

# Manual for Package: open-channel-flow

## Revision 1:4M

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October 29, 2019

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## 1 @Backwater1D

### 1.1 Backwater1D

solve the gradually varied flow equation (backwater equation)  
in one dimension

c.f. Chow, Bresse

### 1.2 backwater\_approximation

approximation of the backwater curve by an exponential function  
note: this is not necessarily a good approximation  
in the case of tide, Qt can be given

### 1.3 backwater\_curve\_iterative

analytic solution of the gradually varied flow equation  
c.f. Bresse, Chow

## 1.4 backwater\_length

backwater length

## 1.5 dh\_dx

change of depth along channel for the backwater equation  
beta : momentum coefficient  
this is effectively an equation in  $h^3$

## 1.6 dzs\_dx

change of surface elevation along channel

## 1.7 gvf\_x\_chow

analytical solution to the gradually varied flow equation (  
backwater equation)  
c.f. Chow, Bresse

## 1.8 invert

determine bed level from surface elevation  
(inverse backwater equation)  
this is ill conditioned, as the surface is smooth for subcritical  
flow,  
even if the bed is not smooth

C : chezy  
W : width  
Q : discharge  
S : bed slope  
y0 : surface elevation at outflow  
lateral inflow

## 1.9 solve

solve the gradually varied flow equation (backwater equation)  
C : chezy  
W : width  
Q : discharge  
S : bed slope  
y0 : surface elevation at outflow

## 1.10 solve\_analytic

analytical solution to the gradually varied flow equation (bresse  
method)  
 $u_{-}^{(n-m)}/(1-u_{-}^n)$

# 2 @Potential\_Flow

## 2.1 Potential\_Flow

numerical solution of the potential flow on a curvilinear grid  
(not necessarily curvilinear)

## 2.2 apply\_boundary\_potential\_old

## 2.3 assemble\_discretization\_matrix\_rectilinear

assemble the discretisation matrix

## 2.4 assemble\_potential\_matrix

assemble the discretisation matrix for potential flow

## 2.5 bc\_dirichlet

apply Dirichlet boundary conditions



## 2.6 boundary\_condition\_side\_outflow

```
apply boundary conditions for side outflow
p*phi + (1-p)*d/db phi = rhs
y : along channel coordinate
```

## 2.7 boundary\_condition\_side\_outflow\_1

```
apply boundary conditions
p*phi + (1-p)*d/db phi = rhs
```

## 2.8 contour

```
contour plot of the potential flow solution
```

## 2.9 cut\_boundary

```
cut the boundary from the domain
wa : width of inlet to side channel
wb : width of side channel
```

## 2.10 cut\_rectangle

```
cut a rectangle from the domain
TODO, this requires also an adaptation of the derivative matrices
-> step over to semi-unstructured mesh
```

## 2.11 infer\_bed\_level

```
note: this is pretty much a broken function for the inference of
stationary
morphology
```

Missing:

- rolling down of transverse slope to balance secondary flow in bends
- quasi time steippong

at stationary state:

- changes of discharge along the streamlines of discharge are balanced
- by a change in depth, to keep the velocity and sediment transport constant along the streamline

$$dz_b/dt = dq_s/dx + dq_s/dn = 0 \quad (i)$$

TODO this only true for infinite bends, as sediment can also move to the side

$$dq_s/ds = d/s(q/h) = 1/h dq/ds - q/h^2 dh/ds = 0$$

TODO this is only true in an infinite bend (ikeda)

$$dq_s/dn = 0$$

streamlines along discharge or velocity -> does not matter eq (i) is direction independent

## 2.12 infer\_bed\_level2

infer the bed level

## 2.13 infer\_bed\_level3

## 2.14 infer\_bed\_level\_loop

the bed level does not completely converge but starts to oscillate, this is presumably due to the non-compact kernel implementation of the laplacian operator

## 2.15 objective\_bed\_level

objective function for determining the bed level

## 2.16 old

## 2.17 plot

surface plot

## **2.18 quiver**

## **2.19 sediment\_transport**

compute the sediment transport

## **2.20 solve\_potential**

solve for the flow potential

## **2.21 streamline**

compute a streamline

## **2.22 surface\_elevation**

compute surface elevation according to Bernoulli's law

## **2.23 test**

## **2.24 velocity\_near\_bed**

determine the velocity near the bed

## **2.25 vertical\_velocity**

determine the vertical velocity from continuity

### 3 @Potential\_Flow\_Analytic

#### 3.1 Potential\_Flow\_Analytic

analytical solutions to various depth-averaged potential flow problems

#### 3.2 derive\_lateral\_outflow

derive potential flow solution to lateral outflow from an infinitely wide main channel

#### 3.3 derive\_lateral\_outflow\_finite\_width

derive coefficients for lateral outflow in the case of potential flow

#### 3.4 lateral\_outflow

potential flow solution to the case of lateral outflow from an infinitely wide channel

#### 3.5 lateral\_outflow\_finite\_width

analytical potential flow solution to lateral outflow from an infinitely wide channel

#### 3.6 streamline

numerically follow path along streamline by integrating the velocity

## 4 @SWE

### 4.1 SWE

Class to solve the (cross sectionally averaged) shallow water  
equation  
(st venant equation)

### 4.2 bc\_incoming\_non\_reflecting

set non-reflecting boundary condition for the 1D SWE

### 4.3 bc\_inflow

inflow boundary condition

### 4.4 bc\_inflow\_low\_pass

set low frequency Dirichlet, high frequency pass boundary condition

### 4.5 bc\_inflow\_non\_reflecting

set non-reflecting boundary condition

### 4.6 bc\_level

set surface level as Dirichlet boundary condition

### 4.7 bc\_level\_sommerfeld

set surface level as boundary condition by sommerfeld method

## 4.8 bc\_nonreflecting

set non-reflecting boundary condition  
extrapolate 0-order

## 4.9 bc\_reflecting

set reflecting boundary condition  
extrapolate 0-order and invert v

## 4.10 dot

time derivative  
(only for matlab internal ode-solver)  
TODO this is not swe specific  
continuity  
 $dA/dt + dQ/dx = I$   
  
momentum  
 $dQ/dt + d/dx(Qu + 1/2 gh^2) = gA(S_f - S_b)$   
 $S_b = dz_b/dx$   
 $S_f = \tau_x/\rho_w = C_f u|u|$

## 4.11 dt\_cfl

determine time step required by cfl

## 4.12 energy

determine total energy as sump of potential and kinetic energy  
this is preserved for fricitionless flows

## 4.13 flux

st venant's shallow water equation fluw

#### 4.14 flux\_lin

linearised st-venant equation

#### 4.15 fluxmateig

eigenvalues und vectors of the swe

#### 4.16 jacobian

Jacobian of the SWE

$$\frac{dq}{dt} + J \frac{dq}{dx} = \text{sourceterm}$$

note:  $\frac{d}{dx}(A*q) = J \frac{dq}{dx}$

#### 4.17 lindot

linearised SWE  
width variation not included, goes into rhs force term

$$\begin{bmatrix} 0, & 1 \\ -u^2+gH, & 2u \end{bmatrix} \begin{bmatrix} A \\ Q \end{bmatrix} = \begin{bmatrix} Q \\ [Q^2/A+1/2gA^2/w]_{dx} - 1/2gA^2/w^2 dw/dx \end{bmatrix}$$

force term

#### 4.18 roe\_average

roe average for the SWE

#### 4.19 solve\_analytic

linearised analytic solution of the swe

#### 4.20 solve\_stationary

stationary solution to the SWE

#### 4.21 source\_bed\_level

source term of the SWE caused by a change of the bed level

Note: this term causes splitting and averaging methods to fail to give accurate predictions of the smooth surface at steps of the bed

#### 4.22 source\_friction

friction source term of the SWE

#### 4.23 source\_width

source term (reaction term) for channels with variable width

#### 4.24 swe\_geometry

predefined functions to set up channel geometry

#### 4.25 swe\_ic

predefined functions of channel geometries

### 5 @SWE\_2d

#### 5.1 SWE\_2d

Dynamic solution of the shallow water equation (depth average, 2D)

#### 5.2 apply\_boundary\_condition\_stationary

apply boundary condition for stationary flow



### 5.3 assemble\_stationary

TODO, g should be replaced by gx,gy,gz, see chaudhri  
assemble discretisation matrix for stationary flow

### 5.4 solve\_stationary

solve SWE for stationary flow ( $dU/dt = dQ/dt = 0$ )

## 6 @Side\_Weir

### 6.1 Side\_Weir

side weir, analytical solution to (critical) lateral outflow

### 6.2 dzs\_dx

side weir, along channel surface gradient

### 6.3 surface\_elevation

along-channel surface elevation for (critical) lateral outflow over  
a side-weir

## 7 open-channel-flow

functions for open channel flow, sub modules:

```
@Backwater1D
    gradually varied flow in 1D (backwater)
@Potential_Flow
    depth averaged potential flow, numerical solution
@Potential_Flow_Analytic
    depth averaged potential flow, analytical solution
rating-curve
    empirical rating curves
@Side_Weir
```

analytical solution to lateral outflow over a side weir  
 @SWE  
 dynamical solution of the shallow water equation (saint-  
 venant-equation)  
 in 1D  
 @SWE\_2d  
 dynamical solution of the shallow water equation (saint-  
 venant-equation)  
 in 2D  
 velocity-profile  
 vertical and transverse velocity profiles of the streamwise  
 velocity

## 7.1 Potential\_Flow\_Map

wrapper to store precomputed streamlines of potential flows

## 7.2 chezy2manning

## 7.3 diffusion\_wave

propagation of a diffusion wave (flood wave), c.f. ponce  
 advection  
 diffusion  
 where is the bed slope?  
 friction slope  
 eddy slope  
 chow 1988  

$$d(A+A_0)/dt + dQ/dx = q$$

$$dQ/dt + d/dx \beta Q^2/A + gA(dh/dx + S_f + S_e) - \beta q_i v_i + W_f B = 0$$
 A0 ignored  
 inflow and wind shear ignored

## 7.4 friction\_slope

friction slope (surface slope) for uniform stationary flow

## 7.5 linear\_wave

linear wave routing (linearised kinematic wave)

## 7.6 manning2chezy

## 7.7 manning2drag

# 8 meander-bend/@Equilibrium\_Bend

## 8.1 Equilibrium\_Bend

Transverse profile of the bed level and bed material grain size in an equilibrium (infintely long) meander bend

## 8.2 bed\_profile

predict transverse bed profile of an equilibrium meander bend

## 8.3 bed\_profile\_uniform

transverse profile of the bed level of an equilibrium meander bend with uniform grain size

## 8.4 calibrate

calibrate bend geometry to given profile

## 8.5 dD\_dr

## 8.6 dh\_dr

across channel derivative of flow depth for a meandering river

## 8.7 dh\_dr\_uniform

transverse gradient of the bed level of an equilibrium meander bend  
for the case of uniform bed material

## 8.8 grain\_size\_profile

transverse (across channel) profile of the bed material grain size  
in a river meander

# 9 meander-bend

## 9.1 Kinoshita

```
% Public properties
% Public get properties
% Private properties
% Constructor
% Setters and getters
% generic methods
```

## 9.2 bend\_transverse\_velocity

transverse velocity profile in a meander bend

## 9.3 bend\_velocity\_near\_bed

near-bed-velocity in a meander bend

## 9.4 kinoshita\_

## 9.5 random\_meander

generate a pseudo random meander

## 9.6 test\_rozovskii

# 10 old

## 10.1 UniformFlow

# 11 rating-curve

## 11.1 ChezyRatingCurve

rating curve, Chezy formalism

## 11.2 DynamicKeuleganRC

Dynamic Rating Curve, Keulegan roughness formulation  
(dynamic = correction for hysteresis loop)

## 11.3 DynamicManningRC

Dynamic Rating Curve, Manning roughness formulation  
(dynamic = correction for hysteresis loop)

## 11.4 DynamicPowerRC

Dynamic Power Law Rating curve  
(dynamic = correction for hysteresis loop)

### 11.5 KeuleganRatingCurve

### 11.6 ManningRatingCurve

### 11.7 PolyRatingCurve

### 11.8 PowerRatingCurve

stationary rating curve, power law

### 11.9 PowerRatingCurveOffset

stationary rating curve, stage-discharge follows power law

### 11.10 RatingCurve

Fri Feb 13 10:02:52 CET 2015  
rating curve superclass

### 11.11 csarea

predict cross sectional area from transverse bed level profile  
and surface elevation

### 11.12 csdischarge

compute discharge

### 11.13 csperimeter

compute wetted perimeter

### 11.14 csradius

compute hydraulic radius of the cross section

### 11.15 cswidth

determine cross section width

### 11.16 test\_PowerRatingCurve

### 11.17 wfunc

determine channel width

## 12 open-channel-flow

functions for open channel flow, sub modules:

- @Backwater1D
  - gradually varied flow in 1D (backwater)
- @Potential\_Flow
  - depth averaged potential flow, numerical solution
- @Potential\_Flow\_Analytic
  - depth averaged potential flow, analytical solution
- rating-curve
  - empirical rating curves
- @Side\_Weir
  - analytical solution to lateral outflow over a side weir
- @SWE
  - dynamical solution of the shallow water equation (saint-venant-equation)
    - in 1D
- @SWE\_2d

dynamical solution of the shallow water equation (saint-  
venant-equation)  
in 2D  
velocity-profile  
vertical and transverse velocity profiles of the streamwise  
velocity

## 12.1 surface\_slope

surface slope for uniform stationary flow

## 12.2 sw\_reflection

reflection coefficients of shallow water waves at a sudden change  
of the  
cross section (sudden change of admittance)  
c.f. lighthill, ippen-harleman

## 12.3 sw\_reflection\_stepwise

time passes and phase shifts  
transmission and reflection coefficient depend on direction !  
iterative (recursive) reflection and transmission

## 12.4 test\_inverse\_backwater\_curve

## 12.5 test\_nse\_nz

# 13 uniform-stationary-flow

## 13.1 chezy2drag



## 13.2 critical\_flow\_depth

critical flow depth in uniform stationary flow

## 13.3 drag2chezy

convert drag coefficient to chezy coefficient  
 $g \frac{dz_s}{dx} + c_d w \frac{u^2}{h} = 0$  (swe formalism)  
-  $S + \frac{1}{C^2} \frac{U^2}{H} = 0$  (chezy formalism)

## 13.4 normal\_flow\_depth

normal flow depth for uniform stationary flow  
function  $H = \text{normal\_flow\_depth}(Q, W, C, S)$

## 13.5 normal\_flow\_depth\_

normal flow depth in uniform stationary flow

## 13.6 normal\_flow\_discharge

normal flow discharge for uniform stationary flow

## 13.7 normal\_flow\_slope

normal flow slope in uniform stationary flow

## 13.8 normal\_flow\_velocity

normal flow velocity in uniform stationary flow

## 14 velocity-profile/@Log\_profile

### 14.1 Log\_profile

logarithmic profile of the streamwise velocity

### 14.2 df\_dh

sensitivity of profile with respect to depth

### 14.3 df\_dh\_

sensitivity of profile with respect to depth

### 14.4 df\_dln\_z0

sensitivity of velocity profile with respect to roughness length

### 14.5 df\_dln\_z0\_

sensitivity of profile with respect to roughness length

### 14.6 profile

vertical profile of the streamwise velocity

### 14.7 profile\_

scale of velocity at instrument depth to depth average velocity  
roughness length and associated standard error can change in time,  
i.e. may be passed as vectors

zs : [1xn] water surface level  
zb : [1x1] bottom level  
za : [1xn] or [1x1]

level of velocity measurement,  
 i.e. level of HADCP beam bin centre, coincides with  
 instrument level,  
 if the HADCP is horizontally aligned  
 only needs to be passed as vector if instrument is  
 redeployed or  
 becomes misaligned  
 ln\_z0 : [1xn] or [1x1]  
 natural logarithm of the roughness length  
 s : [1xn] or [1x1]  
 standard error of ln\_z0  
 function [fz\_mu fz\_s fz\_sp fz\_bias fz\_eps] = log\_profile(zs,zb,za,  
 ln\_z0,s,sp,e)

## 14.8 profile\_bias

## 14.9 regmtx

regression matrix

## 14.10 ubar

depth averaged velocity

# 15 velocity-profile/@Log\_profile\_with\_bend\_correction

## 15.1 Log\_profile\_with\_bend\_correction

vertical velocity profile corrected for bend flow

## 15.2 df\_dc

sensitivity of the velocity profile with respect to the bend  
 correction  
 parameter c

### 15.3 df\_dc\_

### 15.4 du\_dz

### 15.5 fit

fit the vertical velocity profile

### 15.6 profile\_

vertical velocity profile

### 15.7 regmtx

regression matrix

### 15.8 u

streamwise velocity

### 15.9 u\_

streamwise velocity

## 16 velocity-profile/@Log\_profile\_with\_cubic\_wake

### 16.1 Log\_profile\_with\_cubic\_wake

log profile with cubic wake

## 16.2 df\_dc

sensitivity of profile with respect to wave parameter

## 16.3 df\_dc\_

sensitivity of profile with respect to wake parameter

## 16.4 profile\_

vertical velocity profile

## 16.5 regmtx

regression matrix

# 17 velocity-profile/@Log\_profile\_with\_dip

## 17.1 Log\_profile\_with\_dip

Logarithmic profile with dip

## 17.2 fit

fit the vertical velocity profile

# 18 velocity-profile/@Log\_profile\_with\_linear\_bend\_correction

## 18.1 Log\_profile\_with\_linear\_bend\_correction

log profile with linear bend correction

## 18.2 df\_dc

sensitivity of profile with respect to wake parameter

## 18.3 df\_dc\_

sensitivity of velocity profile with respect to wave parameter

## 18.4 du\_dz

velocity shear along vertical

## 18.5 profile\_

velocity profile

## 18.6 regmtx

regression matrix

# 19 velocity-profile/@Log\_profile\_with\_wake

## 19.1 Log\_profile\_with\_wake

logarithmic velocity profile with wake correction  
c.f. coles

## 19.2 df\_dc

sensitivity of profile with respect to wake parameter

## 19.3 df\_dc\_

sensitivity of velocity profile with respect to wake parameter

## 19.4 du\_dz

velocity shear

## 19.5 profile\_

predict velocity profile

## 19.6 regmtx

log law with wake

$$u = u_s/k \ln(z) - u_s/k \ln(z_0) + u_s/k (2/H^2 z - 3/H^3 z^2)$$

# 20 velocity-profile/@VP

## 20.1 VP

velocity profile

## 20.2 process\_joint

## 20.3 process\_transverse\_profile

process the transverse velocity profile

## 20.4 process\_vertical\_profile

predict vertical profile error distribution parameter for HADCP  
error estimate

## 20.5 profile\_prediction\_error

```
input :
U      : [nbin x nens]
        - values for each bin (or across section) and ensemble (or
          reference measurement)
        this are estimates estimates of the discharge or the cross
          sectional averaged
          velocity from the raw values
        - the profile should be limited to the effective profiling
          range,
          abobj 75-100m for a 600kHz ADCP

dn      : distance between HADCP bins
width   : cross section width

objput:
        sd_n : expected standard deviation for increasing profiling
              range
function [s_rel s_err s_dat rho res m2 u_pred fdx] =
        velocity_variation(U)
        hadcp_prediction_error
        TODO take scales and unscaled velocity to do combine with harmmean
          estimate
note: previous versions:
        residual was computed with respect to the predicted local
          velocity
        mse was not upscaled to cs, as profile was expected to cover
          entire cs
        finite width of cs was not considered
parametric estimate from moments, objliers should be filtered
        beforehand
Note that the median absolute deviation is not a good estimate,
because it may excludes rare events like reverse flow of floods
thus, the only acceptable more robust estimate would be mean
        absolute deviation
```

## 21 velocity-profile/@Vertical\_profile

### 21.1 Vertical\_profile

vertical profile of the streamwise velocity, superclass

### 21.2 fit



fit vertical velocity profile parameter

function obj = fit(obj,U,S,h,binmask)

### 21.3 u

predict velocity along the vertical based on profile

## 22 velocity-profile

### 22.1 fit\_displacement\_profile

fit the log profile to the vertical profile of the streamwise velocity

### 22.2 lateral\_division\_method

transverse (across channel) profile of the streamwise velocity  
in a straight channel  
numerical solution  
the eps seems incorrect, use better stationary\_1d\_swe

$$\begin{aligned}\rho g h S - \beta q^2 f / (8 h^2) + d/dy(\epsilon_{s_t} dq/dy) &= 0 \\ \rho g h S - \beta q^2 g / (C^2 h^2) + d/dy(\epsilon_{s_t} dq/dy) &= 0\end{aligned}$$

### 22.3 test\_law\_of\_the\_wall\_fit

### 22.4 transverse\_profile\_parameter

### 22.5 transverse\_velocity\_profile

transverse profile of the streamwise velocity  
c.f. shiono knight

## 22.6 transverse\_velocity\_profile\_olesen

transverse profile of the streamwise velocity in a meander bend

## 22.7 transverse\_velocity\_profile\_rozovskii

transversal velocity distribution in a bend  
Rososkii,  
as in the book central differences along the radius and euler  
forward in space  
are used, note that since the advent of the computer more advanced  
schemes  
could be used (see build in solvers)  
cfl condition is not explicitly checked  
Rosovsky assumes a constant water level, e.g. does not consider  
superelevation

$I_{\theta} = -1/r \, dz/d_{\theta}$  (p. 22)  
 $d_{\theta} = 1/R \, ds|_R$   
 $\Rightarrow I_{\theta} = -R/r \, dz/ds = -R/r \, I_0$   
It : (1.32) drop of level per unit angle, identical across section

## 22.8 transverse\_velocity\_profile\_shiono\_knight

transverse profile of the streamwise velocity, determined  
analytically  
by the method of shiono and knight  
shape of velocity profile only dependent on  $\lambda$ ,  $f$ ,  $H$ , not slope

## 22.9 transverse\_velocity\_profile\_with\_slope

stationary 1D shallow water equation across a river section  
 $0 = -g h S_0 - \tau_b/\rho + d/dn (nu h du/dn)$   
 $0 = -g h S_0 + g u^2/C^2 + d/dn (nu h du/dn)$   
includes tranverse gradient term

note that shiono/knight 1991 provide an `_analytic_` solution,  
which takes the form of an exponentially decaying side wall effect

## **22.10 vertical\_profile\_of\_velocity\_vriend**

vertical profile of the streamwise velocity, method of de vriend

## **22.11 vertical\_velocity\_profile**

vertical profile of the streamwise velocity in non-uniform flow

## **23 wrapper**

### **23.1 discharge2stage**

wrapper function

### **23.2 stage2discharge**