

Manual for Package: tide

Karl Kastner

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1 @T_Tide

1.1 T_Tide

wrapper for TPX0 generated tidal time series

1.2 build_index

build a structure whose field names contain the index

1.3 from_tpxo

read TPX0 output into tidetable object

1.4 get_constituents

extract constituents of tpxo object

1.5 reorder

order constituents as specified by "name"

1.6 select

select a subset of constituents

1.7 shift_time_zone

shift phase according to time zone

2 @Tidal_Envelope

2.1 Tidal_Envelope

process tidal data to extract the tidal envelope

2.2 init

initialize with data

3 @Tide_wft

3.1 Tide_wft

wavelet transform of tidal time series

3.2 transform

```
wavelet transform tidal time series
input:
time   : [1xn] abszissa of input vector, for example time, must be
         equally spaced
val    : [1xn] signal, input data series (e.g water level or
         velocity)
F      : [1xm] base frequencies, 1, 1, 2, ... for mean level,
         diurnal, semidirunal ...
         base periods from base frequencies  $T=1/F$ 
n      : [1xm] wavelet window length in multiple of periods
fc, nc : [scalar] low frequency cutoff and window length in periods
winstr : [char] fourier windows (kaiser (recommended), hanning, box
         , etc)
dt_max : [scalar] maximum time to fill gaps in input data series (
         recommended 3/24 for tide)
output:
tide   : struct with fields
         w_coeff : [1xn] wavelet coefficients (complex)
         amplitude : amplitude
         phase    : phase
         range    :
         h_tide   :
         h_low    :
         h
```

4 @Tidetable

4.1 Tidetable

```
Tide table
```

4.2 analyze

```
extract tidal envelope from time series
```

4.3 export_csv

```
export tide table to csv file
```

4.4 generate

run TPX0 to generate time series

4.5 generate_tpxo_input

generate tpxo input table
Note: superseded by perl script

4.6 import_tpxo

import TPX0 data into tidetable object

4.7 plot_neap_spring

plot average neap and spring tide

5

5.1 constituents

5.2 doodson

frequency of tidal constituents
method of doodson
source: wikipedia

5.3 envelope_amplitude

compute envelopes of hw and low water

5.4 envelope_slack_water

slack water envelope of the tide

5.5 interval_extrema

times and elevations for high and low water

5.6 interval_extrema2

minimum and maximum within intervals of constant length,
intended for periodic functions

5.7 interval_zeros

times of slack water determined from velocity u

5.8 lunar_phase

lunar phase

5.9 rayleigh_criterion

rayleigh criterion for resolving tidal constituents
 $T > 1/|f_1 - f_2|$

6 river-tide/@River_Tide

6.1 River_Tide

river tide in a single 1D channel

6.2 bcfun

boundary conditions

6.3 decompose

decompose the tide into a right and left travelling wave,
i.e. into incoming and reflected wave

6.4 friction_coefficient_dronkers

friction coefficient

6.5 friction_coefficient_godin

friction coefficient of Godin

6.6 friction_coefficient_lorentz

Loren't friction coefficient
c.f. cai
c.f. dronkers

6.7 friction_dronkers

friction determined by Dronker's method

6.8 friction_exponential_dronkers

friction computed by dronkers method

6.9 friction_godin

compute friction by the method of Godin

6.10 friction_trigonometric_dronkers

friction computed by dronkers method
expressed as Fourier series coefficients
c.f. dronkers 1964 eq 8.2 and 8.4
Note: Cai dennominates alpha as phi

6.11 friction_trigonometric_godin

friction computed by the method of godin
expressed in fourier series coefficients

6.12 friction_trigonometric_lorentz

friction computed by the method of Lorent's
expressed as Fourier series coefficients

6.13 init

solve backwater equation for surface level
TODO this should not be solved as a ivp but included in the bvp
iteration
TODO generate the mesh here and precompute fixed values instead of
passing functions

6.14 mwl_offset

offset of the tidally averaged surface elevation caused by tidal
friction
Linear estimate of the mean water level offset (ignoring feed-back
of tide)

6.15 odefun

coefficients of the backwater and wave equation for river-tides

6.16 odefun0

coefficients of the backwater equation for the river tide

6.17 odefun1

differential equation coefficients of the main tidal species
 $f_1 Q'' + f_2 Q' + f_3 Q + f_4 = 0$

6.18 odefun2

ordinary differential equation coefficients of the even overtide

6.19 q2z

tidal component of surface elevation determined from tidal
discharge

by continuity

$\% \quad dz/dt + dq/dx = 0$
 $\Rightarrow i \omega z = - dq/dx$
 $\Rightarrow z = -1/(i\omega) dq/dx$
 $\Rightarrow z = 1i/\omega dq/dx$

TODO allow Q as input

6.20 solve

call stationary or non-stationary solver respectively

6.21 solve_swe

determine river tide by the fully non-stationary FVM and then
extract the tide

6.22 solve_wave

solve for the oscillatory (tidal) componets

6.23 wave_number_analytic

analytic expression of the wave number

valid for both tidally, river dominated and low friction conditions
and converging channels

k : complex wave number in a reach with constant width and bed
slope

$\text{im}(k)$: damping modulus (rate of amplitude change)

$\text{re}(k)$: actual wave number (rate of phase change)

c.f. derive_wave_number

6.24 wave_number_approximation

approximate wave number of the left and right traveling wave for
variable coefficients

7 river-tide/@River_Tide_Cai

7.1 Gamma

Gamma parameter for tidal propagation
c.f. Cai 2014

7.2 River_Tide_Cai

prediction of river tide by the method of Cai (2014)

7.3 river_tide_cai_

determine the surface amplitude of the river tide
c.f. Cai

7.4 rt_quantities

determine the quantities that determine the tidal propagation
c.f. Cai

Note: this computes 4 unknowns following Cai, however,
lambda, mu and epsilon can be substituted
making it an equation in one unknown (delta) only

8 river-tide/@River_Tide_Empirical

8.1 River_Tide_Empirical

class for fitting models to at-a-station time series of tidal
elevation

8.2 fit_amplitude

fit the oscillatory components

8.3 fit_mwl

fit the tidally averaged water level

8.4 fit_phase

fit the phase of the oscillatory components

8.5 fit_range

fit the tidal range

8.6 predict_amplitude

predict the oscillatory components

8.7 predict_mwl

predict the mean water level

8.8 predict_phase

predict tidal phase

8.9 predict_range

predict the tidal range

8.10 rt_model

select the model for fitting

9 river-tide/@River_Tide_Map

9.1 River_Tide_Map

container class to store individual river tide scenarios

9.2 d2au1_dx2

second derivative of the tidal velocity magnitude

note: this is for finding zeros,
the true derivative has to be scaled up by z

9.3 d2az1_dx2

second derivative of the tidal surface elevation

note: this is for finding zeros,
the true derivative has to be scaled up by z

9.4 dkq_dx

along-channel derivative of the wave number of the discharge
neglects width variation

TODO, rederive with g as variable

9.5 dkz_dx

along channel derivative of the wave number of the tidal surface
elevation
ignores width variation dh/dx and second order depth variation (d^2h/dx^2)
TODO rederive with g symbolic

9.6 fun

compute a specific river tide scenario and store it in the hash,
or retrieve the scenario, if it was already computed

9.7 key

key for storing a scenario

9.8 plot

plot result

10 river-tide/@Tidal_River_Network

10.1 Tidal_River_Network

tide in a fluvial delta channel network, extension of 1D river tide
the network is a directed graph

10.2 discharge_amplitude

discharge amplitude

10.3 mean_water_level

predict the mean water level

10.4 plot_mean_water_level

plot tidally averaged water level

10.5 plot_water_level_amplitude

plot surface elevation amplitude

10.6 solve

solve for the tide in a fluvial chanel network

boundary condition at end points not connected to junctions

```
[ channel 1 id, endpoint id (1 or 2), s0, c0  
...  
channel n id, endpoint id (1 or 2), s0, c0]
```

conditions at junctions are specified as cells

```
each cell contains an nx2 array  
n : number of connecting channels  
[channel id1, endpoint id (1 or 2), ...  
channel idn, endpoint id (1 or 2)]
```

every tidal species for each channel has 4 unknowns

these are 2x2 unknowns for the sin + cos of left and right going
wave

10.7 water_level_amplitude

predict the surface elevation amplitude

11 river-tide/River_Tide_JK

11.1 River_Tide_JK

11.2 jk_damping_modulus

damping modulus of the river tide
c.f. Jay and Kukulka

11.3 jk_mean_level

tidally averaged surface elevation
c.f. Jay and Kukulka

11.4 jk_rivertide_predict

predict river tide by the method of jay and kukulka

11.5 jk_rivertide_regress

Regression of tidal coefficients according to Jay & Kukulka

coefficients of the r-regression factor 2 apart for specis (jay C7)
this can be repeated for each tidal species (diurnal, semidiurnal)

11.6 jk_tidal_discharge

tidal discharge
c.f. Jay and Kukulka

11.7 jk_tidal_range

predict tidal range

12 river-tide

analysis and prediction of river tides

12.1 damped_wave_bvp

analytic solution to the river tide formulated as boundary value
problem
in a river with finite length

c.f. Godin 1986

12.2 damped_wave_ivp

linearly damped wave in rectangular channel
 $x_t = Ax + b$

12.3 damping_modulus_river

damping modulus of the tidal wave for river flow only

12.4 damping_modulus_tide

damping modulus of the tide without river flow
c.f. friedrichs, ippen harleman
output :
k : wave number
re(k) : rate of phase change
im(k) : damping rate

12.5 rdamping_to_cdrag_tide

converts damping rate to drag coefficient
c.f. friedrichs, ippen harleman

12.6 rt_celerity

celerity of the tidal wave

12.7 rt_quasi_stationary_complex

quasi-stationary solution of the SWE
TODO staggered grid does not help: q1' needed

12.8 rt_quasi_stationary_trigonometric

quasi stationary form of the SWE

12.9 rt_reflection_coefficient_gradual

reflection coefficient for gradual varying cross section geometry
without damping

12.10 rt_wave_equation

solve river tide as boundary value problem

input:
omega : [nfx1] angluar frequency of tidal component, zero for mean
flow
reach : [nrx1] struct
.L : [1x1] length of reaches
.width(x,h) width
.bed(x,h) bed level
.surface(x,h) surface elevation
.Cd(x,h) drag coefficient
.bc : [nd,nf] boundary/junction conditions
bc(id,if).type : {surface, velocity, discharge} (dirichlet)
bc(id,if).val : value
opt : [1x1] struct
- constant surface elevation
- deactivative advective acceleration
.dx : spatial resolution

dimensions:
nr : nurmber or reaches
nd : upstream/downstream index
nf : frequency index

12.11 `rt_z2q`

determine tidal discharge from water level for tidal wave

12.12 `test_rt_wave_number`

12.13 `tidal_ellipse`

tidal ellipse, numerical ode solution

12.14 `wavetrainz`

determine river tide by iterated integration of the surface
elevation

12.15 `wavetwopassz`

two pass solution for the linearised wave equation, for surface
elevation

13 `test`

13.1 `test_tidal_harmonic_analysis`

14

14.1 `tidal_constituents`

14.2 tidal_energy_transport_1d

energy transport of a tidal wave

14.3 tidal_envelope

envelope of the tide

```
input : t time in days
        f surface elevation
output: tl time of low water
        vl surface elevation at low water
        ldx index of low water
        th time of high water
        vh surface elevation at high water
        hdx index of high water
        ndx neap index
        sdx spring index
        dmax:
        drange: range per day
```

14.4 tidal_envelope2

surface levelation envelope of the tide
low water, high water and tidal range for lunar each day

```
input:
    time :
    L     : surface elevation
    order : interpolation order (default 2)
output:
    timei : vector eqispaced
    lmini : minimum level
    lmaxi : maximum level
    rangei : range
    midrangei : (min + max)/2, usually different from mean
    phii : pseudo phase
```

Note: the pseudo phase ϕ jumps, this is because if the tide is semidiurnal, sometimes the lower hw becomes the next day higher than than the current high water, e.g. there is no smooth transition by

51min but a jump by 12h

14.5 tidal_harmonic_analysis

tidal_harmonic analysis

15 tide-savenije

15.1 savenije_phase_lag

phase lag of high and low water

ϕ : $u_{\text{river}}/u_{\text{tide}} < 1$

$\Delta t_{\text{eps_hw}} = \omega(t_{\text{hws}} - t_{\text{hw}})$

$\Delta t_{\text{eps_hw}} = \omega(t_{\text{lws}} - t_{\text{lw}})$

c.f. savenije

15.2 savenije_tidal_range

tidal range

based on Savenije 2012

x : distance to river mouth

η : range

η_0 : range at river mouth

\bar{h} : mean water depth

ϕ : velocity ratio $u_{\text{tide}}/u_{\text{river}}$

note: this varies in strongly convergent estuaries

K : mannings coefficient

I : residual surface slope I

15.3 savenije_tidal_range1

tidal range

based on Horrevoets/Savenije, 2004

H0 : tidal range at river mouth
h0 : initial water depth
v : velocity scale
b : convergence length
sine : phase lag
K : Mannings coefficient
Q_r : river discharge

15.4 savenije_timing_hw_lw

time of high water and low water
c.f. savenije 2012

15.5 tide-savenije