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MF850 Homework 3

$$Foc \Rightarrow (kv^{2} + (S - \partial yV)v)' = 0$$

$$\Rightarrow 2kv = -(S - \partial yV(S,y))$$

$$\Rightarrow v^{*} = \frac{1}{-2k}(S - \partial yV(S,y))$$

(b) we have
$$V(s,y) = ys + y^2h(s)$$

$$\begin{cases} \frac{\partial sV(s,y) = y^{2} + y^{2}h'}{\partial ssV(s,y) = y'h''} \Rightarrow \frac{1}{2}\sigma^{2}y^{2}h'' + \phi y^{2} + \min_{s} \{-vs - 2yh \cdot v + sv + kv^{2}\}^{2} = 0 \\ \frac{\partial s}{\partial y}V(s,y) = s + 2yh \qquad \qquad y^{2}(\frac{1}{2}\sigma^{2}h'' + \phi) + \min_{s} \{-2yhv + kv^{2}\}^{2} = 0 \\ \Rightarrow y^{2}(\frac{1}{2}\sigma^{2}h'' + \phi - \frac{h^{2}}{h}) = 0 \qquad \qquad y^{2} \neq 0 \end{cases}$$

$$= \frac{1}{2} \int (\frac{1}{2} \int (\frac{1}{2} \int \frac{1}{k} - \frac{1}{k}) = 0 , \quad \frac{1}{2} \int \frac{1}{2} \int \frac{1}{k} \frac{1}{k} = 0$$

=)
$$\frac{1}{2} \sigma^2 h'' + \phi + \min(-2\nu h + k\nu^2) = 0$$
, where $v^* = \frac{1}{k} h(s)$

And
$$h(\bar{s}) = \lambda$$

For the details, please see the code file CC)