Manual for Package: open-channel-flow
Revision 11:12M

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Contents

1 @Backwater1D

1.1 Backwater1D

```
solve the gradually varied flow equation (backwater equation)
in one dimension

c.f. Chow, Bresse
```

1.2 backwater_approximation

```
approximation of the backwater curve by an exponential function
note: this is not necessarily a good approximation
in the case of tide, Qt can be given
```

1.3 backwater_curve_iterative

```
analytic solution of the gradually varied flow equation
c.f. Bresse, Chow
```

1.4 backwater_length

```
backwater length
```

1.5 dh_dx

```
change of depth along channel for the backwater equation
beta : momentum coefficient
this is effectively an equation in h^3
```

1.6 dh_dx_

1.7 dzs_dx

```
change of surface elevation along channel
```

1.8 gvf_x_chow

```
analytical solution to the gradually varied flow equation (
    backwater equation)
c.f. Chow, Bresse
```

1.9 invert

```
determine bed level from surface elevation
(inverse backwater equation)
this is ill conditioned, as the surface is smooth for subcritical
    flow,
```

```
even if the bed is not smoth

C : chezy
W : width
Q : discharge
S : bed slope
y0 : surface elevation at outflow
lateral inflow
```

1.10 solve

```
solve the gradually varied flow equation (backwater equation)
C : chezy
W : width
Q : discharge
S : bed slope
y0 : surface elevation at outflow
```

1.11 solve_analytic

```
 analytical solution to the gradually varied flow equation (bresse
     method)
u_.^(n-m)./(1-u_.^n)
```

1.12 solve_matrix

2 @Compound_Cross_Section

2.1 Compound_Cross_Section

2.2 area

2.3 discharge

2.4 roughness

3 @Cross_Section

3.1 Cross_Section

3.2 average_across_section

3.3 compute_discharge

3.4 compute_sediment_transport

3.5 expand

3.6 fit_bed_level

3.7 flat

3.8 grain_size

3.9 init

3.10 invalidate

3.11 parse_arguments

3.12 wetted_cross_section

3.13 wetted_width

4 bifurcations-and-weirs/@Lateral_Diversion_Finite_Width

4.1 Jb

4.2 Lateral_Diversion_Finite_Width

4.3 dR

4.4 derive

4.5 evalk

4.6 lateral_outflow_finite_width1

4.7 load_functions

4.8 stagnation_point

```
fdx    = isnan(x);
```

4.9 streamline

4.10 u_far

4.11 v_far

4.12 velocity

4.13 velocity_near_bed

5 bifurcations-and-weirs/@Lateral_Diversion_Finite_Width_Gradual

5.1 Jb

5.2 Lateral_Diversion_Finite_Width_Gradual

5.3 coefficients

5.4 condA

5.5 dR

5.6 derive

5.7 evalk

5.8 evalk_

5.9 lateral_outflow_finite_width1

5.10 load_functions

6 bifurcations-and-weirs/@Lateral_Diversion_Finite_Width_Gra

6.1 coefficients_old

7 bifurcations-and-weirs/@Lateral_Diversion_Finite_Width_Gra

7.1 stagnation_point

```
fdx   = isnan(x);
```

7.2 streamline

7.3 streamline_radius_of_curvature

7.4 u_far

7.5 uv1

7.6 uv_side_branch

7.7 v_far

7.8 velocity

7.9 velocity_linear

7.10 velocity_near_bed

7.11 xp

8 bifurcations-and-weirs/@Lateral_Diversion_Wide_Channel

8.1 Lateral_Diversion_Wide_Channel

8.2 derive_lateral_outflow

```
derive potential flow solution to lateral outlfow from an
    infinitely
wide main channel
```

8.3 derive_lateral_outflow_finite_width

```
derive coefficients for lateral outflow in the case of potential
    flow
```

8.4 load_functions

```
load analytical solutions for potential flow field at a lateral
    diversion
with an infinitely wide main channel
```

8.5 stagnation_point

8.6 streamline_radius_of_curvature

9 bifurcations-and-weirs/@Lateral_Diversion_Wide_Channel_Ma

9.1 Lateral_Diversion_Wide_Channel_Map

```
wrapper to store precomputed streamlines of potential flows
```

9.2 streamline

10 bifurcations-and-weirs/@Side_Weir

10.1 Side_Weir

```
side weir, analytical solution to (critical) lateral outflow
```

10.2 dzs_dx

```
side weir, along channel surface gradient
```

10.3 surface_elevation

```
along-channel surface elevation for (critical) lateral outflow over
     a side-weir
```

11 bifurcations-and-weirs

11.1 Lateral_Diversion_Finite_Width_Map

12 bifurcations-and-weirs/bifurcation-empirical

12.1 bifurcation_potential_flow_dividing_streamline_radius

12.2 sediment_division_herrero

12.3 sediment_division_meijer_ksiazek_1

12.4 sediment_division_meijer_ksiazek_2

12.5 sediment_division_raudkivi

12.6 sediment_division_van_der_mark

12.7 sediment_division_wang

13 open-channel-flow

```
functions for open channel flow, sub modules:

@Backwater1D
       gradually varied flow in 1D (backwater)
@Potential_Flow
       depth averaged potential flow, numerical solution
@Potential_Flow_Analytic
       depth averaged potential flow, analytical solution
rating-curve
       empirical rating curves
@Side_Weir
       analytical solution to lateral outflow over a side weir
@SWE
       dynamical solution of the shallow water equation (saint-
           venant-equation)
       in 1D
@SWE_2d
       dynamical solution of the shallow water equation (saint-
           venant-equation)
       in 2D
velocity-profile
       vertical and transverse velocity profiles of the streamwise
           velocity
```

13.1 cdf_hydrograph

13.2 derive_discharge_step_response

13.3 discharge2stage

13.4 eddy_diffusivity

13.5 eddy_viscosity_depth_averaged

13.6 hfilter

13.7 hydraulic_radius

13.8 inv_hydrograph

14 kinematik-and-diffusion-wave

14.1 diffusion_wave

```
propagation of a diffusion wave (flood wave), c.f. ponce
advection
diffusion
where is the bed slope?
friction slope
eddy slope
chow 1988
d(A+A0)/dt + dQ/dx = q
dQ/dt + d/dx betaQ^2/A + gA(dh/dx + Sf + Se) - beta q_i v_i + Wf B
    = 0
A0 ignored
inflow and wind shear ignored
```

14.2 flood_wave_diffusion_coefficient

14.3 linear_wave

```
linear wave routing (linearised kinematic wave)
```

15 meander-bend/@Equilibrium_Bend

15.1 Equilibrium_Bend

```
Transverse profile of the bed level and bed material grain size in
an equilibrium (infintely long) meander bend
```

15.2 Qs

15.3 bed_profile

```
predict transverse bed profile of an equilibrium meander bend
```

15.4 bed_profile_uniform

```
transverse profile of the bed level of an equilibrium meander bend
with uniform grain size
```

15.5 calibrate

```
calibrate bend geometry to given profile
```

15.6 dD_dr

15.7 dh_dr

```
across channel derivative of flow depth for a meandering river
```

15.8 dh_dr_uniform

```
transverse gradient of the bed level of an equilibrium meander bend
for the case of uniform bed material
```

15.9 grain_size_profile

```
transverse (across channel) profile of the bed material grain size
in a river meander
```

16 meander-bend

16.1 Kinoshita

```
% Public properties
% Public get properties
% Private properties
% Constructor
% Setters and getters
% generic methods
```

16.2 bend_transverse_velocity

```
transverse profile of the streamwise velocity in a meander bend
```

16.3 bend_velocity_near_bed

```
near-bed-velocity in a meander bend
```

16.4 kinoshita_

16.5 meander_bend_idealized

16.6 meander_centreline

16.7 random_meander

```
generate a pseudo random meander
```

16.8 secondary_velocity_profile_ikeda

16.9 test_rozovskii

16.10 transverse_slope_rozovskii

17 potential-flow/@Potential_Flow

17.1 Potential_Flow

```
numerical potential flow solver by various methods
analytic (series)
or FDM on non-orthogonal curvilinear grids
or FEM by unstructured meshes
```

17.2 contour

```
contour plot of the potential flow solution
```

17.3 infer_bed_level

```
note: this is pretty much a broken function for the inference of
    stationary
      morphology

Missing:
- rolling down of transverse slope to balance secondary flow in
    bends
```

```
- quasi time steippong

at stationary state:
- changes of discharge along the streamlines of discharge are
    balanced
  by a change in depth, to keep the velocity and sediment transport
       constant along the streamline

dz_b/dt = dqs/dx + dqs/dn = 0               (i)
TODO this only true for infinite bends, as sediment can also move
    to the side
dqs/ds = d/s(q/h) = 1/h dq/ds - q/h^2 dh/ds = 0
TODO this is only true in an ifinite bend (ikeda)
dqs/dn = 0
streamlines along discharge or velocity -> does not matter eq (i)
    is direction independent
```

17.4 infer_bed_level2

```
infer the bed level
```

17.5 infer_bed_level3

17.6 infer_bed_level_loop

```
the bed level does not completely converge but starts to oscillate,
this is presumably due to the non-compact kernel implementation of
    the laplacian oberator
```

17.7 objective_bed_level

```
objective function for determining the bed level
```

17.8 plot

```
surface plot
```

17.9 quiver

17.10 sediment_transport

```
compute the sediment transport
```

17.11 solve_potential

```
solve for the potential
```

17.12 streamline

```
compute a streamline
```

17.13 surface_elevation

```
compute surface elevation according to Bernoulli's law
note : this is likely very different from the true surface
    elevation,
      as streamline curvature causes a transverse pressure gradient
```

17.14 test_case

17.15 velocity_near_bed

```
determine the velocity near the bed
```

17.16 vertical_velocity

```
determine the vertical velocity by continuity
```

18 potential-flow/@Potential_Flow_Analytic

18.1 Potential_Flow_Analytic

```
analytical solutions to various depth-averaged potential flow
    problems
```

18.2 streamline

```
numerically follow path along streamline by integrating the
    velocity
```

19 potential-flow/@Potential_Flow_SM

19.1 Potential_Flow_SM

```
numerical solver for flow on a curvilinear grid (not necessarilly
    orthogonal)
by means of the Finite Difference Method
```

19.2 assemble_discretization_matrix_rectilinear

```
assemble the discretisation matrix
```

19.3 assemble_potential_matrix

```
assemble the discretisation matrix for potential flow
```

19.4 boundary_condition_side_outflow

```
apply boundary conditions for side outflow
p*phi + (1-p)*d/db phi = rhs
y : along channel coordinate
TODO, make this return the bc-struct
```

19.5 boundary_condition_side_outflow_1

```
apply boundary conditions
p*phi + (1-p)*d/db phi = rhs

TODO, make this return the bc-struct
```

19.6 cut_boundary

```
cut the boundary from the domain
wa : width of inlet to side channel
wb : width of side channel
```

19.7 cut_rectangle

```
cut a rectangle from the domain
TODO, this requires also an adaptation of the derivative matrices
     -> step over to semi-unstructured mesh
```

20 potential-flow/@Potential_Flow_UM

20.1 Potential_Flow_UM

```
numerical solver for flow on an unstructured mesh (triangulation)
by means of the Finite Element Method
```

20.2 assemble_potential_matrix

21 potential-flow

21.1 poisseuille_flow_rate

22 rating-curve

22.1 ChezyRatingCurve

```
rating curve, Chezy formalism
```

22.2 DynamicKeuleganRC

```
Dynamic Rating Curve, Keulegan roughness formulation
(dynamic = correction for hysteresis loop)
```

22.3 DynamicManningRC

```
Dynamic Rating Curve, Manning roughness formulation
(dynamic = correction for hysteresis loop)
```

22.4 DynamicPowerRC

```
Dynamic Power Law Rating curve
(dynamic = correction for hysteresis loop)
```

22.5 KeuleganRatingCurve

22.6 ManningRatingCurve

22.7 PolyRatingCurve

22.8 PowerRatingCurve

```
stationary rating curve, power law
```

22.9 PowerRatingCurveOffset

```
stationary rating curve, stage-discharge follows power law
```

22.10 RatingCurve

```
Fri Feb 13 10:02:52 CET 2015
rating curve superclass
```

22.11 csarea

```
predict cross sectional area from transverse bed level profile
and surface elevation
```

22.12 csdischarge

```
compute discharge
```

22.13 csperimeter

```
compute wetted perimeter
```

22.14 csradius

```
compute hydraulic radius of the cross section
```

22.15 cswidth

```
determine cross section width
```

22.16 test_PowerRatingCurve

22.17 wfunc

```
 determine channel width
```

23 open-channel-flow

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	    venant-equation)
	in 1D
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	dynamical solution of the shallow water equation (saint-
	    venant-equation)
	in 2D
velocity-profile
	vertical and transverse velocity profiles of the streamwise
	    velocity
```

23.1 residual_swe

24 shallow-water/@SWE

24.1 SWE

```
 Class to solve the (cross sectionally averaged) shallow water
     equation
 (st venant equation)
```

24.2 bc_incoming_non_reflecting

```
set non-reflecting boundary condition for the 1D SWE
```

24.3 bc_inflow

```
inflow boundary condition
```

24.4 bc_inflow_low_pass

```
set low frequency Dirichlet, high frequency pass boundary condition
```

24.5 bc_inflow_non_reflecting

```
set non-reflecting boundary condition
```

24.6 bc_level

```
set surface level as Dirichlet boundary condition
```

24.7 bc_level_sommerfeld

```
set surface level as boundary condition by sommerfeld method
```

24.8 bc_nonreflecting

```
set non-reflecting boundary condition
extrapolate 0-order
```

24.9 bc_reflecting

```
set reflecting boundary condition
extrapolate 0-order and invert v
```

24.10 dot

```
time derivative
(only for matlab internal ode-solver)
TODO this is not swe specific
continuity
dA/dt + dQ/dx = I

momentum
dQ/dt + d/dx( Qu + 1/2 gh^2) = gA(S_f - S_b)
S_b = dz_b/dx
S_f = tau_x/rho_w = C_f u|u|
```

24.11 dt_cfl

```
determine time step required by cfl
```

24.12 energy

```
determine total energy as sump of potential and kinetic energy
this is preserved for fricitionless flows
```

24.13 flux

```
st venant's shallow water equation fluw
```

24.14 flux_lin

```
linearised st-venant equation
```

24.15 fluxmateig

```
eigenvalues und vectors of the swe
```

24.16 jacobian

```
Jacobian of the SWE

dq/dt + J dq/dx = sourceterm
note: d/dx(A*q) = J dq/dx
```

24.17 lindot

```
linearised SWE
width variation not included, goes into rhs force term

[      0,  1] [A]   = [   Q]
[ -u^2+gH, 2u] [Q]_dx [Q^2/A+1/2gA^2/w]_dx - 1/2gA^2/w^2 dw/dx
                                             force term
```

24.18 roe_average

```
roe average for the SWE
```

24.19 solve_analytic

```
linearised analytic solution of the swe
```

24.20 solve_stationary

```
stationary solution to the SWE
```

24.21 source_bed_level

```
source term of the SWE caused by a change of the bed level

Note: this term causes splitting and averaging methods to fail to
     give accurate predictions of the smooth surface at steps of
         the bed
```

24.22 source_friction

```
friction source term of the SWE
```

24.23 source_width

```
source term (reaction term) for channels with variable width
```

24.24 swe_geometry

```
predefined functions to set up channel geometry
```

24.25 swe_ic

```
predefined functions of channel geometries
```

25 shallow-water/@SWE_2d

25.1 SWE_2d

```
Dynamic solution of the shallow water equation (depth average, 2D)
```

25.2 apply_boundary_condition_stationary

```
apply boundary condition for stationary flow
```

25.3 assemble_stationary

```
TODO, g should be replaced by gx,gy,gz, see chaudhri
assemble discretisation matrix for stationary flow
```

25.4 solve_stationary

```
solve SWE for statinary flow (dU/dt = dQ/dt = 0)
```

26 shallow-water

26.1 sw_reflection

```
reflection coefficients of shallow water waves at a sudden change
    of the
cross section (sudden change of admittance)
c.f. lighthill, ippen-harleman
```

26.2 sw_reflection_stepwise

```
time passes and phase shifts
transmission and reflection coefficient depend on direction !
iterative (recursive) reflection and transmission
```

27 open-channel-flow

```
functions for open channel flow, sub modules:

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           venant-equation)
       in 2D
velocity-profile
       vertical and transverse velocity profiles of the streamwise
           velocity
```

27.1 stage2discharge

28 test/test_Backwater1D

28.1 test_bw1d_solve_matrix

29 test

29.1 test_inverse_backwater_curve

29.2 test_normal_flow

29.3 test_nse_nz

30 open-channel-flow

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functions for open channel flow, sub modules:

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           venant-equation)
       in 2D
velocity-profile
       vertical and transverse velocity profiles of the streamwise
           velocity
```

30.1 test_hydrograph

31 turbulence

31.1 boundary_layer_height

31.2 kolmogorov_length

31.3 kolmogorov_time

31.4 kolmogorov_velocity

32 uniform-stationary-flow

32.1 chezy2drag

32.2 chezy2f

32.3 chezy2manning

```
convert chezy to manning
```

32.4 chezy2z0

32.5 critical_flow_depth

```
critical flow depth in uniform stationary flow
```

32.6 discharge_step_response

```
Q(:) = 0;
```

32.7 drag2chezy

```
convert drag coefficient to chezy coefficient
g dz_s/dx + cd w u^2/h = 0 (swe formalism)
     - S  +  1/C^2 U^2/H = 0 (chezy formalism)
```

32.8 f2chezy

32.9 ks2z0

32.10 manning2chezy

```
manning to chezy conversion
```

32.11 manning2drag

32.12 manning2kc

32.13 manning2z0

32.14 normal_flow_depth

```
normal flow depth for uniform stationary flow
function H = normal_flow_depth(Q,W,C,S)
```

32.15 normal_flow_discharge

```
normal flow discharge for uniform stationary flow
```

32.16 normal_flow_roughness

```
roughness coefficient from uniform stationary flow
```

32.17 normal_flow_slope

```
energy slope (surface slope) for uniform stationary flow
normal flow slope in uniform stationary flow
```

32.18 normal_flow_velocity

```
normal flow velocity in uniform stationary flow
```

32.19 normal_flow_width

```
normal flow width for uniform stationary flow
```

32.20 normal_shear_velocity

32.21 shear_velocity

32.22 z02chezy

32.23 z02ks

33 velocity-profile/@Log_profile

33.1 Log_profile

```
logarithmic profile of the streamwise velocity
```

33.2 df_dh

```
sensitivity of profile with respect to depth
```

33.3 df_dh_

```
sensitivity of profile with respect to depth
```

33.4 df_dln_z0

```
sensitivity of velocity profile with respect to roughness length
```

33.5 df_dln_z0_

```
sensitivity of profile with respect to roughness length
```

33.6 profile

```
vertical profile of the streamwise velocity
```

33.7 profile_

```
scale of velocity at instrument depth to depth average velocity
roughness length and associated standard error can change in time,
i.e. may be passed as vectors

zs    : [1xn] water surface level
zb    : [1x1] bottom level
za    : [1xn] or [1x1]
        level of velocity measurement,
        i.e. level of HADCP beam bin centre, coincides with
            instrument level,
        if the HADCP is horizontally aligned
        only needs to be passed as vector if instrument is
            redeployed or
        becomes misaligned
ln_z0 : [1xn] or [1x1]
        natural logarithm of the roughness length
s     : [1xn] or [1x1]
        standard error of ln_z0
function [fz_mu fz_s fz_sp fz_bias fz_eps] = log_profile(zs,zb,za,
    ln_z0,s,sp,e)
```

33.8 profile_bias

33.9 regmtx

```
regression matrix
```

33.10 ubar

```
depth averaged velocity
```

34 velocity-profile/@Log_profile_with_bend_correction

34.1 Log_profile_with_bend_correction

```
vertical velocity profile corrected for bend flow
```

34.2 df_dc

```
sensitivity of the velocity profile with respect to the bend
    correction
parameter c
```

34.3 df_dc_

34.4 du_dz

34.5 fit

```
fit the vertical velocity profile
```

34.6 profile_

```
vertical velocity profile
```

34.7 regmtx

```
regression matrix
```

34.8 u

```
streamwise velocity
```

34.9 u_

```
streamwise velocity
```

35 velocity-profile/@Log_profile_with_cubic_wake

35.1 Log_profile_with_cubic_wake

```
log profile with cubic wake
```

35.2 df_dc

```
sensitivity of profile with respect to wave parameter
```

35.3 df_dc_

```
sensitivity of profile with respect to wake parameter
```

35.4 profile_

```
vertical velocity profile
```

35.5 regmtx

```
regression matrix
```

36 velocity-profile/@Log_profile_with_dip

36.1 Log_profile_with_dip

```
Logarithmic profile with dip
```

36.2 fit

```
fit the vertical velocity profile
```

37 velocity-profile/@Log_profile_with_linear_bend_correction

37.1 Log_profile_with_linear_bend_correction

```
log profile with linear bend correction
```

37.2 df_dc

```
sensitivity of profile with respect to wake parameter
```

37.3 df_dc_

```
sensitivity of velocity profile with respect to wave parameter
```

37.4 du_dz

```
velocity shear along vertical
```

37.5 profile_

```
velocity profile
```

37.6 regmtx

```
regression matrix
```

38 velocity-profile/@Log_profile_with_wake

38.1 Log_profile_with_wake

```
logarithmic velocity profile with wake correction
c.f. coles
```

38.2 df_dc

```
sensitivity of profile with respect to wake parameter
```

38.3 df_dc_

```
sensitivity of velocity profile with respect to wake parameter
```

38.4 du_dz

```
velocity shear
```

38.5 profile_

```
predict velocity profile
```

38.6 regmtx

```
log law with wake
u = us/k ln(z) - us/k ln(z0) + us/k (2/H^2 z - 3/H^3 z^2)
```

39 velocity-profile/@VP

39.1 VP

```
velocity profile
```

39.2 process_joint

39.3 process_transverse_profile

```
process the transverse velocity profile
```

39.4 process_vertical_profile

```
predict vertical profile error distribution parameter for HADCP
    error estimate
```

39.5 profile_prediction_error

```
input :
U    : [nbin x nens]
       - values for each bin (or across section) and ensemble (or
           reference measurement)
       this are estimates estimates of the discharge or the cross
           sectional averaged
       velocity from the raw values
       - the profile should be limited to the effective profiling
           range,
       abobj 75-100m for a 600kHz ADCP

dn   : distance between HADCP bins
width : cross section width

objput:
     sd_n : expected standard deviation for increasing profiling
         range
function [s_rel s_err s_dat rho res m2 u_pred fdx] =
   velocity_variation(U)
hadcp_prediction_error
TODO take scales and unscaled velocity to do combine with harmmean
    estimate
note: previus versions:
      residual was computed with respect to the predicted local
          velocity
      mse was not upscaled to cs, as profile was expected to cover
          entire cs
      finite width of cs was not considered
parametric estimate from moments, objliers should be filtered
    beforehand
Note that the median absolute deviation is not a good estimate,
because it may excludes rare events like reverse flow of floods
thus, the only acceptible more robust estimate would be mean
    absolute deviation
```

40 velocity-profile/@Vertical_profile

40.1 Vertical_profile

```
vertical profile of the streamwise velocity, superclass
```

40.2 fit

```
fit vertical velocity profile parameter

function obj = fit(obj,U,S,h,binmask)
```

40.3 u

```
predict velocity along the vertical based on profile
```

41 velocity-profile

41.1 fit_displacement_profile

```
fit the log profile to the vertical profile of the streamwise
    velocity
```

41.2 lateral_division_method

```
transverse (across channel) profile of the streamwise velocity
in a straight channel
numerical solution
the eps seems incorrect, use better stationary_1d_swe

rho g h S - beta q^2 f / (8 h^2) + d/dy(eps_t dq/dy) = 0
rho g h S - beta q^2 g / (C^2 h^2) + d/dy(eps_t dq/dy) = 0
```

41.3 test_law_of_the_wall_fit

41.4 transverse_profile_parameter

41.5 transverse_velocity_profile

```
transverse profile of the streamwise velocity
c.f. shiono knight
```

41.6 transverse_velocity_profile_olesen

```
transverse profile of the streamwise velocity in a meander bend
```

41.7 transverse_velocity_profile_rozovskii

```
transversal velocity distribution in a bend
Rososkii,
as in the book central differences along the radius and euler
    forward in space
are used, note that since the advent of the computer more advanced
    schemes
could be used (see build in solvers)
cfl condition is not explicitely checked
Rosovsky assumes a constant water level, e.g. does not consider
    superelevation

I_theta = -1/r dz/d_theta   (p. 22)
d_theta = 1/R ds|_R
=> I_theta = -R/r dz/ds = -R/r I_0
It : (1.32) drop of level per unit angle, identical across section
```

41.8 transverse_velocity_profile_shiono_knight

```
transverse profile of the streamwise velocity, determined
    analytically
by the method of shiono and knight
shape of velocity profile only dependent on lambda, f, H, not slope
```

41.9 transverse_velocity_profile_tidal_channel

41.10 transverse_velocity_profile_with_slope

```
stationary 1D shallow water equation across a river section
0 = - g h S0 - tau_b/rho + d/dn (nu h du/dn)
0 = - g h S0 + g u^2/C^2 + d/dn (nu h du/dn)
includes tranvese gradient term

note that shiono/knight 1991 provide an _analytic_ solution,
which takes the form of an expontially decaying side wall effect
```

41.11 vertical_profile_of_velocity_vriend

```
vertical profile of the streamwise velocity, method of de vriend
```

41.12 vertical_velocity_profile

```
vertical profile of the streamwise velocity in non-uniform flow
```

41.13 z2s_rational

42 wrapper

42.1 discharge2stage

```
wrapper function
```

42.2 stage2discharge