

support and analysis functions both for the discrete (fast) fourier
 transform (dft/fft)
and continuous fourier analysis (fourier series)

### 11.1 amplitude\_from\_peak

```
amplitude and standard deviation of the amplitude of a frequency
    component
represented by a peak in the fourier domain
input :
h : peak height
w : peak width at half height

output:
a : amplitude in real space
s : standard deviation of the frequency (!)
```

#### 11.2 caesaro\_weight

#### 11.3 dftmtx\_man

F : fourier matrix

```
fourier matrix in matlab style with a limited number of rows,
columns of higher frequencies are omitted

input :
n : number of samples
nr : number of columns

output :
```

### 11.4 example\_fourier\_window

#### 11.5 fft2\_cartesian2radial

#### 11.6 fft\_man

```
fast fourier transform for complex input data
input:
F : data in real space
output :
F : fourier transformation of F
```

#### 11.7 fft\_rotate

#### 11.8 fftsmooth

```
smooth the fourier transform and determine upper and lower bound
    confidence intervals

input :
f :
sfunc : a smoothing function (for example fir convolution with
    rectangular window)
        returns filtered (mean) value and normalized fir window
nf : window length
nsigma : number of standard deviations for confidnce intervals

output :
ff : filtered fourier transform
l : lower bound
u : upper bound
```

#### 11.9 fix\_fourier

fill gaps (missing data) by means of fourier extrapolation
fix periodic data series with fourier interpolation
longest gap should not exceed 1/2 of the shortest time span of
 interest (1/cutoff frequency)
note: this limit equals the position of first side lobe of the ft
 of a rectangular window with gap length

#### 11.10 fourier\_2d\_padd

### 11.11 fourier\_2d\_quadrants

#### 11.12 fourier\_axis

#### 11.13 fourier\_axis\_2d

```
function [fx, fy, fr, ft, Tx, Ty, mask, N] = fourier_axis_2d(L,n)
```

#### 11.14 fourier\_cesaro\_correction

#### 11.15 fourier\_coefficient\_piecewise\_linear

fourier series coefficients of a piecewise linear function (not coefficient of discrete fourier transform) function can be discontinuous between intervals scales domain length to 2pi

#### input :

1,r : end points of piecewise linear function

lval, rval: values at end points

L : length of domain

n : number of samples/highest frequency

#### output :

a, b : coefficients for frequency components

### 11.16 fourier\_coefficient\_piecewise\_linear\_1

fourier series coefficients of a piecewise linear function (not coefficient of discrete fourier transform) function can be discontinuous between intervals scales domain length to 2pi

#### input :

X : end points of piecewise linear function

Y : values at end points

#### output :

ab : coefficients for frequency components

### 11.17 fourier\_coefficient\_ramp3

fourier series coefficient of a ramp

### 11.18 fourier\_coefficient\_ramp\_pulse

fourier series coefficient of a ramp pules

#### 11.19 fourier\_coefficient\_ramp\_step

fourier coefficient of a ramp-step

### 11.20 fourier\_coefficient\_square\_pulse

fourier series coefficients of a square pulse

### 11.21 fourier\_complete\_negative\_half\_plane

#### 11.22 fourier\_cubic\_interaction\_coefficients

#### 11.23 fourier\_derivative

derivative via fourier transform exponential convergence for periodic functions results in spurious oscillations for aperiodic functions

#### input:

x : data, sampled in equal intervals

k : order of the derivative

dx : kth-derivative of x

note : 1) the derivative converges with spectral accuracy, i.e. is exact up to rounding condition for L sufficiently large and  ${\bf x}$  being periodic

2) the derivative converges with order p, when x has only p-continous derivatives, including discontinuous derivatives

over the boundary

3) discontinuous derivatives result in gibbs phenomenon  $\ \ \,$ 

### 11.24 fourier\_derivative\_matrix\_1d

#### 11.25 fourier\_derivative\_matrix\_2d

### 11.26 fourier\_expand

expand values of fourier series

#### 11.27 fourier\_fit

fit a fourier series to a set of sample points that are not spaced
 in
equal intervals

# 11.28 fourier\_freq2ind

### 11.29 fourier\_interpolate

interpolate samples y sampled at moments (location) t to locations ti

### 11.30 fourier\_matrix

transformation matrix for a continuous fourier series (not for the discrete  ${\rm dft/fft}$ )

#### 11.31 fourier\_matrix2

transformation matrix for a continuous fourier series (not for the discrete  ${\rm dft/fft}$ )

#### 11.32 fourier\_matrix3

transformation matrix for the continous fourier transform this is a matrix with (2\*n+1) real columns

### 11.33 fourier\_matrix\_exp

transformation matrix for a continuous fourier series (not for the discrete dft/fft)

#### 11.34 fourier\_multiplicative\_interaction\_coefficients

#### 11.35 fourier\_power

```
powers of a continuous fourier series in sin/cos form
powers of a^p = (ur + u1 sin(ot) + u2 sin(ot+dp))^p
phase of first component assumed 0
frequencies higher than 2-omega ignored in input
frequencies higher than 3-omega not computed
```

### 11.36 fourier\_power\_exp

### 11.37 fourier\_predict

expand a continous fourier series at times t

### 11.38 fourier\_quadratic\_interaction\_coefficients

### 11.39 fourier\_random\_phase\_walk

evaluete fourier series where the phase undergoes a brownian motion

### 11.40 fourier\_range

approximate range of a continous Fourier series with 2 components range(y) = max(y) - min(y)

### 11.41 fourier\_regress

fit a continous fourier series to a set of sample points not
 sampled
at equal intervals

### 11.42 fourier\_resampled\_fit

fits coefficients of a continuous fourier transform, but stores them as resampled values

### 11.43 fourier\_resampled\_predict

interpolates a continuous fourier series that has been stored as values at their support points

### 11.44 fourier\_signed\_square

#### 11.45 fourier\_transform

```
continuous fourier transformation of y
(not discrete fourier transformation dft/fft)

input:
    b : data sampled at equal intervals
    T : length of data in time or space, i.e. position of last sample if
    position of first sample is 0
    T_max : maximum period to include

output :
    A : fourier matrix
    p : fourier transformation of b
    tt : TODO
```

### 11.46 fourier\_transform\_fractional

### 11.47 fourier\_truncate\_negative\_half\_plane

### 11.48 hyperbolic\_fourier\_box

#### 11.49 idftmtx\_man

inverse matrix for the discrete fourier transform in matlab style with a limited number of columns, thus ignoring higher frequencies keep 2nc+1 columns (mean and conj-complex pairs of nc frequencies)

#### 11.50 laplace\_2d\_pwlinear

least squares with piecewise integration [x0,p,q,r] piecewise linear polynomials at the boundaries

#### 11.51 mean\_fourier\_power

### 11.52 moments\_fourier\_power

#### 11.53 nanfft

discrete fourier transform of a data series with gaps

#### 11.54 peaks

peaks of the power spectrum of a disctrete fourier transform  $% \left( 1\right) =\left( 1\right) \left( 1\right)$ 

rule for peaks: there is no higher value left or right of the "peak".

until the signal drops to  $p*y_peak$ , p = 0.5

works best, when spectrum has been smoothened

#### input :

f : frequency

y : absolute value of fourier transform (power spectrum)

L : length in space or time of series

#### output :

a0 : amplitude

s0 : standard deviation (error?) of amplitude

w0 : width of peak

lambda = wave length (period?)

pdx : index of peak

f : frequency (if not given as input)

#### 11.55 roots\_fourier

zeros of continuous fourier series series

$$f = a_0 + sum_j = n a_i cos(j x) + b_i sin(j x)$$

### 11.56 spectral\_density

spectral density

#### 11.57 std\_fourier\_power

### 11.58 test\_complex\_exp\_product

### 11.59 test\_fourier\_filter

#### 11.60 test\_idftmtx

### 11.61 var\_fourier\_power

### 12 mathematics

mathematical functions of various kind

12.1 gaussfit\_quantile

# 13 geometry/@Geometry

### 13.1 Geometry

### 13.2 arclength

```
arc length of a two dimensional curve 
8th order accurate does not require the segments length to vary smoothly note: the curve can be considered parametric, e.g. x = x(t), y=y(t) and and t = t(s), but the error term contains derivatives of t, thus a non smooth t (strongly varying distance between points) requires the scaling as done below
```

### 13.3 arclength\_old

arc length of a two dimensional function

### 13.4 arclength\_old2

arc length of a two dimensional function

### 13.5 base\_point

base point (fusspunkt), i.e. point on a line with shortest distance to another point  $\ \ \,$ 

### 13.6 base\_point\_limited

base point (Fusspunkt) of a point on a line

#### 13.7 centroid

centroid of a polygone

#### 13.8 cosa\_min\_max

#### 13.9 cross2

cross product in two dimensions

#### 13.10 curvature

curvature of a function in two dimensions

#### 13.11 ddot

sum of squares of cos of inner angles of triangle

#### 13.12 distance

equclidan distance between two points

#### 13.13 distance2

euclidean distance between two points
this function requires a and be of equal dimensions, or the least
the first pair or second pair to be a scalar

### 13.14 dot

dot product

# 13.15 edge\_length

edge length

### 13.16 enclosed\_angle

angle enclosed between two lines

### 13.17 enclosing\_triangle

smallest enclosing equilateral triangle with bottom site paralle to  $\ensuremath{\mathtt{X}}$  axis

### 13.18 hexagon

coordinates of a hexagon, scaled and rotated

### 13.19 inPolygon

flag points contained in a polygon much faster than matlab internal function

#### 13.20 inTetra

flag points contained in tetrahedron

### 13.21 inTetra2

flag points contained in tetrahedron

### 13.22 inTriangle

flag points contained in triangle
function [flag, c] = inTriangle(P1,P2,P3,P0)

### 13.23 intersect

intersect between two lines

#### 13.24 lineintersect

intersect of two lines

#### 13.25 lineintersect1

intersect of two lines

### 13.26 minimum\_distance\_lines

minimum distance of two lines in three dimensions

### 13.27 mittenpunkt

mittenpunkt of a triangle

### 13.28 nagelpoint

nagelpoint of a triangle

### 13.29 onLine

#### 13.30 orthocentre

orthocentre of triangle

### 13.31 plumb\_line

### 13.32 poly\_area

area of a polygon
function A = poly\_area(x,y)

### 13.33 poly\_edges

edges of a polygon

# 13.34 poly\_set

associate point at arbitary location with a polygon it is contained in and assign the value of the polygon to it

### 13.35 poly\_width

width of polygon width holes by surface normals holes / islands separated with NaN order of points of outer boundary must be cw order of points of holes must be ccw note that this function does not give the true width for expanding sections use voronoi polygons for this

### 13.36 polyxpoly

intersections of two polygons

### 13.37 project\_to\_curve

closest point on a curve with respect to a point at distance to the curve

### 13.38 quad\_isconvex

#### 13.39 random\_disk

draw random points on the unit disk

### 13.40 random\_simplex

random point inside of a triangle

### 13.41 sphere\_volume

volume of a sphere
function v = sphere\_volume(r)

## 13.42 tetra\_volume

volume of a tetrahedron

## 13.43 tobarycentric

cartesian to barycentric coordinates

## 13.44 tobarycentric1

cartesian to barycentric coordinates

## 13.45 tobarycentric2

cartesian to barycentric coordinates

## 13.46 tobarycentric3

cartesian to barycentric coordinates

## 13.47 tri\_angle

cos of angles of a triangle

## 13.48 tri\_area

angle of a triangle

## 13.49 tri\_centroid

centroid of a triangle

## 13.50 tri\_distance\_opposit\_midpoint

distance between corner of a triangle and its opposing mid-point

## 13.51 tri\_edge\_length

edge length of a triangle

## 13.52 tri\_edge\_midpoint

mid point of a triangle

## 13.53 tri\_excircle

excircle of a triangle

## 13.54 tri\_height

height of a triangle

## 13.55 tri\_incircle

incircle of a triangle

## 13.56 tri\_isacute

flag acute triangles

## 13.57 tri\_isobtuse

flag obntuse triangles

## 13.58 tri\_semiperimeter

semiperimeter of a triangle

## 13.59 tri\_side\_length

edge lenght of triangle

## 14 geometry

## 14.1 Polygon

Simple 2D polygon class

Polygon properties:

x - x coordinates of polygon
y - y coordinates of polygon
nnodes - number of nodes in the polygon

#### Polygon methods:

in - checks whether given points lie inside, on the edge, or
 outside of the polygon
area - returns the area of the polygon
centerline - computes the centerline of the river
iscw - check whether polygon is clockwise
reverse - reverse the order of the polygon

## 14.2 bounding\_box

bounding box of X

#### 14.3 curvature\_1d

curvature of a sampled parametric curve in two dimensions

#### 14.4 cvt

centroidal voronoi tesselation

## 14.5 deg\_to\_frac

degree, minutes and seconds to fractions

## 14.6 ellipse

return points on an ellipse
n : number of points
ci : confidence interval, i.e. for 1 sigma

## 14.7 ellipseX

x-coordinates of y-coordinates of an ellipse

## 14.8 ellipseY

## 14.9 first\_intersect

get first intersection between lines in  $\ensuremath{\mathtt{A}}$  and  $\ensuremath{\mathtt{B}}$ 

## 14.10 golden\_ratio

golden ratio

## 14.11 hypot3

hypothenuse in 3D

## 14.12 meanangle

weighted mean of angles

## 14.13 meanangle2

mean angle

## 14.14 meanangle3

mean angle

## 14.15 meanangle4

mean angle

## 14.16 medianangle

```
{\tt median} angle angle, that has the smallest squared distance to all others
```

## 14.17 medianangle2

```
median angle
input
alpha : x*m, [rad] angle

ouput
ma : 1*m, [rad] median angle
sa : 1*m, [rad] standard error of median angle for uncorrelated
    error
```

## 14.18 pilim

limit to +- pi

## 14.19 streamline\_radius\_of\_curvature

```
streamline radius of curvature simplifies when rotatate to streamwise coordinates to R = 1/dv/ds * u
```

## 15 histogram/@Histogram

- 15.1 2x
- 15.2 Histogram
- 15.3 bimodes
- 15.4 cdf
- 15.5 cdfS
- 15.6 chi2test
- 15.7 cmoment
- 15.8 cmomentS

15.9 entropy

15.10 entropyS

 $15.11 \quad export\_csv$ 

15.12 iquantile

15.13 kstest

15.14 kurtosis

15.15 kurtosisS

15.16 mean

15.17 meanS

15.18 median

- 15.19 medianS
- 15.20 mode
- $15.21 \mod S$
- 15.22 moment
- 15.23 momentS
- 15.24 pdf
- 15.25 quantile
- 15.26 quantileS
- 15.27 resample
- 15.28 setup

- 15.29 skewness
- 15.30 skewnessS
- 15.31 stairs
- 15.32 stairsS
- 15.33 std
- 15.34 stdS
- 15.35 var
- 15.36 varS
- 16 histogram
- 16.1 hist\_man

- 16.2 histadapt
- 16.3 histconst
- $16.4 \quad pdf_{-}poly$
- 16.5 plotcdf
- 16.6 test\_histogram

## 17 mathematics

mathematical functions of various kind

- 17.1 imrotmat
- 18 linear-algebra
- $18.1 \quad averaging\_matrix\_2$
- 18.2 colnorm

norms of columns

	• •
18.3	- condest $$
10	COHUEST

estimation of the condition number

## 18.4 connectivity\_matrix

## 19 linear-algebra/coordinate-transformation

## 19.1 barycentric2cartesian

barycentric to cartesian coordinates

## 19.2 barycentric2cartesian3

convert barycentric to cartesian coordinates

## 19.3 cartesian2barycentric

cartesian to barycentric coordinates

## $19.4 \quad cartesian\_to\_unit\_triangle\_basis$

transform coodinates into unit triangle

## 19.5 ellipsoid2geoid

## 19.6 example\_approximate\_utm\_conversion

## 19.7 latlon2utm

transform latitude and longitude to WGS84 UTM  $\,$ 

## 19.8 latlon2utm\_simple

## 19.9 lowrance\_mercator\_to\_wgs84

convert lowrance coordinates to wgs84 based on spreadsheet by D Whitney King and Patty B at Lowrance

#### 19.10 nmea2utm

convert nmea messages to utm coordinates

## $19.11 \quad sn2xy$

convert sn to xy coordinates

## 19.12 unit\_triangle\_to\_cartesian

transform coordinates in unit triangle to cartesian coordinates

## 19.13 utm2latlon

convert wgs84 utm to latitute and longitude

## 19.14 xy2nt

project all points onto the cross section and assign them  $\ensuremath{\text{nz-}}$  coordinates

transform coordinate into N-T reference rotate coordinate, so that cross section goes along x-axis then x and y are n and t respectively scaled by width N and T coordinates  ${\tt N}$ 

## $19.15 \quad xy2sn$

convert cartesian to streamwise coordiantes

## $19.16 \text{ xy}2\text{sn_java}$

use java port for speed up

## 19.17 xy2sn\_old

transform points from cartesian into streamwise coordinates

 $\ensuremath{\mathsf{NOTE}}$  : prefer the java version, this has some problems with round off

## 20 linear-algebra

## 20.1 det2x2

2x2 matrix inverse of 2x2 matrices stacked along dim 3

#### 20.2 det3x3

determinant of stacked 3x3 matrices

## $20.3 \det 4x4$

determinant of stacked 4x4 matrices

## 20.4 diag2x2

 ${\tt diagonal} \ {\tt of} \ {\tt stacked} \ {\tt 2x2} \ {\tt matrices}$ 

20.5 down

## $20.6 \quad eig2x2$

eigenvalues of stacked 2x2 matrices

# 21 linear-algebra/eigenvalue

 ${\bf 21.1 \quad eig\_bisection}$ 

## 21.2 eig\_inverse

21.3 eig\_inverse\_iteration

## ${\bf 21.4 \quad eig\_power\_iteration}$

- 22 linear-algebra/eigenvalue/jacobi-davidson
- 22.1 afun\_jdm
- 22.2 davidson
- 22.3 jacobi\_davidson
- 22.4 jacobi\_davidson\_qr
- 22.5 jacobi\_davidson\_qz
- 22.6 jacobi\_davidson\_simple
- 22.7 jdqr

```
%
%
%
%
% Check for convergence
\% Expand the partial Schur form
Rschur=[[Rschur;zeros(1,k)],Qschur'*MV(u)]; k=k+1;
% Expand preconditioned Schur matrix PinvQ
% Check for shrinking the search subspace
% Solve correction equation
% Expand the subspaces of the interaction matrix
% The JD loop (Harmonic Ritz values)
   Both V and W orthonormal and orthogonal w.r.t. Qschur
%
   V*V=eye(j), Qschur'*V=0, W'*W=eye(j), Qschur'*W=0
%
   (A*V-tau*V)=W*R+Qschur*E, E=Qschur'*(A*V-tau*V), M=W'*V
\mbox{\ensuremath{\mbox{\%}}} Compute approximate eigenpair and residual
%
%
%
% Check for convergence
% Expand the partial Schur form
Rschur=[[Rschur;zeros(1,k)],Qschur'*MV(u)]; k=k+1;
% Expand preconditioned Schur matrix PinvQ
% Check for shrinking the search subspace
% Solve correction equation
% Expand the subspaces of the interaction matrix
% The JD loop (Harmonic Ritz values)
   V W AV.
%
   Both V and W orthonormal and orthogonal w.r.t. Qschur, AV=A*V-
  tau*V
   V*V=eye(j), W'*W=eye(j), Qschur'*V=0, Qschur'*W=0,
%
   (I-Qschur*Qschur')*AV=W*R, M=W'*V; R=W'*AV;
%
% Compute approximate eigenpair and residual
%
%
```

```
%
%
%
% Check for convergence
% Expand the partial Schur form
Rschur=[[Rschur;zeros(1,k)],Qschur'*MV(u)]; k=k+1;
% Expand preconditioned Schur matrix PinvQ
% Check for shrinking the search subspace
% Solve correction equation
% Expand the subspaces of the interaction matrix
% The JD loop (Harmonic Ritz values)
  W orthonormal, V and W orthogonal to Qschur,
   W'*W=eye(j), Qschur'*V=0, Qschur'*W=0
%
   W=(A*V-tau*V)-Qschur*E, E=Qschur'*(A*V-tau*V),
   M=W'*V
%
% Compute approximate eigenpair and residual
%
%
%
% Check for convergence
\% Expand the partial Schur form
Rschur=[[Rschur;zeros(1,k)],Qschur'*MV(u)]; k=k+1;
% Expand preconditioned Schur matrix PinvQ
% Check for shrinking the search subspace
% Solve correction equation
% Expand the subspaces of the interaction matrix
W=V*Q; V=V(:,1:j)/R; E=E/R; R=eye(j); M=Q(1:j,:)'/R;
W=V*H; V(:,j+1)=[]; R=R'*R; M=H(1:j,:)';
%====== ARNOLDI (for initializing spaces)
  _____
%===== END ARNOLDI
  % not accurate enough M=Rw'\(M/Rv);
\%======= COMPUTE SORTED JORDAN FORM
  _____
% compute vectors and matrices for skew projection
% solve preconditioned system
\% 0 step of bicgstab eq. 1 step of bicgstab
```

```
% Then x is a multiple of b
% HIST=[0,1];
explicit preconditioning
% compute norm in 1-space
% HIST=[HIST; [nmv,rnrm/snrm]];
% sufficient accuracy. No need to update r,u
implicit preconditioning
% collect the updates for x in 1-space
% but, do the orth to Q implicitly
% compute norm in 1-space
% HIST=[HIST; [nmv,rnrm/snrm]];
% sufficient accuracy. No need to update r,u
% Do the orth to Q explicitly
% In exact arithmetic not needed, but
% appears to be more stable.
% plot(HIST(:,1),log10(HIST(:,2)+eps),'*'), drawnow, pause
\% 0 step of gmres eq. 1 step of gmres
% Then x is a multiple of b
% O step of gmres eq. 1 step of gmres
\% Then x is a multiple of b
HIST=1;
% Lucky break-down
HIST=[HIST; (gamma~=0)/sqrt(rho)];
% Lucky break-down
% solve in least square sense
HIST=log10(HIST+eps); J=[0:size(HIST,1)-1];
plot(J,HIST(:,1),'*'); drawnow,% pause
r=r/rho; rho=1;
% HIST=rho;
% HIST=[HIST;rho];
HIST=log10(HIST+eps); J=[0:size(HIST,1)-1]';
plot(J,HIST(:,1),'*'); drawnow,% pause
% HIST = rho;
% HIST=[HIST;rho];
HIST=log10(HIST+eps); J=[0:size(HIST,1)-1]';
plot(J,HIST(:,1),'*'); drawnow, pause
% HIST = rho;
% HIST=[HIST;rho];
HIST=log10(HIST+eps); J=[0:size(HIST,1)-1]';
plot(J,HIST(:,1),'*'); drawnow, pause
%----- compute schur form -----
A*Q=Q*S, Q'*Q=eye(size(A));
\% transform real schur form to complex schur form
%----- find order eigenvalues ------
%----- reorder schur form -----
%----- compute qz form ------
%----- sort eigenvalues ------
```

```
%----- sort qz form ------
% i>j, move ith eigenvalue to position j
% determine dimension
% defaults
%% 'v'
```

## 22.8 jdqr\_sleijpen

```
% Read/set parameters
% Initiate global variables
% Return if eigenvalueproblem is trivial
% Initialize V, W:
 V,W orthonormal, A*V=W*R+Qschur*E, R upper triangular
% The JD loop (Standard)
   V orthogonal, V orthogonal to Qschur
%
   V*V=eye(j), Qschur'*V=0,
   W=A*V, M=V'*W
%
%
% Compute approximate eigenpair and residual
%
%
%
% Check for convergence
% Expand the partial Schur form
Rschur=[[Rschur;zeros(1,k)],Qschur'*MV(u)]; k=k+1;
% Expand preconditioned Schur matrix PinvQ
\% Check for shrinking the search subspace
% Solve correction equation
% Expand the subspaces of the interaction matrix
% The JD loop (Harmonic Ritz values)
   Both V and W orthonormal and orthogonal w.r.t. Qschur
%
   V*V=eye(j), Qschur'*V=0, W'*W=eye(j), Qschur'*W=0
%
   (A*V-tau*V)=W*R+Qschur*E, E=Qschur'*(A*V-tau*V), M=W'*V
% Compute approximate eigenpair and residual
%
%
%
```

```
% Check for convergence
% Expand the partial Schur form
Rschur=[[Rschur;zeros(1,k)],Qschur'*MV(u)]; k=k+1;
% Expand preconditioned Schur matrix PinvQ
% Check for shrinking the search subspace
% Solve correction equation
% Expand the subspaces of the interaction matrix
% The JD loop (Harmonic Ritz values)
   V W AV.
%
  Both V and W orthonormal and orthogonal w.r.t. Qschur, AV=A*V-
  tau*V
%
   V*V=eye(j), W'*W=eye(j), Qschur'*V=0, Qschur'*W=0,
%
   (I-Qschur*Qschur')*AV=W*R, M=W'*V; R=W'*AV;
% Compute approximate eigenpair and residual
%
%
%
%
% Check for convergence
\% Expand the partial Schur form
Rschur=[[Rschur;zeros(1,k)],Qschur'*MV(u)]; k=k+1;
% Expand preconditioned Schur matrix PinvQ
% Check for shrinking the search subspace
% Solve correction equation
% Expand the subspaces of the interaction matrix
% The JD loop (Harmonic Ritz values)
   W orthonormal, V and W orthogonal to Qschur,
   W'*W=eye(j), Qschur'*V=0, Qschur'*W=0
%
   W=(A*V-tau*V)-Qschur*E, E=Qschur'*(A*V-tau*V),
   M=W'*V
% Compute approximate eigenpair and residual
%
%
%
%
```

```
% Check for convergence
% Expand the partial Schur form
Rschur=[[Rschur;zeros(1,k)],Qschur'*MV(u)]; k=k+1;
% Expand preconditioned Schur matrix PinvQ
% Check for shrinking the search subspace
% Solve correction equation
% Expand the subspaces of the interaction matrix
W=V*Q; V=V(:,1:j)/R; E=E/R; R=eye(j); M=Q(1:j,:)'/R;
W=V*H; V(:,j+1)=[];R=R'*R; M=H(1:j,:)';
%====== ARNOLDI (for initializing spaces)
   %===== END ARNOLDI
   % not accurate enough M=Rw'\(M/Rv);
%====== COMPUTE SORTED JORDAN FORM
   _____
% compute vectors and matrices for skew projection
\% solve preconditioned system
% O step of bicgstab eq. 1 step of bicgstab
\% Then x is a multiple of b
% HIST=[0,1];
explicit preconditioning
% compute norm in 1-space
% HIST=[HIST; [nmv,rnrm/snrm]];
% sufficient accuracy. No need to update r,u
implicit preconditioning
% collect the updates for x in 1-space
% but, do the orth to Q implicitly
% compute norm in 1-space
% HIST=[HIST; [nmv,rnrm/snrm]];
% sufficient accuracy. No need to update r,u
% Do the orth to Q explicitly
% In exact arithmetic not needed, but
% appears to be more stable.
% plot(HIST(:,1),log10(HIST(:,2)+eps),'*'), drawnow, pause
\% 0 step of gmres eq. 1 step of gmres
% Then x is a multiple of b
% O step of gmres eq. 1 step of gmres
\% Then x is a multiple of b
HIST=1;
% Lucky break-down
HIST=[HIST; (gamma~=0)/sqrt(rho)];
% Lucky break-down
```

```
% solve in least square sense
HIST=log10(HIST+eps); J=[0:size(HIST,1)-1]';
plot(J,HIST(:,1),'*'); drawnow,% pause
r=r/rho; rho=1;
% HIST=rho;
% HIST=[HIST;rho];
HIST=log10(HIST+eps); J=[0:size(HIST,1)-1]';
plot(J,HIST(:,1),'*'); drawnow,% pause
% HIST = rho;
% HIST=[HIST;rho];
HIST=log10(HIST+eps); J=[0:size(HIST,1)-1]';
plot(J,HIST(:,1),'*'); drawnow, pause
% HIST = rho;
% HIST=[HIST;rho];
HIST=log10(HIST+eps); J=[0:size(HIST,1)-1]';
plot(J,HIST(:,1),'*'); drawnow, pause
%----- compute schur form -----
A*Q=Q*S, Q'*Q=eye(size(A));
\% transform real schur form to complex schur form
%----- find order eigenvalues ------
\%----- reorder schur form ------
%----- compute qz form ------
%----- sort eigenvalues ------
%----- sort qz form -----
% i>j, move ith eigenvalue to position j
% determine dimension
% defaults
%% 'v'
```

#### 22.9 jdqr\_vorst

```
% Read/set parameters
% Initiate global variables
% Return if eigenvalueproblem is trivial
% Initialize V, W:
  V,W orthonormal, A*V=W*R+Qschur*E, R upper triangular
% The JD loop (Standard)
   V orthogonal, V orthogonal to Qschur
%
   V*V=eye(j), Qschur'*V=0,
%
   W=A*V, M=V, *W
% Compute approximate eigenpair and residual
%
%
%
```

```
% Check for convergence
\mbox{\ensuremath{\mbox{\%}}} Expand the partial Schur form
Rschur=[[Rschur;zeros(1,k)],Qschur'*MV(u)]; k=k+1;
% Expand preconditioned Schur matrix PinvQ
\% Check for shrinking the search subspace
% Solve correction equation
% Expand the subspaces of the interaction matrix
% The JD loop (Harmonic Ritz values)
   Both V and W orthonormal and orthogonal w.r.t. Qschur
   V*V=eye(j), Qschur'*V=0, W'*W=eye(j), Qschur'*W=0
   (A*V-tau*V)=W*R+Qschur*E, E=Qschur'*(A*V-tau*V), M=W'*V
%
%
% Compute approximate eigenpair and residual
%
%
%
% Check for convergence
% Expand the partial Schur form
Rschur=[[Rschur;zeros(1,k)],Qschur'*MV(u)]; k=k+1;
% Expand preconditioned Schur matrix PinvQ
% Check for shrinking the search subspace
% Solve correction equation
% Expand the subspaces of the interaction matrix
% The JD loop (Harmonic Ritz values)
%
   V W AV.
%
   Both V and W orthonormal and orthogonal w.r.t. Qschur, AV=A*V-
  tau*V
   V*V=eye(j), W'*W=eye(j), Qschur'*V=0, Qschur'*W=0,
%
   (I-Qschur*Qschur')*AV=W*R, M=W'*V; R=W'*AV;
% Compute approximate eigenpair and residual
%
%
%
%
```

```
% Check for convergence
% Expand the partial Schur form
Rschur=[[Rschur;zeros(1,k)],Qschur'*MV(u)]; k=k+1;
% Expand preconditioned Schur matrix PinvQ
% Check for shrinking the search subspace
% Solve correction equation
% Expand the subspaces of the interaction matrix
% The JD loop (Harmonic Ritz values)
  W orthonormal, V and W orthogonal to Qschur,
   W'*W=eye(j), Qschur'*V=0, Qschur'*W=0
  W=(A*V-tau*V)-Qschur*E, E=Qschur'*(A*V-tau*V),
%
   M=W'*V
% Compute approximate eigenpair and residual
%
%
%
% Check for convergence
% Expand the partial Schur form
Rschur=[[Rschur;zeros(1,k)],Qschur'*MV(u)]; k=k+1;
% Expand preconditioned Schur matrix PinvQ
% Check for shrinking the search subspace
% Solve correction equation
% Expand the subspaces of the interaction matrix
W=V*Q; V=V(:,1:j)/R; E=E/R; R=eye(j); M=Q(1:j,:)'/R;
W=V*H; V(:,j+1)=[]; R=R'*R; M=H(1:j,:)';
%====== ARNOLDI (for initializing spaces)
  %===== END ARNOLDI
  % not accurate enough M=Rw'\(M/Rv);
%====== COMPUTE SORTED JORDAN FORM
  _____
% accepted separation between eigenvalues:
% no preconditioning
\% solve left preconditioned system
% compute vectors and matrices for skew projection
% precondion and project r
% solve preconditioned system
```

```
% no preconditioning
\% solve two-sided expl. precond. system
% compute vectors and matrices for skew projection
% precondion and project r
% solve preconditioned system
% "unprecondition" solution
%%%% u(:,j+1)=Atilde*u(:,j)
%%%% r(:,j+1)=Atilde*r(:,j)
%----- compute schur form -----
A*Q=Q*S, Q'*Q=eye(size(A));
\% transform real schur form to complex schur form
%----- find order eigenvalues ------
%----- reorder schur form -----
%----- compute qz form ------
%----- sort eigenvalues ------
%----- sort qz form -----
% i>j, move ith eigenvalue to position j
% determine dimension
% defaults
```

## 22.10 jdqz

```
% Read/set parameters
% Return if eigenvalueproblem is trivial
% Initialize target, test space and interaction matrices
% V=RepGS(Qschur,V); [AV,BV]=MV(V); %%% more stability??
% W=RepGS(Zschur,eval(testspace)); %%% dangerous if sigma~lambda
% Solve the preconditioned correction equation
\% Expand the subspaces and the interaction matrices
% Check for stagnation
% Solve projected eigenproblem
% Compute approximate eigenpair and residual
\%=== an alternative, but less stable way of computing z =====
% display history
% save history
% check convergence
% EXPAND Schur form
\% Expand preconditioned Schur matrix MinvZ=M\Zschur
% check for conjugate pair
\mbox{\ensuremath{\mbox{\%}}} 
 To detect whether another eigenpair is accurate enough
% Initialize target, test space and interaction matrices
% additional stabilisation. May not be needed
% V=RepGS(Zschur,V); [AV,BV]=MV(V);
% end add. stab.
% Solve the preconditioned correction equation
\% expand the subspaces and the interaction matrices
```

```
% Check for stagnation
\% compute approximate eigenpair
% Compute approximate eigenpair and residual
% display history
% save history
% check convergence
% expand Schur form
% ZastQ=Z'*Q0
% the final Qschur
% check for conjugate pair
% t perp Zschur, t in span(Q0,imag(q))
% To detect whether another eigenpair is accurate enough
% restart if dim(V)> jmax
%===== END JDQZ
  ______
%-----
%====== PREPROCESSING
  _____
%====== ARNOLDI (for initial spaces)
\mbox{\ensuremath{\%}\xspace}\xspace then precond=I and target = 0: apply Arnoldi with A
%===== END ARNOLDI
  %====== POSTPROCESSING
  _____
%-----
%====== SORT QZ DECOMPOSITION INTERACTION MATRICES
  ===========
%====== COMPUTE SORTED JORDAN FORM
  %===== END JORDAN FORM
  _____
%====== OUTPUT
%====== UPDATE PRECONDITIONED SCHUR VECTORS
```

```
%====== SOLVE CORRECTION EQUATION
  % solve preconditioned system
%====== LINEAR SOLVERS
   _____
% [At,Bt]=MV(x); At=theta(2)*At-theta(1)*Bt;
% xtol=norm(r-At+Z*(Z'*At))/norm(r);
%===== Iterative methods
  % 0 step of bicgstab eq. 1 step of bicgstab
% Then x is a multiple of b
% HIST=[0,1];
explicit preconditioning
% compute norm in 1-space
% HIST=[HIST; [nmv,rnrm/snrm]];
% sufficient accuracy. No need to update r,u
implicit preconditioning
% collect the updates for x in 1-space
% but, do the orth to Z implicitly
% compute norm in 1-space
% HIST=[HIST; [nmv,rnrm/snrm]];
% sufficient accuracy. No need to update r,u
% Do the orth to Z explicitly
% In exact arithmetic not needed, but
% appears to be more stable.
% plot(HIST(:,1),log10(HIST(:,2)+eps),'*'), drawnow
\% 0 step of gmres eq. 1 step of gmres
% Then x is a multiple of b
%-----
% O step of gmres eq. 1 step of gmres
% Then x is a multiple of b
HIST=1;
% Lucky break-down
HIST=[HIST; (gamma~=0)/sqrt(rho)];
% Lucky break-down
% solve in least square sense
HIST=log10(HIST+eps); J=[0:size(HIST,1)-1]';
plot(J,HIST(:,1),'*'); drawnow
%====== END SOLVE CORRECTION EQUATION
  _____
```

```
%====== BASIC OPERATIONS
 y(1:5,1), pause
%====== COMPUTE r AND z
% E*u=Q*sigma, sigma(1,1)>sigma(2,2)
\%====== END computation r and z
%====== Orthogonalisation
 _____
%====== END Orthogonalisation
 %====== Sorts Schur form
 kappa=max(norm(A,inf)/max(norm(B,inf),1.e-12),1);
 kappa=2^(round(log2(kappa)));
%----- compute the qz factorization ------
%----- scale the eigenvalues ------
\%----- sort the eigenvalues -----
\%----- swap the qz form -----
% repeat SwapQZ if angle is too small
%-----
%-----
% i>j, move ith eigenvalue to position j
% compute q s.t. C*q=(t(i,1)*S-s(i,1)*T)*q=0
C*P=Q*R
check whether last but one diag. elt r nonzero
C*q
% end computation q
%===== END sort QZ decomposition interaction matrices
%====== INITIALIZATION
```

```
% defaults
           %%%% search for 'xx' in fieldnames
%% 'ma'
%% 'sch'
%% 'to'
%% 'di'
% jmin=nselect+p0 %%%% 'jmi'
% jmax=jmin+p1 %%%% 'jma'
%% 'te'
%% 'pai'
%% 'av'
%% 'tr'
%% 'fix'
%% 'ns'
%% 'ch'
%% 'lso'
%% 'ls_m'
%% 'ls_t'
%% 'ls_e'
%% 'ty'
%% '1_'
%% 'u_'
%% 'p_'
%% 'sca'
%% 'v0'
initiation
'standard'
'harmonic'
'searchspace'
% or Operator_Form=3 or Operator_Form=5???
%====== DISPLAY FUNCTIONS
  _____
%_____
```

## $22.11 \quad mfunc_{-j}dm$

## 22.12 mgs

- $22.13 \quad minres_{-}$
- 22.14 mv\_jacobi\_davidson
- 23 linear-algebra
- 23.1 first

## 23.2 gershgorin\_circle

range of eigenvalues determined by the gershgorin circle theorem

## 23.3 haussdorff

```
haussdorf dimension
box counting: count cectangles passed through by line (covered by polygon)
```

```
Koch snow flake 3:4 -> 1.2619

Kantor set 2:3, (4:9) -> 0.6309

quadrat 4:2, 9:3, 16:4 -> 2
```

## 23.4 ieig2x2

reconstruct matrix from eigenvalue decomposition

# 23.5 inv2x2 2x2 inverse of stacked matrices 23.6 inv3x3 23.7 inv4x4 inverse of stacked 4x4 matrices 23.8 kernel2matrix ${\bf 24}\quad {\bf linear-algebra/lanczos}$ 24.1 arnoldi 24.2 arnoldi\_new 24.3 eigs\_lanczos\_man 24.4 lanczos

 $24.5 \quad lanczos_{-}$ 

 ${\bf 24.6 \quad lanczos\_biorthogonal}$  ${\bf 24.7} \quad lanczos\_biorthogonal\_improved$  $lanczos\_ghep$ 24.8 24.9mv\_lanczos 24.10 reorthogonalise 24.11 test\_lanczos linear-algebra 25laplacian\_eigenvalue 25.2 laplacian\_eigenvector

 $laplacian\_power$ 

25.3

## $25.4 \quad least\_squares\_perpendicular\_offset$

## 25.5 left

left element of vector, leftmost column is extrapolated

## 26 linear-algebra/linear-systems

## $26.1 \quad gmres\_man$

break on convergence

## $26.2 \quad minres\_recycle$

## 27 linear-algebra

## 27.1 lpmean

mean of pth-power of a

## 27.2 lpnorm

norm of lth-power of a

## 27.3 matvec3

matrix-vector product of stacked matrices and vectors

## $27.4 \quad \text{max2d}$

 $\hbox{\tt maximum value and $i$-j index for matrix}$ 

## 27.5 mid

mid point between neighbouring vector elements

## 27.6 mpoweri

approximation of A^p, where p is not integer by quadtratic interpolation

## $27.7 \quad \text{mtimes} 2x2$

## 27.8 mtimes3x3

product of stacked 3x3 matrices

## 27.9 nannorm

norm of a vector, skips nan-values

## 27.10 nanshift

shift vector, but set out of range values to NaN

## 27.11 nl

number rows (lines) of a matrix analogue to unix nl command

## 27.12 normalise

normalise a vector or the columns of a matrix
note that the columns are independently normalised, and hence not
 necessarily
orthogonal to each other use the gram schmidt algorithm for this (
 qr or orth)

## 27.13 normalize1

normalize columns in x to [-1,1]

## 27.14 normrows

## 27.15 orth2

make matrix A orhogonal to B

## 27.16 orth\_man

orthogonalize the columns of A

## 27.17 orthogonalise

 $\quad \text{make } \textbf{x} \text{ orthogonal to } \textbf{Y}$ 

## 27.18 padd2

padd values around a 2d (image) matrix, constant exprapolation

## 27.19 paddext

```
padd values to vactor
not suitable for noisy data
order = 0 : constant extrapolation (hold)
order = 1 : linear extrapolation
```

## 27.20 paddval1

padd values at end of x

## 27.21 paddval2

padd values to x

# 28 linear-algebra/polynomial

## 28.1 chebychev

chebycheff polynomials

## 28.2 piecewise\_polynomial

evaluate piecewise polynomial

## 28.3 roots1

roots of linear functions

## 28.4 roots2

```
roots of quadratic function c1 x^2 + c2 x + c3 = 0
```

# $28.5 \quad roots2poly$

 $28.6 \quad roots3$ 

28.7 roots4

 $28.8 \quad roots\_piecewise\_linear$ 

 $28.9 test\_roots4$ 

## 28.10 vanderi\_1d

vandermonde matrix of an integral

# 29 linear-algebra

### 29.1 randrot

random rotation matrix

## 29.2 right

get right column by shifting columns to left extrapolate rightmost column  $\,\,$ 

## 29.3 rot2

rotation matrix from angle

## $29.4 \quad rot2dir$

rotation matrix from direction vector

29.5 rot3

29.6 rotR

29.7 rownorm

 ${\bf 29.8 \quad simmilarity\_matrix}$ 

29.9 spnorm

frobenius norm

29.10 spzeros

allocate a sparze matrix of zeros

 $29.11 \quad test\_roots3$ 

## 29.12 transform\_minmax

## 29.13 transpose3

transpose stacked 3x3 matrices

## 29.14 transposeall

29.15 up

## 29.16 vander\_nd

## 29.17 vanderd\_2d

# 30 logic

bitwise operations on integers

## 30.1 bitor\_man

bitwise OR of the numbers of the columns of A
input:
 A (positive integer)

# 31 master/plot

## 31.1 attach\_boundary\_value

- $31.2 \quad cartesian\_polar$  $31.3 img_vargrid$ 31.4 plot\_basis\_functions 31.5 plot\_convergence  $31.6 \quad plot\_dof$ 31.7 plot\_eigenbar 31.8 plot\_error\_estimation 31.9 plot\_error\_estimation\_2
- 31.11 plot\_fdm\_kernel

31.10 plot\_error\_fem

- $31.12 \quad plot\_fdm\_vs\_fem$
- 31.13 plot\_fem\_accuracy
- $31.14 \quad plot\_function\_and\_grid$
- 31.15 plot\_hat
- 31.16 plot\_hydrogen\_wf
- $31.17 \quad plot\_mesh$
- $31.18 \quad plot\_mesh\_2$
- 31.19 plot\_refine
- 31.20 plot\_refine\_3d
- 31.21 plot\_runtime

- ${\bf 31.22 \quad plot\_spectrum}$
- 31.23 plot\_wavefunction
- 32 master/ported
- ${\bf 32.1}\quad assemble\_2d\_phi\_phi$
- 32.2 assemble\_ $3d_dphi_dphi$
- 32.3 assemble\_ $3d_phi_phi$
- $32.4 \quad dV_{-}2d_{-}$
- 32.5 derivative\_2d
- 32.6 derivative\_3d
- 32.7 element\_neighbour\_2d

- $32.8 \quad prefetch\_2d\_$
- $32.9 \quad promote\_2d\_3\_10$
- 32.10 promote\_ $2d_3_15$
- $32.11 \quad promote\_2d\_3\_21$
- $32.12 \quad promote\_2d\_3\_6$
- $32.13 \quad promote\_3d\_4\_10$
- $32.14 \quad promote\_3d\_4\_20$
- $32.15 \quad promote\_3d\_4\_35$
- 32.16 vander\_2d
- 32.17 vander\_3d

## 33 mathematics

mathematical functions of various kind

### 33.1 monotoneous\_indices

## 33.2 nearest\_fractional\_timestep

## 34 number-theory

### 34.1 ceiln

floor to leading n-digits

## 34.2 digitsb

number of digits with respect to specified base

### 34.3 floorn

floor to n-digits

### 34.4 iseven

true for even numbers in X

### 34.5 multichoosek

all combinations of lenght k from set values with repetitions c.f. nchoosek, combinations without repetition

input :

 ${\bf x}$  : scalar integer or vector of arbitrary numbers

k : length of subsets

output :

if x scalar : number of combinations if x vector : the exact combinations

## 34.6 nchoosek\_man

vecotrised binomial coefficient
b = N!/K!(N-K)!

## 34.7 pythagorean\_triple

pythagorean triple

### 34.8 roundn

round to n digits

## 35 numerical-methods

## 35.1 advect\_analytic

## 36 numerical-methods/differentiation

### 36.1 derivative1

first derivative on variable mesh second order accurate

## 36.2 derivative2

second derivative on a variable mesh

## 37 numerical-methods

## 37.1 diffuse\_analytic

## 38 numerical-methods/finite-difference

### 38.1 cdiff

```
differences of columns of X
degree = 1 : central first order differences
degreee = 2 : central second order differences
```

### 38.2 cdiffb

```
differences of columns of X
degree = 1 : central first order differences
degreee = 2 : central second order differences
TODO use difference matrix function for simplicity
```

## 38.3 central\_difference

### 38.4 cmean

```
single gaussian smoothing step with kernel 1/4*[1,2,1]
```

## 38.5 cmean 2

### 38.6 derivative\_matrix\_1\_1d

finite difference matrix of first derivative in one dimensions n : number of grid points h = L/(n+1) constant step with function [D1, d1] = derivative\_matrix\_1d(n,L,order)

### 38.7 derivative matrix 2 1d

finite derivative matrix of second derivative in one dimension

### 38.8 derivative\_matrix\_2d

finite difference derivative matrix in two dimensions

### 38.9 derivative\_matrix\_curvilinear

derivative matrix on a curvilinear grid

### 38.10 derivative\_matrix\_curvilinear\_2

derivative matrix on a two dimensional curvilinear grid the grid has not necessarily to be orthogonal

### 38.11 difference\_kernel

difference kernels for equispaced grids
c.f. Computing the Spectrum of the Confined Hydrogen Atom, Kastner,
2012

## $38.12 \quad diffusion\_matrix\_2d\_anisotropic$

## 38.13 diffusion\_matrix\_2d\_anisotropic2

## 38.14 directional\_neighbour

### **38.15** distmat

distance matrix for a 2 dimensional rectangular matrix

### 38.16 downwind\_difference

## 38.17 gradpde2d

```
objective function gradiend on two dimensional regular grid numeric gradient for non-linear least squares optimisation of a PDE on a rectangular grid x_* = \min(f(x)) f = (v(x) - v(x_*))^2 = f(x) + A dx + O(dx^2) a_ij = df_i/dx_j
```

## 38.18 laplacian

## 38.19 laplacian\_fdm

finite difference matrix of the laplacian  ${\tt RC}$ 

### 38.20 lrmean

 $\ensuremath{\mathsf{mean}}$  of the left and right element

39	numerical-methods/finite-difference/master
39.1	$fdm_adaptive_grid$
39.2	$fdm\_adaptive\_refinement\_old$
39.3	$fdm\_assemble\_d1\_2d$
39.4	$fdm\_assemble\_d2\_2d$
39.5	${ m fdm\_confinement}$
39.6	${ m fdm_{-}d_{-}vargrid}$
39.7	$fdm_{-}h_{-}unstructured$
39.8	fdm_hydrogen_vargrid
39.9	fdm_mark_unstructured_2d

39.10	$fdm_{-}plot$
39.11	$fdm\_plot\_series$
39.12	fdm_refine_2d
39.13	$fdm_refine_3d$
39.14	$fdm\_refine\_unstructured\_2d$
39.15	$fdm\_schroedinger\_2d$
39.16	$fdm\_schroedinger\_3d$

- $40\quad numerical-methods/finite-difference$
- 40.1 mid

39.17 relocate

mid point between neighbouring vector elements

## 40.2 pwmid

segment end point to segment mid point transformation for regular 1  $\,$  d grids  $\,$ 

### 40.3 ratio

ratio of two subsequent values

## 40.4 steplength

step length of a vector if it were equispaced

## 40.5 swapoddeven

swap odd and even elements in a vector

## 40.6 test\_derivative\_matrix\_2d

### 40.7 test\_derivative\_matrix\_curvilinear

## 40.8 test\_difference\_kernel

## 40.9 upwind\_difference

- $41\quad numerical-methods/finite-element$
- 41.1 Mesh\_2d\_java
- $41.2 \quad Tree\_2d\_java$
- $41.3 \quad assemble\_1d\_dphi\_dphi$
- $41.4 \quad assemble\_1d\_phi\_phi$
- $41.5 \quad assemble\_2d\_dphi\_dphi\_java$
- 41.6 assemble\_2d\_phi\_phi\_java
- $41.7 \quad assemble\_3d\_dphi\_dphi\_java$
- 41.8 assemble\_3d\_phi\_phi\_java
- 41.9 boundary\_1d

- 41.10 boundary\_2d
- $41.11 \quad boundary\_3d$
- 41.12 check\_area\_2d
- 41.13 circmesh
- 41.14 cropradius
- $41.15 \quad display\_2d$
- $41.16 \quad display\_3d$
- 41.17 distort
- 41.18 err\_2d
- 41.19 estimate\_err\_2d\_3

- $41.20 \quad example\_1d$
- $41.21 \quad example\_2d$
- 41.22 explode
- $41.23 \quad fem\_2d$
- 41.24 fem\_2d\_heuristic\_mesh
- $41.25 \quad fem\_get\_2d\_radial$
- ${\bf 41.26 \quad fem\_interpolation}$
- 41.27 fem\_plot\_1d
- $41.28 \quad fem\_plot\_1d\_series$
- 41.29 fem\_plot\_2d

41.30	$fem\_plot\_2d\_series$		
41.31	$fem_plot_3d$		
41.32	$fem_plot_3d_series$		
41.33	$fem\_plot\_confine\_series$		
41.34	$fem_radial$		
adaptive grid constant grid			
41.35	$\mathrm{flip}_{-2}\mathrm{d}$		
41.36	$get\_mesh\_arrays$		
41.37	hashkey		
<b>42</b> n	${f numerical-methods/finite-element/int}$		
42.1	$\mathrm{int\_1d\_gauss}$		

- $42.2 \quad int\_1d\_gauss\_1$
- $42.3 \quad int\_1d\_gauss\_2$
- $42.4 \quad int\_1d\_gauss\_3$
- $42.5 \quad int\_1d\_gauss\_4$
- 42.6 int\_1d\_gauss\_5
- $42.7 \quad int\_1d\_gauss\_6$
- $42.8 \quad int\_1d\_gauss\_lobatto$
- $42.9 \quad int\_1d\_gauss\_n$
- $42.10 \quad int\_1d\_nc\_2$
- $42.11 \quad int_1d_nc_3$

- 42.12 int\_1d\_nc\_4
- $42.13 \quad int\_1d\_nc\_5$
- $42.14 \quad int\_1d\_nc\_6$
- 42.15 int\_1d\_nc\_7
- 42.16 int\_1d\_nc\_7\_hardy
- $42.17 \quad int\_2d\_gauss\_1$
- $42.18 \quad int\_2d\_gauss\_12$
- $42.19 \quad int\_2d\_gauss\_13$
- $42.20 \quad int\_2d\_gauss\_16$
- $42.21 \quad int\_2d\_gauss\_19$

- $42.22 \quad int\_2d\_gauss\_25$
- $42.23 \quad int\_2d\_gauss\_3$
- $42.24 \quad int\_2d\_gauss\_33$
- $42.25 \quad int\_2d\_gauss\_4$
- $42.26 \quad int\_2d\_gauss\_6$
- $42.27 \quad int\_2d\_gauss\_7$
- $42.28 \quad int\_2d\_gauss\_9$
- $42.29 \quad int\_2d\_nc\_10$
- 42.30 int\_2d\_nc\_15
- 42.31 int\_2d\_nc\_21

- 42.32 int\_2d\_nc\_3
- $42.33 \quad int_2d_nc_6$
- $42.34 \quad int_3d_gauss_1$
- $42.35 \quad int\_3d\_gauss\_11$
- $42.36 \quad int_3d_gauss_14$
- $42.37 \quad int\_3d\_gauss\_15$
- $42.38 \quad int\_3d\_gauss\_24$
- $42.39 \quad int\_3d\_gauss\_4$
- $42.40 \quad int\_3d\_gauss\_45$
- $42.41 \quad int\_3d\_gauss\_5$

42.42	int_3d_nc_11
42.43	$int_3d_nc_4$
42.44	int_3d_nc_6
42.45	int_3d_nc_8
13 n	numerical-methods/finite-element
	interpolation_matrix
<b>43.2</b>	mark
<b>43.3</b>	$ m mark_{ extsf{ iny 1}}d$
<b>43.4</b>	${ m mesh}_{-}1{ m d}_{-}{ m uniform}$

 $43.5 \quad mesh\_3d\_uniform$ 

43.6	$\operatorname{mesh\_interpolate}$
43.7	$ m neighbour\_1d$
43.8	old
43.9	$ m pdeeig\_1d$
43.10	$ m pdeeig\_2d$
43.11	$ m pdeeig\_3d$
43.12	${\bf polynomial\_derivative\_1d}$
43.13	${\bf potential\_const}$
43.14	${\bf potential\_coulomb}$
43.15	potential_harmonic_oscillator

- 43.16 project\_circle
- 43.17 project\_rectangle
- $43.18 \quad promote\_1d\_2\_3$
- $43.19 \quad promote\_1d\_2\_4$
- $43.20 \quad promote\_1d\_2\_5$
- $43.21 \quad promote\_1d\_2\_6$
- 43.22 quadrilaterate
- $43.23 \quad recalculate\_regularity\_2d$
- 43.24 refine\_1d
- 43.25 refine\_2d\_21

- 43.26 refine\_2d\_structural
- $43.27 \quad regularity\_1d$
- $43.28 \quad regularity\_2d$
- 43.29 regularity\_3d
- T = [1 2 3 4];
- 43.30 relocate\_2d
- 43.31 test\_circmesh
- 43.32 test\_hermite
- 43.33 tri\_assign\_points
- 43.34 triangulation\_uniform

### 43.35 vander\_1d

van der Monde matrix

### 43.36 vanderd\_1d

### 43.37 vanderi\_1d

# 44 numerical-methods/finite-volume/@Advection

### 44.1 Advection

FVM treatment of the Advection equation

### 44.2 dot\_advection

advection equation

# 45 numerical-methods/finite-volume/@Burgers

## 45.1 burgers\_split

```
viscous Burgers' equation, mixed analytic and numerical derivative in frequency space by splitting sheme u_t = -(0.5*u^2)_x + c*u_xx
```

## 45.2 dot\_burgers\_fdm

```
viscous burgers' equation

u_t = -d/dx (1/2*u^2) + c d^2/dx^2 u_xx
```

### 45.3 dot\_burgers\_fft

viscous Burgers' equation in frequency space  $u_t + (0.5*u^2)_x = c*u_xx$ 

## 46 numerical-methods/finite-volume/@Finite\_Volume

### 46.1 Finite\_Volume

finite volume method for partial differential equations 1+1
 dimensions
(time and space)

### 46.2 apply\_bc

apply boundary conditions

#### 46.3 solve

### 46.4 step\_split\_strang

step in time, treat inhomogeneous part by Strang splitting this scheme is not suitable for stationary solutions, for example steady shallow water flow

### 46.5 step\_unsplit

step in time, without splitting the inhomogeneous term  $% \left( 1\right) =\left( 1\right) \left( 1\right$ 

# 47 numerical-methods/finite-volume/@Flux\_Limiter

### 47.1 Flux\_Limiter

class of flux limiters

## 47.2 beam\_warming

beam warming sheme
low resolution
note: works only if sign of eigenvalues point into the same
direction according to RL

### 47.3 fromm

fromme limiter
low res

### 47.4 lax\_wendroff

lax wendroff scheme second order accurate, but no tvd this is effectively not a limiter eq. 6.39 in randall, leveque

### 47.5 minmod

min-mod schock limiter

### 47.6 monotized\_central

monotonized central flux limiter

#### 47.7 muscl

muscl flux limiter

## 47.8 superbee

superbee limiter

## 47.9 upwind

godunov scheme
godunov, first order accurate

### 47.10 vanLeer

van Leer limiter

# 48 numerical-methods/finite-volume/@KDV

## $48.1 \quad dot_kdv_fdm$

korteweg de vries equation  $u_t + (0.5*u^2)_x = c*u_xxx$ 

## $48.2 \quad dot_kdv_fft$

korteweg de vries equation compute derivatives in frequency space  $u_t + (0.5*u^2)_x = c*u_xxx$ 

## $48.3 \text{ kdv\_split}$

korteweg de vries equation in frequency space, derivative treated by splitting scheme

# 49 numerical-methods/finite-volume/@Reconstruct\_Average\_E

## 49.1 Reconstruct\_Average\_Evolve

```
Reconstruct Average Evolve Finite Volume Method for treatment of
    1+1D pdes

McCronack Scheme
err = 0(dt^2) + 0(dx^2), except as discontinuities
error:
    h_xxx(3:end-2) = 1/dx^3*( -0.5*h(1:end-4) + h(2:end-3) - h(4:end-1) + 0.5*h(5:end) );
    th = -1/6*dx^2*qh_.*(1 - (qh_*dt/dx).^2).*h_xxx;
```

### 49.2 advect\_highres

single time step for the reconstruct evolve algorithm

### 49.3 advect\_lowress

```
single time step
low resolution
```

## 50 numerical-methods/finite-volume

### 50.1 Godunov

Godunov, upwind method for systems of pdes

### 50.2 Lax\_Friedrich

```
Lax-Friedrich-Method
for hyperbolic conservation laws
err = O(dt) + O(dx)
|a dt/dx| < 1
```

### 50.3 Measure

### 50.4 Roe

non linear roe solver for the SWE (randall, leveque 15.3.1)

The roe solver guarantess:

- A is diagonalisable with real eigenvalues (15.12)
- can be determined by a closed formula  $% \left( \frac{1}{2}\right) =0$
- is an efficient replacement for true Rieman solver

### 50.5 fv\_swe

wrapper for solving SWE

## 50.6 staggered\_euler

forward euler method with staggered grid

## 50.7 staggered\_grid

staggered grid approximation to the SWE

## 51 numerical-methods

## 51.1 grid2quad

extract rectangular elements of a structured grid in form of an unstructured quad-mesh format

## 52 numerical-methods/integration

### 52.1 cumintL

cumulative integral from left to right

## 52.2 cumintR

cumulative integral from right to left

## 52.3 cumint\_trapezoidal

integrate y along x with the trapezoidal rule

## 52.4 int\_trapezoidal

integrate y along x with the trapezoidal rule

## 53 numerical-methods/interpolation/@Kriging

### 53.1 Kriging

class for Kriging interpolation

### 53.2 estimate\_semivariance

estimate the parameter of the semivariance model for Kriging interpolation  $% \left( 1\right) =\left( 1\right) \left( 1\right) +\left( 1\right) \left( 1\right) \left( 1\right) +\left( 1\right) \left( 1$ 

% set up the regression matrix and solve for parameters

## 53.3 interpolate\_

interpolate with Krieging method

this function may interpolate several quantities per coordinate, using the same variogram, if the semivariance of the quantities differs,

the user may prefer to estimate the semivariance and interpolate each quantity individually

Xs : source point coordinates

Vs : value at source points
Xt : targe point coordinates
Vt : value at target points

E2t : squared interpolation error at target points

## 54 numerical-methods/interpolation/@RegularizedInterpolator1

## 54.1 RegularizedInterpolator1

class for regularized interpolation (Thikonov) on a 1D mesh

#### 54.2 init

initialize the interpolator with a set of sampling points

## 55 numerical-methods/interpolation/@RegularizedInterpolator2

### 55.1 RegularizedInterpolator2

class for regularized interpolation on an unstructures mesh (
 interpolation)

### 55.2 init

initialize the interpolator with a set of point samples

## 56 numerical-methods/interpolation/@RegularizedInterpolator3

## 56.1 RegularizedInterpolator3

class for regularized interpolation (Tikhonov) on a triangulation (unstructured mesh)

#### 56.2 init

initialize the interpolator with a set of sampling points

# 57 numerical-methods/interpolation

### 57.1 IDW

spatial averaging by inverse distance weighting

## **57.2** IPoly

polynomial interpolation class

### 57.3 IRBM

## 57.4 ISparse

sparse interpolation class

### 57.5 Inn

nearest neighbour interpolation

## 57.6 Interpolator

interpolator super-class

fprintf(1,'Progress: %f%% %fs\n',100\*
 idx/size(Xt,1),t);

### 57.7 fixnan

fill nan-values in vector with gaps

## 57.8 idw1

spatial average ny inverse distance weighting

## 57.9 idw2

spatial average by inverse distance weighting

## 57.10 inner2outer

linear interpolation of segment mit point to grid points at segment ends assumes equal grid spacing

## 57.11 inner2outer2

interpolate from element (segment) centres to edge points

## 57.12 interp1\_circular

## 57.13 interp1\_limited

interpolate values, but not beyond a certain distance
this function is idempotent, i.e. it will not extrapolate over into
 gaps
exceedint the limit and thus not spuriously extend the series when
 called a second time on the same data

## 57.14 interp1\_man

interpolate

## 57.15 interp1\_piecewise\_linear

## 57.16 interp1\_save

make interpolation save to round off errors
the matlab internal interpolation suffers from rounding errors,
 which
are unacceptable when values of X and Y are large (for example UTm
 coordinates)
this normalization prevents this

## 57.17 interp1\_slope

quadratic interpolation returning value and derivative(s)

## 57.18 interp1\_smooth

## 57.19 interp1\_unique

matlab fails to interpolate, when  ${\bf x}$  values are not unique this function makes the values unique before use

## 57.20 interp2\_man

nearest neighbour interpolation in two dimensions

## 57.21 interp\_angle

interpolate an angle

## 57.22 interp\_fourier

interpolation by the fourier method

## 57.23 interp\_fourier\_batch

batch interpolation by the fourier interpolation

## 57.24 interp\_sn

```
interpolate along streamwise coordinates
This gives similar result to setting aspect ratio for sN to
   infinity,
but not quite,as the input point set is not dense (scale for sN to
   infinity does not work)
        sdx = sdx(sdx_);
```

## 57.25 interp\_sn2

interpolation in streamwise coordinates

## 57.26 interp\_sn3

## 57.27 interp\_sn\_

## 57.28 limit\_by\_distance\_1d

```
smooth subsequent values along a curve such that v(x0+dx) < v(x0) + (ratio-1)*dx if v is the edge length in a resampled polygon, then v_i/v_i+1) < ratio ratio^1 = exp(a*1)
```

## 57.29 resample1

interpolation along a parametric curve with variable step width

## 57.30 resample\_d\_min

resample a function

## 57.31 resample\_vector

resample a track so that velocity vectors do not run into each other  $% \left( 1\right) =\left( 1\right) \left( 1\right)$ 

## 57.32 test\_interp1\_limited

## 58 numerical-methods

58.1 inverse\_complex

## 58.2 maccormack\_step

58.3 minmod

# 59 numerical-methods/multigrid

## 59.1 mg\_interpolate

## $59.2 mg_restrict$

# 60 numerical-methods/ode/@BVPS\_Characteristic

## 60.1 BVPS\_Characteristic

solve coupled first- and second-order 1D boundary-value problems

#### 60.2 assemble1 A

assemble the discretisation matrix for a first order ode (mean component, zero frequency)

## 60.3 assemble $1_A_Q$

assemble the discretisation matrix for a first order ode (mean component, zero frequency)

## 60.4 assemble 2 A

assemble the discretisation matrix for a second-order ode (non-zero frequency component)

#### 60.5 assemble\_AA

assemble the discretisation matrix for each channel iteratively calls assembly for each frequency components

## 60.6 assemble\_AAA

assemble the discretisation matrix for the entire network iteratively calls assembly for each channel

60.7	$assemble\_Ic$
60.8	bvp1c
60.9	$check\_arguments$
60.10	${ m couple\_junctions}$
60.11	derivative
60.12	init
60.13	$inner2outer\_bvp2c$
60.14	reconstruct

 $60.15 \quad resample \\$ 

#### 60.16 solve

```
solve system of non-linear second order odes (in more than one
   variable)
as boundary value problems

odefun provides ode coefficients c:
c(x,1) y''(x) + c(x,2) y'(x) + c(x,3) y = c(x,4)
   c_1 y" + c_2 y' + c_3 y + c_4 = c_4

subject to the boundary conditions
bcfun provides v and p and optionally q, so that:

b_1 y + b_2 y' = f
   q(x,1)*( p(x,1) y_1(x) + p(x,2) y_1'(x)
   + q(x,2)*( p(x,1) y_r(x) + p(x,2) y_r'(x) = v(x)

where q weighs the waves travelling from left to right and right to
   left (default [1 1])
```

#### 60.17 test\_assemble1\_A

#### 60.18 test\_assemble2\_A

- 61 numerical-methods/ode/@Time\_Stepper
- 61.1 Time\_Stepper
- 61.2 solve
- 62 numerical-methods/ode
- 62.1 bvp2fdm

solve system of non-linear second order odes (in more than one variable)

as boundary value problems by the finite difference method

```
odefun provides ode coefficients c: c(x,1) y''(x) + c(x,2) y'(x) + c(x,3) y = c(x,4) c_1 y" + c_2 y' + c_3 y + c_4 = 0
```

subject to the boundary conditions befun provides  ${\bf v}$  and  ${\bf p}$  and optionally  ${\bf q}$ , so that:

```
b_1 y + b_2 y' = f

q(x,1)*(p(x,1) y_1(x) + p(x,2) y_1'(x)

+ q(x,2)*(p(x,1) y_r(x) + p(x,2) y_r'(x) = v(x)

where q weighs the waves travelling from left to right and right to

left (default [1 1])
```

## 62.2 bvp2wavetrain

solve second order boundary value problem by repeated integration

## 62.3 bvp2wavetwopass

two pass solution for the linearised wave equation solve first for the wave number k, and then for y

## 62.4 ivp\_euler\_forward

solve intial value problem by the euler forward method

## 62.5 ivp\_euler\_forward2

## 62.6 ivprk2

solve initial value problem by the two step runge kutta method

## 62.7 ode2\_matrix

transformation matrix of second order ode to left and right going wave

```
c = odefun(x)
c1 y'' + c2' y + c3 y == 0
y = y_p + y_m, left and right going wave
d/dx [y_p, y_m] = A*[y_m, y_p]
```

## 62.8 ode2characteristic

second order odes transmittded and reflected wave

## 62.9 step\_trapezoidal

single trapezoidal step

## 62.10 test\_bvp2

# 63 numerical-methods/optimisation

## 63.1 aitken\_iteration

#### 63.2 anderson\_iteration

## 63.3 armijo\_stopping\_criterion

armijo stopping criterion for optimizations

## **63.4** astar

astar path finding alforithm

## 63.5 binsearch

binary search on a line

## 63.6 bisection

bisection

## 63.7 box1

test objective function for optimisation routines

## 63.8 box2

## 63.9 cauchy

## 63.10 cauchy2

solve non-linear system by cuachy's method slower than quadratic optimisation, but does not require a hessian

fun : objective function, returns

 ${\tt f}\ :$  scalar, objective function value

g : nx1, gradient
x : nx1, initial position

opt : options

## 63.11 directional\_derivative

```
directional (projected) derivative
d : derivative, highest first
p : series expansion around x0
```

## 63.12 dud

optimization by the dud algorithm

#### 63.13 extreme3

```
extract maxima by quadratic approximation from sampled function val
    (t)
intended to be called after [mval, mid] = max(val) for refinement
    of
locatian and maximum

input
t    : sampling time (uniformly spaced)
v    : values at sampling times
ouput:
tdx    : index where extremum should be computed
t0    : location of the extremum
val0    : value of extremum

v'(dt0) = 0 and v''(dt0) determines type of extremum
```

## 63.14 extreme\_quadratic

## 63.15 ftest

#### 63.16 fzero\_bisect

## 63.17 fzero\_newton

## 63.18 grad

numerical gradient

## 63.19 hessian

numerical hessian

## 63.20 hessian\_from\_gradient

numerical hessian from gradient

## 63.21 hessian\_projected

numerical hessian projected to one dimenstion

## 63.22 line\_search

bisection routine

## 63.23 line\_search2

#### bisection method

fun : objective funct
x0 : start value

 ${\tt f0}$  : objective function value at  ${\tt x0}$ 

g : gradient at x0

p : search direction from x0 (p = g for steepest descend)

h : initial step length (default 1)

 $\begin{array}{lll} \mbox{1b} & : \mbox{lower bound for } x \\ \mbox{up} & : \mbox{upper bound for } x \end{array}$ 

## 63.24 line\_search\_polynomial

polynomial line search
fun : objective funct
x0 : start value
f0 : objective function value at x0
g : gradient at x0
dir : search direction from x0 (p = g for steepest descend)
h : initial step length (default 1)
lb : lower bound for x
up : upper bound for x

## 63.25 line\_search\_polynomial2

cubic line search
fun : objective funct
x0 : start value
f0 : objective function value at x0
g : gradient at x0
dir : search direction from x0 (p = g for steepest descend)
h : initial step length (default 1)
lb : lower bound for x
up : upper bound for x

## 63.26 line\_search\_quadratic

quadratic line search
fun : objective funct
x0 : start value
f0 : objective function value at x0
g : gradient at x0
dir : search direction from x0 (p = g for steepest descend)
h : initial step length (default 1)
lb : lower bound for x
up : upper bound for x

## 63.27 line\_search\_quadratic2

quadratic line search

## 63.28 line\_search\_wolfe

line search by wolfe method
c.f.: OPTIMIZATION THEORY AND METHODS - Nonlinear Programming, Sun,
 Yuan

## 63.29 ls\_bgfs

least squares by the bgfs method

## 63.30 ls\_broyden

## 63.31 ls\_generalized\_secant

least squares by the secant method Barnes, 1965 Wolfe, 1959 Fletcher 1980, 6.3 seber 2003 gerber

## 63.32 nlcg

non-linear conjugate gradient
input:
x : nx1 start vectort

. HAI BUGIO VOCUOIO

 ${\tt opt}$  :  ${\tt struct}$  options

 ${\tt fdx} \,:\, {\tt gradient} \,\, {\tt constraint}$ 

## 63.33 nlls

non-linear least squares

## 63.34 picard

picard iteration

## 63.35 poly\_extrema

extrema of a polynomial

## 63.36 quadratic\_function

evaluate quadratic function in higher dimensions

## 63.37 quadratic\_programming

optimize by quadratic programming

## 63.38 quadratic\_step

single step of the quadratic programming

## 63.39 rosenbrock

rosenbrock test function

## $63.40 \quad sqrt\_heron$

Heron's method for the square root

- 63.41 test\_directional\_derivative
- 63.42 test\_dud
- 63.43 test\_fzero\_newton
- $63.44 \quad test\_line\_search\_quadratic2$
- 63.45 test\_ls\_generalized\_secant
- 63.46 test\_nlcg\_6\_order
- 63.47 test\_nlls

$$f = w'*(p*abs(x-1).^4) + w'*(1-p)*abs(x-1).^2;$$

- 64 numerical-methods/pde
- 64.1 laplacian2d\_fundamental\_solution

## 65 numerical-methods/piecewise-polynomials

## 65.1 Hermite1

hermite polynomial interpolation in 1d

## $65.2 \text{ hp2\_fit}$

fit a hermite polynomial
coefficients are derivative free
x0 : left point of first segment
x1 : right point of last segment
n : number of segments
x : sample x-value

c : coefficients (values at points, no derivatives)

## $65.3 \text{ hp2\_predict}$

val : sample y-value

prediction with pw hermite polynomial
c are values at support points

## 65.4 hp\_predict

predict with piecewise hermite polynomial

## 65.5 hp\_regress

fit piecewise hermite polynomial coefficients are values and derivatives

## 65.6 lp\_count

lagrangian basis for interpolation count number of valid samples

## $65.7 \quad lp\_predict$

lagrangian basis piecwie interpolation, predicor

- 65.8 lp\_regress
- 65.9 lp\_regress\_
- 66 numerical-methods
- 66.1 test\_adams\_bashforth

## 67 mathematics

mathematical functions of various kind

67.1 oversample NZ

- 68 regression/@PolyOLS
- 68.1 PolyOLS

class for polynomial least squares

68.2 coefftest

## 68.3 detrend

detrending by polynomial regression

## 68.4 fit

fit a polynomial function like polyfit, but returns parameter error estimates TODO automatically activate scaleflag

68.5 fit\_

fit a polynomial function

## 68.6 predict

predict polynomial function values

68.7 predict\_

## 68.8 slope

slope by linear regression

# 69 regression/@PowerLS

## 69.1 PowerLS

class for power law regression

## 69.2 fit

```
fit a power law
like polyfit, but returns parameter error estimates
```

## 69.3 predict

```
predict with power law
    S2 = diag((A*obj.C)*A');
    L = Y - S;
    U = Y + S;
```

## 69.4 predict\_

# 70 regression/@Theil

## 70.1 Theil

Kendal-Theil-Sen robust regression

## 70.2 detrend

linear detrending of a set of samples by the Theil-Senn Slope

## **70.3** fit

fit slope and intercept to a set of sample with the Theil-Sen  $\tt method$ 

```
c : confidence interval c = 2*ns*normcdf(1) for ns-sigma
intervals
```

param : itercept and slope
P : confidence interval

## 70.4 predict

predict values and confidence intervals with the Theil-Sen method

## 70.5 slope

fit the slope with the Theil-Sen method

# 71 regression

linear and non-linear regression

## 71.1 Theil\_Multivariate

extension of the Theil-Senn regression to higher dimensions by means of the Gauss-Seidel iteration

## 71.2 areg

regression using the pth-fraction of samples with smallest residual

## 71.3 ginireg

gini regression

## 71.4 hessimplereg

```
hessian, gradient and objective function value of the simple regression  {\tt rhs} \, = \, p(1) \, + \, p(2) \, \, {\tt x} \, + \, {\tt eps}
```

#### 71.5 l1lin

solve  $||Ax - b||_L1$  by means of linear programming

## 71.6 lsq\_sparam

parameter covariance of the least squares regression

fun : model function for predtiction

b : sample values

f(p) = b

p : parameter at point of evaluation (preferably optimum)

## 71.7 polyfitd

fit a polynomial of order n to a set of sampled values and sampled values

of the derivative

x0 must contain at least for conditioning as otherwise the intercept cannot be determined

## 71.8 regression\_method\_of\_moments

fit linear function  $||a b x = y||_L2$  by the method of moments y+eps = alpha + beta\*x

## 71.9 robustling

fit a linear function by splitting the x-values at their median  $(med(y\_left) - med(y\_right))/(med(x\_left)-med(x\_right)$  this approach performs poorly compared to the theil-senn operator

## 71.10 theil2

Theil senn-estimator for two dimensions (glm)

## 71.11 theil\_generalised

generalization of the Theil-Senn operator to higher dimensions,
for arbitrary functions such as polynomials and multivariate
 regression
either higher order polynomials or glm
c.f. "On theil's fitting method", Pegoraro, 1991

## 71.12 total\_least\_squares

total least squares

## 71.13 weighted\_median\_regression

weighted median regression c.f. Scholz, 1978

## 72 set-theory

## 72.1 issubset

test if set B is subset of A in O(n)-runtime

A : first set
B : second set

P : set of primes (auxiliary)

## 73 mathematics

mathematical functions of various kind

#### 73.1 shuffle\_index

# 74 signal-processing

## 74.1 asymwin

creates asymmetrical filter windows filter will always have negative weights

# 75 signal-processing/autocorrelation

## 75.1 acf\_radial

## 75.2 acfar1

Autocorrelation function of the finite AR1 process

$$a_k = 1/(n-k)sum x_ix_i+1 + (xi + xi+k)mu + mu^2$$
  
=  $r^k + 1/n sum_ij + 1/n$   
pause

## $75.3 \quad acfar1_2$

autocorrelation of the ar1 process

## 75.4 acfar2

impulse response of the ar2 process

## $75.5 \quad acfar2_2$

```
autocorrelation of the ar2 process X_i + a1 X_{i-1} + a2 X_{i-2} = 0
```

## 75.6 ar1\_cutoff\_frequency

## 75.7 ar1\_effective\_sample\_size

effective sample size correction for autocorrelated series

## 75.8 ar1\_mse\_mu\_single\_sample

standard error of a single sample of an ar1 correlated process

## $75.9 \quad ar1\_mse\_pop$

variance of the population mean of a single realisation around zero  ${\tt E[(mu_N-0)^2] = E[mu_N^n]}$ 

## 75.10 ar1\_mse\_range

mean standard error of the mean of a range of values taken from an ar1 process

## 75.11 ar1\_spectrum

spectrum of the ar1 process

## 75.12 ar1\_to\_tikhonov

convert ar1 correlation to tikhonovs lambda

#### 75.13 ar1\_var\_factor

75.14 ar1\_var\_factor\_

```
variance correction factor for an autocorrelated finite process n: [1 .. inf] population size m: [1 .. n] samples size rho: [ -1 < rho < 1 (for convergence) ] correlation of samples
```

variance of an autocorrelated finite process

## $75.15 \quad ar1\_var\_range2$

```
variance of sub sample starting at the end of the series from the finite length first order autocorrelated process s2 = 1/m^2 \ sum\_i^m \ sum\_j^m \ rho^-|i-j|
```

## 75.16 ar1delay

## 75.17 ar1delay\_old

autocorrelation of the residual

#### 75.18 ar2\_acf2c

determine coefficients of the ar2 process from the first two lags of the autocorrelation function

#### 75.19 ar2conv

```
coefficients of the ar2 process determined from the two leading
   correlations
of the acf [1,r1,r2,...]
```

#### 75.20 ar2dof

effective samples size for the ar2 process

## 75.21 ar2param

ar2 parameter estimation from first two terms of acf
acf = [1 a1 a2 ...]

## 75.22 autocorr2

75.23 autocorr\_angular

## $75.24 \quad autocorr\_bandpass$

## 75.25 autocorr\_decay\_rate

estimate exponential decay of the autocorrelation

## $75.26 \quad autocorr\_effective\_sample\_size$

effective sample size from acf

## 75.27 autocorr\_fft

estimate sample autocorrelation function

## 75.28 autocorr\_forest

autocorrelation function
75.30 autocorr_highpass
75.31 autocorr_lowpass
$75.32  autocorr\_periodic\_additive\_noise$
$75.33$ autocorr_periodic_windowed
75.34 autocorr_radial
75.35 autocorr_radial_hexagonal_pattern
75.36 autocorrelation_max
76 signal-processing
76.1 average_wave_shape

 $75.29 \quad autocorr\_genton$ 

extract waves with varying length from a wave train and and average

their shape

## 76.2 bandpass

bandpass filter

## 76.3 bandpass\_continuous\_cdf

#### 76.4 bartlett

```
Effective sample size factor for bartlett window c.f. thiebaux c.f spectral analysis-jenkins, eq. (6.3.27) c = acf note: results seams always to be 1 tac too low T : reduction factor for dof for ar1 with a = rho^k = \exp(-k/L), T = 2L
```

#### 76.5 bin1d

```
bin values of v sampled at x into bins bounded by "edges" apply function v to it
```

#### 76.6 bin2d

```
bin values of V sampled at X and Y into the grid structured grid ex
    ,ey
apply function func to all walues in the bin
func = mean : default
func = sum : non-normalized frequency histogram in 2D
```

## 76.7 binormrnd

generate two correlated normally distributed vectors

#### 76.8 coherence

## 76.9 conv1\_man

convolutions with padding

## $76.10 \quad conv2\_man$

convolution in 2d

## 76.11 conv2z

## 76.12 conv30

convolve with rectangular window of length  $\boldsymbol{n}$  circular boundaries

## $76.13 \quad conv_{-}$

convolution of a with b

## 76.14 conv\_centered

convolve x with filter window f
when length of f is even, this guarantees a symmetric result (no
 off by on
displacement) by making the lenght of f odd at first

#### 76.15 convz

## 76.16 cosexpdelay

## 76.17 csmooth

smooth recursively with [1,2,1]/4 kernel function x = csmooth(x,n,p,circ)

## 76.18 daniell\_window

Daniell window for smoothing the power spectrum c.f. Daniell 1946
Bloomfield 2000
meko 2015

## 76.19 db2neper

convert decibel to neper

## 76.20 db2power

power ratio from db

## $76.21 \quad derive\_bandpass\_continuous\_scale$

## $76.22 \quad derive\_danielle\_weight$

## 76.23 derive\_limit\_0\_acfar

## 76.24 detect\_peak

detect peaks in a vector
requires function value to fall to p\*max before new value is
 allowed

## $76.25 \quad determine\_phase\_shift$

## 76.26 determine\_phase\_shift1

average phase and phase shift per time step of a train of waves

## 76.27 doublesum\_ij

double sum of r^i

## 76.28 effective\_mask\_size

## 76.29 effective\_sample\_size\_to\_ar1

convert effective sample size to ar1 correlation

## 76.30 fcut2Lw\_gausswin

## 76.31 fcut\_gausswin

## 76.32 filt\_hodges\_lehman

# 77 signal-processing/filters

## 77.1 circfilt2

smooth (filter) the 2D image z with a circular disk of radius nf apply periodic boundary conditions

## **77.2** filter1

filter along one dimension

## 77.3 filter2

filter columns of x (matlab does only support vector input)

#### 77.4 filter\_

invalidate values that exceed n-times the robust standard deviation

## 77.5 filter\_r\_to\_f0

## 77.6 filter\_rho\_to\_f0

## 77.7 filter\_twosided

## 77.8 filteriir

```
filter adcp t-n data over time
```

v : nz,nt : values to be filtered
H : nt,1 : depth of ensemble

last :  $\operatorname{nt}, 1$  : last bin above bottom that can be sampled without

side lobe interference

nf : scalar : number of reweighted iterations

#### when samples

 distance to bed is reference (advantageous for near-bed suspended transport)

TODO for wash load: distance to surface is more relevant

#### interpolate depending on z

when depth changes, neighbouring indices do not correspond to same
 relative position in the water column
relative possition in the colum (s-coordinate) smoothes values
near the bed: absolute distance to bed is chosen
near surface: absolute distance to surface is chosen
-> cubic transformation of index

faster and avoid alising (smoothing along z)
 resample ensemble to same number of bins in S -> filter ->
 resample back
 use nonlinear transform z-s coordinates
-> resampling has to be local (Hi -> H-filtered)

filtered profile coordinates to sample coordinates

zf -> zi (special transform)

corresponding indices and fractions

filtration step (update of hf and vf)

sample coordinates to updated profile coordinates

(the inverse step is actually not necessary)

write filtered value

## 77.9 filterp

## 77.10 filterp1

fir filter with some fancy extras

#### 77.11 filterstd

## 77.12 gaussfilt2

smooth (filter) the 2D image z with a gaussian window apply periodic boundary conditions

## 77.13 lowpass\_discrete

```
design coefficients of a low pass filter with specified cut of
    frequency
and sampling period
alalogue low pass with pole at s=-omega_c=1/tau=1/RC
Ha = tau/(tau + s) = 1/(1 + omega_c*s)
```

## 77.14 meanfilt2

filter with a rectangular window along both dimensions

#### 77.15 medfilt1\_man

moving median filter, supports columnwise operation

#### 77.16 medfilt1\_man2

moving median filter with special treatment of boundaries

## 77.17 medfilt1\_padded

median filter with padding

## 77.18 medfilt1\_reduced

median filter with padding

#### 77.19 trifilt1

filter with triangular window
trifilt1 is ident to twice applying rectfilt1 (meanfilt1) with half
 the domain size
note : inifnitely many convolution yield a gaussian

## **77.20** trifilt2

filter with a triangular window along both dimensions

# 78 signal-processing

## 78.1 firls\_man

design finite impulse response filter by the least squares method

## 78.2 fit\_spectral\_density

fit (spectral) densities

## 78.3 fit\_spectral\_density\_2d

fit spectral densities

## 78.4 fit\_spectral\_density\_radial

fit spectral densities

## 78.5 flattopwin

the flat top window

## 78.6 frequency\_response\_boxcar

frquency response of a boxcar filter

## 78.7 freqz\_boxcar

frequncy response of a boxcar filter

## 78.8 gaussfilt1

filter data series with a gaussian window, assumes periodic bc

## 78.9 hanchangewin

hanning window for change point detection

## 78.10 hanchangewin2

nanning window for chage point detection

#### 78.11 hanwin

hanning filter window

#### 78.12 hanwin\_

hanning filter window

## $78.13 \quad high\_pass\_1d\_simple$

## 78.14 kaiserwin

kaiser filter window

#### **78.15** kalman

Kalman filter

#### 78.16 lanczoswin

Lanczos window

#### 78.17 last

lake tail, but for matrices

#### 78.18 maxfilt1

#### 78.19 meanfilt1

moving average filter with special treatment of the boundaries

## $78.20 \quad mid\_term\_single\_sample$

variance of single sample, mid term

## 78.21 minfilt1

## **78.22** minmax

#### 78.23 mu2ar1

error variance of the mean of the finite length ar1 process

 $(mu)^2 = (sum \ epsi)^2 = sum_i \ sum_j \ eps_i \ eps_j = sum_ii(rho,n)/n^2$  this has the limit s^2 for rho->1

## 78.24 mysmooth

#### 78.25 nanautocorr

autocorrelation with nan-values

## 78.26 nanmedfilt1

medfilt1, skipping nans

## 78.27 neper2db

convert neper to db

## 78.28 oscillator\_noisy

# 79 signal-processing/passes

## 79.1 bandpass1d

## 79.2 bandpass1d\_fft

filter input vector with a spatial (two-sided) bandpass in fourier space

## 79.3 bandpass1d\_implicit

## 79.4 bandpass2

bandpass filter

- 79.5 bandpass2d
- 79.6 bandpass $2d_{-}2$
- 79.7 bandpass2d\_fft
- $79.8 \quad bandpass 2d\_ideal$
- 79.9 bandpass2d\_implicit
- $79.10 \quad bandpass2d\_iso$

## 79.11 bandpass\_arg

determine correlation coefficient from frequency of mode for the  $\operatorname{symmetric}$ 

## 79.12 bandpass\_f0\_to\_rho

correlation coefficient for the pth-order symmetric bandpass filter
 with
maximum at f0 (when rho\_lp = rho\_hp)

79.13	bandpass_max
79.14	$bandpass\_max2$
79.15	highpass
high pa	ass filter
79.16	$highpass1d\_fft\_cos$
filter spa	the input vector with a cosine-shaped highpass in frequency ce
79.17	$highpass 1 \\ d\_implicit$
79.18	$highpass2d_{-}fft$
79.19	$highpass 2d\_ideal$
79.20	${ m highpass 2d\_implicit}$
79.21	highpass_arg

79.22	$highpass\_fc\_to\_rho$			
79.23	lowpass			
low pass filter				
79.24	$lowpass1d\_fft$			
79.25	$lowpass 1 \\ d\_implicit$			
79.26	lowpass2			
design	low pass filter with cutoff-frequency f1			
79.27	$lowpass2d_2$			
79.28	$lowpass 2 \\ d\_anisotropic$			
79.29	$lowpass2d\_fft$			

 $79.30 \quad lowpass 2 \\ d\_ideal$ 

## 79.31 lowpass2d\_implicit

79.32 lowpass\_arg

79.33 lowpass\_fc\_to\_rho

## 79.34 lowpass\_iir

iir-low pass

## 79.35 lowpass\_iir\_symmetric

two-sided iir low pass filter (for symmetry)

## 79.36 lowpassfilter 2

low-pass filter of data

## 80 signal-processing

## 80.1 peaks\_man

peaks of a periodogram

# 81 signal-processing/periodogram

## 81.1 periodogram

compute the normalized periodogram

## 81.2 periodogram\_2d

compute the normalized periodogram in two dimensions

## 81.3 periodogram\_align

## 81.4 periodogram\_angular

## 81.5 periodogram\_bartlett

estimate the spectral density nonparametrically with Bartlett's  $\tt method$ 

## 81.6 periodogram\_bootstrap

## 81.7 periodogram\_confidence\_interval

confidence interval for periodogram values

## 81.8 periodogram\_filter

## 81.9 periodogram\_median

## 81.10 periodogram\_p\_value

#### 81.11 periodogram\_qq

qq-plot of a spectral density estimate by smoothing against the
 expected
beta-density

## 81.12 periodogram\_quantiles

quantiles of a periodogram

## 81.13 periodogram\_radial

## 81.14 periodogram\_std

standard deviation of a periodogram

#### 81.15 periodogram\_test\_periodicity

test a periodogram for hidden periodic frequency components

function [p,ratio,maxShat,mdx,fdx,S] = periodogram\_test\_periodicity
 (fx,Shat,nf,fmin,fmax,S,mode)

input:
 fx : frequengcies
 Shat : corresponding periodogram values
 nf : number of bins to test for periodicity, ignored when S
 is given
 fmin, fmax : frequency range limits to test
 S : exact (a priori known theoretical spectral density,
 must not be estimated from the periodogram)
 mode : automatically set to "exact", when S given
 inclusive : estimate density by smoothing including the
 central bin

exclusive : estimate density by smoothing excluding the central bin

note: inclusive and exclusive lead to different distribution but identical p-values

TODO pass L and not fx

#### 81.16 periodogram\_test\_periodicity\_2d

```
test a periodogram for hidden periodic frequency components
[p,stat,ratio] = periodogram_test_periodicity_2d(b, L, nf, bmsk,
   fmsk, ns)
input:
      b
           (nx * ny): image to test for presence of hidden
          periodicities,
           i.e. periodicities where the frequency is not known a
              priori
         = nfr or [nfx, nfy]
            radius of circular disk (in number of bins) used for
                smoothing
           the periodogram to estimate the spectral density,
            or axes of ellipses for smoothing
            when b is not square a good choice is nfx/nfy ~ Lx/Ly
    bmsk : mask in real space selecting parts of the image to
        include in
            the analysis default is entire image
            the mask can have non-integer values to feather the
                borders of the mask
      fmsk : mask in frequency selecting frequencies to test for
          periodicity
            default is all frequencies
            note: when b is real, one half plane can always be
                excluded
            because of symmetry. This slightly increases the
                significance
          : number of samples for the monte-carlo determination of
            the test statistics, mc is only used when parts of the
                image are masked
            otherwise the analytic test statistic is used
influence of masking the input file:
            - the root-mean-square energy of the ordinates is
               proportional
             to the number of unmasked points
```

- values in the periodogram are not any more linearly independent so that the dof of the filter window is not nf^2

## 81.17 periodogram\_test\_stationarity

test a periodogram for statoinarity
note : the method works, but is of little practical use,
as it requires about 50 periods and a small dx to detect a
 frequency change by a factor of 2

## 81.18 periodogram\_welsh

# 82 signal-processing

## 82.1 polyfilt1

polynomial filter, can be achieved by iteratively processing the data with a mean (zero-order) filter

## 82.2 qmedfilt1

medfilt1, after fitting a quadratic polynomial

## 82.3 quadratfilt1

## 82.4 quadratwin

#### 82.5 randar1

generate random ar1 process
e1 = randar1(sigma,p,n,m)

#### 82.6 randar1\_dual

draw random variables of two corrlated ar1 processes

#### 82.7 randar2

generate ar2 process

## 82.8 randarp

randomly generate the instance of an ar-p process

#### 82.9 rectwin

rectangular window

#### 82.10 recursive\_sum

## 82.11 select\_range

## 82.12 smooth1d\_parametric

smooth position of p0=x0,y0 between p1=x1,y1 and p2=x2,y2, so that distance to p1 and p2 becomes equal and the chord length remains the same  $\frac{1}{2}$ 

#### 82.13 smooth2

 ${\tt smooth}$  vectos of X

## $82.14 \quad smooth\_man$

## 82.15 smooth\_parametric

 $\label{eq:smooth} \mbox{smooth a parametric function given in $x$-$y coordinates} \\ \mbox{matvec2x2(R,[dxc;dyc])}$ 

## $82.16 \quad smooth\_parametric2$

parametrically smooth the curve

## $82.17 \quad smooth\_with\_splines$

#### 82.18 smoothfft

filter with fast fourier transform

# 83 signal-processing/spectral-density

## $83.1 hex_angular_pdf$

## 83.2 hex\_angular\_pdf\_max

83.3	hex_angular_pdf_max2par
83.4	$spectral\_density\_ar2$
83.5	${\bf spectral\_density\_area}$
integ	rate the spectral density
83.6	$spectral\_density\_estimate\_2d$
83.7	$spectral\_density\_flat$
flat	spectral density of a random vector woth iid elements
83.8	$spectral\_density\_forest$
83.9	$spectral\_density\_gausswin$
83.10	spectral_density_lorentzian

 $83.11 \quad spectral\_density\_lorentzian\_max$ 

lorentzian spectral density

 $\hbox{mode (maximum) of the lorentzian spectral density}$ 

## $83.12 \quad spectral\_density\_lorentzian\_max2par$

transform maximum of the lorentzian spectral density to its distribution parameters  $% \left( 1\right) =\left( 1\right) +\left( 1\right)$ 

## 83.13 spectral\_density\_lorentzian\_scale

normalization scale of the lorentzian spectral density

## $83.14 \quad spectral\_density\_maximum\_bias\_corrected$

## 83.15 spectral\_density\_periodic\_additive\_noise

## 83.16 spectral\_density\_rectwin

## 83.17 spectral\_density\_wperiodic

# 84 signal-processing

## 84.1 spectrogram

spectrogram

## 84.2 sum\_i\_lag

sum of ar1 matrix with lag
sum\_i=1^n rho^|i-k|

#### $84.3 \quad sum_i$

sum of ar1 matrix
sum\_i=1^n sum\_j=1^n rho^|i-j|
this is for the variance, take square root for the standard
 deviation factor

84.4 sum\_ii\_

## $84.5 \quad sum_{ij}$

 $84.6 \quad sum_ij_$ 

84.7 sum\_ij\_partial\_

#### $84.8 \quad sum\_multivar$

sum of matrix entries of bivariate ar1 process

## 84.9 test\_acfar1

## 84.10 tikhonov\_to\_ar1

convert coefficient of the tikhonov regularization to correlatioon of the arl process

## 84.11 trapwin

trapezoidal filter window

#### 84.12 triwin

triangular filter window

#### 84.13 triwin2

triangular filter window

## 84.14 tukeywin\_man

#### 84.15 varar1

error variance of a single sample of a finite length ar1 process with respect to the mean, averaged over the population

## 84.16 welch\_spectrogram

welch spectrogram

## 84.17 wfilt

filter with window

## 84.18 winbandpass

filter with bandpass

# 85 signal-processing/windows

#### 85.1 circwin

## 85.2 danielle\_window

danielle fourier window

85.3 gausswin

85.4 gausswin1

## 85.5 gausswin2

#### 85.6 radial\_window

radial filter window in the 2d-frequency domain

## 85.7 range\_window

range of values within a certain range of indices (window)

## 85.8 rectwin\_cutoff\_frequency

## $85.9 \quad std\_window$

moving block standard deviation

#### $85.10 \quad window2d$

#### 85.11 window\_make\_odd

# 86 signal-processing

#### 86.1 winfilt0

filter with window

## 86.2 winlength

window length for desired cutoff frequency
power at fc is halved
H(wf) = 1/sqrt(2) H(f)
if the filter window were used as a low pass filter
note: the user should prefer a windowed ideal low pass filter
TODO, relate this to DOF

#### 86.3 wmeanfilt

mean filter with window

#### 86.4 wmedfilt

median filter with window

#### 86.5 wordfilt

weighted order filter

## 86.6 wordfilt\_edgeworth

weighed order filter

## 86.7 wrapphase

86.8 xar1

#### 86.9 xcorr\_man

cross correlation of two sampled ar1 processes

# 87 sorting

#### 87.1 sort2

sort two numbers

#### 87.2 sort2d

sort elements of matrix in  ${\tt X}$  returns row and column index of sorted values

# 88 spatial-pattern-analysis/@Spatial\_Pattern

## 88.1 Spatial\_Pattern

class for analysis of remotely sensed and model generated vegetation patterns

## 88.2 analyze\_grid

analyze a 2D spatial pattern, estimate regularity and test for periodicity  $% \left( 1\right) =\left( 1\right) \left( 1\right) +\left( 1\right) \left( 1\right) \left( 1\right) +\left( 1\right) \left( 1$ 

## 88.3 analyze\_transect

analyze 1D transect through a spatial pattern, either remotely sensed or model generated

## 88.4 fit\_parametric\_densities

fit parametric spectral densities to the empirical density

#### 88.5 imread

read an image file containing a pattern, mask and geospatial data

## 88.6 plot

plot the pattern or densities

## 88.7 plot\_transect

plot 1D pattern

## 88.8 report

report statistics of analysis

## 88.9 resample\_functions

resample empirical densities to a comman grid

#### 88.10 tabulate

summarize properties of multiple patterns in a single struct

- 89 spatial-pattern-analysis
- 89.1 approximate\_ratio\_distribution
- 89.2 banded\_pattern

## 89.3 hexagonal\_pattern

- 89.4 patch\_size\_1d
- 89.5 patch\_size\_2d
- 89.6 reconstruct\_isotropic\_density

89.7	$separate\_isotropic\_from\_anisotropic\_density$
89.8	$suppress\_low\_frequency\_lobe$
90	spatial-statistics
90.1	average_corr_2d
91	special-functions
91.1	bessel_sphere
sphei	rical Bessel function of the first kind
91.2	$besseliln\_large\_x$
91.3	beta_man
91.4	betainc_man
91.5	digamma_man
91.6	$\exp 10$

## 91.7 hankel\_sphere

spherical Hankel function for the far field (incident plane wave) first  ${\tt kind}$ 

#### 91.8 hermite

probabilistic's hermite polynomial by recurrence relation

input :
n : order
x : value

output:
f : H\_n(x)
df : d/dx H\_n(x)

## 91.9 lambertw\_numeric

lambert-w function

## 91.10 legendre\_man

legendre polynomials

## 91.11 neumann\_sphere

spherical Neumann function
Bessel function of the second kind

## 92 statistics

#### 92.1 atan\_s2

stadard deviation of the arcus tangens by means of taylor expansion

#### 92.2 binomial

generalized binomial coefficient, working for non-integer arguments , in contrast to the matlab buildin function nchoosek

- 92.3 coefficient\_of\_determination
- 92.4 conditional\_expectation\_normal
- 92.5 correlation\_confidence\_pearson

confience intervals of the correlation coefficient c.f. Fischer 1921

- 93 statistics/distributions
- 93.1 PDF

class for quasi-distributions from a set of sampling points

- 94 statistics/distributions/beta
- 94.1 beta\_kurt
- 94.2 beta\_mean

## 94.3 beta\_moment2param

transform central moments (mean and sd) to parameters of the beta function  $% \left( \frac{1}{2}\right) =\frac{1}{2}\left( \frac{1}{2}\right) +\frac{1}{2}\left( \frac{1}{2}\right) +$ 

#### 94.4 beta\_skew

#### 94.5 beta\_std

# 95 statistics/distributions/bivariate-normal

## 95.1 binorm\_separation\_coefficient

separation coefficient of a bimodal normal distribution

#### 95.2 binormcdf

bio-modal gaussian distribution

#### 95.3 binormfit

fit sum of to normal distribution to a histogram

## 95.4 binormpdf

# 96 statistics/distributions/chi2

#### 96.1 chi2\_kurt

#### 96.2 chi2\_mean

96.3 chi2\_skew

96.4 chi2\_std

# 97 statistics/distributions/circular-normal

#### 97.1 wnormpdf

wrapped normal distribution to the unit circle  ${\tt c.f.}$  stephens

# 98 statistics/distributions

## 98.1 edgeworth\_cdf

edgeworth expansion of an unknown cumulative distribution with mean mu, standard deviation sigma, and third and fourth cumulants c.f. Rao 2010

## 98.2 edgeworth\_pdf

probability density of and unknown distribution
with mean mu, standard deviation sigma, and third and fourth
 cumulants
c.f. Rao 2010

## $98.3 \quad exppdf_max2par$

99	statistics/distributions/fisher
99.1	fisher_mean
99.2	$fisher\_moment2param$
99.3	fisher_std
100	statistics/distributions/gamma
100.1	gamma_mean
100.2	gamma_mode
100.3	gamma_mode2par
	gamma_moment2param
	form modes (mu,sd) to parameters of the gamma distribution
100.5	$ m gamma\_std$

100.6 gamma\_stirling

100.7	gampdf₋man
-------	------------

100.8 generalized\_gamma\_mean

# 101 statistics/distributions/hotelling-t2

101.1 t2cdf

Hotelling's T-squared cumulative distribution

## 101.2 t2inv

inverse of Hotelling's T-squared cumulative distribution

# $102 \quad statistics/distributions/kurt-normal$

102.1 kurtncdf

## 102.2 kurtnpdf

# 103 statistics/distributions/log-triangular

## 103.1 logtrialtcdf

pdf of a logarithmic triangular distribution

#### 103.2 logtrialtiny

inverse of the logarithmic triangular distribution
= (d F log(a) log(b) + a log(b) - b log(a) - d F log(a) log(c) - a
 log(c) + d F log(b) log(c) + b log(c) - d F log^2(b))/((log(a)
 - log(b)) W((a^(-1/(log(a) - log(b))) (b^(-log(c)/log(a) - 1/
 log(a)) c)^(-log(a)/(log(a) - log(b))) (-d F log^2(b) + a log(b
 ) + d F log(a) log(b) + d F log(c) log(b) - b log(a) - a log(c)
 + b log(c) - d F log(a) log(c)))/(log(a) - log(b)))
x = (d F log(a) log(b) + a log(b) - b log(a) - d F log(a) log(c) - a
 log(c) + d F log(b) log(c) + b log(c) - d F log^2(b))/((log(a)
 - log(b)) W((a^(-1/(log(a) - log(b))) (b^(-log(c)/log(a) - 1/log
 (a)) c)^(-log(a)/(log(a) - log(b))) (-d F log^2(b) + a log(b) +
 d F log(a) log(b) + d F log(c) log(b) - b log(a) - a log(c) + b
 log(c) - d F log(a) log(c)))/(log(a) - log(b))))

## 103.3 logtrialtmean

mean of the logarithmic triangular distribution

#### 103.4 logtrialtpdf

density of the logarithmic triangular distribution

#### 103.5 logtrialtrnd

#### 103.6 logtricdf

cumulative distribution of the logarithmic triangular distribution

## 103.7 logtriinv

invere of the logarithmic triangular distribution

## 103.8 logtrimean

mean of the logarithmic triangular distribution

## 103.9 logtripdf

 $probability \ density \ of \ the \ logarithmic \ triangular \ distribution$ 

## 103.10 logtrirnd

# 104 statistics/distributions/log-uniform

## 104.1 logu\_median

median of the log-uniform distribution

## 104.2 logucdf

probability density of the logarithmic uniform distribution

## 104.3 logucm

central moments of the log-uniform distribution

## 104.4 loguinv

inverse of the log-uniform distribution

## 104.5 logumean

mean of the log-uniform distribution

## 104.6 logupdf

pdf of the log uniform distribution

## 104.7 logurnd

random numbers following a log-uniform distribution

## 104.8 loguvar

variance of the log-uniform distribution

# 105 statistics/distributions/loglog

105.1 loglogpdf

# 106 statistics/distributions/lognormal

 $106.1 \log n_{mean}$ 

## $106.2 \quad logn\_mode$

mode (maximum) of the log-normal density

## $106.3 \quad logn\_mode2param$

## $106.4 logn_moment2param$

transform the mode (mu,sd) to parameters of the  $\log$  normal distribution

## $106.5 \quad logn\_param2moment$

transform parameters to mode (mu, sd) for the log normal distribution  $% \left( 1\right) =\left( 1\right) \left( 1$ 

 $106.6 \quad logn\_skewness$ 

 $106.7 \quad logn\_std$ 

 $106.8 \quad lognpdf_{-}$ 

log normal distribution called by modes rather than parameters

106.9 lognpdf\_entropy

- 107 statistics/distributions/logskew
- 107.1 logskewcdf
- 107.2 logskewpdf
- 108 statistics/distributions/mise
- 108.1 misespdf

## 109 statistics/distributions

#### 109.1 ncx2\_moment2param

# 110 statistics/distributions/normal

## 110.1 normpdf\_entropy

## 111 statistics/distributions/passes

## 111.1 bandpass1d\_continuous\_pdf

#### 111.2 bandpass1d\_continuous\_pdf\_max

maximum of the bandpass spectral density

## $111.3 \quad bandpass1d\_continuous\_pdf\_max2par$

transform mode (maxima) of the bandpass spectral density into the
 paramter
of the underlying distribution

## 111.4 bandpass1d\_continuous\_pdf\_scale

normaliztation scale of the spatial bandpass density

## $111.5 \quad bandpass1d\_discrete\_pdf$

spectral density of the discrete spatial (two-sided) bandpass filter  $% \left( \frac{1}{2}\right) =\left( \frac{1}{2}\right) +\left( \frac{1}{2}\right)$ 

## 111.6 bandpass2d\_discrete\_pdf

## 111.7 bandpass2d\_pdf

## 111.8 bandpass2d\_pdf\_mode

## $111.9 \quad bandpass2d\_pdf\_mode2par$

transform mode (maxima) of the bandpass spectral density into the
 paramter
of the underlying distribution

## 111.10 bandpass2d\_pdf\_scale

# consine shaped spectral density of a highpass filter 111.12 highpass $1d_pdf$ $111.13 \quad highpass 2d\_discrete\_pdf$ $111.14 \quad highpass2d\_pdf$ $111.15 \quad lowpass1d\_continuous\_pdf$ $111.16 \quad lowpass1d\_continuous\_pdf\_scale$ $111.17 \quad lowpass1d\_discrete\_pdf$ 111.18 lowpass1d\_one\_sided\_pdf $111.19 \quad lowpass2d\_discrete\_pdf$

 $111.11 \quad highpass1d\_discrete\_cos\_pdf$ 

 $111.20 \quad lowpass2d\_pdf$ 

# 112 statistics/distributions

## 112.1 pdfsample

pdf from sample distribution
Note: better use kernal density estimates

- 113 statistics/distributions/phase\_drift
- 113.1 phase\_drift\_acf
- 113.2 phase\_drift\_acf\_2d
- 113.3 phase\_drift\_acf\_across
- 113.4 phase\_drift\_cdf
- 113.5 phase\_drift\_inv
- 113.6 phase\_drift\_patch\_size\_distribution
- 113.7 phase\_drift\_pdf

spectral density of a fourier series where the phase undergoes
 brownian motion
with standard deviation s per unit distance

- $113.8 \quad phase\_drift\_pdf\_2d$
- 113.9 phase\_drift\_pdf\_across
- 113.10 phase\_drift\_pdf\_across\_max
- 113.11 phase\_drift\_pdf\_across\_max2par
- $113.12 \quad phase\_drift\_pdf\_across\_mode2par$
- 113.13 phase\_drift\_pdf\_mode

 ${\tt mode}$   $({\tt maximum})$  of the spectral density of the fourier series with brownian phase

113.14 phase\_drift\_pdf\_mode2par

transform mode to parameters of the brownian phase spectral density

- 113.15 phase\_drift\_pdf\_reg2par
- $113.16 \quad phase\_drift\_pdf\_scale$

normalization scale of the brownian phase spectral density

114 statistics/distributions/	'skew-normal
-------------------------------	--------------

- 114.1 skew\_generalized\_normal\_fit
- $114.2 \quad skew\_generalized\_normpdf$
- 114.3 skewcdf
- 114.4 skewparam\_to\_central\_moments
- 114.5 skewpdf

skew-normal distribution c.f. Azzalini 1985

114.6 skewpdf\_entropy

# 115 statistics/distributions/triangular

115.1 tricdf

 ${\tt cumulative\ distribution\ of\ the\ log-triangular\ distribution}$ 

115.2 triinv

inverse of the triangular distribution

### 115.3 trimedian

median of the triangular distribution

## 115.4 tripdf

probability density of the triangular distribution

### 115.5 trirnd

random numbers of the triangular distribution

# 116 statistics/distributions/wrapped-normal

116.1 normpdf\_wrapped

# 116.2 normpdf\_wrapped\_mode

 $116.3 \quad normpdf\_wrapped\_mode2par$ 

# 117 statistics

117.1 error\_propagation\_fraction

# 117.2 error\_propagation\_product

117.3	$example\_standard\_error\_of\_sample\_quantiles$
117.4	$f_{\text{var}}$ finite
	on of variance when sampling from a finite population replacement
117.5	${ m gaussfit}3$
117.6	$\mathbf{gaussfit\_quantile}$
117.7	geoserr

# $117.9 \quad hodges\_lehmann\_correlation$

hodges\_lehmann correlatoon coefficient

c.f. Shamos 1976

117.8 geostd

- c.f. Bickel and Lehmann 1976
- c.f. rousseeuw 1993
- c.f. Shevlyakov 2011

## 117.10 hodges\_lehmann\_dispersion

# 118 statistics/information-theory

## 118.1 akaike\_information\_criterion

```
akaike information criterion
serr : rmse of model prediction
n : effective sample size
k : number of parameters
c.f. akaike (1974)
c.f. sugiura 1978
```

## 118.2 bayesian\_information\_criterion

bayesian information criterion

## 119 statistics

## 119.1 jackknife\_block

## 119.2 kurtosis\_bias\_corrected

bias corrected kurtosis

## 119.3 limit

limit a by lower and upper bound

# 119.4 logfactorial

approximate log of the factorial

# 119.5 lognfit\_quantile

# $119.6 \quad max_{-}exprnd$

## 119.7 maxnnormals

expected maximum of n normal variables c.f. Wolperts this is the median, not the mean of the maximum! see median of gumbel

## 119.8 mean\_angle

#### 119.9 mean\_max\_n

#### 119.10 mean\_min\_n

## 119.11 midrange

mid range of columns of  ${\tt X}$ 

### 119.12 minavg

solution of the minimum variance problem minimise the variance of the weighted sum of n-independent random variables with equal mean and individual variance

#### 119.13 mode\_man

# 120 statistics/moment-statistics

## 120.1 autocorr\_man3

autoccorrelation of the columns of X

### 120.2 autocorr\_man4

autocorrelation for x if x is a vector, or indivvidually for the columns of x if x is a matrix

c.f. box jenkins 2008 eq. 2.1.12

Note that it is faster to compute the acf in frequency space as done in the matlab internal function  $% \left( 1\right) =\left( 1\right) +\left( 1\right$ 

### 120.3 autocorr\_man5

autocorrellation of the columns of X

### 120.4 blockserr

estimate the standard error of potetially sequentilly correlated data  $% \left( 1\right) =\left( 1\right) \left( 1\right) +\left( 1\right) \left( 1\right) \left( 1\right) +\left( 1\right) \left( 1\right) \left($ 

by blocking

block length should be sufficiently larger than correlation length and sufficiently smaller than data length

this uses a sliding block approach, which reduces the variation of the error estimate

#### 120.5 comoment

 $\begin{array}{c} {\tt non-central\ higher\ order\ moments\ of\ the\ multivariate\ normal} \\ {\tt distribution} \end{array}$ 

 $\ensuremath{\text{c.f.}}$  Moments and cumulants of the multivariate real and complex Gaussian distributions

note : there seem to be some typos in the original paper, for  $x^4$  cii<sup>2</sup>, the square seems to be missing

mu : nx1 mean vector

C : nxn covariance matrix

k : nx1 powers of variables in moments

#### 120.6 corr\_man

correlation of two vectors

## 120.7 cov\_man

covariance matrix of two vectors

## 120.8 dof

mininum number of support points for a polynomial of degree order in dim dimensions

## 120.9 edgeworth\_quantile

inverse edgeworth expansion c.f. cornis fisher 1937 c.f. Rao 2010 c.f. 2.50 in hall CHERNOZHUKOV 3.3

## 120.10 effective\_sample\_size

effective sample size of the weighted mean of uncorrelated data  ${\tt c.f.}$  Kish

### 120.11 f\_correlation

correction factor for standard error of the mean of n ar1-correlated iid samples

### 120.12 f\_finite

reduction factor of standard error for sampling from a finite
 distribution
without replacement

### 120.13 lmean

mean of x.^l, not of abs

# 120.14 lmoment

1-moment of vector x

### 120.15 maskmean

mean of the masked values of X

### 120.16 masknanmean

### 120.17 mean1

mean of x

## 120.18 mean\_man

mean and standard error of X

### 120.19 mse

mean squared error of residual vector res this is de-facto the std for an unbiased residual

#### 120.20 nanautocorr\_man1

autocorrelation of a vector with nan-values

### 120.21 nanautocorr\_man2

autocorrelation of a vector with nan-values

## 120.22 nanautocorr\_man4

compute autocorrelation for x if x is a vector, or indivvidually
 for the
columns of x if x is a matrix
box jenkins 2008 eq. 2.1.12
TODO nan is problematic!
Note that it is faster to compute the acf in frequency space
as done in the matlab internal function

#### 120.23 nancorr

(co)-correlation matrix when samples a NaN

# 120.24 nancumsum

cumulative sum, setting nan values to zero

### 120.25 nanlmean

mean of the 1-th power of the absolute value of  $\boldsymbol{x}$ 

### 120.26 nanr2

coefficient of determination when samples are invalid

# 120.27 nanrms

root mean square value when sample contains nan-values

#### 120.28 nanrmse

root mean square error from vector of residuals this is de-facto the std for an unbiased residual

### 120.29 nanserr

standard error of  $\boldsymbol{x}$  with respect to mean when  $\boldsymbol{x}$  contains nan values

#### 120.30 nanwmean

```
weighted mean
min_x sum w (x-mu)^2 => mu = sum(wx)/sum(w)
varargin can be dim
function [mu serr] = nanwmean(w,x)
```

### 120.31 nanwstd

weighed standard deviation

### 120.32 nanwvar

```
weighted variance of columns, corrected for degrees of freedom ( \ensuremath{\mathsf{bessel}}\xspace)
```

```
s^2 = sum(w*(x-sum(wx)/sum(w))^2)/sum(w)
```

### 120.33 nanxcorr

### 120.34 pearson

pearson correlation coefficient

# 120.35 pearson\_to\_kendall

conversion of pearson to kendall correlation coefficient c.f. Kruskal 1958  $\,$ 

## 120.36 pool\_samples

pooled mean and standard deviation of several groups of different size, mean and standard deviation

## 120.37 qmean

trimmed mean

## 120.38 range\_mean

#### $120.39 \quad rmse_{-}$

root mean square error computed from a residual vector this is de-facto the std for an unbiased residual

### 120.40 serr

standard error of the mean of a set of uncorrelated samples

### 120.41 serr1

## 120.42 test\_qskew

# 120.43 test\_qstd\_qskew\_optimal\_p

### 120.44 wautocorr

autocorrelation for x if x is a vector, or indivvidually for the columns of x if x is a matrix samples can be weighted

c.f. box jenkins 2008 eq. 2.1.12

### c.f. autocorr\_man4

Note that it is faster to compute the acf in frequency space as done in the matlab internal function  $\ \ \,$ 

## 120.45 wcorr

correlation of two vectors when samples are weighted

### 120.46 wcov

covariance of two vectors when samples are weighted

### 120.47 wdof

effective degrees of freedom for weighted samples

### 120.48 wkurt

kurtosis with weighted samples

# 120.49 wmean

```
weighted mean
min_x sum w (x-mu)^2 => mu = sum(wx)/sum(w)
varargin can be dim
function [mu serr] = wmean(w,x)
```

## 120.50 wrms

weighted root mean square

### 120.51 wserr

weighted root mean square error

### 120.52 wskew

```
skewness of a weighted set of samples function sk = wskew(w,x)
```

#### 120.53 wstd

weighed standard deviation

#### 120.54 wvar

```
weighted variance of columns, corrected for degrees of freedom (
   bessel)
variance of the weighted sample mean of samples with same mean (but
   not necessarily same variance)
s^2 = sum (w^2(x-sum(wx)^2))
s2_mu : error of mean, s2_mu : sd of prediction
```

## 121 statistics

# 121.1 nangeomean

## 121.2 nangeostd

geometric standard deviation ignoring nan-values

# 122 statistics/nonparametric-statistics

#### 122.1 kernel1d

```
X : ouput x axis bins
xi : samples along x
m : number of bins in X
fun : kernel function
```

 $\operatorname{pdf}$  : propability density of  $\operatorname{xi}$ 

#### 122.2 kernel2d

 ${\tt kernel\ density\ estimate\ in\ two\ dimensions}$ 

## 123 statistics

### 123.1 normmoment

expected norm of x.^n, when values  ${\bf x}$  in  ${\bf x}$  are iid normal with mu and sigma

## 123.2 normpdf2

pdf of the bivariate normal distribution

# 124 statistics/order-statistics

## 124.1 hodges\_lehmann\_location

hodges lehman location estimator

Asymptotic rms efficency of location estimte:

mean: 1 s/sqrt(n)

hodges lehman: sqrt(pi/3)\*s ~ 1.0233 ~ s/sqrt(n) median: pi/2 ~ s/sqrt(n) ~ 1.25 ~ s ~ / sqrt(n)

#### 124.2 kendall

kendall correlation coefficient

### 124.3 kendall\_to\_pearson

convert kendall rank correlation coefficient to the person product
 moment
correlation coefficient

c.f. Kruskal, 1958, p. 823

#### $124.4 \mod 2sd$

transform median absolute deviation to standard deviation for normal distributed values

### 124.5 madcorr

proxy correlation by median absolute deviation

### 124.6 median2\_holder

### 124.7 median\_ci

median and its confidence intervals under assumption of normality  $se_me = sqrt(1/2 pi) 1.25331 * sd/sqrt(n)$ 

### 124.8 median\_man

median and confidence intervals c is a P value for the confidence interval, default is 0.95 (2-sigma) median of the colums of  $\rm X$ 

### 124.9 mediani

index of median, if median is not unique, any of the values is chosen

### 124.10 nanmadcorr

proxy correlation by median absolute deviation

### 124.11 nanwmedian

weighted median, skips nan-values

## 124.12 nanwquantile

weighted quantile, skips nan values

## 124.13 oja\_median

```
two dimensional oja median note: the multivariate median is not unique oja 1983, for extension to multivariate function, see chaudhri
```

## 124.14 qkurtosis

kurosis computed for quantiles

```
Note: this is a measurement of shape-tailedness and yields the same value for the normal distribution as "kurtosis"

However, this is a separate statistic and hence requires different methods for calculating P-values and hypothesis testing
```

### 124.15 qmoments

moments estimated from quantiles

## 124.16 qskew

skewness estimated from quantiles

```
Note: this is a measurement of shape-symmetry and yields the same value for the skew-normal distribution as "skewness"

However, this is an own statistic and hence requires different methods for calculating P-values and hypothesis testing
```

# 124.17 qskewq

skewness estimated by quantiles

# 124.18 qstdq

proxy standard deviation determined by quantiles

# 124.19 quantile1\_optimisation

# $124.20 \quad quantile 2\_breckling$

qunatile regression

# 124.21 quantile2\_chaudhuri

quantile regression

# 124.22 quantile 2\_projected

quantile in two dimensions

# 124.23 quantile 2\_projected 2

spatial qunatile for chosen direction

# 124.24 quantile\_envelope

# 124.25 quantile\_regression\_simple

simple quantile regression

# 124.26 ranking

ranking for spearman statistics

# 124.27 spatial\_median

c.f. Oja 2008
is this the same as the oja simplex median (c.f. small 1990)?

# 124.28 spatial\_quantile

spatial quantile

# 124.29 spatial\_quantile2

spatial quantile

# 124.30 spatial\_quantile3

spatial quantile

# 124.31 spatial\_rank

unsigned rank

# 124.32 spatial\_sign

spatial sign

# 124.33 spatial\_signed\_rank

signed rank

Note: this is only a true rank if  ${\tt X}$  is normal with zero mean, abitrary variance

# 124.34 spearman

spearman's product moment coefficient

# 124.35 spearman\_rank

## $124.36 \quad spearman\_to\_pearson$

conversion of spearman rank to person product moment correlation coefficient  $% \left( 1\right) =\left( 1\right) \left( 1\right) +\left( 1\right) \left( 1\right) \left( 1\right) +\left( 1\right) \left( 1\right) \left($ 

# 124.37 wmedian

weighted median

# 124.38 wquantile

weighted quantile

## 125 statistics

## 125.1 qstd

# 125.2 quantile\_extrap

# 125.3 quantile\_sin

# 126 statistics/random-number-generation

# 126.1 laplacernd

 ${\tt random}\ {\tt number}\ {\tt of}\ {\tt laplace}\ {\tt distribution}$ 

### 126.2 randc

correlate to correlated standard normally distributed vectors

## 126.3 skewness2param

# 126.4 skewpdf\_central\_moments

# 126.5 skewrnd

random numbers of the skew normal distribution

## 127 statistics

## 127.1 range

range and mid range of input

# 127.2 resample\_with\_replacement

# 128 statistics/resampling-statistics/@Jackknife

### 128.1 Jackknife

class for leave out 1 (delete 1) Jackknife estimates

- note 1 : the 1-delete jackknife does not yield consistend estimates
   for all functions,
  - in particular it will perform poorly on robust estimation functions
  - this is overcome by the d-delete jacknife, where d has to exceed the breakdown point
  - of the estimating function, for example sqrt(n) for the median
  - as this leads to unreasonably large number of repetitions, bootstrap
  - is recommended for large sample cases (or blocking for sequential data)
- note 2 : as a linearisation, jackknife underestimates the error variance in case of

dependence in the data

note 3 : studentisation and the leave out 1 jackknife are related note 4 : the double 1 sample jacknife performs iferior to the d1 jacknife  $\,$ 

### 128.2 estimated\_STATIC

jacknife estimate of mean, bias and standard error

 $\verb|theta0|: estimate from all samples|\\$ 

thetad : set of estimates obtained by leaving out one data point  $\dot{}$ 

each

last dimension of theta is assumed to be the jackknife dimension

# 128.3 matrix1\_STATIC

matrix of estimation for leaving out two samples at a time

#### 128.4 matrix2

matrix of estimations for jacknive with two samples left out

# 129 statistics/resampling-statistics

## 129.1 block\_jackknife

## 129.2 jackknife\_moments

moments determined by the jacknife

func : function of interest on the samples (e.g. mean)

A : parameter matrix columns : parameters

rows : samples of the parameter sets

d : number of samples left out

### 129.3 moving\_block\_jackknife

```
blocked Jacknfife for autocorrelated data
sliding block, statistically more efficient but computationally
    expensive
note, number of blocks must be sufficiently large h ~ sqrt(n)? << n</pre>
```

### 129.4 randblockserr

standard error of sequentilly correlated data by blocking block length should be sufficiently larger than correlation length and sufficiently smaller than data length

this uses a sliding block approach, which reduces the variation of the error estimate  $% \left( 1\right) =\left( 1\right) \left( 1\right) +\left( 1\right) \left( 1\right) \left( 1\right) +\left( 1\right) \left( 1\right)$ 

 $\ensuremath{\mathsf{TODO}}$  this does not work, randomly picking samples does not reveal the correlation

### 129.5 resample

```
resample a vector and apply function to it

TODO, should be with replacement

n : number of samples
```

m : number of subsamples

cx : maximum number of combinations

# 130 statistics

## 130.1 scale\_quantile\_sd

scale factor for the standard deviation of the asymtpotic distibution of sample quantiles (for normal distribution) see cadwell, 1952

# 130.2 sd\_sample\_quantiles

## 130.3 spatialrnd

### 130.4 trimmed\_mean

trimmed mean

### 130.5 $ttest2_man$

```
two-sample t-test here posix return value standard: h=0 accepted, h=1 failed note: the matlab logic is inverse : h=1 accepted, h=0 failed two sided univariate t-test
```

#### 130.6 ttest\_man

two-sample t-test
unequal sample size
equal variance

# 130.7 ttest\_paired

```
paired t-test unequal sample size equal variance more powerfull than unpaired test, as long as correlation between {\tt x1} and {\tt x2} > 0
```

# 130.8 uniformpdf

## 130.9 wgeomean

```
weighted geometric mean
function mu = wgeomean(w,x)
```

# 130.10 wgeovar

variance of the weighted geometric mean

## 130.11 wharmean

weighted harmonic mean

## 130.12 wharstd

### 130.13 wharvar

## 131 stochastic

# 131.1 brownian\_drift\_hitting\_probability

131.2	$brownian\_drift\_hitting\_probability2$
131.3	brownian_field
pa: Refere	te Fractional Brownian field on unit disk, with Hurst rameter 'H'; nce: %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
131.4	$brownian\_motion\_1d\_acf$
131.5	$brownian\_motion\_1d\_cov$
131.6	$brownian\_motion\_1d\_fft$
131.7	$brownian\_motion\_1d\_fourier$
131.8	$brownian\_motion\_1d\_interleave$

 $131.9 \quad brownian\_motion\_1d\_laplacian$ 

131.10 brownian\_motion\_2d\_cov

131.11	$brownian\_motion\_2d\_fft$
131.12	$brownian\_motion\_2d\_fft\_old$
131.13	$brownian\_motion\_2d\_fourier$
131.14	$brownian\_motion\_2d\_interleave$
131.15	$brownian\_motion\_2d\_interleaving$
131.16	brownian_motion_2d_kahunen
131.17	$brownian\_motion\_2d\_laplacian$
131.18	$brownian\_motion\_with\_drift\_hitting\_probability$
131.19	$ornstein\_uhlenbeck\_cov$

131.20 ornstein\_uhlenbeck\_mean

- $131.21 \quad ornstein\_uhlenbeck\_spectral\_density$
- 131.22 ornstein\_uhlenbeck\_std
- 132 mathematics

mathematical functions of various kind

- 132.1 ternary\_diagram
- 133 test/finance
- 133.1 test\_gbb\_mean
- 133.2 test\_gbb\_std
- 133.3 test\_gbm\_mean
- $133.4 \quad test\_gbm\_mean\_entire\_series$
- 133.5 test\_gbm\_moment2par

- $133.6 \quad test\_gbm\_moment2par\_entire\_series$
- $133.7 \quad test\_gbm\_std$
- 133.8 test\_gbm\_std\_entire\_series
- 134 test/fourier
- 134.1 test\_fourier\_freq2ind
- 135 test/master
- $135.1 \quad dat\_test\_lanczos\_3d\_k\_20\_n\_40$
- 135.2 poisson2d\_blk
- $135.3 \quad qr\_implicit\_givens\_2$
- 135.4 spectral\_derivative\_2d
- 135.5 test\_2d\_eigensolver\_hydrogen

- 135.6 test\_2d\_refine
- 135.7 test\_3d\_eigensolver\_hydrogen
- 135.8 test\_FEM
- 135.9 test\_Mesh\_3d
- 135.10 test\_arnoldi
- 135.11 test\_arpackc
- 135.12 test\_assemble
- 135.13 test\_assembly\_performance
- 135.14 test\_bc\_one\_sided
- 135.15 test\_compare\_solvers

- $135.16 \quad test\_complete$
- 135.17 test\_convergence
- 135.18 test\_convergence\_b
- 135.19 test\_df\_2d
- 135.20 test\_eig\_algs
- $135.21 \quad test\_eig\_inverse$
- $135.22 \quad test\_eigs\_lanczos$
- 135.23 test\_eigs\_lanczos\_1
- $135.24 \quad test\_eigs\_lanczos\_2$
- 135.25 test\_eigs\_lanczos\_performance

- 135.26 test\_fdm
- 135.27 test\_fdm\_d\_vargrid
- 135.28 test\_fdm\_spectral
- 135.29 test\_fem
- 135.30 test\_fem\_1d
- 135.31 test\_fem\_1d\_higher\_order
- 135.32 test\_fem\_2d\_adaptive
- 135.33 test\_fem\_2d\_higher\_order
- 135.34 test\_fem\_3d\_higher\_order
- 135.35 test\_fem\_3d\_refine

- $135.36 \quad test\_fem\_b$
- 135.37 test\_fem\_derivative
- 135.38 test\_fem\_quadrature
- 135.39 test\_final
- 135.40 test\_fix\_substitution
- 135.41 test\_forward
- 135.42 test\_get\_sparse\_arrays
- 135.43 test\_harmonic\_oscillator
- $135.44 \quad test\_high\_order\_fdm\_periodic\_bc$
- 135.45 test\_hydrogen\_wf

- 135.46 test\_ichol
- 135.47 test\_interpolation
- 135.48 test\_inverse\_problem
- 135.49 test\_it\_vs\_exact
- 135.50 test\_jama
- 135.51  $test\_jd$
- 135.52  $test\_jdqz$
- 135.53 test\_lanczos\_2
- 135.54 test\_lanczos\_biorthogonal
- 135.55 test\_laplacian

- $135.56 \quad test\_laplacian\_non\_uniform$
- $135.57 \quad test\_laplacian\_simple$
- 135.58 test\_mesh\_2d\_uniform
- 135.59 test\_mesh\_2d\_uniform\_2
- 135.60 test\_mesh\_circle
- $135.61 \quad test\_mesh\_generation$
- $135.62 \quad test\_mesh\_interpolate$
- 135.63 test\_mg
- 135.64 test\_minres\_recycle
- 135.65 test\_multigrid

- 135.66 test\_nc
- 135.67 test\_nonuniform\_symmetric
- 135.68 test\_pde
- 135.69 test\_permutation
- 135.70 test\_poison\_fem
- 135.71 test\_polar
- 135.72 test\_potential
- 135.73 test\_powers
- 135.74 test\_precondition
- 135.75 test\_project\_rectangle

 $135.76 \quad test\_qr$ 

 $135.77 \quad test\_quantum\_well$ 

 $135.78 \quad test\_radial\_adaptive$ 

135.79 test\_radial\_confinement

135.80 test\_radial\_fixes

135.81 test\_refine\_2d

135.82 test\_refine\_2d\_b

135.83 test\_refine\_3d

135.84 test\_refine\_structural

135.85 test\_regularisation

- 135.86 test\_round\_off
- 135.87 test\_schrödinger\_potentials
- 135.88 test\_uniform\_mesh
- 135.89 test\_vargrid
- 136 test/signal-processing/autocorrelation
- 136.1 test\_acf
- 136.2 test\_acf\_bias
- 136.3 test\_acfar1\_2
- 136.4 test\_acfar1\_3
- 136.5 test\_acfar1\_4

136.6 test\_acfar2

136.7 test\_ar1\_var\_factor

136.8 test\_ar1\_var\_factor\_2

 $136.9 \quad test\_ar1\_var\_mu\_single\_sample$ 

136.10  $test_ar1_var_pop$ 

136.11  $test_ar1_var_pop_1$ 

136.12 test\_ar1delay

136.13  $test_ar2$ 

 $136.14 \quad test\_phase\_drift\_acf$ 

- $137 \quad test/signal\text{-}processing/passes$
- 137.1 test\_bandpass2d\_ideal
- 137.2 test\_lowpass1d\_fft
- 137.3 test\_lowpass1d\_implicit
- $137.4 \quad test\_lowpass2d\_anisotropic$
- 137.5 test\_lowpass2d\_fft
- 137.6 test\_lowpass2d\_rho
- 138 test/signal-processing/periodogram
- 138.1 test\_periodicity\_test\_2d
- $138.2 \quad test\_periodogram\_bartlett\_se$
- 138.3 test\_periodogram\_gauss

138.4	$test\_periodogram\_radial$
138.5	$test\_periodogram\_test$
138.6	$test\_periodogram\_test\_periodicity\_2d$
138.7	$test\_periogogram\_significance$
139	test/signal-processing/spectral-density
139.1	$test\_phase\_drift\_pdf$
139.2	$test\_phase\_drift\_pdf\_2d$
139.3	$test\_phase\_drift\_pdf\_across$
139.4	$test\_phase\_drift\_pdf\_across\_mode2par$

 $139.5 \quad test\_phase\_drift\_pdf\_mode$ 

- $139.6 \quad test\_phase\_drift\_pdf\_mode2par$
- 139.7 test\_phase\_drift\_pdf\_scale
- 139.8 test\_spectral\_density\_2
- 139.9 test\_spectral\_density\_bandpass\_2d
- $139.10 \quad test\_spectral\_density\_bandpass\_2d\_max2par$
- 139.11 test\_spectral\_density\_bandpass\_continuous

 $\label{lem:lemma$ 

- $139.12 \quad test\_spectral\_density\_bandpass\_continuous\_1$
- 139.13 test\_spectral\_density\_bandpass\_maximum
- $139.14 \quad test\_spectral\_density\_bandpass\_scale$
- 139.15 test\_spectral\_density\_bp

139.16	$test\_spectral\_density\_bp\_2d$
139.17	$test\_spectral\_density\_bp\_approx$
139.18	$test\_spectral\_density\_flat$
139.19	$test\_spectral\_density\_hp\_cos$
139.20	$test\_spectral\_density\_lorentzian\_max$
139.21	$test\_spectral\_density\_lorentzian\_scale$
139.22	$test\_spectral\_density\_lowpass$
139.23	$test\_spectral\_density\_lowpass\_continuous$
139.24	$test\_spectral\_density\_lowpass\_continuous\_1$

 $139.25 \quad test\_spectral\_density\_maxiumum\_bias\_corrected$ 

- 140 test/signal-processing
- 140.1 test\_autocorrelation\_max
- $140.2 \quad test\_cdf\_bandpass\_continuous$
- 140.3 test\_fit\_spectral\_density
- $140.4 \quad test\_phase\_drift\_cdf$
- 141 test/spatial-pattern-analysis
- 141.1 test\_approximate\_ratio\_distribution
- 141.2 test\_approximate\_ratio\_quantile
- 141.3 test\_separate\_isotropic\_density
- 142 test/statistics/distributions/gamma
- $142.1 \quad test\_generalized\_gamma\_mean$

143	test/	statistics,	/distri	butions/	log-uniform

- 143.1 test\_logurnd
- 144 test/statistics/distributions/passes
- $144.1 \quad test\_bandpass2d\_pdf$
- 145 test/statistics/distributions/skew-normal
- 145.1 test\_skew\_generalized\_normpdf
- 146 test/statistics/distributions
- $146.1 \quad test\_normpdf\_wrapped$
- 147 test/statistics/moment-statistics
- 147.1 test\_wmean
- 148 test/statistics
- 148.1 test\_fisher\_moment2param
- 148.2 test\_gamma\_mode

- 149 test/stochastics
- 149.1 test\_brownian\_surface
- 150 test
- 150.1 test\_S
- 150.2 test\_advect\_analytic
- 150.3 test\_asymbp
- 150.4 test\_bandpass2d
- 150.5 test\_bandwidth
- 150.6 test\_bartlett\_angle
- 150.7 test\_bartlett\_distribution
- 150.8 test\_bartlett\_expansion

150.9	$\operatorname{test\_beta}$
150.10	${f test\_betainc}$
150.11	$test\_bivariate\_covariance\_term$
150.12	$test\_brownian\_drift\_hitting\_probability$
150.13	$test\_brownian\_drift\_hitting\_probability2$
150.14	$test\_brownian\_motion\_1d$
150.15	$test\_brownian\_motion\_2d\_cov$
150.16	$test\_brownian\_motion\_2d\_fft$

 $150.17 \quad test\_brownian\_noise\_1d$ 

150.18 test\_brownian\_noise\_2d

150.20 test\_coherence 150.21 test\_combined\_spectral\_density 150.22 test\_continuous\_fourier\_transform 150.23 test\_convexity 150.24  $test_d2$  $150.25 \quad test\_determine\_phase\_shift$ 150.26 test\_diffuse\_analytic

150.27 test\_diffusion\_matrix

150.28 test\_ellipse

150.19 test\_brownian\_noise\_interleave

 $150.29 \quad test\_error\_propagation\_fraction$ 

150.30  $test_f$ 

150.31 test\_f2

 $150.32 \quad test\_fit\_2d\_spectral\_density$ 

150.33 test\_fourier

150.34 test\_fourier\_derivative

150.35 test\_fourier\_derivative\_1

150.36 test\_fourier\_integral

150.37 test\_fourier\_mask\_covariance\_matrix

150.38  $test_ft_p$ 

- $150.39 \quad test\_gam$
- 150.40 test\_gamma\_distribution
- 150.41 test\_gampdf\_man
- 150.42 test\_gaussfit3
- 150.43 test\_gaussian\_flat
- 150.44  $test\_geoserr$
- $150.45 \quad test\_hexagonal\_pattern$
- 150.46 test\_iafrate
- $150.47 \quad test\_implicit\_ode$
- 150.48 test\_imrotmat

150.49 test\_integration

150.50 test\_ivp

150.51 test\_jacobian

150.52 test\_lanczoswin

150.53 test\_laplacian\_power

 $150.54 \quad test\_lognfit\_quantile$ 

 $150.55 \quad test\_ls\_perpendicular\_offset$ 

150.56 test\_madcorr

 $150.57 \quad test\_mask$ 

150.58 test\_max\_normal

- 150.59 test\_moments
- $150.60 \quad test\_moments\_fourier\_power$
- 150.61 test\_mtimes3x3
- 150.62 test\_noisy\_oscillator
- $150.63 \quad test\_nonperiodic\_pattern$
- 150.64 test\_normalizatation
- 150.65 test\_ols
- 150.66 test\_parcorr
- 150.67 test\_positivity\_preserving
- 150.68 test\_randar1

 $150.69 \quad test\_randar1\_multivariate$ 

150.70 test\_randar2

150.71 test\_ratio\_distributions

150.72 test\_sd\_rectwin

150.73 test\_spatialrnd

 $150.74 \quad test\_spectrum\_additivity$ 

150.75 test\_stationarity

150.76 test\_stationarity2

150.77 test\_sum\_ij

150.78 test\_sum\_multivar

150.79 test\_trifilt1

150.80 test\_wautocorr

150.81 test\_wavelet\_transform

150.82 test\_whittle

150.83 test\_window

 $150.84 \quad test\_wordfilt$ 

150.85 test\_xar1\_mid\_term

# 151 mathematics

mathematical functions of various kind

# 151.1 trapezoidal\_fixed

## 152 wavelet

### 152.1 continuous\_wavelet\_transform

continuous wavelet transform
follows "The Illustrated Wavelet Transform Handbook: Introductory
 Theory and ..."

#### 152.2 cwt\_man

continuous fourier transform as of time of implmentation, the matlab interal cwt is affected by serious round-off errors and has issues with the scaling, which is not the case here

### 152.3 cwt\_man2

# 152.4 example\_wavelets

## 152.5 phasewrap

wrap the phase to +/- pi

### 152.6 test\_cwt\_man

## 152.7 test\_phasewrap

### 152.8 test\_wavelet

### 152.9 test\_wavelet2

## 152.10 test\_wavelet\_analysis

### 152.11 test\_wavelet\_reconstruct

### 152.12 test\_wtc

### 152.13 wavelet

wavelet windows

### 152.14 wavelet\_reconstruct

iverses wavelet transform for single frequency (reconstruction of time series) n: window lengths in multiples of filter period 1/f0

### 152.15 wavelet\_transform

wavelet transform for single frequency n: window lengths in multiples of filter period 1/f0