

Manual for Package: tide

Revision 24M

Karl Kästner

May 2, 2021

Contents

| | | |
|----------|-------------------------------|-----------|
| 1 | @T_Tide | 7 |
| 1.1 | T_Tide | 7 |
| 1.2 | build_index | 7 |
| 1.3 | from_tpxo | 8 |
| 1.4 | get_constituents | 8 |
| 1.5 | reorder | 8 |
| 1.6 | select | 8 |
| 1.7 | shift_time_zone | 8 |
| 2 | @Tidal_Envelope | 8 |
| 2.1 | Tidal_Envelope | 8 |
| 2.2 | init | 8 |
| 3 | @Tide_wft | 9 |
| 3.1 | Tide_wft | 9 |
| 3.2 | transform | 9 |
| 4 | @Tidetable | 9 |
| 4.1 | Tidetable | 9 |
| 4.2 | analyze | 10 |
| 4.3 | export_csv | 10 |
| 4.4 | generate | 10 |
| 4.5 | generate_tpxo_input | 10 |
| 4.6 | import_tpxo | 10 |
| 4.7 | plot_neap_spring | 10 |
| 5 | tide | 10 |
| 5.1 | constituents | 10 |
| 5.2 | doodson | 11 |
| 5.3 | envelope_amplitude | 11 |

| | | |
|----------|--|-----------|
| 5.4 | envelope_slack_water | 11 |
| 5.5 | interval_extrema | 11 |
| 5.6 | interval_extrema2 | 11 |
| 5.7 | interval_zeros | 11 |
| 5.8 | lunar_phase | 11 |
| 5.9 | rayleigh_criterion | 12 |
| 6 | river-tide/@Bifurcation | 12 |
| 6.1 | Bifurcation | 12 |
| 6.2 | confluence_rule | 12 |
| 6.3 | sediment_division | 12 |
| 6.4 | sediment_division_geometric | 12 |
| 7 | river-tide/@River_Tide | 12 |
| 7.1 | River_Tide | 15 |
| 7.2 | check_continuity | 15 |
| 7.3 | check_momentum | 15 |
| 7.4 | coefficient_frequency_components | 15 |
| 7.5 | d2au1_dx2 | 15 |
| 7.6 | d2az1_dx2 | 16 |
| 7.7 | decompose | 16 |
| 7.8 | derive_lorentz | 16 |
| 7.9 | discharge2level | 16 |
| 7.10 | dkq_dx | 16 |
| 7.11 | dkz_dx | 17 |
| 7.12 | energy | 17 |
| 7.13 | even_overtide_analytic | 17 |
| 7.14 | fourier_derivative | 17 |
| 7.15 | friction_coefficient | 17 |
| 7.16 | friction_coefficient_dronkers | 17 |
| 7.17 | friction_coefficient_godin | 18 |
| 7.18 | friction_coefficient_lorentz | 18 |
| 7.19 | friction_dronkers | 18 |
| 7.20 | friction_exponential_dronkers | 19 |
| 7.21 | friction_godin | 19 |
| 7.22 | friction_lorentz | 19 |
| 7.23 | friction_quadratic | 19 |
| 7.24 | friction_trigonometric_dronkers | 19 |
| 7.25 | friction_trigonometric_godin | 19 |
| 7.26 | friction_trigonometric_lorentz | 20 |
| 7.27 | mwL_offset | 20 |
| 7.28 | mwL_offset_2 | 20 |
| 7.29 | mwL_offset_analytic | 20 |
| 7.30 | odefun | 20 |

| | | |
|-----------|---|-----------|
| 7.31 | odefunQ0 | 20 |
| 7.32 | odefun_advective_acceleration | 20 |
| 7.33 | odefun_friction | 21 |
| 7.34 | odefun_ghof | 21 |
| 7.35 | odefun_swe_jacobian | 21 |
| 7.36 | odefun_width | 21 |
| 7.37 | odefunk_1 | 21 |
| 7.38 | odefunk_1_ | 21 |
| 7.39 | odefunk_2 | 22 |
| 7.40 | odefunk_3 | 22 |
| 7.41 | odefunz0 | 22 |
| 7.42 | wave_number_analytic | 22 |
| 7.43 | wave_number_approximation | 22 |
| 8 | river-tide/@River_Tide_Cai | 23 |
| 8.1 | Gamma | 23 |
| 8.2 | River_Tide_Cai | 23 |
| 8.3 | river_tide_cai_ | 23 |
| 8.4 | rt_quantities | 23 |
| 9 | river-tide/@River_Tide_Channel | 23 |
| 9.1 | River_Tide_Channel | 23 |
| 9.2 | bcfun | 24 |
| 9.3 | check_continuity | 24 |
| 9.4 | decompose | 24 |
| 9.5 | extract | 24 |
| 9.6 | initial_value | 25 |
| 9.7 | odefun | 25 |
| 9.8 | postprocess | 25 |
| 9.9 | sediment_transport | 25 |
| 9.10 | transform_bc | 25 |
| 10 | river-tide/@River_Tide_Empirical | 25 |
| 10.1 | River_Tide_Empirical | 25 |
| 10.2 | fit_amplitude | 26 |
| 10.3 | fit_mwl | 26 |
| 10.4 | fit_phase | 26 |
| 10.5 | fit_range | 26 |
| 10.6 | predict_amplitude | 26 |
| 10.7 | predict_mwl | 26 |
| 10.8 | predict_phase | 26 |
| 10.9 | predict_range | 26 |
| 10.10 | rt_model | 27 |

| | |
|---|-----------|
| 11 river-tide/@River_Tide_Hydrodynamics_Map | 27 |
| 11.1 River_Tide_Hydrodynamics_Map | 27 |
| 11.2 fun | 27 |
| 11.3 plot | 27 |
| 12 river-tide/@River_Tide_IVP | 27 |
| 12.1 solve | 27 |
| 13 river-tide/@River_Tide_JK | 27 |
| 13.1 River_Tide_JK | 27 |
| 13.2 damping_modulus | 28 |
| 13.3 mean_level | 28 |
| 13.4 rivertide_predict | 28 |
| 13.5 rivertide_regress | 28 |
| 13.6 tidal_discharge | 28 |
| 13.7 tidal_range | 28 |
| 14 river-tide/@River_Tide_Morphodynamics_Map | 29 |
| 14.1 River_Tide_Morphodynamics_Map | 29 |
| 14.2 fun | 29 |
| 15 river-tide/@River_Tide_Network | 29 |
| 15.1 River_Tide_Network | 29 |
| 15.2 dzb_dt | 29 |
| 15.3 evolve_bed_level | 29 |
| 15.4 evolve_bed_level_scenario | 29 |
| 15.5 generate_delft3d | 29 |
| 15.6 init | 30 |
| 15.7 mg_interpolate | 30 |
| 15.8 mg_prepare | 30 |
| 15.9 mg_restrict | 30 |
| 15.10 mg_step | 30 |
| 15.11 read_cfg | 30 |
| 15.12 sediment_transport | 30 |
| 15.13 solve | 30 |
| 16 river-tide/@River_Tide_Network_Simple | 31 |
| 16.1 River_Tide_Network_Simple | 31 |
| 16.2 discharge_amplitude | 31 |
| 16.3 mean_water_level | 31 |
| 16.4 plot_mean_water_level | 31 |
| 16.5 plot_water_level_amplitude | 31 |
| 16.6 solve | 31 |
| 16.7 water_level_amplitude | 32 |

| | |
|---|-----------|
| 17 river-tide/@River_Tide_SWE | 32 |
| 17.1 solve | 32 |
| 18 river-tide | 32 |
| 18.1 damped_wave_bvp | 32 |
| 18.2 damped_wave_ivp | 33 |
| 18.3 damping_modulus_river | 33 |
| 18.4 rdamping_to_cdtag_tide | 33 |
| 18.5 river_tide_godin | 33 |
| 18.6 river_tide_transport_scale | 33 |
| 18.7 river_tide_transport_scale_5 | 33 |
| 18.8 rt_celerity | 33 |
| 18.9 rt_quasi_stationary_complex | 34 |
| 18.10 rt_quasi_stationary_trigonometric | 34 |
| 18.11 rt_reflection_coefficient_gradual | 34 |
| 18.12 rt_transport | 34 |
| 18.13 rt_wave_equation | 34 |
| 18.14 rt_z2q | 35 |
| 18.15 tidal_ellipse | 35 |
| 18.16 tide_slack_exp | 35 |
| 18.17 wave_number_tide | 35 |
| 18.18 wavetrainz | 35 |
| 18.19 wavetwopassz | 35 |
| 19 test/river-tide-hydrodynamics | 36 |
| 19.1 example_river_tide | 36 |
| 19.2 example_river_tide_map | 36 |
| 19.3 example_river_tide_read_cfg | 36 |
| 19.4 hydrodynamic_scenario | 36 |
| 19.5 river_tide_test_plot | 36 |
| 19.6 test_bvp2c2 | 36 |
| 19.7 test_bvp2c_sym | 36 |
| 19.8 test_celerity | 36 |
| 19.9 test_characteristic_rate_of_change | 36 |
| 19.10 test_complex_even_overtide | 37 |
| 19.11 test_dronkers_compound | 37 |
| 19.12 test_fourier_power_exp | 37 |
| 19.13 test_friction | 37 |
| 19.14 test_friction_dronkers | 37 |
| 19.15 test_friction_dronkers2 | 37 |
| 19.16 test_fv_compare_schemes | 37 |
| 19.17 test_fv_convergence | 37 |
| 19.18 test_power_series | 37 |
| 19.19 test_reflection | 37 |

| | | |
|--|---|-----------|
| 19.20 | test_reflection_coefficient_gradual | 38 |
| 19.21 | test_ricatti | 38 |
| 19.22 | test_river_tide_hydrodynamics_01 | 38 |
| 19.23 | test_river_tide_hydrodynamics_02 | 38 |
| 19.24 | test_river_tide_hydrodynamics_03 | 38 |
| 19.25 | test_river_tide_hydrodynamics_04 | 38 |
| 19.26 | test_river_tide_hydrodynamics_05 | 38 |
| 19.27 | test_river_tide_hydrodynamics_06 | 38 |
| 19.28 | test_river_tide_hydrodynamics_07 | 38 |
| 19.29 | test_river_tide_hydrodynamics_08 | 39 |
| 19.30 | test_river_tide_hydrodynamics_09 | 39 |
| 19.31 | test_river_tide_hydrodynamics_10 | 39 |
| 19.32 | test_river_tide_hydrodynamics_11 | 39 |
| 19.33 | test_river_tide_hydrodynamics_12 | 39 |
| 19.34 | test_river_tide_hydrodynamics_13 | 39 |
| 19.35 | test_river_tide_hydrodynamics_14 | 39 |
| 19.36 | test_river_tide_hydrodynamics_15 | 39 |
| 19.37 | test_river_tide_hydrodynamics_50 | 39 |
| 19.38 | test_river_tide_hydrodynamics_60 | 40 |
| 19.39 | test_river_tide_hydrodynamics_90 | 40 |
| 19.40 | test_river_tide_hydrodynamics_batch | 40 |
| 19.41 | test_river_tide_metadata | 40 |
| 19.42 | test_river_tide_models | 40 |
| 19.43 | test_rt_d3d_evaluate | 40 |
| 19.44 | test_rt_reflection | 40 |
| 19.45 | test_rt_wave_number | 40 |
| 19.46 | test_rt_zs0 | 40 |
| 19.47 | test_swe | 40 |
| 19.48 | test_tidal_river_network | 41 |
| 19.49 | test_tidal_river_network_z0 | 41 |
| 19.50 | test_tide_slack_exp | 41 |
| 19.51 | test_wave_number_godin | 41 |
| 19.52 | test_wave_numer_aproximation | 41 |
| 19.53 | test_wave_twopass | 41 |
| 20 test/river-tide-morphodynamics | | 41 |
| 20.1 | rtm_plot | 41 |
| 20.2 | test_river_tide_morphodynamics_01 | 41 |
| 20.3 | test_river_tide_morphodynamics_02 | 41 |
| 20.4 | test_river_tide_morphodynamics_03 | 42 |
| 20.5 | test_river_tide_morphodynamics_04 | 42 |
| 20.6 | test_river_tide_morphodynamics_16 | 42 |
| 20.7 | test_river_tide_morphodynamics_17 | 42 |
| 20.8 | test_river_tide_morphodynamics_18 | 42 |

| | | |
|-----------|---|-----------|
| 20.9 | test_river_tide_transport_scale | 42 |
| 21 | test/river-tide-network | 42 |
| 21.1 | test_river_tide_network_01 | 42 |
| 21.2 | test_river_tide_network_02 | 42 |
| 21.3 | test_river_tide_network_03 | 42 |
| 21.4 | test_river_tide_network_04 | 43 |
| 21.5 | test_river_tide_network_05 | 43 |
| 22 | test | 43 |
| 22.1 | test_rt_transport | 43 |
| 22.2 | test_stokes_transport | 43 |
| 22.3 | test_tidal_harmonic_analysis | 43 |
| 23 | tide | 43 |
| 23.1 | tidal_constituents | 43 |
| 23.2 | tidal_energy_transport_1d | 43 |
| 23.3 | tidal_envelope | 44 |
| 23.4 | tidal_envelope2 | 44 |
| 23.5 | tidal_harmonic_analysis | 44 |
| 23.6 | tidal_range_exp | 45 |
| 23.7 | tidal_range_tri | 45 |
| 24 | tide-savenije | 45 |
| 24.1 | savenije_phase_lag | 45 |
| 24.2 | savenije_tidal_range | 45 |
| 24.3 | savenije_tidal_range1 | 46 |
| 24.4 | savenije_timing_hw_lw | 46 |
| 24.5 | tide-savenije | 46 |
| 25 | tide | 46 |
| 25.1 | tide_low_high_exp | 46 |
| 25.2 | tide_low_high_tri | 46 |

1 @T_Tide

1.1 T_Tide

wrapper for TPX0 generated tidal time series

1.2 build_index

build a structure whose field names contain the index

1.3 from_tpxo

read TPXO output into tidetable object

1.4 get_constituents

extract constituents of tpxo object

1.5 reorder

order constituents as specified by "name"

1.6 select

select a subset of constituents

1.7 shift_time_zone

shift phase according to time zone

2 @Tidal_Envelope

2.1 Tidal_Envelope

process tidal data to extract the tidal envelope

2.2 init

initialize with data

3 @Tide_wft

wavelet analysis of tidal data

3.1 Tide_wft

wavelet transform of tidal time series

3.2 transform

wavelet transform tidal time series

input:

time : [1xn] abszissa of input vector, for example time, must be
equally spaced

val : [1xn] signal, input data series (e.g water level or
velocity)

F : [1xm] base frequencies, 1, 1, 2, ... for mean level,
diurnal, semidirunal ...

base periods from base frequencies $T=1/F$

n : [1xm] wavelet window length in multiple of periods

fc, nc : [scalar] low frequency cutoff and window length in periods

winstr : [char] fourier windows (kaiser (recommended), hanning, box
, etc)

dt_max : [scalar] maximum time to fill gaps in input data series (
recommended 3/24 for tide)

output:

tide : struct with fields

w_coeff : [1xn] wavelet coefficients (complex)

amplitude : amplitude

phase : phase

range :

h_tide :

h_low :

h

4 @Tidetable

class for generating tidetable data

4.1 Tidetable

Tide table

4.2 analyze

extract tidal envelope from time series

4.3 export_csv

export tide table to csv file

4.4 generate

run TPX0 to generate time series

4.5 generate_tpxo_input

generate tpxo input table
Note: superseded by perl script

4.6 import_tpxo

import TPX0 data into tidetable object

4.7 plot_neap_spring

plot average neap and spring tide

5 tide

analysis prediction of tides in rivers and estuaries by empirical
and theoretical methods

5.1 constituents

5.2 doodson

frequency of tidal constituents
method of doodson
source: wikipedia

5.3 envelope_amplitude

compute envelopes of hw and low water

5.4 envelope_slack_water

slack water envelope of the tide

5.5 interval_extrema

times and elevations for high and low water

5.6 interval_extrema2

minimum and maximum within intervals of constant length,
intended for periodic functions

5.7 interval_zeros

times of slack water determined from velocity u

5.8 lunar_phase

lunar phase

5.9 rayleigh_criterion

raleigh criterion for resolving tidal constituents
 $T > 1/|f_1 - f_2|$

6 river-tide/@Bifurcation

6.1 Bifurcation

6.2 confluence_rule

6.3 sediment_division

6.4 sediment_division_geometric

7 river-tide/@River_Tide

predict tide in a backwater affected river with a sloping/varying
bed

Assumptions and capabilities:

- tidal dynamics follow the 1D-Shallow-Water-Equation
(depth and cross-sectionally averaged Navier-Stokes-
Equation)
- rectangular cross section
- width can vary along the channel
- friction coefficient (cd) constant along channel and over
time (Chezy)
- advective acceleration term is considered, but can be
deactivated
- vertical profile of streamwise velocity is constant
(Boussinesq coefficient is unity (1))

Limitations / TODO list:

- single channel dynamics only (no tidal networks)
 - no wind-shear stress (no storm surges)
 - no tidal flats / intertidal areas (width constant in time)
 - no flood-plain during high-river flow
 - no stratification or along-channel salinity gradient
 - negligible head loss in channel bends
 - negligible feed-back of the sediment concentration on the propagation of the tide
 - low Froude Number (no hydraulic jumps due to cataracts or tidal bores)
-
- At present, only two tidal components are supported (either D1 with D2 or D2 with D4, in addition to the mean water level z_0), for mixed diurnal-semidiurnal cases with dominant semidiurnal component, the class has to be extended to support three components (D1, D2 and D4)
 - At present, the tripel overtide is not computed (D3 for diurnal, D6 for semidiurnal tide), note that this is the main overtide for the case of low river flow
 - At present, the $1/h$ non-linearity is only included in the approximations of the backwater curve, but not it's influence on the tidal frequency components

Method:

This class calls numerical solvers for second order ordinary differential equation boundary value problems

Tides is represented as exponential series in form of total discharge $Q = \sum Q_i = Q_0 + Q_1 + Q_2$, as discharge is conserved (balanced), the equations are simpler than for level z and velocity u , and the frequency components of z are straight forward determined by differentiation of Q

Class and function structure:

```
River_Tide :  
    computes river tide, provides the ode coefficients to  
    the boundary value solver  
bvp2c, bvp2fdm :  
    solve the underlying second order boundary value  
    problem
```

River_Tide_Map :
 provides convenient batch runs and processing of
 River_Tide instances

Minimum working example, c.f. example_rive_tide.m and
 example_river_tide_map.m

input:

Q0 : scalar, river discharge (m^3/s)
 omega : scalar, angular frequency main tidal species in (1/
 seconds)
 x : 2x1 vector, left and right end of computational
 domain of the river (m)
 w(x) : function of width along the river (m)
 cd(x) : function of drag coefficient along the river (1)
 zb(x) : function of bed level along the river (m)

opt : structure with options
 opt.model_str = 'wave' (other solver are not supported at the
 moment)
 opt.solver = @bvp2c or @bvp2fdm
 opt.nx : number of grid points along channel
 opt.ns : base for logarithmic spacing of grid points, 1 :
 linear spacing

bc : structure array of boundary conditions
 r, row 1..2 : left and right end, respectively
 c, column 1 : mean (river) component
 2..n : condition form column-1 frequency
 component

$$\begin{pmatrix} q(1)*(p(1) y^-(x_0) + p(2) dy^-/dx(x_0) \dots \\ + q(2)*(p(1) y^+(x_0) + p(2) dy^+/dx(x_0)) = bc(c \\ ,r).val \\ = val(0) \end{pmatrix}$$

bc(c,r).var : Quantity, either 'z' or 'Q'
 bc(c,r).val : complex amplitude of chosen variable
 (c.f. (1 + 0i) [m] for surface elevation
 amplitude of 1m)
 (value has to be real for mean component)
 mean component requires z and Q to be specified
 at opposit ends

bc(c,r).p : factor for Dirichlet p(1) or Neumann p(2)
 condition
 p = [1,0] : pure Dirichlet
 p = [0,1] : pure Neumann
 sum of abs(p) must be nonzero for each end and

each frequency component
`bc(c,r).q` : factor for left and right going wave, only
 available for `bvp2c`
`q = [1,1]` : total water level / discharge
`q = [1,0]` : only left going wave
`q = [0,1]` : only right going wave
`q` has no meaning for the mean component and is
 ignored
`q` is only supported by `bvp2c`,
`bvpfdm` uses default `q = [1,1]`
 sum of `abs(q)` for each frequency component must
 be zero

7.1 River_Tide

physical functions for computation of river tides in a single 1D
 channel
 combined with BVP-solver in child-classes to determine the
 hydrodynamics

7.2 check_continuity

7.3 check_momentum

7.4 coefficient_frequency_components

7.5 d2au1_dx2

second derivative of the tidal velocity magnitude

note: this is for finding zeros,
 the true derivative has to be scaled up by `z`

7.6 d2az1_dx2

second derivative of the tidal surface elevation

note: this is for finding zeros,
the true derivative has to be scaled up by z

7.7 decompose

decompose the tide into a right and left travelling wave,
i.e. into incoming and reflected wave
TODO subtract forcing term

7.8 derive_lorentz

7.9 discharge2level

determines tidal water surface amplitude (non-zero frequency
components of surface elevation)
from tidal discharge (non-zero frequency components of the
discharge)

by continuity :

$$\begin{aligned} dz/dt + dq/dx &= 0 \\ \Rightarrow i \omega z &= - dq/dx \\ \Rightarrow z &= -1/(i\omega) dq/dx \\ \Rightarrow z &= 1i/\omega dq/dx \end{aligned}$$

7.10 dkq_dx

along-channel derivative of the wave number of the discharge
neglects width variation

TODO, rederive with g as variable

7.11 dkz_dx

along channel derivative of the wave number of the tidal surface
elevation
ignores width variation dh/dx and second order depth variation (d^2h/dx^2)
TODO rederive with g symbolic

7.12 energy

7.13 even_overtide_analytic

7.14 fourier_derivative

7.15 friction_coefficient

```
function cf = friction_coefficient(obj,Qmid,Qhr)
```

7.16 friction_coefficient_dronkers

friction coefficient according to Dronkers

the coefficients are semi-autogenerated

c.f. dronkers 1964

c.f. Cai 2016

```
p = [p0,p1,p2,p3];
```

```
alpha = Ur/Ut = river velocity / tidal velocity amplitude = (umax+  
umin)/(umax-umin)
```

```
function p = friction_coefficient_dronkers(alpha,order)
```

7.17 friction_coefficient_godin

friction coefficient according to Godin
these coefficients are identical to Dronker's for $U_R = \phi = 0$

```
function G = friction_coefficient_godin(obj,phi)
```

7.18 friction_coefficient_lorentz

coefficients of the Fourier expansion of the signed square of the $|Q|Q$
of the friction term

Lorentz used this first for the case of no river flow

identical to Dronker's coefficient for zero river flow
and a single frequency component
c.f. Cai
c.f. Dronkers ($\gamma = \alpha$)

note difference in coefficients due to different definitions:
definition used here:

$$Q = Q_0 + 1/2 * (\sum_k Q_k e(k i \omega t) + \text{conj}(Q_k e(k i \omega t)))$$

but Dronkers defines

$$Q = Q + \sum_k Q_k e(k i \omega t)$$

```
function L = friction_coefficient_lorentz(obj,phi)
```

7.19 friction_dronkers

friction determined by Dronker's method

input :

u : velocity time series
Umid : arithmetic mean of minimum and maximum velocity
(not the mean of the velocity, usually non-zero even
without river flow)
Uhr : half-range of the velocity, less than the sum of
the frequency amplitudes, except at perigean spring
tides

```
function [uau_sum uau p] = friction_dronkers(u,Umid,Uhr,order)
```

7.20 friction_exponential_dronkers

friction coefficients for the frequency components computed by
Dronkers method

c.f. Dronker's 1964 eq 8.2 and 8.4

Note: Cai denominates alpha as phi

```
function [c uau uau_p] = friction_trigonometric_dronkers(u,dp,Umid
,Uhr,order,psym)
```

7.21 friction_godin

compute friction with the method of Godin

7.22 friction_lorentz

7.23 friction_quadratic

friction determined by Dronker's method

7.24 friction_trigonometric_dronkers

friction computed by the method of Dronkers

expressed as coefficients for the frequency components

c.f. dronkers 1964 eq 8.2 and 8.4

Note: Cai denominates alpha as phi

7.25 friction_trigonometric_godin

friction computed by the method of Godin

expressed as coefficients of the frequency components (
trigonometric form)

Chebyshev coefficients for zero river flow

(albeit applied by Godin to cases with river flow)

c.f. godin 1990, table 1, column Ch

Note: the coefficients do indeed not (exactly) sum up to 1

Note: Godin tries several slightly different sets of coefficients,
of which the Chebysheff set is best

7.26 friction_trigonometric_lorentz

friction computed by the method of Lorent's
expressed as coefficients of the frequency components (
trigonometric form)

7.27 mwl_offset

offset of the tidally averaged surface elevation caused by tidal
friction
Linear estimate of the mean water level offset (ignoring feed-back
of tide)

7.28 mwl_offset_2

7.29 mwl_offset_analytic

7.30 odefun

coefficients of the wave equation for river-tides decomposed in
frequency components
zero frequency component corresponds to backwater equation with
tidal influence

7.31 odefunQ0

7.32 odefun_advective_acceleration

7.33 odefun_friction

7.34 odefun_ghof

7.35 odefun_swe_jacobian

Jacobian matrix of the Shallow-Water Equation
 $d(A,Q)/dt + J(A,Q) d(A,Q)/dx = \text{forcing terms}$

$$\begin{aligned} dA/dt + [0, 1] dA/dx &= [f_c] \quad (c) \\ dQ/dt + [-Q^2/A^2, 2 Q/A] dQ/dx &= [f_m] \quad (m) \end{aligned}$$

$$\begin{aligned} dm/dt \\ d^2Q/dt^2 - d/dt Q^2/A^2 - 2 d/dt (Q/A) dQ/dx &= d/dt f_m \\ d^2Q/dt^2 - d/dt Q^2/A^2 - 2 (1/A dQ/dt - Q/A^2 dA/dt) dQ/dx &= d/dt f_m \\ d^2Q/dt^2 - d/dt Q^2/A^2 - 2 (1/A dQ/dt + Q/A^2 dQ/dx) dQ/dx &= d/dt f_m \end{aligned}$$

$$\begin{aligned} ode &= -1/(g h w) d^2/dt^2 Q + 1/w d^2/dx^2 Q = 0 \\ &= -1 (iko)^2/(g h w) Q + 1/w Q'' \\ &= (k^2 o^2)/(g h w) Q + 1/w Q'' \end{aligned}$$

7.36 odefun_width

forcing by along-channel width-variation

7.37 odefunk_1

7.38 odefunk_1_

coefficients of the ordinary differential equation of the k-th
 frequency
 component of the tide

$$f1 Q'' + f2 Q' + f3 Q + f4 = 0$$

```
function [f, F3] = odefunk(obj, k, Q, QQ, Qhr, h0, dh0_dx, dz0_dx,
    w0, dw0_dx, Cd, c, D1_dx)
```

7.39 odefunk_2

7.40 odefunk_3

7.41 odefunz0

coefficients of the backwater equation for the river tide
 TODO merge with backwater class

7.42 wave_number_analytic

analytic expression of the wave number of river tides

valid for both tidally, river dominated and low friction conditions
 and converging channels

k10 : complex wave number for k and z in a reach with constant
 width and bed slope

im(k) : damping modulus (rate of amplitude change)

re(k) : actual wave number (rate of phase change)

kq : wave number for Q for a reach with changing width and depth

kz : wave number for z for a reach with changing width and depth

c.f. derive_wave_number

7.43 wave_number_approximation

approximate wave number of the left and right traveling wave for
variable coefficients

TODO merge with wave_number_analytic

```
function [k, k0, dk0_dx_rel, obj] = wave_numer_aproximation(obj)
```

8 river-tide/@River_Tide_Cai

Prediction of river tide by the method of Cai
c.f. Cai 2013, Cai 2015

8.1 Gamma

Gamma parameter for tidal propagation
c.f. Cai 2014

8.2 River_Tide_Cai

prediction of river tide by the method of Cai (2014)

8.3 river_tide_cai_

determine the surface amplitude of the river-tide
c.f. Cai

8.4 rt_quantities

determine the quantities that determine the tidal propagation
c.f. Cai

Note: this computes 4 unknowns following Cai, however,
lambda, mu and epsilon can be substituted
making it an equation in one unknown (delta) only

9 river-tide/@River_Tide_Channel

9.1 River_Tide_Channel

9.2 bcfun

Robin (mixed) boundary conditions for the river tide,
supplied for each frequency component,
wrapper that copies values are from the member struct "bc"

```
q*(p*Q_1^- + (1-p)*dQ_1^-/dx
input :
    cid : channel index
    bif : 1,2 : index for left/right end of channel
    fid : frequency component index
          (1 = 0 omega (mean), 2 : 1 omega, 3 : 2 omega, ... )
columns of bc : frequency
rows of bc, left, right boundary
output :
    p : [2x1] linear combination of Dirichlet and Neumann
        boundary condition
    p(1) -> weight Dirichlet boundary condition
    p(2) -> weight Neumann boundary condition
    q linear combination of left and right travelling (incoming and
        outgoing) wave
    q(1) weight left going wave
    q(2) weight right going wave
    rhs = 0 -> homogeneous boundary condition

function [rhs, p, q, obj] = bcfun(obj,cid,bid,fid)
```

9.3 check_continuity

compute residual for the continuity equation
 $dA/dt + dQ/dx = Q_{in}$

9.4 decompose

decompose the tide into a right and left travelling wave,
i.e. into incoming and reflected wave
TODO subtract forcing term

9.5 extract

extract values of individual variables from BVP-solver result
vector

9.6 initial_value

9.7 odefun

coefficients of the backwater and wave equation for river-tides

9.8 postprocess

postprocess hydrodynamic solver output

9.9 sediment_transport

compute sediment transport for a single channel

9.10 transform_bc

transform arbitrary to cs-integrated discharge boundary condition

10 river-tide/@River_Tide_Empirical

Empirical fit to measurement and prediction (from tide at sea and
river discharge)
of the river tide

10.1 River_Tide_Empirical

class for fitting models to at-a-station time series of tidal
elevation

10.2 fit_amplitude

fit the oscillatory components

10.3 fit_mwl

fit the tidally averaged water level

10.4 fit_phase

fit the phase of the oscillatory components

10.5 fit_range

fit the tidal range

10.6 predict_amplitude

predict the oscillatory components

10.7 predict_mwl

predict the mean water level

10.8 predict_phase

predict tidal phase

10.9 predict_range

predict the tidal range

10.10 rt_model

select the model for fitting

11 river-tide/@River_Tide_Hydrodynamics_Map

hash container for a set of River_Tide predictions for different boundary conditions

11.1 River_Tide_Hydrodynamics_Map

container class to store multiple river-tide scenarios

11.2 fun

compute river tide for a scenario with specific boundary conditions
and store it in the hash,
or retrieve the scenario, if it was already computed

11.3 plot

quick plot of scenario result

```
function obj = plot(obj,Xi,Q0,W0,S0,z1_downstream,cd,zb_downstream,  
    omega,q,opt)
```

12 river-tide/@River_Tide_IVP

12.1 solve

13 river-tide/@River_Tide_JK

empirical analysis and prediction of river tides by the method of
Jay and Kukulka

13.1 River_Tide_JK

13.2 damping_modulus

damping modulus of the river tide
c.f. Jay and Kukulka
function r = damping_modulus(obj,h0,b,Qr)

13.3 mean_level

tidally averaged surface elevation
c.f. Jay and Kukulka

13.4 rivertide_predict

predict river tide by the method of jay and kukulka
TODO rename

13.5 rivertide_regress

Regression of tidal coefficients according to Jay & Kukulka

coefficients of the r-regression factor 2 apart for specis (jay C7)
this can be repeated for each tidal species (diurnal, semidiurnal)

13.6 tidal_discharge

tidal discharge
c.f. Jay and Kukulka
function Qt = tidal_discharge(obj,x,R0,h0,b,Qr)

13.7 tidal_range

predict tidal range

14 river-tide/@River_Tide_Morphodynamics_Map

14.1 River_Tide_Morphodynamics_Map

container class to store multiple river-tide morphodynamics scenarios

14.2 fun

morphodynamics of a tidal river
either retrieve a precomputed scenario or compute and store a new scenario

15 river-tide/@River_Tide_Network

15.1 River_Tide_Network

hydrodynamics and morphodynamics of 1D tidal channel networks

15.2 dzb_dt

change of bed level over time, when width constant over time
$$dzb/dt + 1/(p \rho w) dQs/dx = 0$$

15.3 evolve_bed_level

evolve the bed level of the tidal river network over time

15.4 evolve_bed_level_scenario

shortcut function for batch simulation runs

15.5 generate_delft3d

generate a Delft3D 4 model for the channel network

15.6 init

```
initial condition  
function obj = init(obj)
```

15.7 mg_interpolate

15.8 mg_prepare

15.9 mg_restrict

15.10 mg_step

15.11 read_cfg

15.12 sediment_transport

```
compute sediment transport for the channel network, including  
    routing at  
junctions
```

15.13 solve

```
determine hydrodynamics
```

16 river-tide/@River_Tide_Network_Simple

16.1 River_Tide_Network_Simple

tide in a fluvial delta channel network, extension of 1D river tide
the network is a directed graph
TODO convert from trig-to exponential form

16.2 discharge_amplitude

discharge amplitude

16.3 mean_water_level

predict the mean water level

16.4 plot_mean_water_level

plot tidally averaged water level

16.5 plot_water_level_amplitude

plot surface elevation amplitude

16.6 solve

solve for the tide in a fluvial chanel network

boundary condition at end points not connected to junctions
[channel 1 id, endpoint id (1 or 2), s0, c0
...
channel n id, endpoint id (1 or 2), s0, c0]

conditions at junctions are specified as cells
each cell contains an nx2 array
n : number of connecting channels
[channel id1, endpoint id (1 or 2), ...

channel idn, endpoint id (1 or 2)]

every tidal species for each channel has 4 unknowns
these are 2x2 unknowns for the sin + cos of left and right going
wave

16.7 water_level_amplitude

predict the surface elevation amplitude

17 river-tide/@River_Tide_SWE

17.1 solve

determine river tide by the fully non-stationary FVM and then
extract the tide
this is experimental and not yet fully working

18 river-tide

analysis and prediction of river tides

Sub-Classes:

@River_Tide
- prediction of river tide in a backwater affected river with
a sloping bed
@River_Tide_Cai
- prediction of river tide, method of Cai
@River_Tide_Empirical
- prediction of river tide, empirical
@River_Tide_JK
- prediction of river tide, empirical after Jay and Kukulka
@River_Tide_Map
- multiple-scenarios container for River_Tide
@River_Tide_Network
- extension of River_Tide to networks

18.1 damped_wave_bvp

solved damped wave equation
 $z'' + a z = 0$
 $z(0) = z_0, z(L) = 0$

18.2 damped_wave_ivp

linearly damped wave in rectangular channel
solve tide as initial value problem
damped wave approximation

$$z'' + a z = 0$$

$$x_t = Ax + b$$

18.3 damping_modulus_river

damping modulus of the tidal wave for river flow only

18.4 rdamping_to_cdrag_tide

converts damping rate to drag coefficient
c.f. friedrichs, ippen harleman

18.5 river_tide_godin

analytic solution to the river tide formulated as boundary value
problem
in a river with finite length
c.f. Godin 1986

18.6 river_tide_transport_scale

18.7 river_tide_transport_scale_5

18.8 rt_celerity

celerity of the tidal wave

18.9 rt_quasi_stationary_complex

quasi-stationary solution of the SWE
TODO staggered grid does not help: q1' needed

18.10 rt_quasi_stationary_trigonometric

quasi stationary form of the SWE

18.11 rt_reflection_coefficient_gradual

reflection coefficient for gradual varying cross section geometry
without damping

18.12 rt_transport

18.13 rt_wave_equation

solve river tide as boundary value problem

input:
omega : [nfx1] angluar frequency of tidal component, zero for mean
flow
reach : [nrx1] struct
.L : [1x1] length of reaches
.width(x,h) width
.bed(x,h) bed level
.surface(x,h) surface elevation
.Cd(x,h) drag coefficient
.bc : [nd,nf] boundary/junction conditions
bc(id,if).type : {surface, velocity, discharge} (dirichlet)
bc(id,if).val : value
opt : [1x1] struct
- constant surface elevation
- deactivative advective acceleration
.dx : spatial resolution

dimensions:
nr : nurmber or reaches

nd : upstream/downstream index
nf : frequency index

18.14 rt_z2q

determine tidal discharge from water level for tidal wave
in contrast to the inverse, discharge to level,
this is not unique, due to the integration constant

18.15 tidal_ellipse

tidal ellipse, numerical ode solution

18.16 tide_slack_exp

18.17 wave_number_tide

wave number of the tide without river flow
c.f. friedrichs, ippen harleman
output :

k : wave number, such that
$$z(t,x) = z_1(t,0) \exp(1i*(\omega*t - k*x))$$

re(k) : rate of phase change
-im(k) : damping rate

function [k k_low k_high] = damping_modulus_tide(ω ,cd,h0,az1)

18.18 wavetrainz

determine river tide by iterated integration of the surface
elevation

18.19 wavetwopassz

two pass solution for the linearised wave equation, for surface
elevation

19 test/river-tide-hydrodynamics

19.1 example_river_tide

19.2 example_river_tide_map

19.3 example_river_tide_read_cfg

19.4 hydrodynamic_scenario

19.5 river_tide_test_plot

19.6 test_bvp2c2

19.7 test_bvp2c_sym

19.8 test_celerity

19.9 test_characteristic_rate_of_change

19.10 test_complex_even_overtide

19.11 test_dronkers_compound

19.12 test_fourier_power_exp

19.13 test_friction

19.14 test_friction_dronkers

19.15 test_friction_dronkers2

19.16 test_fv_compare_schemes

19.17 test_fv_convergence

19.18 test_power_series

19.19 test_reflection

19.20 test_reflection_coefficient_gradual

19.21 test_ricatti

19.22 test_river_tide_hydrodynamics_01

19.23 test_river_tide_hydrodynamics_02

19.24 test_river_tide_hydrodynamics_03

19.25 test_river_tide_hydrodynamics_04

19.26 test_river_tide_hydrodynamics_05

19.27 test_river_tide_hydrodynamics_06

19.28 test_river_tide_hydrodynamics_07

19.29 test_river_tide_hydrodynamics_08

```
hold on;  
plot(x,abs(z),'--');  
hold on;  
plot(x,angle(z),'--');
```

19.30 test_river_tide_hydrodynamics_09

19.31 test_river_tide_hydrodynamics_10

19.32 test_river_tide_hydrodynamics_11

19.33 test_river_tide_hydrodynamics_12

19.34 test_river_tide_hydrodynamics_13

19.35 test_river_tide_hydrodynamics_14

19.36 test_river_tide_hydrodynamics_15

19.37 test_river_tide_hydrodynamics_50

19.38 test_river_tide_hydrodynamics_60

19.39 test_river_tide_hydrodynamics_90

19.40 test_river_tide_hydrodynamics_batch

river tide test case batch run

19.41 test_river_tide_metadata

19.42 test_river_tide_models

19.43 test_rt_d3d_evaluate

19.44 test_rt_reflection

19.45 test_rt_wave_number

19.46 test_rt_zs0

19.47 test_swe

19.48 test_tidal_river_network

19.49 test_tidal_river_network_z0

19.50 test_tide_slack_exp

19.51 test_wave_number_godin

19.52 test_wave_numer_aproximation

19.53 test_wave_twopass

20 test/river-tide-morphodynamics

20.1 rtm_plot

20.2 test_river_tide_morphodynamics_01

20.3 test_river_tide_morphodynamics_02

20.4 test_river_tide_morphodynamics_03

20.5 test_river_tide_morphodynamics_04

20.6 test_river_tide_morphodynamics_16

20.7 test_river_tide_morphodynamics_17

20.8 test_river_tide_morphodynamics_18

20.9 test_river_tide_transport_scale

21 test/river-tide-network

21.1 test_river_tide_network_01

21.2 test_river_tide_network_02

21.3 test_river_tide_network_03

21.4 test_river_tide_network_04

21.5 test_river_tide_network_05

22 test

22.1 test_rt_transport

22.2 test_stokes_transport

22.3 test_tidal_harmonic_analysis

23 tide

analysis prediction of tides in rivers and estuaries by empirical
and theoretical methods

23.1 tidal_constituents

23.2 tidal_energy_transport_1d

energy transport of a tidal wave

23.3 tidal_envelope

envelope of the tide

```
input : t time in days
        f surface elevation
output : tl time of low water
        vl surface elevation at low water
        ldx index of low water
        th time of high water
        vh surface elevation at high water
        hdx index of high water
        ndx neap index
        sdx spring index
        dmax:
        drange: range per day
```

23.4 tidal_envelope2

surface levelation envelope of the tide
low water, high water and tidal range for lunar each day

```
input:
  time :
  L    : surface elevation
  order : interpolation order (default 2)
output:
  timei : vector eqispaced
  lmini : minimum level
  lmaxi : maximum level
  rangei : range
  midrangei : (min + max)/2, usually different from mean
  phii : pseudo phase
```

Note: the pseudo phase phi jumps, this is because if the tide is semidiurnal, sometimes the lower hw becomes the next day higher then than the current high water, e.g. there is no smooth transition by 51min but a jump by 12h

23.5 tidal_harmonic_analysis

tidal_harmonic analysis

23.6 tidal_range_exp

23.7 tidal_range_tri

24 tide-savenije

24.1 savenije_phase_lag

phase lag of high and low water

ϕ : $u_{\text{river}}/u_{\text{tide}} < 1$

$\Delta t_{\text{eps_hw}} = \omega \cdot (t_{\text{hws}} - t_{\text{hw}})$

$\Delta t_{\text{eps_hw}} = \omega \cdot (t_{\text{lws}} - t_{\text{lw}})$

c.f. savenije

24.2 savenije_tidal_range

tidal range

based on Savenije 2012

x : distance to river mouth

η : range

η_0 : range at river mouth

\bar{h} : mean water depth

ϕ : velocity ratio $u_{\text{tide}}/u_{\text{river}}$

note: this varies in strongly convergent estuaries

K : mannings coefficient

I : residual surface slope

24.3 savenije_tidal_range1

tidal range

based on Horrevoets/Savenije, 2004

H0 : tidal range at river mouth
h0 : initial water depth
v : velocity scale
b : convergence length
sine : phase lag
K : Mannings coefficient
Q_r : river discharge

24.4 savenije_timing_hw_lw

time of high water and low water
c.f. savenije 2012

24.5 tide-savenije

25 tide

analysis prediction of tides in rivers and estuaries by empirical
and theoretical methods

25.1 tide_low_high_exp

25.2 tide_low_high_tri