

Manual for Package: mesh

Revision 8M

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1 @Mesh

1.1 Mesh

1.2 match_boundary_condition

match user specified boundary conditions (as line) with
boundary of discretized computational domain
 $p \cdot \phi + (1-p) \cdot d/db \phi = rhs$

2 @StructuredMesh

2.1 StructuredMesh

structured mesh processing
compatible with Delft3D
also provides set-up of discretisation matrices

2.2 `apply_boundary_condition`

apply boundary condition and the four sides of the domain
TODO: allow for interior boudaries

2.3 `bc_from_shp`

read boundary condition from shape file

2.4 `bc_index`

TODO this is deprecated
generate indices for boundary edges

2.5 `bc_isinvalid`

check boundary conditions for stacked domains

2.6 `block`

stack multiple meshes to complex domain

2.7 `boundary_chain`

return chain of boundary points

2.8 `boundary_direction`

return direction of boundary segment

2.9 `boundary_indices`

indices of boundary segments
id : index of boundary point
jd : index of

2.10 cat

2.11 centreline

domain (channel) centreline along chosen dimension

2.12 child

hierarchical mesh generation (for bifurcations)

2.13 copy

2.14 corner_indices

indices of domain corners

2.15 cut_from_domain

cut subdomain

2.16 export_delft3d_bnd

export the boundary in delft3d compatible format

2.17 export_delft3d_dep

export bathymetry data in Delft3D dep-format

2.18 export_delft3d_grd

export mesh in deltares delft3D grd file format

2.19 export_delft3d_ini

export delft3D compatible initial condition file

2.20 export_delft3d_inisedthick

export initial sediment_thickness file for Delft3D4

2.21 export_delft3d_rgh

```
export roughness bathymetry data in Delft3D dep-format
if (nargin() > 2)
    Z = [Z(:,1),Z];
    Z = [Z,Z(:,1)];
    Z = [Z(1,:);Z];
    Z = Z';
```

2.22 export_delft3d_sdb

2.23 export_shp

export mesh elements as shape file

2.24 extend_straight_reach

2.25 extract_elements

element indices from grid

2.26 flip_dimension

flip left and right or top and down

2.27 from_1d_mesh

convert a 1D mesh to 2D mesh consisting of quadrilaterals

2.28 generate_bifurcation

creates a mesh for bifurcation with bluff, which is required for
delft3d grids
TODO do not fix indices
TODO determine p individually
bank : bankline shapefile
nn : number of points across branches
ds: spacing along s
p : fraction of right side branch
level : generate hierarchical mesh,
 grid points in each branch will be 2^{n+1} ,
 and sub meshes until level 1 will be generated

for lower levels the connecting volumes remain narrow,
as the two volumes left and right of the division line are not
scaled
-> post smoothing required

nn: n=6; for idx=1:5; n(end+1) = 2*(n(end)-3)+3, end
ns: n=18; for idx=1:5; n(end+1) = 2*(n(end)-2)+2, end (should be
improved to $2*(n-1)+1$

2.29 generate_delft3d

2.30 generate_disk

generate semicircular domain
R1 : inner diameter
R2 : outer diameter
Theta(1) : start angle

Theta(2) : end angle
n(1) : along channel number of points
n(2) : across channel number of points

2.31 generate_from_centreline

generate a mesh from a given centreline
TODO : avoid crossing of inner bed points in sharp bends

2.32 generate_meander_bend

2.33 generate_rectangle

discretize a rectangular domain

2.34 generate_structured_grid

generate a structured mesh consisting of several sub-meshes

2.35 generate_tidal_funnel

2.36 grid_block

mesh a subdomain

2.37 improve

improve (smooth) the mesh

2.38 interp_elem2point

interpolate values sampled at element centres to element corners
TODO allow also interpolation to u and v points

2.39 mesh_polygon

mesh a 1D channel, where boundaries are given as polygon
TODO, this should better use voronoi-tesselation (see centreline
class)

2.40 orthogonality

orthogonality of elements, computed at edges

2.41 orthogonalize

orthogonalize mesh
set x of point coordinates to 1/2

2.42 plot

plot the mesh

2.43 plot_boundary

plot the mesh boundary

2.44 plot_coupling

plot connected vertices, see vertex_connection_matrix.m

2.45 plot_orthogonality

plot mesh with edges colored by orthogonality condition

2.46 quiver

quiver plot of velocity

2.47 read_delft3d_dep

depth in dat file is defined at volume centres (water level point)
first row, first column and last column are buffer
but last column is not (only when outflow?)

2.48 read_delft3d_grd

read mesh in delft3D grd format

2.49 refine

2.50 regenerate

2.51 scale_channel_width

2.52 smooth_cubic

cubically smooth the mesh coordinates

2.53 smooth_curvilinear

```
smooth the mesh
relax = (10+relax)/11;
relax = min(0.5,relax);
```

2.54 smooth_laplacian

```
smooth the mesh coordinates
```

```
better than before, but causes dn in inner bends to be narrower
    than in outer bends
(straightens the lines)
better smooth p: i.e. fractional distance from left to right,
this is complicated at the bif
better: two neighbour smooth: smooth dn and ds with left/right, top
    bottom only
```

2.55 smooth_simple

```
smooth the mesh coordinates
```

2.56 smooth_sn

```
smooth the mesh coordinates
```

2.57 snap

```
snap two meshes that connect at their domain boundaries
```

2.58 statistic

```
compute mesh statistics
```

2.59 to_UnstructuredMesh

convert to unstructured mesh

2.60 transpose_dimension

transpose dimensions

2.61 vertex_connection_matrix

connectivity of neighbouring vertices
TODO same for elements

3 @UnstructuredMesh

3.1 UnstructuredMesh

class containing some meshing functionality
complementary to Mesh_2d, Mesh_3d, Tree_2d and Tree_3d

3.2 add_element

add an element with vertex indices, vertices already exist

3.3 add_vertex

add a vertex

3.4 angle

interior angles of each element

3.5 `apply_boundary_condition`

3.6 `apply_boundary_condition_hermite`

3.7 `assemble_2d_dphi_dphi_hermite`

3.8 `assemble_2d_dphi_dphi_lagrange`

3.9 `assemble_2d_dphi_dphi_morley`

3.10 `assemble_2d_dphidn_phi_hermite`

3.11 `assemble_2d_dphidn_phi_lagrange`

3.12 `assign_1d`

assign coordinates (x_0, y_0) to containing element
TODO this can fail, if triangulation is not delaunay

3.13 `assign_2d`

assign coordinates (x_0, y_0) to containing element

3.14 assign_3d

assign coordinates (P0,y0) to containing element

3.15 associate_boundary

3.16 bnd_1d

left and right end points for 1D meshes

3.17 boundary_1d

convert 1D mesh to 2D mesh

3.18 boundary_chain2

get chained indices of boundary segments,
used for setting up higher order polynomials along the boundary

3.19 boundary_length_and_direction

edge length and direction of boundary segments
TODO, this should be just edge length and direction

3.20 cat

concatenate two meshes

3.21 chain_1d

chain 1D elements (segments)

3.22 `check_duplicate_elements`

check if elements are duplicate elements
TODO, this does not check if elements cover each other, for example
hierarchical meshes or ABC+BCD and ABD+ACD
TODO check overlap by computation of area

3.23 `check_edge_intersection`

3.24 `clip`

clip mesh to polygonal domain
TODO only works for triangles

3.25 `compute_elem2elem`

set up element2element neighbourhood relation

3.26 `connect_1d_2d`

auto merge 1d and 2d mesh
this silently requires that 1d segments consist at least of 3
elements
TODO only implemented for triangles

3.27 `convert_2d_to_1d`

3.28 `copy`

copy constructor

3.29 cross_section

get cross-sections for 1D elements

3.30 delete_element

delete an element

3.31 derivative_matrices

3.32 derivative_matrices_1d

first order first derivative discretisation matrix on the 1d mesh

3.33 derivative_matrices_2d

first order first derivative discretisation matrix on the mesh

3.34 derivative_matrix_2d_2

second order derivative matrix on a triangulation

3.35 derivative_matrix_2d_hermite

3.36 derivative_matrix_3d

first order first derivative discretisation matrix on the mesh

3.37 distance

distance along edges from a point set to all other points

open : id of start point(s)
countflag : if set use number of hops as distance not the euclidean
distance

3.38 dual_mesh

dual mesh formed by the centre of circumference
the dual mesh consists not only of triangles
TODO rename in generate dual mesh

3.39 edge_direction

3.40 edge_length

euclidean edge length

3.41 edge_midpoint

edge mid-points

3.42 edges_from_elements

edges and boundaries from elements

3.43 eigs

eigenvalues of the lapalcian on the mesh

3.44 elem2edge_

pointer of element to edge

3.45 elem2elem_matrix

matrix with neighbourhood relations for each element

3.46 element_area

area of elements
1d elements have zero area and are not processed

3.47 element_centroid

centroids of elements

3.48 element_midpoint

barymetric centre of elements

3.49 elements_from_edges

2D elements from edges

3.50 eval2pval

element (centroid) value to vertex value
TODO, use dual mesh or triangulation

3.51 export_delft3d_net

export into DFLOWFM delft3d net.nc file

3.52 export_msh

export mesh in GMSH msh format

3.53 export_pos

export triangles and vertex values to gmsh pos-file format (x,y,z,
val)
intended for re-meshing with values representing local mesh size

3.54 export_shp

export edges to GIS shapefile
each element as separate polygon with one z-value

3.55 facing_element

get triangle ndx that is opposit, e.g. "facing" the vertex vdx of
triangle tdx

3.56 filter_neighbour

apply a function on the values on connected vertices

3.57 find_encroached_edges

find encroached edges in a triangulation,
i.e. edges for which on of the two facing point false into their
enclosing
circle

3.58 flip

```
flip edges between two triangles
  flip
  for each side
    if (connection between opposit points shorter than
        between edges, swap edge)
      this-> flip
      that-> flip
  end
```

3.59 flip_global

```
recursively flip edges, i.e ABC+BCD -> ABD+ADC,
when new edge (diagonal) is shorter
TODO this is buggy, it cannot be always swapped, only if abcd is
convex!
```

3.60 flip_quality

```
flip edges, when mesh quality constraint improves
```

3.61 gaussmat_2d

```
matrix for gauss integration on a triangulation
```

3.62 generate_chews_first

```
triangulate domain with chew's first algorithm
```

3.63 generate_from_centrelines

```
generate a mesh from centrelines
```

3.64 generate_from_centreline_2d

generate mesh from centreline
TODO allow number of segments to change

sets up a simple quadrilateral mesh in S-N coordinates
centreline (must be sorted in streamwise direction)
input variables:
cS : S (streamwise) coordinates of centreline
cL : N (spanwise) coordinate of left bank
cR : N (spanwise) coordinate of right bank
input variables controlling output resolution:
S : S coordinate of slices in S-direction (diff(S) is element
width)
must be sorted in s-direction
n : n number of points per cross section
(n-1) is number of elements per cross section
output variables:
mesh.{X,Y,S,N} : point coordinates
mesh.T : point indices of elements (corners of the
quadrilaterals)
-> make it orthogonal to banks by using a spline along n

3.65 generate_frontal

3.66 generate_ghost_elements

generate ghost elements, i.e. elements at the domain boundary,
these
elements can overlap

when the project flag set, ghost points are projected to the
boundary,
the project flag is set for dual mesh generation
the project flag is unset for application of the boundary condition

3.67 generate_gmsh

generate a mesh from a polygon using gmsh

`inshp` : file name of shape file of preloaded shape file
containing a polygon
`obase` : base of output file name
`resolution` : struct containing default mesh resolution settings
`resfile_C` : file names of shape files, defining local resolution in
polygonal regions
`opt` : options, see below

this is a Static function

3.68 `generate_hierarchical`

generate a hierachical mesh by recursively splitting elements
containing boundary points

3.69 `generate_triangle`

generate a mesh from a polygon using the programme "Triangle"

3.70 `generate_uniform_1d`

generate a uniformly spaced 1D mesh

3.71 `generate_uniform_quadrilateral`

generate a uniform 2D mesh

3.72 `generate_uniform_tetra`

uniformly tessellate a rhombic domain in 3D into tetrahedra

3.73 `generate_uniform_triangulation`

uniformly tessellate a rectangular (2d) domain into triangles

3.74 `get_facing_and_shared_vertices`

for a pairwise list (array) of triangles, determine there common
and facing edges

3.75 `grid2tri`

topologically split a uniform mesh on a rectangular domain into
triangles

3.76 `import_delft3d_net`

import mesh from Delft3d file ({filename}_net.nc)

3.77 `import_msh`

import mesh from {filename}.msh files as generated by GSMH

3.78 `import_triangle`

import a mesh generated with triangle (ele and node)

3.79 `improve_iterative_relocate_insert`

iteratively improve the mesh by inserting vertices and smoothing
fprintf('Iteration %d, %d elements, %d vertices, %d
obtuse elements (%g%%)\n', iter, obj.nelem, obj.np
, nobtuse, nobtuse./obj.nelem);

3.80 `improve_iterative_relocate_uniform`

improve mesh by smoothing following by uniform refinement
fprintf('Iteration %d, %d elements, %d vertices, %d
obtuse elements (%g%%)\n', iter, obj.nelem, obj.np
, nobtuse, nobtuse./obj.nelem);

3.81 improve_relocate_global1

iteratively improve angles to remove obtuse triangles

3.82 improve_relocate_global2

improve mesh globally

3.83 improve_relocate_global_3

improve mesh quality globally

3.84 improve_relocate_local

iteratively improve angles to remove obtuse triangles

3.85 improve_relocate_local_old

iteratively improve angles to remove obtuse triangles

3.86 improve_topology

improve mesh topology

3.87 insert_mid_points

insert mid points into the mesh
the new mesh is of much lower quality, but if all edges are flipped
,
this leads to the $\sqrt{2}$ refinement

3.88 insert_steiner_points

refine mesh by inserting steiner points (centre of circumference)
for elements specified by tdx

3.89 integrate_1d

integrate a quantity val across the mesh

3.90 integrate_discharge

integrate discharge

3.91 interp_1d

interpolate on a 1D mesh

3.92 interp_2d

interpolate on a 2D mesh

3.93 interp_fourier

interpolate values on the mesh using fourier methods

3.94 interp_tikhonov_1d

interpolation with Tikhonov regularisation

3.95 interp_tikhonov_2d

interpolation with Tikhonov regularisation in 2D

3.96 `interp_tikhonov_3d`

3.97 `interpolate_from_boundary`

interpolate interior values from the boundary

3.98 `interpolate_point`

interpolate from samples to mesh points by IDW method

3.99 `interpolation_error_1d`

estimate interpolation error in 1D

3.100 `interpolation_error_2d`

interpolate error in 2D

3.101 `interpolation_error_3d`

estimate interpolation error in 3D

3.102 `interpolation_matrix_1d`

linear interpolation matrix from mesh points to arbitrary
coordinates P0

3.103 `interpolation_matrix_2d`

3.104 interpolation_matrix_3d

interpolation matrix for interpolation in 3D

3.105 isacute

determine acute triangles

3.106 isobtuse

determine obtuse triangles

3.107 iterate_smooth2

iteratively improve the mesh by smoothing

3.108 limit_by_distance

max edge length
minimum distance
TODO, this will always be zero

3.109 make_elements_ccw

make all 2D elements clock wise (such that their area is positive)

3.110 merge_duplicate_points

merge duplicate points

3.111 merge_facing_blunt_triangles

merge blunt triangles that face each other

3.112 mesh1

mesh in 1D

3.113 mesh_1d

extract the 1d mesh

3.114 mesh_2d

extract the 1d mesh

3.115 mesh_junctions

mesh junctions of a channel network
hold on

3.116 nearest_boundary

determine nearest boundary segment for each input coordinate

3.117 nedge_

3.118 nonobtuse_refinement

nonobtuse refinement according to Korotov
not feasible for most obtuse triangles

3.119 objective_A

one objective function value per angle

3.120 objective_T

wrapper for mesh optimisation objective functions univariate in triangles

3.121 objective_angle

objective function for iterative angle improvement

3.122 optimum_angle

optimum angle for each vertex = $360^\circ / \text{number of connected edges}$

3.123 orthogonality_quadrilaterals

orthogonality condition for quadrilaterals

3.124 path

path along edges

3.125 plot

plot the mesh (and a discretised function) as a surface and net

3.126 plot1d

plot 1D mesh

3.127 plot3

plot mesh and values

3.128 plotcs

plot cross section

3.129 project_to_boundary

project a point to the boundary

3.130 pval2eval

vertex to element value

3.131 quad2tri

quadrilaterals to triangles

3.132 quiver

3.133 raster_boundary

3.134 recover_edges

recover (boundary) edges

3.135 refine

refine by splitting marked triangles

3.136 refine_edge_halving

mesh refinement by longest edge bisection

3.137 remove_empty_triangles

remove degenerated triangles with zero area

3.138 remove_isolated_vertices

remove points that are not part of the mesh
(gmsh leaves sometimes spurious points in the msh file)

3.139 remove_points

remove points and associated elements

3.140 remove_quartered_triangles

point has connectivity 4 and is not on the boundary

3.141 remove_small_islands

delft3D requires islands to have at least 7 edges
this functions splits edges surrounding small islands

3.142 remove_triply_connected_boundary_vertices

remove boundary vertices that are connected only to three vertices

3.143 remove_trisected_triangles

remove trisected triangles
point has connectivity 3 and is not on the boundary

3.144 `renumber_point_indices`

`renumber vertex indices`

3.145 `resolve_8_vertices`

improve mesh by removing one edge from vertices with 8-edges
(an interior vertex in a regular triangulation has 6 neighbours,
and unstructured meshes with local refinement are possible with
5 and 7 neighbours, 4,3, or 8 and more connected vertices are not
necessary)

3.146 `restore_acuteness`

restore acuteness
Laplacian smoothing may at some places decrease the mesh quality,
this locally restores acute elements

3.147 `retriangulate`

`retriangulate the mesh`

3.148 `ruppert`

`refine the mesh using ruppert's algorithm`

3.149 `scale_to_boundary`

`scale hierarchical mesh to match boundary coordinates`
`experimental`

3.150 `scatterplot`

`scatterplot of data on mesh`

3.151 section

3.152 segment

segment the mesh into parts according to laplacian eigenvalues

3.153 smooth2

Laplacian smoothing of vertex coordinates,
replace every point by the average coordinate of its neighbours

3.154 smooth_1d

smoothes values in each reach
does not smooth the values at the connection points

3.155 smooth_val

smooth values on the mesh
TODO allow for smoothing boundary only along boundary

3.156 smoothness

mesh smoothness as ratio of maximum edge length and minimum edge
length

3.157 split3

split those triangles that contain a boundary point in three pieces
,
for hierarchical mesh generation

3.158 split_edge

split an edge

3.159 split_edge_perpendicular

split edge perpendicularly

3.160 split_elem_1d

split a 1d element

3.161 split_encroached_edges

recursively split encroached edges

3.162 split_obtuse

split obtuse elements

3.163 split_unsmooth_edges

split unsmooth edges

3.164 statistics

compute mesh statistics

3.165 streamwise_derivative_matrix

streamwise derivative matrix

3.166 thalweg

thalweg (deepest point along channel)

3.167 to_single

TODO, also with indices

3.168 uncross_elements

make sure, that 4 point elements span an area, and do not form a
cross
a call to this function should be succeeded by make_ccw
this operator is idempotent

3.169 uncross_quadrilaterals

make sure, that 4 point elements span an area, and do not form a
cross
a call to this function should be succeeded by make_ccw
this operator is idempotent

3.170 vertex_distance

connectivity of directly connected vertices

3.171 vertex_to_edge

connectivity matrix between vertices and adjacent edges

3.172 vertex_to_element

connectivity matrix between vertices and elements

3.173 vertex_to_vertex

connectivity matrix between vertices

3.174 vertices_1d

3.175 weighed_laplacian_smoothing

weighed Laplacian smoothing

3.176 xy2xys

for boundary points: convert XY coordinate into a 1Dparametric
coordinate,
applied in mesh optimization, where movement of boundary points is
constrained on the boundary

3.177 xys2xy

convert parametric 1D coordinate of boundary point back to
cartesian XYc oordinate

4 mesh

mesh generation, manipulation, analysis, refinement and optimization

4.1 add_to_rhs

4.2 append2buffer_asym

4.3 `append2buffer_dphi_dphi`

4.4 `dxlr2ak`

5 `grid/@Grid1`

5.1 `Grid1`

`lump` spatiotemporal data into a 1-dimensional grid

5.2 `binop`

operate function `fun` on data `val` within the context of a grid cell
(for fitting grid cell values from sampled values)

5.3 `build_index`

compute the grid-cell index for samples sampled at points `X1`

`name` : name of the index field

`X1` : coordinate of source points

`R` : cut off radius (if not supplied ident to mesh width)

5.4 `fit`

`lump` (fit) sampled values into the corresponding grid cell

5.5 `predict`

interpolate from lumped data to specified location

6 grid/@Grid2

6.1 Grid2

lump spatiotemporal data into a 2-dimensional grid

6.2 binop

operate function fun on data val within the context of a grid cell
(for fitting grid cell values from sampled values)

6.3 build_index

compute the grid-cell index for samples sampled at points X1
X1 : coordinate along first dimension
X2 : coordinate along second dimension

6.4 plot

6.5 predict

interpolate from lumped data to specified location

7 grid/@Grid3

7.1 Grid3

lump spatiotemporal data into a 3-dimensional grid

7.2 build_index

compute the grid-cell index for samples sampled at points X1
X1 : coordinate along first dimension
X2 : coordinate along second dimension
X3 : coordinate along third dimension

8 mesh1d

8.1 dxspace

8.2 dxspace2

8.3 dzmesh

8.4 mesh1

8.5 mesh1d

8.6 nlogstep

9 mesh

mesh generation, manipulation, analysis, refinement and optimization

9.1 nxfun

10 optimization

10.1 `improve_smooth_insert`

10.2 `objective0_angle1_barycentric`

10.3 `objective0_angle2_barycentric`

10.4 `objective0_angle2_barycentric9`

10.5 `objective0_angle_2_cartesian`

10.6 `objective0_angle_inf_cartesian`

10.7 `objective0_barycentric9`

10.8 `objective0_pythagoras1_barycentric9`

10.9 `objective0_pythagoras1_cartesian`

10.10 objective0_pythagoras2_barycentric9

10.11 objective0_pythagoras2_cartesian

10.12 objective_3_angle

10.13 objective_A_bnd

10.14 objective_P_angle

10.15 objective_P_angle_scaled

10.16 objective_P_angle_scaled_area

10.17 objective_P_midpoint

10.18 objective_angle

10.19 objective_angle2_barycentric

10.20 objective_angle_p

10.21 objective_angle_scaled_area

10.22 objective_angle_scaled_circumference

10.23 objective_cosa

10.24 objective_cosa_p

10.25 objective_cosa_scaled_side_length

10.26 objective_distance_edge_centre

10.27 objective_distance_edge_centre_perpendicular

10.28 objective_distance_orthocentre_excentre

10.29 objective_incentre_excentre

10.30 objective_length_min_max

10.31 objective_length_var

10.32 objective_thales

10.33 objective_thales_difference

10.34 test_objective_cosa_p

11 mesh

mesh generation, manipulation, analysis, refinement and optimization

11.1 plot_vtk

11.2 preload_msh

11.3 read_vtk

11.4 read_vtk2

% read header %%%

12 sparsemesh/@SparseMesh1

12.1 SparseMesh1

lump time series of sampled spatial data in one dimension (
projected)

12.2 assign

assign (lump) data "v0" sampled at sample times/location to field "
field"

12.3 assignS

lump sequentially sampled data "v0" and assign to field "field"

12.4 init

initialize, segment sampling locations/times into blocks the
sampled
data is lumped to

12.5 interp

interpolate data stored in field "field" to coordinates Xi
ignore invalid data
TODO, check if convex

12.6 interpS

interpolate data stored in field "field" to coordinates Xi,
do not ignore invalid data

12.7 rmse_interp

interpolation part of the error :
 $e \sim 1/2 * d^2 v / dx^2 * dx^2 + \text{higher order terms}$
 $\sim 1/2 * d^2 v$
the other part of the error is the sampling error (gaussian noise)

the mesh is optimal, when $e_{\text{nois}} \sim e_{\text{interp}}$

13 sparsemesh/@SparseMesh2

13.1 SparseMesh2

lump time series of sampled spatial data (track recordings) along
two dimensions,
e.g 1 projected spatial dimension and one for time
TODO : better blocks (all neighbours within mahalanobis distance)
TODO : do not use simple mean, but allow for least squares
regression
TODO : precompute the least squares weights for accummarray

13.2 assign

assign (lump) data "v0" sampled at sample times/location to field "
field"

13.3 assignS

lump sequentially sampled data "v0" and assign to field "field"

13.4 init

initialize, segment sampling locations/times into blocks the
sampled
data is lumped to

13.5 interp

interpolate data stored in field "field" to coordinates Xi
ignore data outside of the domain (convex interpolation)

13.6 interpS

interpolate data stored in field "field" to coordinates Xi,
extrapolate beyond domain

13.7 rmse_interp

interpolation part of the error :
$$e \sim \frac{1}{2} d^2 v / dx^2 * dx^2 + \text{higher order terms}$$
$$\sim \frac{1}{2} d^2 v$$
the other part of the error is the sampling error (gaussian noise)

the mesh is optimal, when $e_{\text{nois}} \sim e_{\text{interp}}$

TODO this is $e \sim f'$, not f''

14 sparsemesh

lumping and interpolation of spatio-temporal data into a "mesh" that
is spaced
optimally for the local density of sample points

allows for processing of large data sets with lower memory
consumption and run time

intended for ADCP data processing

Overcomes the limitation of gridding, where some grid cells can have
an insufficient
number of samples

14.1 SparseMesh

SparseMesh superclass

15 mesh

mesh generation, manipulation, analysis, refinement and optimization

15.1 stepnumber_smesh

16 test

16.1 test_MMesh_segment

16.2 test_derivative_matrix_curvilinear_2

17 mesh

mesh generation, manipulation, analysis, refinement and optimization

17.1 test_nxfun

17.2 tidal_funnel_idealized

17.3 trimesh_fast