

Manual for Package: tide

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Contents

1	@T_Tide	7
1.1	T_Tide	7
1.2	build_index	7
1.3	from_tpxo	7
1.4	get_constituents	7
1.5	reorder	7
1.6	select	7
1.7	shift_time_zone	8
2	@Tidal_Envelope	8
2.1	Tidal_Envelope	8
2.2	init	8
3	@Tide_wft	8
3.1	Tide_wft	8
3.2	transform	8
4	@Tidetable	9
4.1	Tidetable	9
4.2	analyze	9
4.3	export_csv	9
4.4	generate	9
4.5	generate_tpxo_input	9
4.6	import_tpxo	10
4.7	plot_neap_spring	10
5	tide	10
5.1	constituents	10
5.2	doodson	10
5.3	envelope_amplitude	10

5.4	envelope_slack_water	10
5.5	interval_extrema	10
5.6	interval_extrema2	11
5.7	interval_zeros	11
5.8	lunar_phase	11
5.9	rayleigh_criterion	11
6	river-tide/@Bifurcation	11
6.1	Bifurcation	11
6.2	confluence_rule	11
6.3	sediment_division	11
6.4	sediment_division_geometric	11
7	river-tide/@River_Tide	12
7.1	River_Tide	14
7.2	check_continuity	15
7.3	check_momentum	15
7.4	d2au1_dx2	15
7.5	d2az1_dx2	15
7.6	decompose	15
7.7	dkq_dx	15
7.8	dkz_dx	16
7.9	even_overtide_analytic	16
7.10	friction_coefficient	16
7.11	friction_coefficient_dronkers	16
7.12	friction_coefficient_godin	16
7.13	friction_coefficient_lorentz	17
7.14	friction_dronkers	17
7.15	friction_exponential_dronkers	17
7.16	friction_godin	17
7.17	friction_lorentz	17
7.18	friction_quadratic	18
7.19	friction_trigonometric_dronkers	18
7.20	friction_trigonometric_godin	18
7.21	friction_trigonometric_lorentz	18
7.22	mwloffset	18
7.23	mwloffset_2	18
7.24	mwloffset_analytic	19
7.25	odefun	19
7.26	odefunQ0	19
7.27	odefun_advective_acceleration	19
7.28	odefun_friction	19
7.29	odefun_ghof	19
7.30	odefun_swe_jacobian	19

7.31	odefun_width	19
7.32	odefunk	20
7.33	odefunz0	20
7.34	wave_number_analytic	20
7.35	wave_number_approximation	20
8	river-tide/@River_Tide_BVP	21
8.1	River_Tide_BVP	21
8.2	bc_transformation	21
8.3	bcfun	21
8.4	check_continuity	21
8.5	check_momentum	22
8.6	decompose	22
8.7	discharge2level	22
8.8	dzb_dt	22
8.9	evolve_bed_level	22
8.10	evolve_bed_level_scenario	22
8.11	extract	22
8.12	generate_delft3d	23
8.13	init	23
8.14	initial_value	23
8.15	odefun	23
8.16	postprocess	23
8.17	sediment_transport	23
8.18	sediment_transport_	23
8.19	solve	23
9	river-tide/@River_Tide_Cai	24
9.1	Gamma	24
9.2	River_Tide_Cai	24
9.3	river_tide_cai_	24
9.4	rt_quantities	24
10	river-tide/@River_Tide_Empirical	24
10.1	River_Tide_Empirical	24
10.2	fit_amplitude	25
10.3	fit_mwl	25
10.4	fit_phase	25
10.5	fit_range	25
10.6	predict_amplitude	25
10.7	predict_mwl	25
10.8	predict_phase	25
10.9	predict_range	25
10.10	rt_model	26

11 river-tide/@River_Tide_IVP	26
11.1 solve	26
12 river-tide/@River_Tide_JK	26
12.1 River_Tide_JK	26
12.2 damping_modulus	26
12.3 mean_level	26
12.4 rivertide_predict	26
12.5 rivertide_regress	27
12.6 tidal_discharge	27
12.7 tidal_range	27
13 river-tide/@River_Tide_Map	27
13.1 River_Tide_Map	27
13.2 fun	27
13.3 plot	27
14 river-tide/@River_Tide_Morphodynamics_Map@	28
14.1 River_Tide_Morphodynamics_Map	28
14.2 fun	28
15 river-tide/@River_Tide_Network_Simple	28
15.1 River_Tide_Network_Simple	28
15.2 discharge_amplitude	28
15.3 mean_water_level	28
15.4 plot_mean_water_level	28
15.5 plot_water_level_amplitude	28
15.6 solve	29
15.7 water_level_amplitude	29
16 river-tide/@River_Tide_SWE	29
16.1 solve	29
17 river-tide	29
17.1 damped_wave_bvp	30
17.2 damped_wave_ivp	30
17.3 damping_modulus_river	30
17.4 rdamping_to_cdrag_tide	30
17.5 river_tide_godin	30
17.6 rt_celerity	31
17.7 rt_quasi_stationary_complex	31
17.8 rt_quasi_stationary_trigonometric	31
17.9 rt_reflection_coefficient_gradual	31
17.10 rt_transport	31
17.11 rt_wave_equation	31

17.12	rt_z2q	32
17.13	tidal_ellipse	32
17.14	tide_slack_exp	32
17.15	wave_number_tide	32
17.16	wavetrainz	32
17.17	wavetwopassz	33
18	tide	33
18.1	river_tide_transport_scale	33
19	test/river-tide-morphodynamics	33
19.1	river_tide_morphodynamics_test_01	33
19.2	river_tide_morphodynamics_test_02	33
19.3	river_tide_morphodynamics_test_03	33
19.4	river_tide_morphodynamics_test_04_seasons	33
19.5	rtm_plot	33
20	test/river-tide-network	34
20.1	river_tide_network_test_01	34
20.2	river_tide_network_test_02	34
20.3	river_tide_network_test_03	34
20.4	river_tide_network_test_04	34
20.5	river_tide_network_test_05	34
21	test/river-tide	34
21.1	example_river_tide	34
21.2	example_river_tide_map	34
21.3	river_tide_test_01	34
21.4	river_tide_test_02	34
21.5	river_tide_test_03	35
21.6	river_tide_test_04	35
21.7	river_tide_test_05	35
21.8	river_tide_test_06	35
21.9	river_tide_test_07	35
21.10	river_tide_test_08	35
21.11	river_tide_test_09	35
21.12	river_tide_test_10	35
21.13	river_tide_test_11	35
21.14	river_tide_test_12	36
21.15	river_tide_test_13	36
21.16	river_tide_test_batch	36
21.17	river_tide_test_metadata	36
21.18	river_tide_test_plot	36
21.19	test_bvp2c2	36

21.20	test_bvp2c_sym	36
21.21	test_celerity	36
21.22	test_characteristic_rate_of_change	36
21.23	test_complex_even_overtide	36
21.24	test_dronkers_compound	37
21.25	test_fourier_power_exp	37
21.26	test_friction	37
21.27	test_friction_dronkers	37
21.28	test_friction_dronkers2	37
21.29	test_fv_compare_schemes	37
21.30	test_fv_convergence	37
21.31	test_power_series	37
21.32	test_reflection	37
21.33	test_reflection_coefficient_gradual	37
21.34	test_ricatti	38
21.35	test_river_tide_models	38
21.36	test_rt_reflection	38
21.37	test_rt_wave_number	38
21.38	test_rt_zs0	38
21.39	test_swe	38
21.40	test_tidal_river_network	38
21.41	test_tidal_river_network_z0	38
21.42	test_tide_slack_exp	38
21.43	test_utm2latlon	38
21.44	test_wave_number_godin	39
21.45	test_wave_numer_aproximation	39
21.46	test_wave_twopass	39
22	test	39
22.1	test_rt_transport	39
22.2	test_tidal_harmonic_analysis	39
23	tide	39
23.1	tidal_constituents	39
23.2	tidal_energy_transport_1d	39
23.3	tidal_envelope	40
23.4	tidal_envelope2	40
23.5	tidal_harmonic_analysis	40
23.6	tidal_range_exp	41
23.7	tidal_range_tri	41
24	tide-savenije	41
24.1	savenije_phase_lag	41
24.2	savenije_tidal_range	41

24.3	savenije_tidal_range1	42
24.4	savenije_timing_hw_lw	42
24.5	tide-savenije	42
25	tide	42
25.1	tide_low_high_exp	42
25.2	tide_low_high_tri	42

1 @T_Tide

1.1 T_Tide

wrapper for TPX0 generated tidal time series

1.2 build_index

build a structure whose field names contain the index

1.3 from_tpxo

read TPX0 output into tidetable object

1.4 get_constituents

extract constituents of tpxo object

1.5 reorder

order constituents as specified by "name"

1.6 select

select a subset of constituents

1.7 shift_time_zone

shift phase according to time zone

2 @Tidal_Envelope

2.1 Tidal_Envelope

process tidal data to extrac the tidal envelope

2.2 init

initialize with data

3 @Tide_wft

wavelet analysis of tidal data

3.1 Tide_wft

wavelet transform of tidal time series

3.2 transform

wavelet transform tidal time series

input:

time : [1xn] abszissa of input vector, for example time, must be
equally spaced

val : [1xn] signal, input data series (e.g water level or
velocity)

F : [1xm] base frequencies, 1, 1, 2, ... for mean level,
diurnal, semidirunal ...

base periods from base frequencies $T=1/F$

n : [1xm] wavelet window length in multiple of periods

fc, nc : [scalar] low frequency cutoff and window length in periods

winstr : [char] fourier windows (kaiser (recommended), hanning, box
, etc)

dt_max : [scalar] maximum time to fill gaps in input data series (
recommended 3/24 for tide)


```

output:
tide  : struct with fields
      w_coeff : [1xn] wavelet coefficients (complex)
      amplitude : amplitude
      phase    : phase
      range    :
      h_tide   :
      h_low    :
      h

```

4 @Tidetable

class for generating tidetable data

4.1 Tidetable

Tide table

4.2 analyze

extract tidal envelope from time series

4.3 export_csv

export tide table to csv file

4.4 generate

run TPX0 to generate time series

4.5 generate_tpxo_input

generate tpxo input table
 Note: superseded by perl script

4.6 import_tpxo

import TPX0 data into tidetable object

4.7 plot_neap_spring

plot average neap and spring tide

5 tide

analysis prediction of tides in rivers and estuaries by empirical
and theoretical methods

5.1 constituents

5.2 doodson

frequency of tidal constituents
method of doodson
source: wikipedia

5.3 envelope_amplitude

compute envelopes of hw and low water

5.4 envelope_slack_water

slack water envelope of the tide

5.5 interval_extrema

times and elevations for high and low water

5.6 interval_extrema2

minimum and maximum within intervals of constant length,
intended for periodic functions

5.7 interval_zeros

times of slack water determined from velocity u

5.8 lunar_phase

lunar phase

5.9 rayleigh_criterion

rayleigh criterion for resolving tidal constituents
 $T > 1/|f_1 - f_2|$

6 river-tide/@Bifurcation

6.1 Bifurcation

6.2 confluence_rule

6.3 sediment_division

6.4 sediment_division_geometric

7 river-tide/@River_Tide

predict tide in a backwater affected river with a sloping/varying bed

Assumptions and capabilities:

- tidal dynamics follow the 1D-Shallow-Water-Equation (depth and cross-sectionally averaged Navier-Stokes-Equation)
- rectangular cross section
- width can vary along the channel
- friction coefficient (cd) constant along channel and over time (Chezy)
- advective acceleration term is considered, but can be deactivated
- vertical profile of streamwise velocity is constant (Boussinesq coefficient is unity (1))

Limitations / TODO list:

- single channel dynamics only (no tidal networks)
- no wind-shear stress (no storm surges)
- no tidal flats / intertidal areas (width constant in time)
- no flood-plain during high-river flow
- no stratification or along-channel salinity gradient
- negligible head loss in channel bends
- negligible feed-back of the sediment concentration on the propagation of the tide
- low Froude Number (no hydraulic jumps due to cataracts or tidal bores)
- At present, only two tidal components are supported (either D1 with D2 or D2 with D4, in addition to the mean water level z0),
for mixed diurnal-semidiurnal cases with dominant semidiurnal component,
the class has to be extended to support three components (D1, D2 and D4)
- At present, the tripel overtide is not computed (D3 for diurnal, D6 for semidiurnal tide),
note that this is the main overtide for the case of low river flow
- At present, the 1/h non-linearity is only included in the approximations of
the backwater curve, but not it's influence on the tidal frequency components

Method:

This class calls numerical solvers for second order ordinary differential equation boundary value problems

Tides is represented as exponential series in form of total discharge $Q = \sum Q_i = Q_0 + Q_1 + Q_2$, as discharge is conserved (balanced), the equations are simpler than for level z and velocity u , and the frequency components of z are straight forward determined by differentiation of Q

Class and function structure:

```
River_Tide :
    computes river tide, provides the ode coefficients to
    the boundary value solver
bvp2c, bvp2fdm :
    solve the underlying second order boundary value
    problem
River_Tide_Map :
    provides convenient batch runs and processing of
    River_Tide instances
```

Minimum working example, c.f. example_rive_tide.m and example_river_tide_map.m

input:

```
Q0    : scalar, river discharge (m3/s)
omega : scalar, angular frequency main tidal species in (1/
seconds)
x      : 2x1 vector, left and right end of computational
domain of the river (m)
w(x)   : function of width along the river (m)
cd(x)  : function of drag coefficient along the river (1)
zb(x)  : function of bed level along the river (m)

opt    : structure with options
opt.model_str = 'wave' (other solver are not supported at the
moment)
opt.solver = @bvp2c or @bvp2fdm
opt.nx : number of grid points along channel
opt.ns : base for logarithmic spacing of grid points, 1 :
linear spacing

bc : structure array of boundary conditions
    r, row 1..2 : left and right end, respectively
    c, column 1 : mean (river) component
                2..n : condition form column-1 frequency
                    component
```

```

(      q(1)*(p(1) y^-(x0) + p(2) dy^-/dx(x0) ...
+ q(2)*(p(1) y^+(x0) + p(2) dy^+/dx(x0) ) = bc(c
,r).val
      = val(0)

bc(c,r).var : Quantity, either 'z' or 'Q'
bc(c,r).val : complex amplitude of chosen variable
              (c.f. (1 + 0i) [m] for surface elevation
                amplitude of 1m)
              (value has to be real for mean component)
              mean component requires z and Q to be specified
                at opposit ends
bc(c,r).p : factor for Dirichlet p(1) or Neumann p(2)
condition
      p = [1,0] : pure Dirichlet
      p = [0,1] : pure Neumann
      sum of abs(p) must be nonzero for each end and
        each frequency component
bc(c,r).q : factor for left and right going wave, only
available for bvp2c
      q = [1,1] : total water level / discharge
      q = [1,0] : only left going wave
      q = [0,1] : only right going wave
      q has no meaning for the mean component and is
        ignored
      q is only supported by bvp2c,
      bvpfdm uses default q = [1,1]
      sum of abs(q) for each frequency component must
        be zero

```

7.1 River_Tide

river tide in a single 1D channel

TODO split in two classes:

one that stores data (RT_Solve), one that provides equations (RT_Analytic)

```

function out = out(obj)
    out = obj.odesolver.out;
end

TODO

Q = obj.Q_;
if (nargin()>1)
    Q = interp1(obj.x,Q,x,'linear');
else
    x = obj.x;
end
w = obj.fun.width(x);
h0 = obj.h0(x);

```

```
y = bsxfun(@times,Q,1./(w.*h0));
```

7.2 check_continuity

7.3 check_momentum

7.4 d2au1_dx2

second derivative of the tidal velocity magnitude

note: this is for finding zeros,
the true derivative has to be scaled up by z

7.5 d2az1_dx2

second derivative of the tidal surface elevation

note: this is for finding zeros,
the true derivative has to be scaled up by z

7.6 decompose

decompose the tide into a right and left travelling wave,
i.e. into incoming and reflected wave
TODO subtract forcing term

7.7 dkq_dx

along-channel derivative of the wave number of the discharge
neglects width variation

TODO, rederive with g as variable

7.8 dkz_dx

along channel derivative of the wave number of the tidal surface
elevation
ignores width variation dh/dx and second order depth variation (d^2h/dx^2)
TODO rederive with g symbolic

7.9 even_overtide_analytic

7.10 friction_coefficient

7.11 friction_coefficient_dronkers

friction coefficient according to Dronkers
the coefficients are semi-autogenerated
c.f. dronkers 1964
c.f. Cai 2016
 $p = [p_0, p_1, p_2, p_3];$
 $\alpha = U_r/U_t = \text{river velocity} / \text{tidal velocity amplitude} = (u_{\max} + u_{\min}) / (u_{\max} - u_{\min})$
 $\text{function } p = \text{friction_coefficient_dronkers}(\alpha, \text{order})$

7.12 friction_coefficient_godin

friction coefficient according to Godin
these coefficients are identical to Dronker's for $U_R = \phi = 0$
 $\text{function } G = \text{friction_coefficient_godin}(\text{obj}, \phi)$

7.13 friction_coefficient_lorentz

friction coefficient according to Lorent's
identical to Dronker's coefficient for zero river flow
and a single frequency component
c.f. Cai
c.f. Dronkers

```
function L = friction_coefficient_lorentz(obj,phi)
```

7.14 friction_dronkers

friction determined by Dronker's method

input :

- u : velocity time series
- Umid : arithmetic mean of minimum and maximum velocity
(not the mean of the velocity, usually non-zero even
without river flow)
- Uhr : half-range of the velocity, less than the sum of
the frequency amplitudes, except at perigean spring
tides

```
function [uau_sum uau p] = friction_dronkers(u,Umid,Uhr,order)
```

7.15 friction_exponential_dronkers

friction coefficients for the frequency components computed by
Dronkers method
c.f. Dronker's 1964 eq 8.2 and 8.4
Note: Cai denominates alpha as phi

```
function [c uau uau_ p] = friction_trigonometric_dronkers(u,dp,Umid  
,Uhr,order,psym)
```

7.16 friction_godin

compute friction with the method of Godin

7.17 friction_lorentz

7.18 friction_quadratic

friction determined by Dronker's method

7.19 friction_trigonometric_dronkers

friction computed by the method of Dronkers
expressed as coefficients for the frequency components
c.f. dronkers 1964 eq 8.2 and 8.4
Note: Cai dennominates alpha as phi

7.20 friction_trigonometric_godin

friction computed by the method of Godin
expressed as coefficients of the frequency components (
trigonometric form)

```
function [c, uau] = friction_trigonometric_godin(obj,u,dp,Umax)
```

7.21 friction_trigonometric_lorentz

friction computed by the method of Lorentz
expressed as coefficients of the frequency components (
trigonometric form)

7.22 mwl_offset

offset of the tidally averaged surface elevation caused by tidal
friction
Linear estimate of the mean water level offset (ignoring feed-back
of tide)

7.23 mwl_offset_2

7.24 `mw1_offset_analytic`

7.25 `odefun`

coefficients of the backwater and wave equation for river-tides

7.26 `odefunQ0`

7.27 `odefun_advective_acceleration`

7.28 `odefun_friction`

7.29 `odefun_ghof`

7.30 `odefun_swe_jacobian`

7.31 `odefun_width`

7.32 odefunk

coefficients of the ordinary differential equation of the k-th
frequency
component of the tide

$$f_1 Q'' + f_2 Q' + f_3 Q + f_4 = 0$$

TODO rename f into c
TODO better pass dzb_dx instead of dz0_dx
TODO aa, oh and gh terms are not tested for width ~ 1

7.33 odefunz0

coefficients of the backwater equation for the river tide
TODO merge with backwater

7.34 wave_number_analytic

analytic expression of the wave number

valid for both tidally, river dominated and low friction conditions
and converging channels

k10 : complex wave number for k and z in a reach with constant
width and bed slope

im(k) : damping modulus (rate of amplitude change)

re(k) : actual wave number (rate of phase change)

kq : wave number for Q for a reach with changing width and depth

kz : wave number for z for a reach with changing width and depth

c.f. derive_wave_number

7.35 wave_number_approximation

approximate wave number of the left and right traveling wave for
variable coefficients

TODO merge with wave_number_analytic

function [k, k0, dk0_dx_rel, obj] = wave_numer_aproximation(obj)

8 river-tide/@River_Tide_BVP

8.1 River_Tide_BVP

river tide in a single 1D channel
TODO split in two classes:
one that stores data (RT_Solve), one that provides equations (
RT_Analytic)

8.2 bc_transformation

8.3 bcfun

Robin (mixed) boundary conditions for the river tide,
supplied for each frequency component,
wrapper that copies values are from the member struct "bc"

```
q*(p*Q_1^- + (1-p)*dQ_1^-/dx
input :
    x          : coordinate (left or right end)
    id,ccdx    : frequency component index
                  (1 = 0 omega (mean), 2 : 1 omega, 3 : 2 omega, ...)
columns of bc : frequency
rows of bc, left, right boundary
output :
    p : [2x1] linear combination of Dirichlet and Neumann
        boundary condition
    p(1) -> weight Dirichlet boundary condition
    p(2) -> weight Neumann boundary condition
    q linear combination of left and right travelling (incoming and
        outgoing) wave
    q(1) weight left going wave
    q(2) weight right going wave
    rhs = 0 -> homogeneous boundary condition
```

```
function [rhs, p, q, obj] = bcfun(obj,x,y,ccdx)
```

8.4 check_continuity

8.5 check_momentum

8.6 decompose

decompose the tide into a right and left travelling wave,
i.e. into incoming and reflected wave
TODO subtract forcing term

8.7 discharge2level

tidal component of surface elevation determined from tidal
discharge

by continuity :

$$\begin{aligned} dz/dt + dq/dx &= 0 \\ \Rightarrow i \omega z &= - dq/dx \\ \Rightarrow z &= -1/(i\omega) dq/dx \\ \Rightarrow z &= 1i/\omega dq/dx \end{aligned}$$

TODO rename into Qt_to_zt
Mon 7 Oct 19:04:14 PST 2019 : added correction for change of width

8.8 dzb_dt

8.9 evolve_bed_level

8.10 evolve_bed_level_scenario

8.11 extract

8.12 generate_delft3d

8.13 init

```
provide initial condition by solving the backwater equation for
    surface level
TODO this should not be solved as a ivp but included in the bvp
    iteration
TODO generate the mesh here and precompute fixed values instead of
    passing functions
TODO Q0 should not be a function
function obj = init(obj, Xi)
```

8.14 initial_value

8.15 odefun

```
coefficients of the backwater and wave equation for river-tides
```

8.16 postprocess

8.17 sediment_transport

8.18 sediment_transport_

8.19 solve

9 river-tide/@River_Tide_Cai

Prediction of river tide by the method of Cai
c.f. Cai 2013, Cai 2015

9.1 Gamma

Gamma parameter for tidal propagation
c.f. Cai 2014

9.2 River_Tide_Cai

prediction of river tide by the method of Cai (2014)

9.3 river_tide_cai_

determine the surface amplitude of the river-tide
c.f. Cai

9.4 rt_quantities

determine the quantities that determine the tidal propagation
c.f. Cai

Note: this computes 4 unknowns following Cai, however,
lambda, mu and epsilon can be substituted
making it an equation in one unknown (delta) only

10 river-tide/@River_Tide_Empirical

Empirical fit to measurement and prediction (from tide at sea and
river discharge)
of the river tide

10.1 River_Tide_Empirical

class for fitting models to at-a-station time series of tidal
elevation

10.2 fit_amplitude

fit the oscillatory components

10.3 fit_mwl

fit the tidally averaged water level

10.4 fit_phase

fit the phase of the oscillatory components

10.5 fit_range

fit the tidal range

10.6 predict_amplitude

predict the oscillatory components

10.7 predict_mwl

predict the mean water level

10.8 predict_phase

predict tidal phase

10.9 predict_range

predict the tidal range

10.10 rt_model

select the model for fitting

11 river-tide/@River_Tide_IVP

11.1 solve

12 river-tide/@River_Tide_JK

empirical analysis and prediction of river tides by the method of
Jay and Kukulka

12.1 River_Tide_JK

12.2 damping_modulus

damping modulus of the river tide
c.f. Jay and Kukulka
function r = damping_modulus(obj,h0,b,Qr)

12.3 mean_level

tidally averaged surface elevation
c.f. Jay and Kukulka

12.4 rivertide_predict

predict river tide by the method of jay and kukulka
TODO rename

12.5 rivertide_regress

Regression of tidal coefficients according to Jay & Kulkulka

coefficients of the r-regression factor 2 apart for specis (jay C7)
this can be repeated for each tidal species (diurnal, semidiurnal)

12.6 tidal_discharge

tidal discharge
c.f. Jay and Kukulka
function Qt = tidal_discharge(obj,x,R0,h0,b,Qr)

12.7 tidal_range

predict tidal range

13 river-tide/@River_Tide_Map

hash container for a set of River_Tide predictions for different
boundary conditions

13.1 River_Tide_Map

container class to store multiple river-tide scenarios

13.2 fun

compute river tide for a scenario with specific boundary conditions
and store it in the hash,
or retrieve the scenario, if it was already computed

13.3 plot

quick plot of scenario result

function obj = plot(obj,Xi,Q0,W0,S0,z1_downstream,cd,zb_downstream,
omega,q,opt)

14 river-tide/@River_Tide_Morphodynamics_Map@

14.1 River_Tide_Morphodynamics_Map

container class to store multiple river-tide morphodynamics scenarios

14.2 fun

morphodynamics of a tidal river
either retrieve a precomputed scenario or compute and store a new scenario

15 river-tide/@River_Tide_Network_Simple

15.1 River_Tide_Network_Simple

tide in a fluvial delta channel network, extension of 1D river tide
the network is a directed graph
TODO convert from trig-to exponential form

15.2 discharge_amplitude

discharge amplitude

15.3 mean_water_level

predict the mean water level

15.4 plot_mean_water_level

plot tidally averaged water level

15.5 plot_water_level_amplitude

plot surface elevation amplitude

15.6 solve

solve for the tide in a fluvial channel network

boundary condition at end points not connected to junctions
[channel 1 id, endpoint id (1 or 2), s0, c0
...
channel n id, endpoint id (1 or 2), s0, c0]

conditions at junctions are specified as cells
each cell contains an nx2 array
n : number of connecting channels
[channel id1, endpoint id (1 or 2), ...
channel idn, endpoint id (1 or 2)]

every tidal species for each channel has 4 unknowns
these are 2x2 unknowns for the sin + cos of left and right going
wave

15.7 water_level amplitude

predict the surface elevation amplitude

16 river-tide/@River_Tide_SWE

16.1 solve

determine river tide by the fully non-stationary FVM and then
extract the tide
this is experimental and not yet fully working

17 river-tide

analysis and prediction of river tides

Sub-Classes:

@River_Tide
- prediction of river tide in a backwater affected river with
a sloping bed
@River_Tide_Cai
- prediction of river tide, method of Cai

```

@River_Tide_Empirical
    - prediction of river tide, empirical
@River_Tide_JK
    - prediction of river tide, empirical after Jay and Kukulka
@River_Tide_Map
    - mulitple-scenaria container for River_Tide
@River_Tide_Network
    - extension of River_Tide to networks

```

17.1 damped_wave_bvp

solved damped wave equation
 $z'' + a z = 0$
 $z(0) = z_0, z(L) = 0$

17.2 damped_wave_ivp

linearly damped wave in rectangular channel
 solve tide as initial value problem
 damped wave approximation

$$z'' + a z = 0$$

$$x_t = Ax + b$$

17.3 damping_modulus_river

damping modulus of the tidal wave for river flow only

17.4 rdamping_to_cdrag_tide

converts damping rate to drag coefficient
 c.f. friedrichs, ippen harleman

17.5 river_tide_godin

analytic solution to the river tide formulated as boundary value
 problem
 in a river with finite length
 c.f. Godin 1986

17.6 rt_celerity

celerity of the tidal wave

17.7 rt_quasi_stationary_complex

quasi-stationary solution of the SWE
TODO staggered grid does not help: q1' needed

17.8 rt_quasi_stationary_trigonometric

quasi stationary form of the SWE

17.9 rt_reflection_coefficient_gradual

reflection coefficient for gradual varying cross section geometry
without damping

17.10 rt_transport

17.11 rt_wave_equation

solve river tide as boundary value problem

input:
omega : [nfx1] angluar frequency of tidal component, zero for mean
flow
reach : [nrx1] struct
.L : [1x1] length of reaches
.width(x,h) width
.bed(x,h) bed level
.surface(x,h) surface elevation
.Cd(x,h) drag coefficient
.bc : [nd,nf] boundary/junction conditions
bc(id,if).type : {surface, velocity, discharge} (dirichlet)
bc(id,if).val : value
opt : [1x1] struct

- constant surface elevation
- deactivative advective acceleration
- .dx : spatial resolution

dimensions:

- nr : number of reaches
- nd : upstream/downstream index
- nf : frequency index

17.12 rt_z2q

determine tidal discharge from water level for tidal wave

17.13 tidal_ellipse

tidal ellipse, numerical ode solution

17.14 tide_slack_exp

17.15 wave_number_tide

wave number of the tide without river flow

c.f. friedrichs, ippen harleman

output :

k : wave number, such that

$$z(t,x) = z_1(t,0) \exp(1i*(\omega t - kx))$$

re(k) : rate of phase change

-im(k) : damping rate

function [k k_low k_high] = damping_modulus_tide(omega,cd,h0,az1)

17.16 wavetrainz

determine river tide by iterated integration of the surface elevation

17.17 wavetwopassz

two pass solution for the linearised wave equation, for surface elevation

18 tide

analysis prediction of tides in rivers and estuaries by empirical and theoretical methods

18.1 river_tide_transport_scale

19 test/river-tide-morphodynamics

19.1 river_tide_morphodynamics_test_01

19.2 river_tide_morphodynamics_test_02

19.3 river_tide_morphodynamics_test_03

19.4 river_tide_morphodynamics_test_04_seasons

19.5 rtm_plot

20 test/river-tide-network

20.1 river_tide_network_test_01

20.2 river_tide_network_test_02

20.3 river_tide_network_test_03

20.4 river_tide_network_test_04

20.5 river_tide_network_test_05

21 test/river-tide

21.1 example_river_tide

21.2 example_river_tide_map

21.3 river_tide_test_01

21.4 river_tide_test_02

21.5 river_tide_test_03

21.6 river_tide_test_04

21.7 river_tide_test_05

21.8 river_tide_test_06

21.9 river_tide_test_07

21.10 river_tide_test_08

```
hold on;  
plot(x,abs(z),'--');  
hold on;  
plot(x,angle(z),'--');
```

21.11 river_tide_test_09

21.12 river_tide_test_10

21.13 river_tide_test_11

21.14 `river_tide_test_12`

21.15 `river_tide_test_13`

21.16 `river_tide_test_batch`

21.17 `river_tide_test_metadata`

21.18 `river_tide_test_plot`

21.19 `test_bvp2c2`

21.20 `test_bvp2c_sym`

21.21 `test_celerity`

21.22 `test_characteristic_rate_of_change`

21.23 `test_complex_even_overtide`

21.24 test_dronkers_compound

21.25 test_fourier_power_exp

21.26 test_friction

21.27 test_friction_dronkers

21.28 test_friction_dronkers2

21.29 test_fv_compare_schemes

21.30 test_fv_convergence

21.31 test_power_series

21.32 test_reflection

21.33 test_reflection_coefficient_gradual

21.34 test_ricatti

21.35 test_river_tide_models

21.36 test_rt_reflection

21.37 test_rt_wave_number

21.38 test_rt_zs0

21.39 test_swe

21.40 test_tidal_river_network

21.41 test_tidal_river_network_z0

21.42 test_tide_slack_exp

21.43 test_utm2latlon

21.44 test_wave_number_godin

21.45 test_wave_numer_aproximation

21.46 test_wave_twopass

22 test

22.1 test_rt_transport

22.2 test_tidal_harmonic_analysis

23 tide

analysis prediction of tides in rivers and estuaries by empirical
and theoretical methods

23.1 tidal_constituents

23.2 tidal_energy_transport_1d

energy transport of a tidal wave

23.3 tidal_envelope

envelope of the tide

```
input : t time in days
        f surface elevation
output : tl time of low water
        vl surface elevation at low water
        ldx index of low water
        th time of high water
        vh surface elevation at high water
        hdx index of high water
        ndx neap index
        sdx spring index
        dmax:
        drange: range per day
```

23.4 tidal_envelope2

surface levelation envelope of the tide
low water, high water and tidal range for lunar each day

```
input:
    time :
    L     : surface elevation
    order : interpolation order (default 2)
output:
    timei : vector eqispaced
    lmini : minimum level
    lmaxi : maximum level
    rangei : range
    midrangei : (min + max)/2, usually different from mean
    phii : pseudo phase
```

Note: the pseudo phase phi jumps, this is because if the tide is semidiurnal, sometimes the lower hw becomes the next day higher then than the current high water, e.g. there is no smooth transition by 51min but a jump by 12h

23.5 tidal_harmonic_analysis

tidal_harmonic analysis

23.6 tidal_range_exp

23.7 tidal_range_tri

24 tide-savenije

24.1 savenije_phase_lag

phase lag of high and low water

ϕ : $u_{\text{river}}/u_{\text{tide}} < 1$

$\Delta t_{\text{eps_hw}} = \omega \cdot (t_{\text{hws}} - t_{\text{hw}})$

$\Delta t_{\text{eps_hw}} = \omega \cdot (t_{\text{lws}} - t_{\text{lw}})$

c.f. savenije

24.2 savenije_tidal_range

tidal range

based on Savenije 2012

x : distance to river mouth

η : range

η_0 : range at river mouth

\bar{h} : mean water depth

ϕ : velocity ratio $u_{\text{tide}}/u_{\text{river}}$

note: this varies in strongly convergent estuaries

K : mannings coefficient

I : residual surface slope

24.3 savenije_tidal_range1

tidal range

based on Horrevoets/Savenije, 2004

H0 : tidal range at river mouth
h0 : initial water depth
v : velocity scale
b : convergence length
sine : phase lag
K : Mannings coefficient
Q_r : river discharge

24.4 savenije_timing_hw_lw

time of high water and low water
c.f. savenije 2012

24.5 tide-savenije

25 tide

analysis prediction of tides in rivers and estuaries by empirical
and theoretical methods

25.1 tide_low_high_exp

25.2 tide_low_high_tri