

Manual for Package: tide

Revision 6M

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1 @T_Tide

1.1 T_Tide

wrapper for TPX0 generated tidal time series

1.2 `build_index`

build a structure whose field names contain the index

1.3 `from_tpxo`

read TPX0 output into tidetable object

1.4 `get_constituents`

extract constituents of tpxo object

1.5 `reorder`

order constituents as specified by "name"

1.6 `select`

select a subset of constituents

1.7 `shift_time_zone`

shift phase according to time zone

2 `@Tidal_Envelope`

2.1 `Tidal_Envelope`

process tidal data to extract the tidal envelope

2.2 `init`

initialize with data

3 @Tide_wft

wavelet analysis of tidal data

3.1 Tide_wft

wavelet transform of tidal time series

3.2 transform

wavelet transform tidal time series

input:

time : [1xn] abszissa of input vector, for example time, must be
equally spaced

val : [1xn] signal, input data series (e.g water level or
velocity)

F : [1xm] base frequencies, 1, 1, 2, ... for mean level,
diurnal, semidirunal ...

base periods from base frequencies $T=1/F$

n : [1xm] wavelet window length in multiple of periods

fc, nc : [scalar] low frequency cutoff and window length in periods

winstr : [char] fourier windows (kaiser (recommended), hanning, box
, etc)

dt_max : [scalar] maximum time to fill gaps in input data series (
recommended 3/24 for tide)

output:

tide : struct with fields

w_coeff : [1xn] wavelet coefficients (complex)

amplitude : amplitude

phase : phase

range :

h_tide :

h_low :

h

4 @Tidetable

class for generating tidetable data

4.1 Tidetable

Tide table

4.2 analyze

extract tidal envelope from time series

4.3 export_csv

export tide table to csv file

4.4 generate

run TPX0 to generate time series

4.5 generate_tpxo_input

generate tpxo input table
Note: superseded by perl script

4.6 import_tpxo

import TPX0 data into tidetable object

4.7 plot_neap_spring

plot average neap and spring tide

5 tide

analysis prediction of tides in rivers and estuaries by empirical
and theoretical methods

5.1 constituents

5.2 doodson

frequency of tidal constituents
method of doodson
source: wikipedia

5.3 envelope_amplitude

compute envelopes of hw and low water

5.4 envelope_slack_water

slack water envelope of the tide

5.5 interval_extrema

times and elevations for high and low water

5.6 interval_extrema2

minimum and maximum within intervals of constant length,
intended for periodic functions

5.7 interval_zeros

times of slack water determined from velocity u

5.8 lunar_phase

lunar phase

5.9 rayleigh_criterion

rayleigh criterion for resolving tidal constituents
 $T > 1/|f_1 - f_2|$

6 river-tide/@River_Tide

predict tide in a backwater affected river with a sloping/varying
bed

Assumptions and capabilities:

- tidal dynamics follow the 1D-Shallow-Water-Equation (depth and cross-sectionally averaged Navier-Stokes-Equation)
- rectangular cross section
- width can vary along the channel
- friction coefficient (cd) constant along channel and over time (Chezy)
- advective acceleration term is considered, but can be deactivated
- vertical profile of streamwise velocity is constant (Boussinesq coefficient is unity (1))

Limitations / TODO list:

- single channel dynamics only (no tidal networks)
- no wind-shear stress (no storm surges)
- no tidal flats / intertidal areas (width constant in time)
- no flood-plain during high-river flow
- no stratification or along-channel salinity gradient
- negligible head loss in channel bends
- negligible feed-back of the sediment concentration on the propagation of the tide
- low Froude Number (no hydraulic jumps due to cataracts or tidal bores)
- At present, only two tidal components are supported (either D1 with D2 or D2 with D4, in addition to the mean water level z0),
for mixed diurnal-semidiurnal cases with dominant semidiurnal component,
the class has to be extended to support three components (D1, D2 and D4)
- At present, the tripel overtide is not computed (D3 for diurnal, D6 for semidiurnal tide),
note that this is the main overtide for the case of low river flow

- At present, the $1/h$ non-linearity is only included in the approximations of the backwater curve, but not its influence on the tidal frequency components

Method:

This class calls numerical solvers for second order ordinary differential equation boundary value problems

Tides is represented as exponential series in form of total discharge $Q = \sum Q_i = Q_0 + Q_1 + Q_2$, as discharge is conserved (balanced), the equations are simpler than for level z and velocity u , and the frequency components of z are straight forward determined by differentiation of Q

Class and function structure:

```
River_Tide :
    computes river tide, provides the ode coefficients to
    the boundary value solver
bvp2c, bvp2fdm :
    solve the underlying second order boundary value
    problem
River_Tide_Map :
    provides convenient batch runs and processing of
    River_Tide instances
```

Minimum working example, c.f. example_rive_tide.m and example_river_tide_map.m

input:

```
Q0    : scalar, river discharge (m3/s)
omega : scalar, angular frequency main tidal species in (1/
seconds)
x      : 2x1 vector, left and right end of computational
domain of the river (m)
w(x)   : function of width along the river (m)
cd(x)  : function of drag coefficient along the river (1)
zb(x)  : function of bed level along the river (m)

opt    : structure with options
opt.model_str = 'wave' (other solver are not supported at the
moment)
opt.solver = @bvp2c or @bvp2fdm
opt.nx : number of grid points along channel
opt.ns : base for logarithmic spacing of grid points, 1 :
```

```

linear spacing

bc : structure array of boundary conditions
    r, row 1..2 : left and right end, respectively
    c, column 1 : mean (river) component
                2..n : condition form column-1 frequency
                    component

    (
        q(1)*(p(1) y-(x0) + p(2) dy-/dx(x0) ...
        + q(2)*(p(1) y+(x0) + p(2) dy+/dx(x0) ) = bc(c
        ,r).val
        = val(0)

bc(c,r).var : Quantity, either 'z' or 'Q'
bc(c,r).val : complex amplitude of chosen variable
              (c.f. (1 + 0i) [m] for surface elevation
                amplitude of 1m)
              (value has to be real for mean component)
              mean component requires z and Q to be specified
                at opposit ends
bc(c,r).p : factor for Dirichlet p(1) or Neumann p(2)
            condition
            p = [1,0] : pure Dirichlet
            p = [0,1] : pure Neumann
            sum of abs(p) must be nonzero for each end and
                each frequency component
bc(c,r).q : factor for left and right going wave, only
            available for bvp2c
            q = [1,1] : total water level / discharge
            q = [1,0] : only left going wave
            q = [0,1] : only right going wave
            q has no meaning for the mean component and is
                ignored
            q is only supported by bvp2c,
            bvpfdm uses default q = [1,1]
            sum of abs(q) for each frequency component must
                be zero

```

6.1 River_Tide

```

river tide in a single 1D channel
TODO split in two classes:
one that stores data (RT_Solve), one that provides equations (
RT_Analytic)

```

6.2 bc_transformation

6.3 bcfun

Robin (mixed) boundary conditions for the river tide,
supplied for each frequency component,
wrapper that copies values are from the member struct "bc"

```
    q*(p*Q_1^- + (1-p)*dQ_1^-/dx
input :
    x      : coordinate (left or right end)
    id,ccdx : frequency component index
              (1 = 0 omega (mean), 2 : 1 omega, 3 : 2 omega, ...)
columns of bc : frequency
rows of bc, left, right boundary
output :
    p : [2x1] linear combination of Dirichlet and Neumann
          boundary condition
    p(1) -> weight Dirichlet boundary condition
    p(2) -> weight Neumann boundary condition
    q linear combination of left and right travelling (incoming and
          outgoing) wave
    q(1) weight left going wave
    q(2) weight right going wave
    rhs = 0 -> homogeneous boundary condition

function [rhs, p, q, obj] = bcfun(obj,x,y,ccdx)
```

6.4 check_continuity

6.5 check_momentum

6.6 d2au1_dx2

second derivative of the tidal velocity magnitude

note: this is for finding zeros,
the true derivative has to be scaled up by z

6.7 d2az1_dx2

second derivative of the tidal surface elevation

note: this is for finding zeros,
the true derivative has to be scaled up by z

6.8 decompose

decompose the tide into a right and left travelling wave,
i.e. into incoming and reflected wave

6.9 discharge2level

tidal component of surface elevation determined from tidal
discharge

by continuity :

$$\begin{aligned} dz/dt + dq/dx &= 0 \\ \Rightarrow i \omega z &= - dq/dx \\ \Rightarrow z &= -1/(\omega) dq/dx \\ \Rightarrow z &= 1i/\omega dq/dx \end{aligned}$$

TODO allow Q as input

TODO rename into Q1_to_z1

Mon 7 Oct 19:04:14 PST 2019 : added correction for change of width

6.10 dkq_dx

along-channel derivative of the wave number of the discharge
neglects width variation

TODO, rederive with g as variable

6.11 dkz_dx

along channel derivative of the wave number of the tidal surface
elevation

ignores width variation dh/dx and second order depth variation (d^2h/dx^2)
TODO rederive with g symbolic

6.12 even_overtide_analytic

6.13 friction_coefficient_dronkers

friction coefficient according to Dronkers

the coefficients are semi-autogenerated

c.f. dronkers 1964

c.f. Cai 2016

```
p = [p0,p1,p2,p3];  
alpha =  $U_r/U_t$  = river velocity / tidal velocity amplitude =  $(u_{max} + u_{min}) / (u_{max} - u_{min})$ 
```

```
function p = friction_coefficient_dronkers(alpha,order)
```

6.14 friction_coefficient_godin

friction coefficient according to Godin

these coefficients are identical to Dronker's for $U_R = \phi = 0$

```
function G = friction_coefficient_godin(obj,phi)
```

6.15 friction_coefficient_lorentz

friction coefficient according to Lorentz

identical to Dronker's coefficient for zero river flow
and a single frequency component

c.f. Cai

c.f. Dronkers

```
function L = friction_coefficient_lorentz(obj,phi)
```

6.16 friction_dronkers

friction determined by Dronker's method

```
input :
    u      : velocity time series
    Umid   : arithmetic mean of minimum and maximum velocity
            (not the mean of the velocity, usually non-zero even
              without river flow)
    Uhr    : half-range of the velocity, less than the sum of
            the frequency amplitudes, except at perigean spring
            tides

function [uau_sum uau p] = friction_dronkers(u,Umid,Uhr,order)
```

6.17 friction_exponential_dronkers

friction coefficients for the frequency components computed by
Dronkers method

c.f. Dronker's 1964 eq 8.2 and 8.4

Note: Cai denominates alpha as phi

```
function [c uau uau_p] = friction_trigonometric_dronkers(u,dp,Umid
,Uhr,order,psym)
```

6.18 friction_godin

compute friction with the method of Godin

6.19 friction_trigonometric_dronkers

friction computed by the method of Dronkers

expressed as coefficients for the frequency components

c.f. dronkers 1964 eq 8.2 and 8.4

Note: Cai denominates alpha as phi

6.20 friction_trigonometric_godin

friction computed by the method of Godin
expressed as coefficients of the frequency components (
trigonometric form)

```
function [c, uau] = friction_trigonometric_godin(obj,u,dp,Umax)
```

6.21 friction_trigonometric_lorentz

friction computed by the method of Lorentz
expressed as coefficients of the frequency components (
trigonometric form)

6.22 init

provide initial condition by solving the backwater equation for
surface level
TODO this should not be solved as a ivp but included in the bvp
iteration
TODO generate the mesh here and precompute fixed values instead of
passing functions
TODO Q0 should not be a function
function obj = init(obj, Xi)

6.23 mwl_offset

offset of the tidally averaged surface elevation caused by tidal
friction
Linear estimate of the mean water level offset (ignoring feed-back
of tide)

6.24 mwl_offset_2

6.25 mwl_offset_analytic

6.26 odefun

coefficients of the backwater and wave equation for river-tides

6.27 odefun0

coefficients of the backwater equation for the river tide
TODO merge with backwater

6.28 odefun1

coefficients of the differential equation of the main tidal species

$$f1 Q'' + f2 Q' + f3 Q + f4 = 0$$

TODO rename f into c
TODO better pass dzb_dx instead of dz0_dx
TODO aa, oh and gh terms are not tested for width ~ 1

6.29 odefun2

coefficients of the ordinary differential quation of the even
overtide

6.30 solve

call stationary or non-stationary solver respectively

function obj = solve(obj)

6.31 solve_swe

determine river tide by the fully non-stationary FVM and then
extract the tide
this is experimental and not yet fully working

6.32 solve_wave

solve for the oscillatory (tidal) componets

```
function obj = solve_wave(obj)
```

6.33 wave_number_analytic

analytic expression of the wave number

valid for both tidally, river dominated and low friction conditions
and converging channels

k : complex wave number in a reach with constant width and bed
slope

$\text{im}(k)$: damping modulus (rate of amplitude change)

$\text{re}(k)$: actual wave number (rate of phase change)

c.f. derive_wave_number

6.34 wave_number_approximation

approximate wave number of the left and right traveling wave for
variable coefficients

TODO merge with wave_number_analytic

```
function [k, k0, dk0_dx_rel, obj] = wave_numer_aproximation(obj)
```

7 river-tide/@River_Tide_Cai

Prediction of river tide by the method of Cai
c.f. Cai 2013, Cai 2015

7.1 Gamma

Gamma parameter for tidal propagation
c.f. Cai 2014

7.2 River_Tide_Cai

prediction of river tide by the method of Cai (2014)

7.3 river_tide_cai_

determine the surface amplitude of the river-tide
c.f. Cai

7.4 rt_quantities

determine the quantities that determine the tidal propagation
c.f. Cai

Note: this computes 4 unknowns following Cai, however,
lambda, mu and epsilon can be substituted
making it an equation in one unknown (delta) only

8 river-tide/@River_Tide_Empirical

Empirical fit to measurement and prediction (from tide at sea and
river discharge)
of the river tide

8.1 River_Tide_Empirical

class for fitting models to at-a-station time series of tidal
elevation

8.2 fit_amplitude

fit the oscillatory components

8.3 fit_mwl

fit the tidally averaged water level

8.4 fit_phase

fit the phase of the oscillatory components

8.5 fit_range

fit the tidal range

8.6 predict_amplitude

predict the oscillatory components

8.7 predict_mwl

predict the mean water level

8.8 predict_phase

predict tidal phase

8.9 predict_range

predict the tidal range

8.10 rt_model

select the model for fitting

9 river-tide/@River_Tide_JK

empirical analysis and prediction of river tides by the method of
Jay and Kukulka

9.1 River_Tide_JK

9.2 damping_modulus

damping modulus of the river tide
c.f. Jay and Kukulka
function r = damping_modulus(obj,h0,b,Qr)

9.3 mean_level

tidally averaged surface elevation
c.f. Jay and Kukulka

9.4 rivertide_predict

predict river tide by the method of jay and kukulka
TODO rename

9.5 rivertide_regress

Regression of tidal coefficients according to Jay & Kukulka

coefficients of the r-regression factor 2 apart for specis (jay C7)
this can be repeated for each tidal species (diurnal, semidiurnal)

9.6 tidal_discharge

tidal discharge
c.f. Jay and Kukulka
function Qt = tidal_discharge(obj,x,R0,h0,b,Qr)

9.7 tidal_range

predict tidal range

10 river-tide/@River_Tide_Map

hash container for a set of River_Tide predictions for different boundary conditions

10.1 River_Tide_Map

container class to store individual river tide scenarios

10.2 fun

compute river tide for a scenario with specific boundary conditions and store it in the hash, or retrieve the scenario, if it was already computed

10.3 key

key for storing a scenario

```
function [key obj] = key(obj,varargin)
```

10.4 plot

quick plot of scenario result

```
function obj = plot(obj,Xi,Q0,W0,S0,z1_downstream,cd,zb_downstream,omega,q,opt)
```

11 river-tide/@River_Tide_Network

predict tides in a fluvial channel network

11.1 River_Tide_Network

tide in a fluvial delta channel network, extension of 1D river tide the network is a directed graph
TODO convert from trig-to exponential form

11.2 discharge_amplitude

discharge amplitude

11.3 mean_water_level

predict the mean water level

11.4 plot_mean_water_level

plot tidally averaged water level

11.5 plot_water_level_amplitude

plot surface elevation amplitude

11.6 solve

solve for the tide in a fluvial channel network

boundary condition at end points not connected to junctions

[channel 1 id, endpoint id (1 or 2), s0, c0

...

channel n id, endpoint id (1 or 2), s0, c0]

conditions at junctions are specified as cells

each cell contains an nx2 array

n : number of connecting channels

[channel id1, endpoint id (1 or 2), ...

channel idn, endpoint id (1 or 2)]

every tidal species for each channel has 4 unknowns

these are 2x2 unknowns for the sin + cos of left and right going
wave

11.7 water_level_amplitude

predict the surface elevation amplitude

12 river-tide

analysis and prediction of river tides

Sub-Classes:

```
@River_Tide
    - prediction of river tide in a backwater affected river with
      a sloping bed
@River_Tide_Cai
    - prediction of river tide, method of Cai
@River_Tide_Empirical
    - prediction of river tide, empirical
@River_Tide_JK
    - prediction of river tide, empirical after Jay and Kukulka
@River_Tide_Map
    - mulitple-scenaria container for River_Tide
@River_Tide_Network
    - extension of River_Tide to networks
```

12.1 damped_wave_bvp

solved damped wave equation
 $z'' + a z = 0$
 $z(0) = z_0, z(L) = 0$

12.2 damped_wave_ivp

linearly damped wave in rectangular channel
solve tide as initial value problem
damped wave approximation

$z'' + a z = 0$

$x_t = Ax + b$

12.3 damping_modulus_river

damping modulus of the tidal wave for river flow only

12.4 rdamping_to_cdrag_tide

converts damping rate to drag coefficient
c.f. friedrichs, ippen harleman

12.5 river_tide_godin

analytic solution to the river tide formulated as boundary value
problem
in a river with finite length

c.f. Godin 1986

12.6 rt_celerity

celerity of the tidal wave

12.7 rt_quasi_stationary_complex

quasi-stationary solution of the SWE
TODO staggered grid does not help: q1' needed

12.8 rt_quasi_stationary_trigonometric

quasi stationary form of the SWE

12.9 rt_reflection_coefficient_gradual

reflection coefficient for gradual varying cross section geometry
without damping

12.10 rt_wave_equation

solve river tide as boundary value problem

input:
omega : [nfx1] angluar frequency of tidal component, zero for mean
flow
reach : [nrx1] struct

```

.L      : [1x1] length of reaches
          .width(x,h)  width
          .bed(x,h)    bed level
          .surface(x,h) surface elevation
          .Cd(x,h)     drag coefficient
.bc     : [nd,nf] boundary/junction conditions
          bc(id,if).type : {surface, velocity, discharge} (dirichlet)
          bc(id,if).val  : value
opt      : [1x1] struct
          - constant surface elevation
          - deactivative advective acceleration
          .dx : spatial resolution

dimensions:
  nr : number of reaches
  nd : upstream/downstream index
  nf : frequency index

```

12.11 rt_z2q

determine tidal discharge from water level for tidal wave

13 river-tide/test/test

13.1 test_bvp2c_sym

13.2 test_celerity

13.3 test_characteristic_rate_of_change

13.4 test_dronkers_compound

13.5 test_friction_dronkers

13.6 test_fv_compare_schemes

13.7 test_fv_convergence

13.8 test_power_series

13.9 test_reflection_coefficient_gradual

13.10 test_ricatti

13.11 test_river_tide_models

13.12 test_rt_reflection

13.13 test_rt_zs0

13.14 test_swe

13.15 test_utm2latlon

13.16 test_wave_twopass

14 river-tide/test

14.1 test_bvp2c2

14.2 test_complex_even_overtide

14.3 test_fourier_power_exp

14.4 test_friction

14.5 test_reflection

14.6 test_rt_wave_number

14.7 test_tidal_river_network

14.8 test_tidal_river_network_z0

14.9 test_wave_number_godin

14.10 test_wave_numer_aproximation

15 river-tide

analysis and prediction of river tides

Sub-Classes:

```
@River_Tide
    - prediction of river tide in a backwater affected river with
      a sloping bed
@River_Tide_Cai
    - prediction of river tide, method of Cai
@River_Tide_Empirical
    - prediction of river tide, empirical
@River_Tide_JK
    - prediction of river tide, empirical after Jay and Kukulka
@River_Tide_Map
    - mulitple-scenaria container for River_Tide
@River_Tide_Network
    - extension of River_Tide to networks
```

15.1 tidal_ellipse

tidal ellipse, numerical ode solution

15.2 wave_number_tide

wave number of the tide without river flow
c.f. friedrichs, ippen harleman
output :
k : wave number, such that

$$z(t,x) = z_1(t,0) \exp(i(\omega t - kx))$$

re(k) : rate of phase change

-im(k) : damping rate

function [k k_low k_high] = damping_modulus_tide(omega,cd,h0,az1)

15.3 wavetrainz

determine river tide by iterated integration of the surface
elevation

15.4 wavetwopassz

two pass solution for the linearised wave equation, for surface
elevation

16 test/river-tide

16.1 example_river_tide

16.2 example_river_tide_map

16.3 river_tide_test

16.4 river_tide_test_01

16.5 river_tide_test_02

16.6 river_tide_test_03

16.7 river_tide_test_04

16.8 river_tide_test_05

16.9 river_tide_test_06

16.10 river_tide_test_07

16.11 river_tide_test_08

```
hold on;  
plot(x,abs(z),'--');  
hold on;  
plot(x,angle(z),'--');
```

16.12 river_tide_test_09

16.13 river_tide_test_10

16.14 river_tide_test_plot

17 test

17.1 test_tidal_harmonic_analysis

18 tide

analysis prediction of tides in rivers and estuaries by empirical and theoretical methods

18.1 tidal_constituents

18.2 tidal_energy_transport_1d

energy transport of a tidal wave

18.3 tidal_envelope

envelope of the tide

input : t time in days
 f surface elevation
output : tl time of low water
 vl surface elevation at low water
 ldx index of low water
 th time of high water
 vh surface elevation at high water
 hdx index of high water
 ndx neap index
 sdx spring index
 dmax:
 drange: range per day

18.4 tidal_envelope2

surface levelation envelope of the tide
low water, high water and tidal range for lunar each day

```

input:
    time :
    L     : surface elevation
    order : interpolation order (default 2)
output:
    timei : vector eqispaced
    lmini : minimum level
    lmaxi : maximum level
    rangei : range
    midrangei : (min + max)/2, usually different from mean
    phii : pseudo phase

```

Note: the pseudo phase ϕ jumps, this is because if the tide is semidiurnal, sometimes the lower hw becomes the next day higher then than the current high water, e.g. there is no smooth transition by 51min but a jump by 12h

18.5 tidal_harmonic_analysis

tidal_harmonic_analysis

19 tide-savenije

19.1 savenije_phase_lag

phase lag of high and low water

$\phi : u_{\text{river}}/u_{\text{tide}} < 1$

$\Delta t_{\text{eps_hw}} = \omega \cdot (t_{\text{hws}} - t_{\text{hw}})$

$\Delta t_{\text{eps_hw}} = \omega \cdot (t_{\text{lws}} - t_{\text{lw}})$

c.f. savenije

19.2 savenije_tidal_range

tidal range

based on Savenije 2012

x : distance to river mouth
eta : range
eta0 : range at river mouth
hbar : mean water depth
phi : velocity ratio $u_{\text{tide}}/u_{\text{river}}$
note: this varies in strongly convergent estuaries
K : mannings coefficient
I : residual surface slope I

19.3 savenije_tidal_range1

tidal range

based on Horrevoets/Savenije, 2004

H0 : tidal range at river mouth
h0 : initial water depth
v : velocity scale
b : convergence length
sine : phase lag
K : Mannings coefficient
Q_r : river discharge

19.4 savenije_timing_hw_lw

time of high water and low water
c.f. savenije 2012

19.5 tide-savenije