

# Fundamentals of Air-Breathing Propulsion

Presented by:

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Georgia Institute of Technology  
*Aerospace Systems Design Laboratory*



# Module Outline

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## Thrust vs. Efficiency - basic concepts

### Turbojet Engine

**How it works**

**Thrust/SFC varying with Velocity/Altitude**

### Turbofan Engine

**How it works**

**Thrust/SFC varying with Velocity/Altitude**

### Turboprop

**How it works**

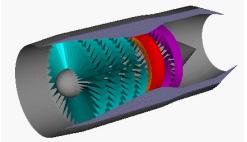
**Thrust/SFC varying with Velocity/Altitude**

### Reciprocating Engines with Prop

**How it works**

**Power/SFC varying with Velocity/Altitude**

# Trading Thrust and Efficiency

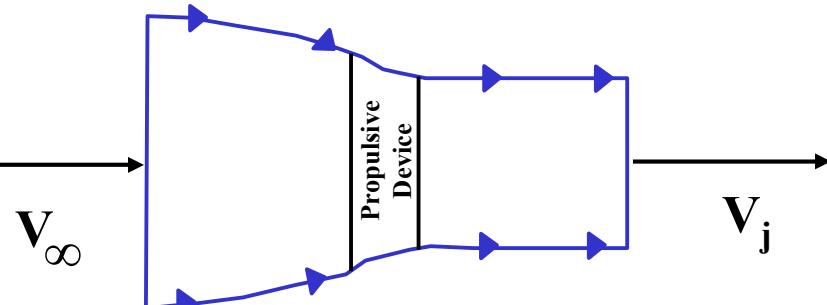
|                                                                                                                  | Thrust      | Efficiency |
|------------------------------------------------------------------------------------------------------------------|-------------|------------|
|  Propeller/reciprocating engine | Low         | High       |
|  Turbojet                       | Higher      | Lower      |
|  Rocket Engine                  | Substantial | Poor       |

*In general, more thrust = less efficiency*

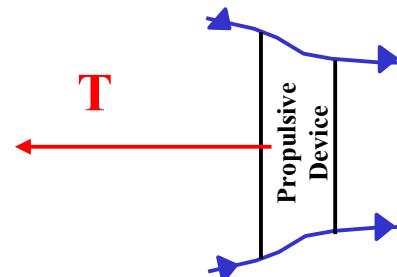
This tradeoff helps explain why there are different propulsive devices in use today.

# How Thrust is Produced

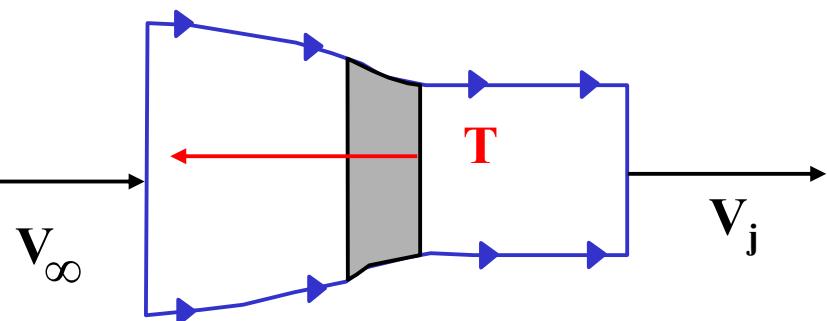
Generic propulsive device (jet engine, propeller, etc.) whose function is to produce **thrust,  $T$** , acting towards the left



Regardless of type of device, the **thrust** exerted on the *device* is the net resultant of **pressure and shear distributions**, at points where air contacts device (internal and external)

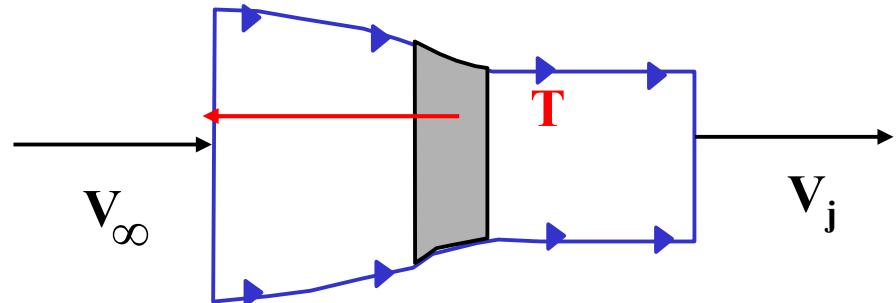


Air experiences **equal and opposite** reaction (Newton's 3rd Law) to thrust



# How Thrust is Produced

Air is accelerated to velocity  $V_j$ , called the jet velocity



Newton's 2nd Law: the force on an object is equal to the time rate of change of momentum of that object

$$T = \dot{m} (V_j - V_\infty)$$

**THRUST EQUATION**  
for generic thrust device

*time rate of change of  
momentum*

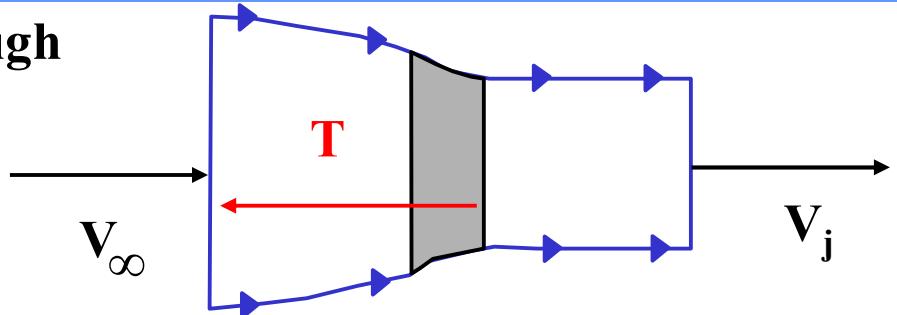
$\dot{m} V_j$   
↓  
*momentum per unit time  
entering stream tube*

$\dot{m} V_\infty$   
↓  
*momentum per unit time  
exiting stream tube*

(Note: we are neglecting the pressure force on the stream tube for this simplified analysis)

# Propulsive Efficiency

Instead of considering air moving through device, picture device moving through room of stationary air.



Before device enters the room, air is stationary and has no kinetic energy  
After device leaves room, air is moving at velocity  $V_j - V_\infty$  and has kinetic energy of

$$\frac{1}{2} (V_j - V_\infty)^2 \quad \text{wasted energy-source of inefficiency}$$

Recall: power = force x velocity

$$P_A = T V_\infty \quad \text{this is the useful power available}$$

Since power is **energy per unit time**, the power **wasted** in the air jet behind the device:

$$\frac{1}{2} \dot{m} (V_j - V_\infty)^2$$

# Propulsive Efficiency

$$\text{Total power generated by device} = TV_{\infty} + \frac{1}{2} \dot{m} (V_j - V_{\infty})^2$$

Propulsive efficiency

$$\eta_p = \frac{\text{useful power available}}{\text{total power generated}}$$

Substituting in previous expressions,

$$\eta_p = \frac{TV_{\infty}}{TV_{\infty} + \frac{1}{2} \dot{m} (V_j - V_{\infty})^2}$$

Recall:

$$T = \dot{m} (V_j - V_{\infty})$$

and substitute to get...

# Propulsive Efficiency

$$\eta_p = \frac{\dot{m}(V_j - V_\infty) V_\infty}{\dot{m}(V_j - V_\infty) V_\infty + \frac{1}{2} \dot{m} (V_j - V_\infty)^2}$$

Divide by:

$$\dot{m}(V_j - V_\infty) V_\infty$$

$$\eta_p = \frac{1}{1 + \frac{1}{2} (V_j - V_\infty) / V_\infty} = \frac{1}{\frac{1}{2} (1 + V_j/V_\infty)}$$

$$\eta_p = \frac{2}{1 + V_j/V_\infty}$$

$$T = \dot{m} (V_j - V_\infty)$$

Max efficiency occurs when  $V_j = V_\infty$   
( $\eta_p = 1$ ) but then  $T=0$  (ultimate  
efficiency but no propulsive force)

# Propulsive Efficiency and Engines



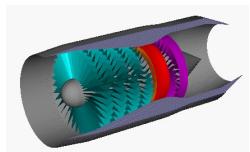
low



speed



high



Propeller provides large  $\dot{m}$  but small  $V_j - V_\infty$  so has high efficiency

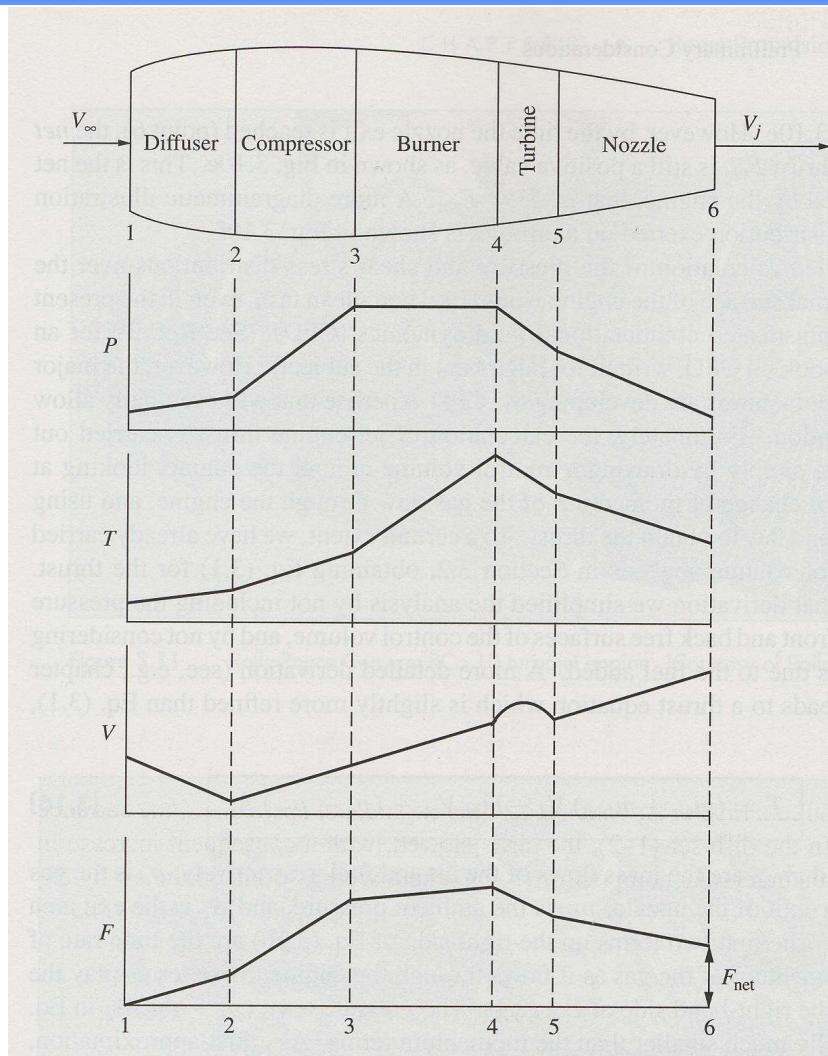
*Q: so why don't we use propellers on faster aircraft?*

*A: as speed increases, the tip speed increases. At high enough speeds, shock waves will form. This increases drag, which increases the torque on the reciprocating engine, which reduces the rotational speed (rpm) of the engine, which reduces power obtained from the engine, which reduces thrust. Also, shock waves on the propeller airfoils increase drag, reducing thrust.*

Gas turbine jet engines give a smaller mass of air a larger increase in velocity, but at a lesser efficiency.

Turbofans try to combine the thrust generating capabilities of the jet engine with the efficiency of a propeller. Similarly, the turboprop tries to achieve the same.

# The Turbojet Engine



**Work is done by  
the compressor**

**Work is extracted by  
the turbine and is  
transmitted via a  
shaft to the compressor**

# Turbojet Engine

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**Diffuser-** slows the air, with increase in pressure and temperature

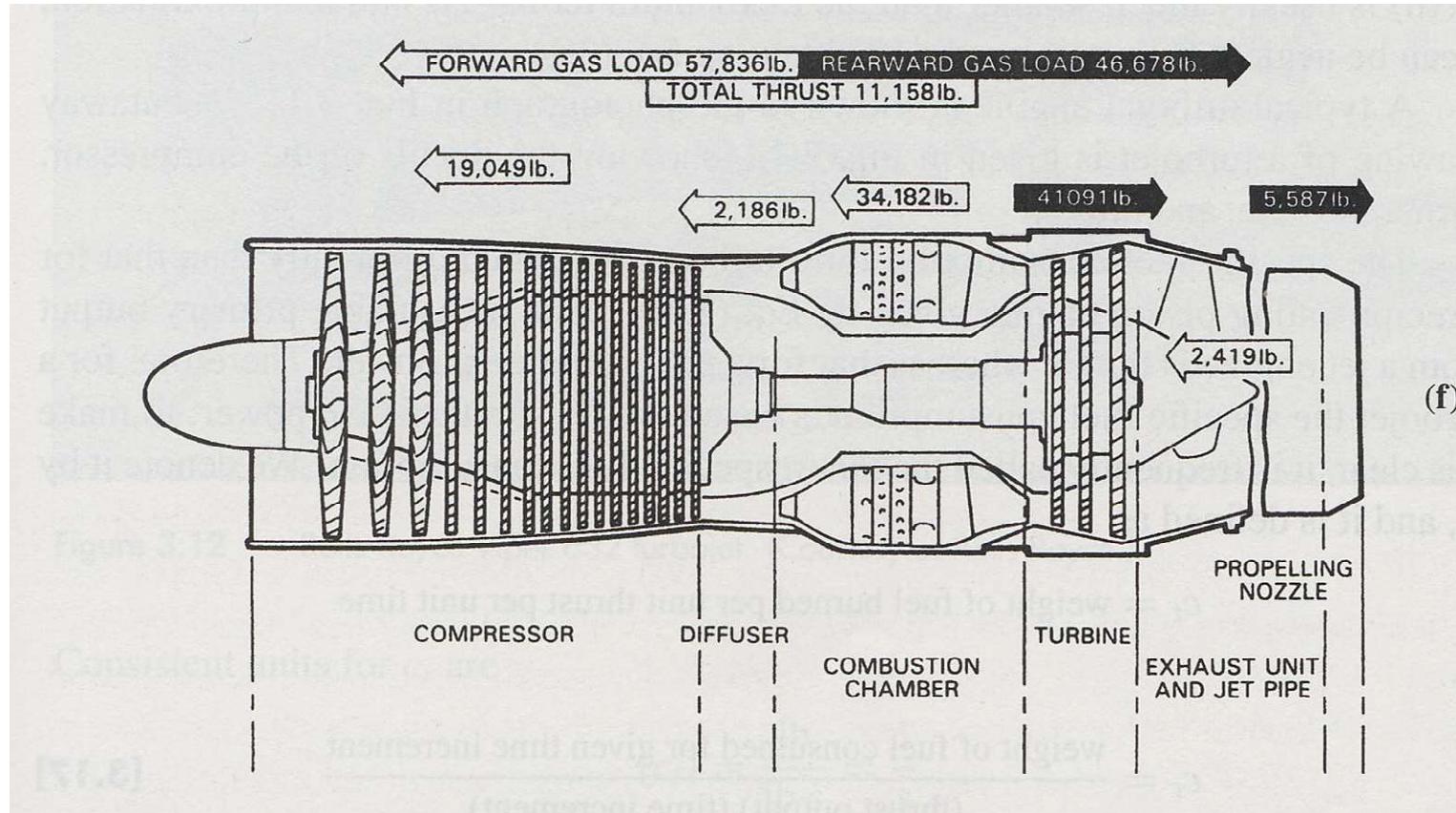
**Compressor-** work is done on the air by the rotating compressor blades, greatly increasing pressure and temperature

**Burner (combustor)-** air is mixed with fuel and burned at essentially constant pressure

**Turbine-** burned air-fuel mixture then expands through a turbine, which extracts work from the gas. The turbine is connected to the compressor by a shaft, and the work extracted by the turbine is thus used to operate the compressor.

**Nozzle-** the gas expands through a nozzle and is exhausted into the air with velocity  $V_j$ .

# Generation of Thrust



**The thrust generated by the engine is due to the net resultant of the pressure and shear stress distributions acting on the exposed surface areas, external and internal**

# Calculation of Thrust

The detailed calculation of the pressure and shear distribution over the complete internal surface of the engine would be a Herculean task, even in the present day of sophisticated computational fluid dynamics (CFD)

Fortunately, the calculation of jet engine thrust is carried out infinitely more simply by drawing a control volume around the engine, looking at the time rate of change of momentum of the gas flow through the engine, and using Newton's 2nd law to obtain the thrust.

Simplified, this is the result we got earlier:

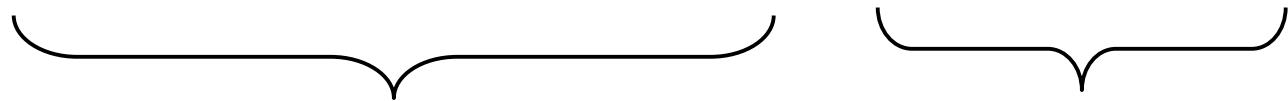
$$T = \dot{m} (V_j - V_\infty)$$

Now, add in pressure acting on the front and back free surfaces, and the extra mass due to the fuel added:

$$T = (\dot{m}_{air} + \dot{m}_{fuel}) V_j - \dot{m}_{air} V_\infty + (p_e - p_\infty) A_e$$

# Turbojet Thrust Equation

$$T = (\dot{m}_{\text{air}} + \dot{m}_{\text{fuel}}) V_j - \dot{m}_{\text{air}} V_{\infty} + (p_e - p_{\infty}) A_e$$



time rate of change of momentum  
of the gas as it flows through the  
engine



usually much smaller than  
momentum terms and can  
be neglected at times

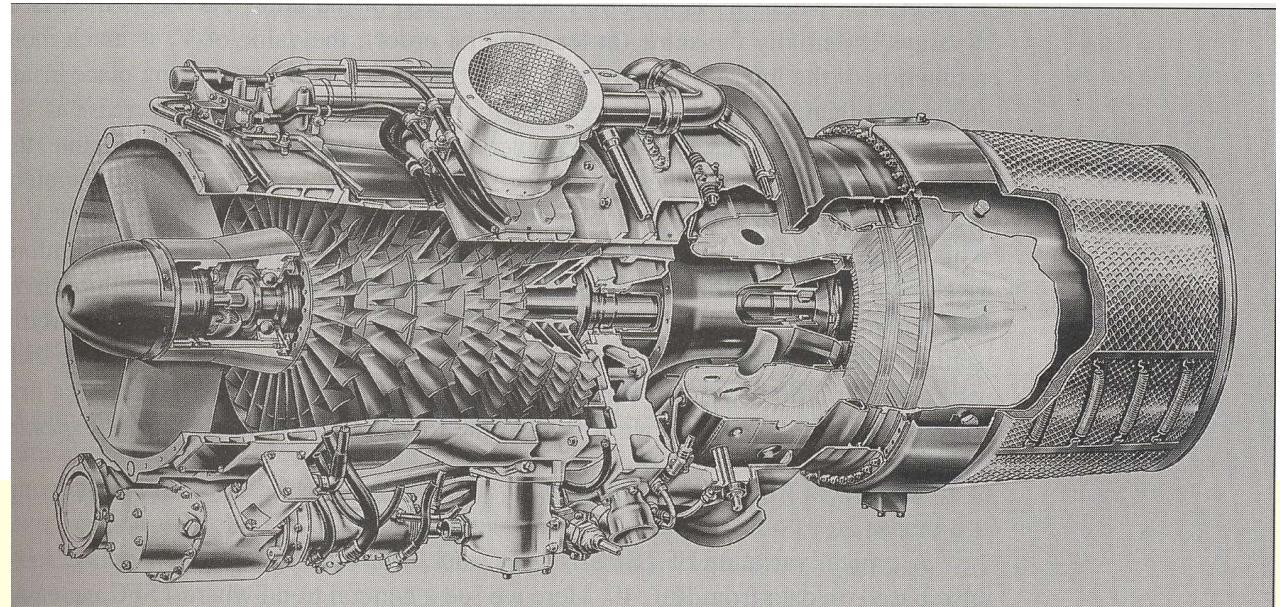
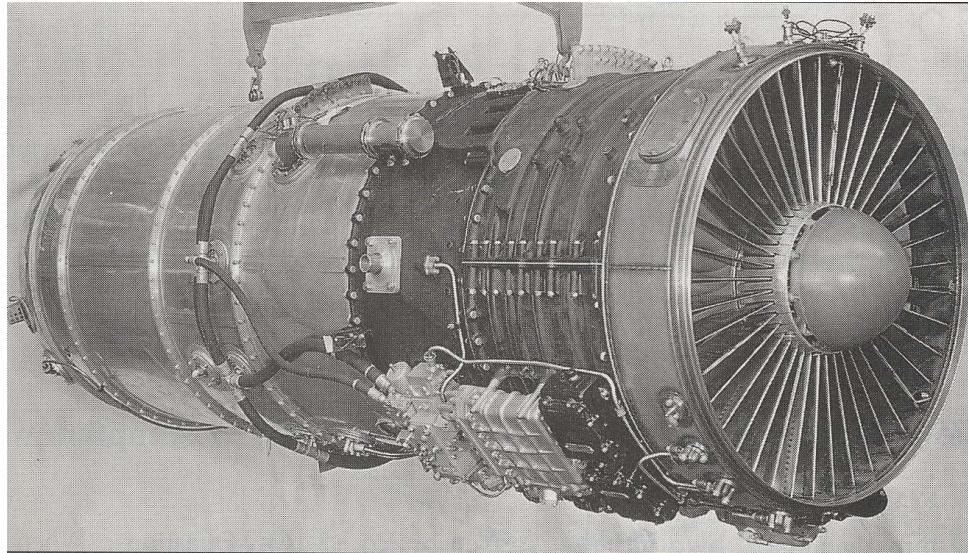
**p<sub>e</sub>** is the gas pressure at the exit of the nozzle

**p<sub>∞</sub>** is the ambient pressure

**A<sub>e</sub>** is the exit area of the nozzle

# Example of a Turbojet

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# SFC for a Turbojet

SFC for a turbojet is defined differently than for a reciprocating engine

Jet → Thrust

Piston → Power

To be very clear, we say **thrust** specific fuel consumption

$c_t$  = weight of fuel burned per unit thrust per unit time

$c_t$  = weight of fuel consumed for given time increment  
(thrust output)(time increment)

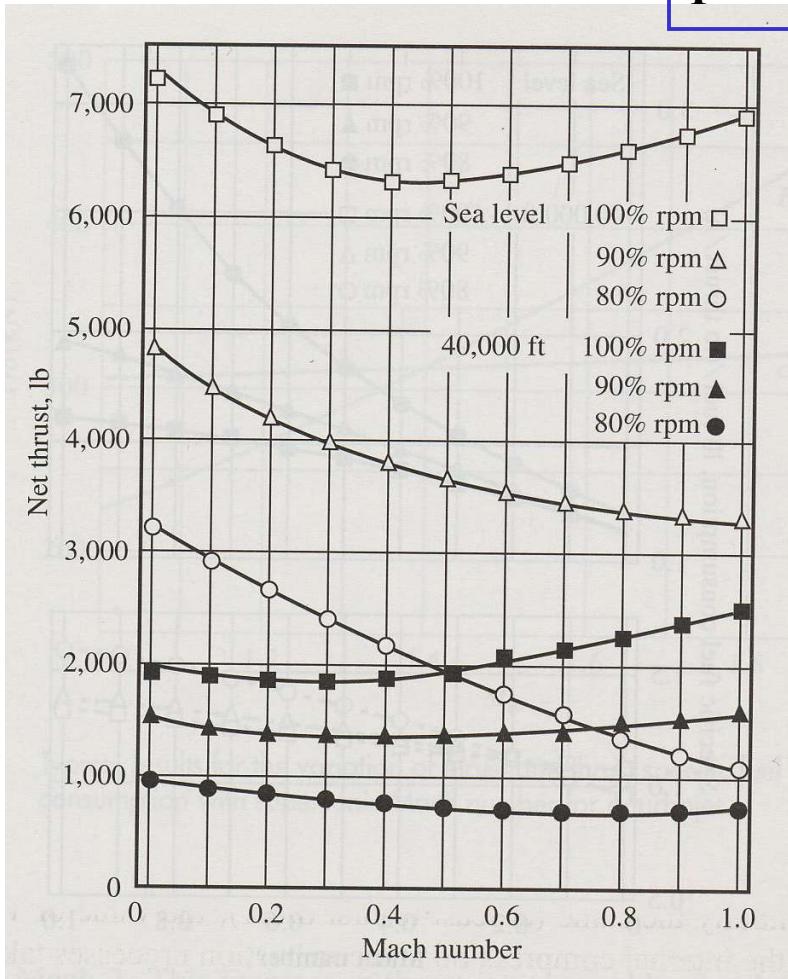
$$c_t = \frac{N}{N \cdot s} = \frac{1}{s}$$

$$[TSFC] = \frac{\text{lb}}{\text{lb} \cdot \text{hr}} = \frac{1}{\text{h}}$$

# Thrust varying Velocity and Altitude

For subsonic speeds,

$$T = (\dot{m}_{\text{air}} + \dot{m}_{\text{fuel}}) V_j - \dot{m}_{\text{air}} V_{\infty} + (p_e - p_{\infty}) A_e$$



Remember  $\dot{m}_{\text{air}} = \rho_{\infty} A_1 V_{\infty}$

so  $\dot{m}_{\text{air}}$  is directly proportional to  $\rho$ . As altitude increases,  $\rho$  decreases,  $\dot{m}_{\text{air}}$  decreases, and from the equation above, T must decrease.

Thrust is strongly degraded as altitude increases

Can approximate thrust changing with altitude by:

$$\frac{T}{T_0} = \frac{\rho}{\rho_0}$$

Note that T is THRUST in this equation, not temperature!

$T_0$  is sea level thrust

# TSFC varies with Velocity and Altitude

TSFC increases with Mach number

At low speed, can use approximation:

$$\text{TSFC} = 1 \frac{\text{lb}}{\text{hp} \cdot \text{h}}$$

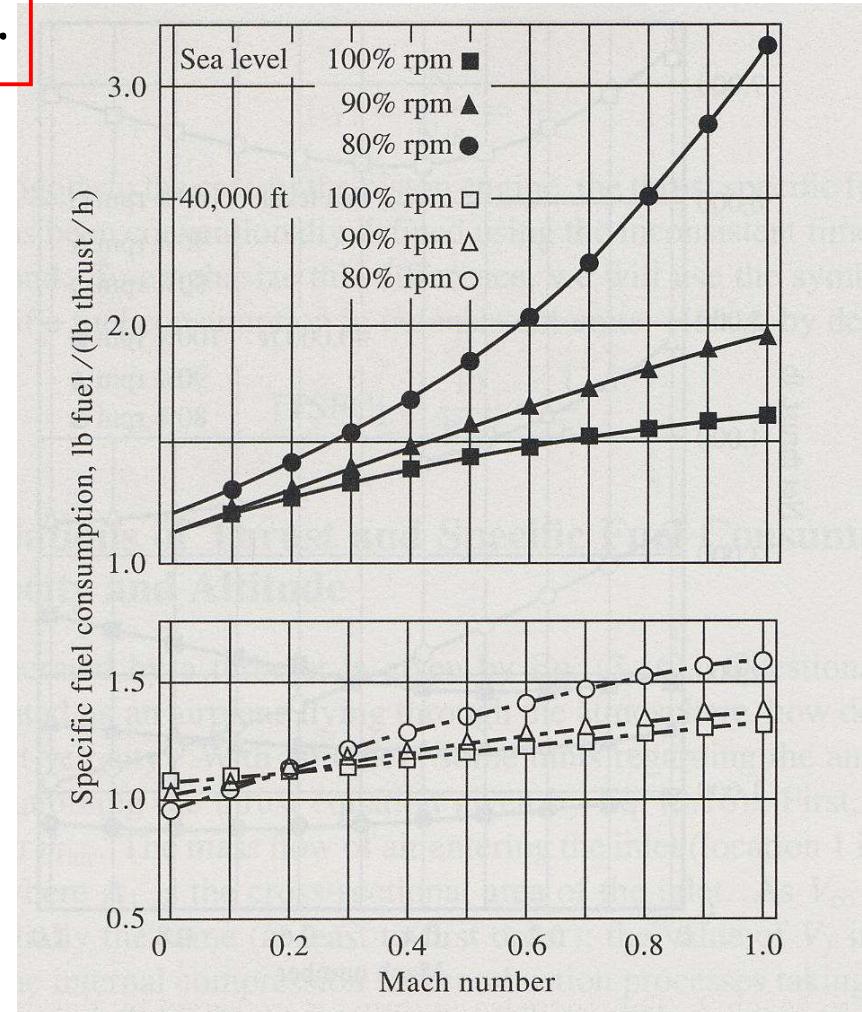
At high speeds, use:

$$\text{TSFC} = 1.0 + k M_\infty$$

where  $k$  is engine specific, but on the order of 0.5

TSFC is constant with altitude

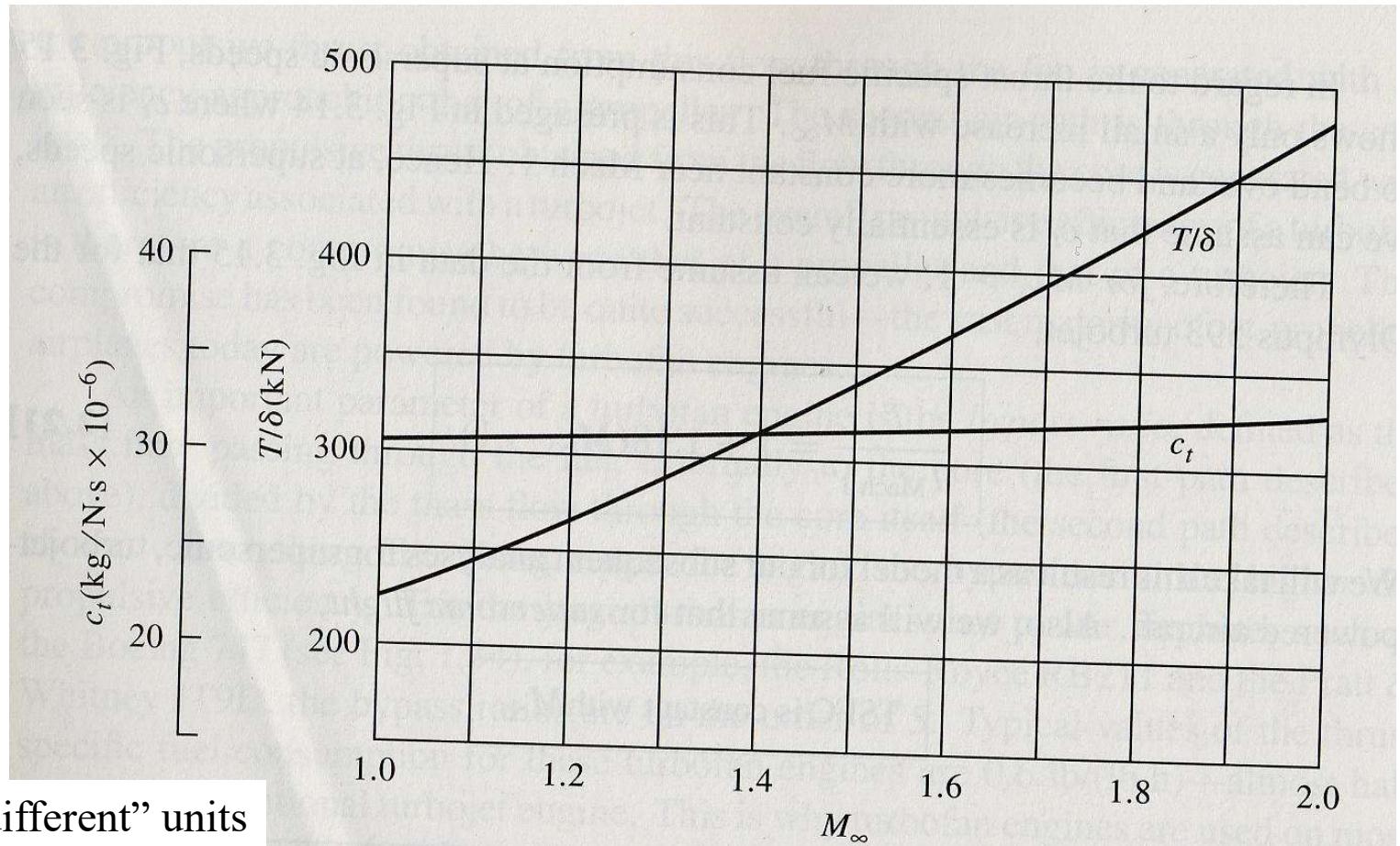
There is actually a weak effect, but we ignore it for preliminary analysis



# Supersonic Variations

The Concorde uses turbojets instead of turbofans because of the better supersonic thrust SFC at Mach 2.2, shown below.

$$\delta = \frac{p}{p_0}$$



Note use of “different” units

# Supersonic Variation Comments

Why does T increase with M in the supersonic regime, whereas it is relatively constant in the subsonic regime? The answer lies in part in the large total pressures recovered in the supersonic inlet diffuser as  $M_\infty$  increases (ram effect).

$$\frac{p_{\text{total}}}{p_{\text{static}}} = \left[ 1 + \frac{\gamma - 1}{2} M^2 \right]^{\frac{\gamma}{\gamma - 1}}$$

*(isentropic)*

As  $M_\infty$  increases,  $p_{\text{total}}$  increases dramatically, increasing  $V_j$

Also,  $m_{\text{air}}^\bullet$  increases. Both of these increase T.

For  $M_\infty > 1$ , we can use the Concorde turbojet data as a model and approximation:

$$\frac{T}{T_{\text{Mach}}} = 1 + 1.18 (M_\infty - 1)$$

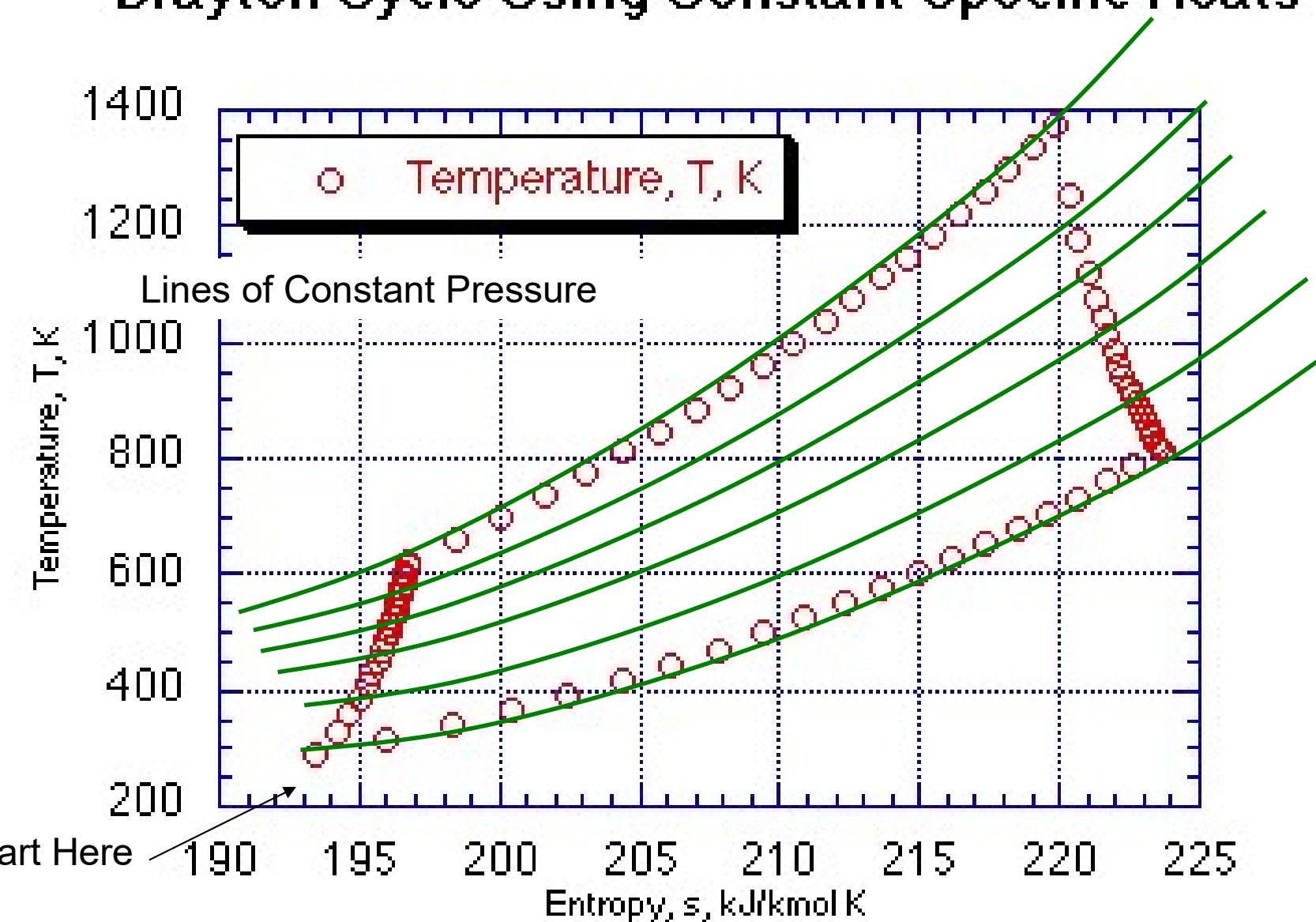
TSFC is constant with supersonic  $M_\infty$

# Brayton Cycle

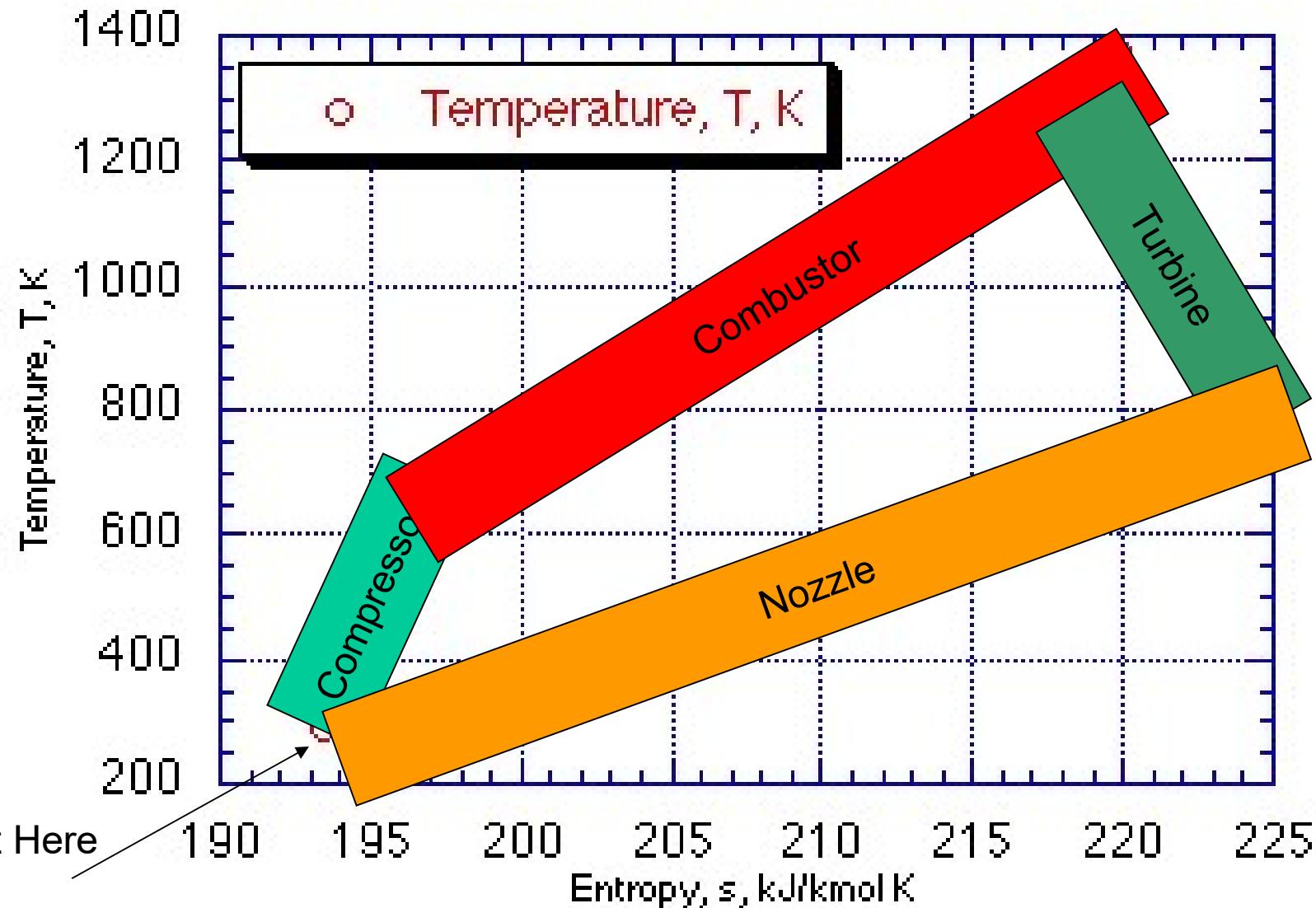
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- Four Steps:
  - Compressor working fluid
    - Use a compressor. Adiabatic compression.
  - Heat Added to Fluid
    - Combustion Chamber. Do this at high pressure for increased efficiency.
  - Extract Work from Fluid
    - Use a turbine to do this. Turbine work runs the compressor.
  - Cool the Fluid
    - This usually happens in the atmosphere after the aircraft passes.

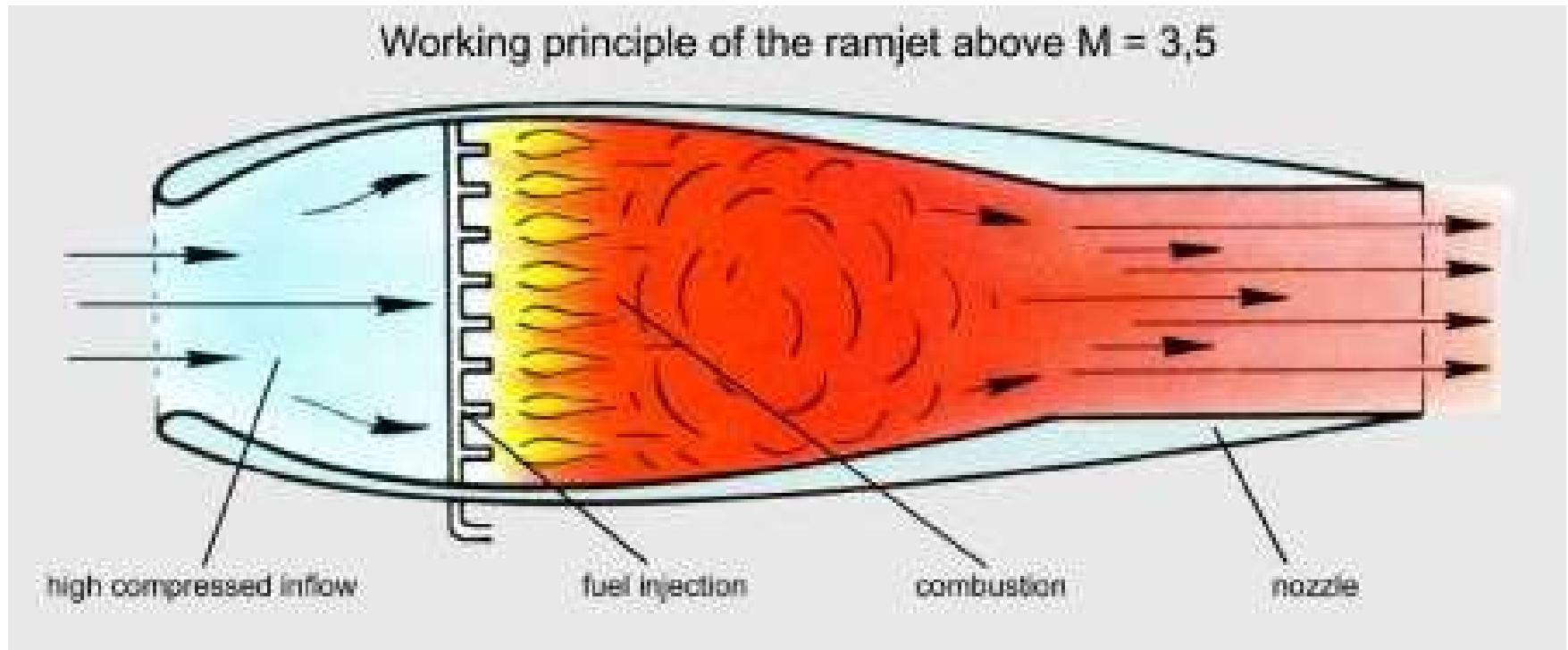
## Brayton Cycle Using Constant Specific Heats



# Brayton Cycle Using Constant Specific Heats

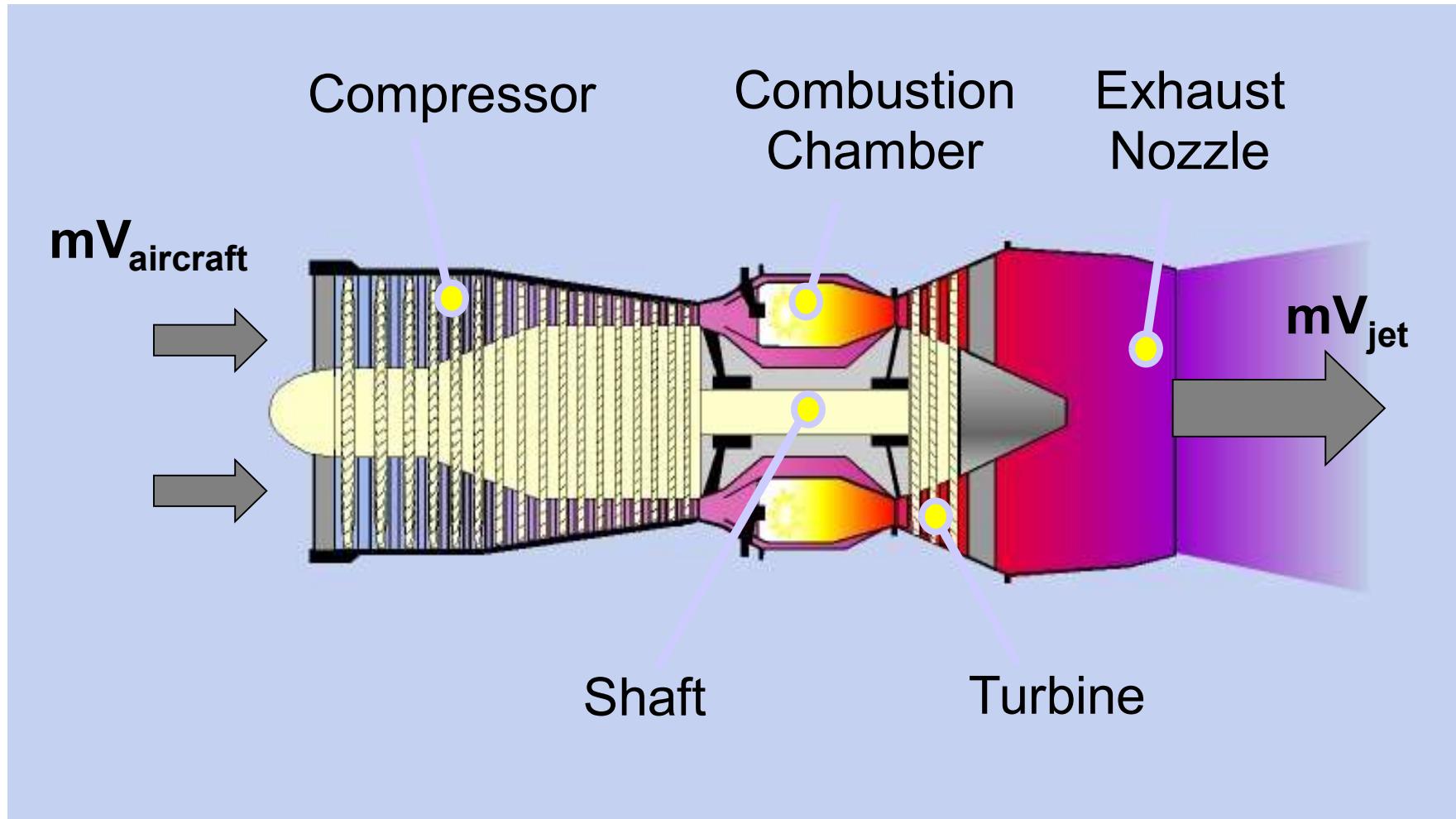


# Ideal Engine: Ramjet



- Three Parts: Inlet, Combustor, Nozzle
- Pro: No Moving Parts
- Con: Needs “High Compressed Inflow”

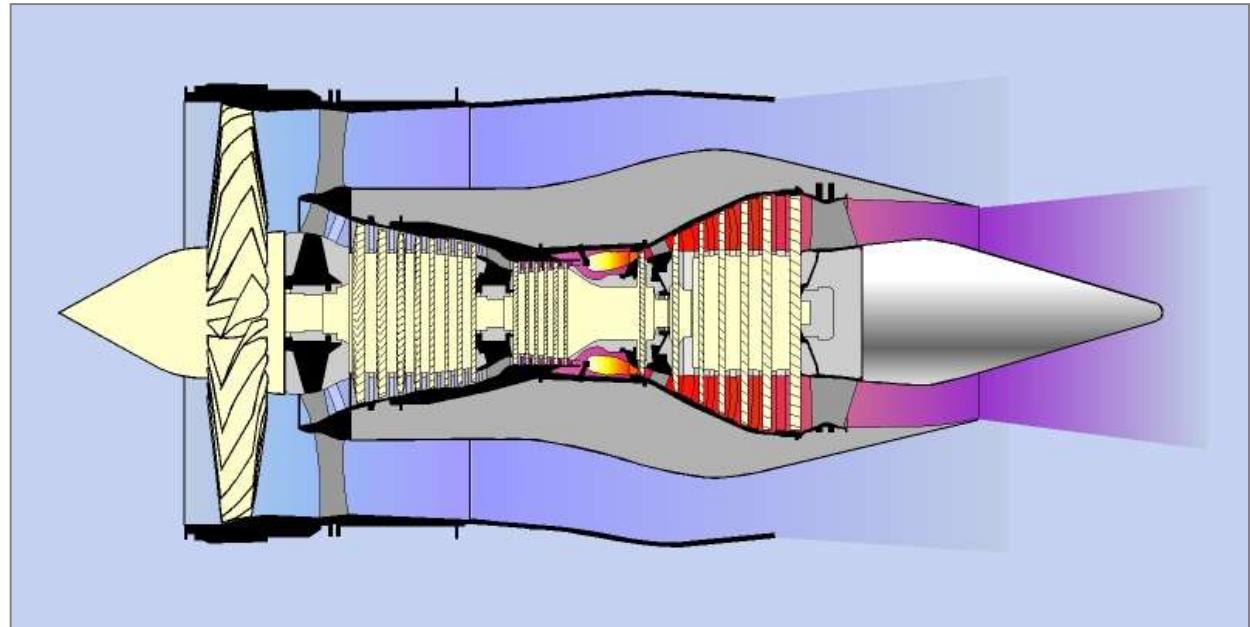
# Standard Engine Components: Turbojet



# Modification: Turbofan

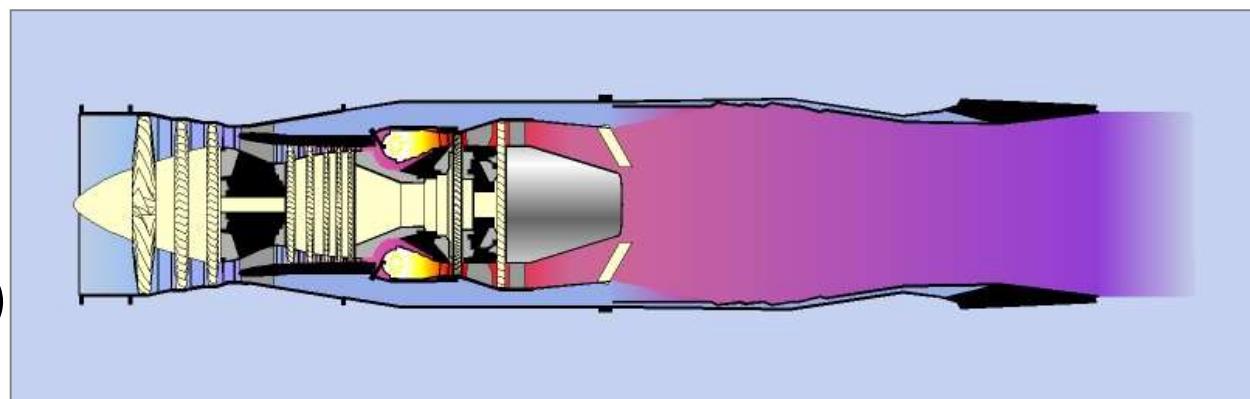
“High Bypass  
Ratio Turbofan”

300 PAX  
RR Trent 800  
GE 90



“Low Bypass Ratio  
Turbofan”

EJ200 (Eurofighter)



# What They Look Like...

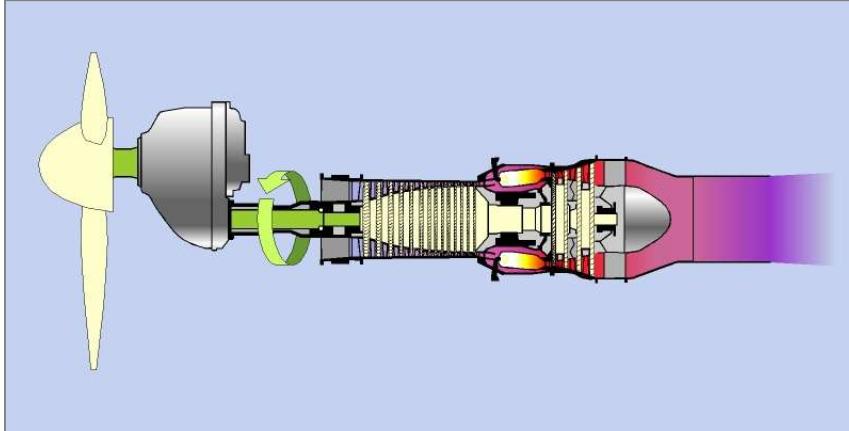
**EJ200-Eurofighter**



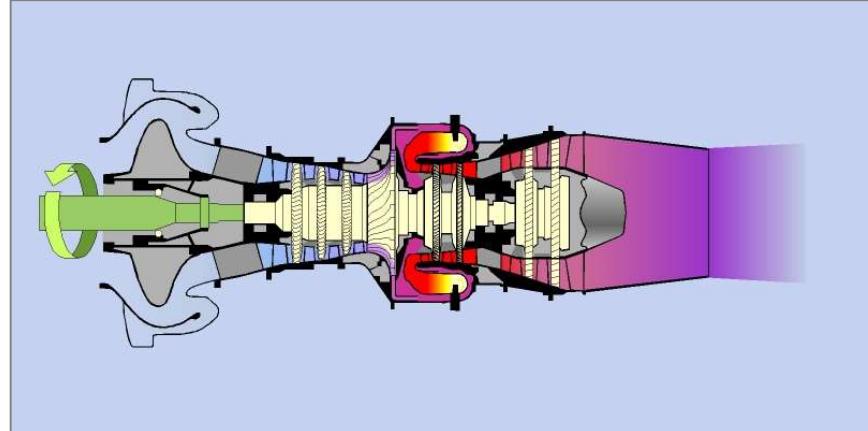
**Trent 800  
Boeing 777**



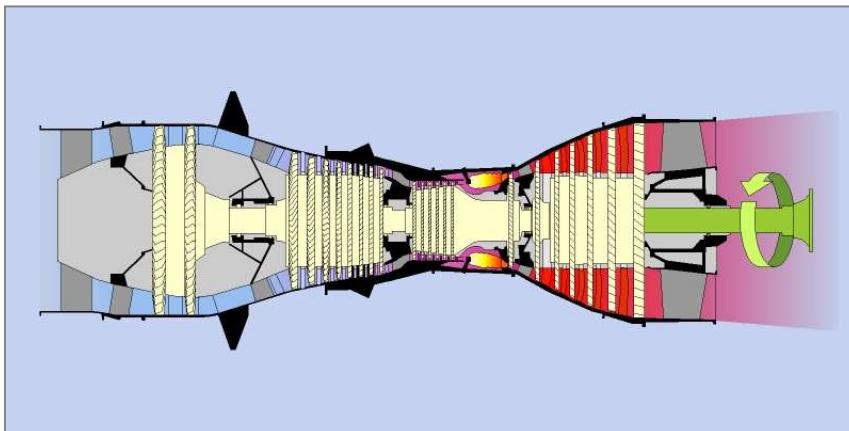
# Different Jet Engine Types -



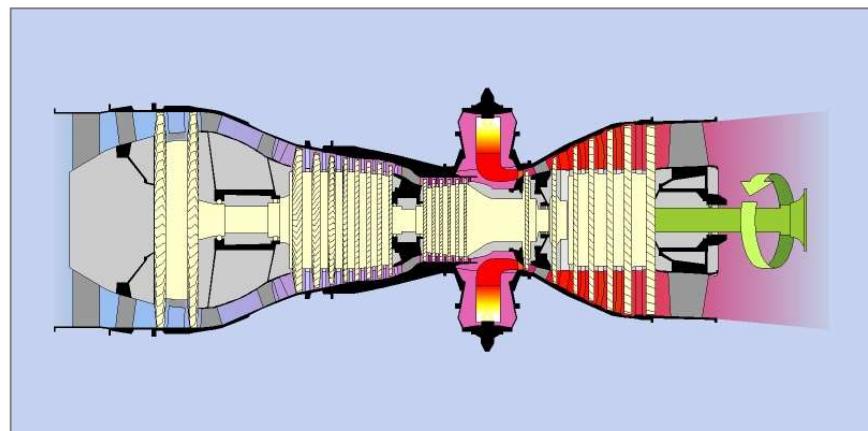
Turboprop - AE 2100



Turboshaft - RTM322

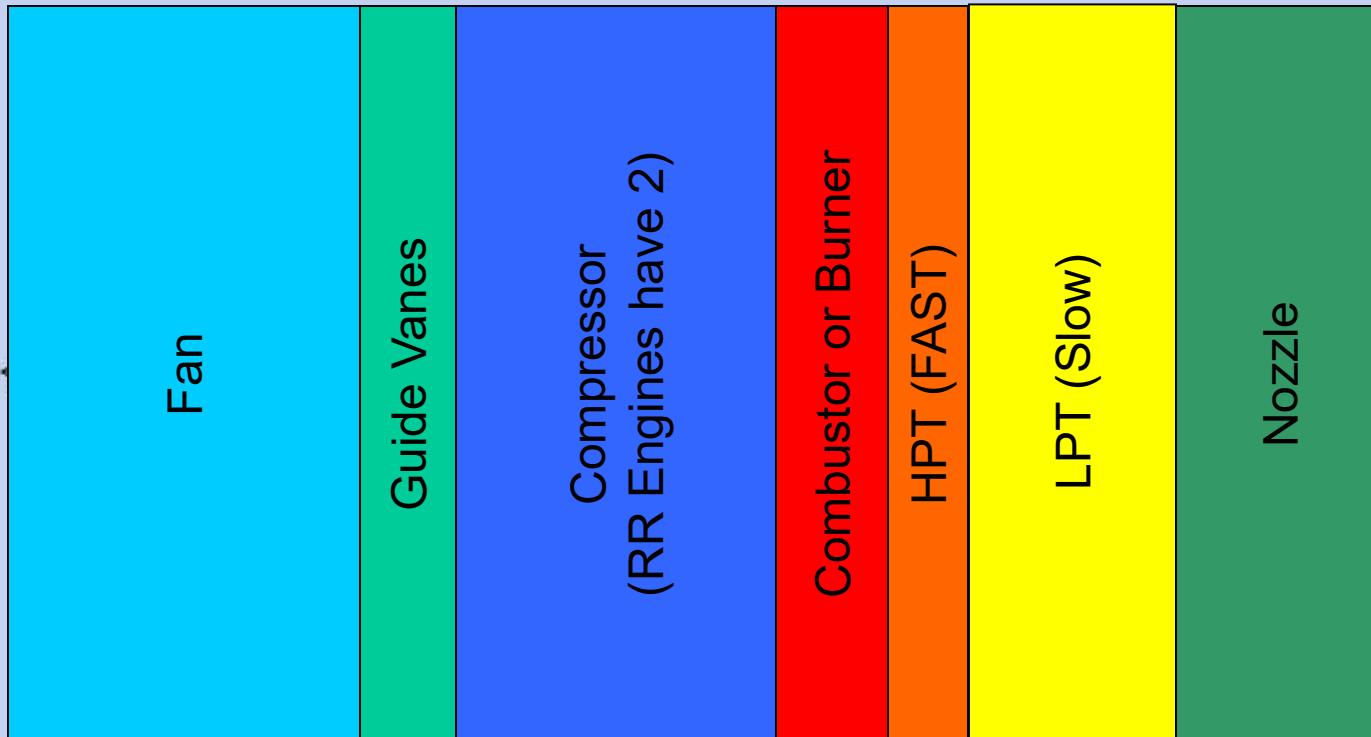


Marine Trent

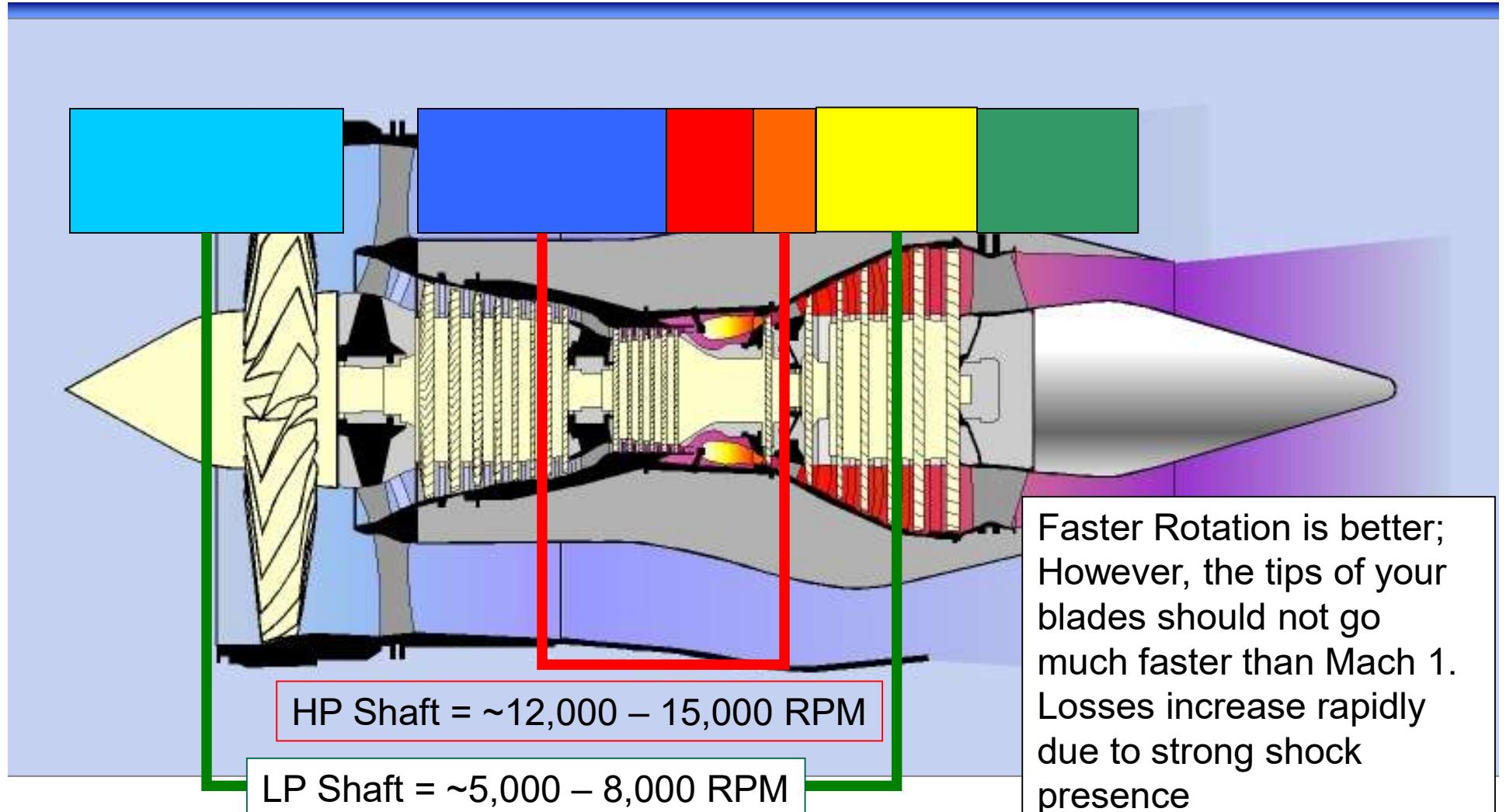


Industrial Trent

# Turbofan Engine Components

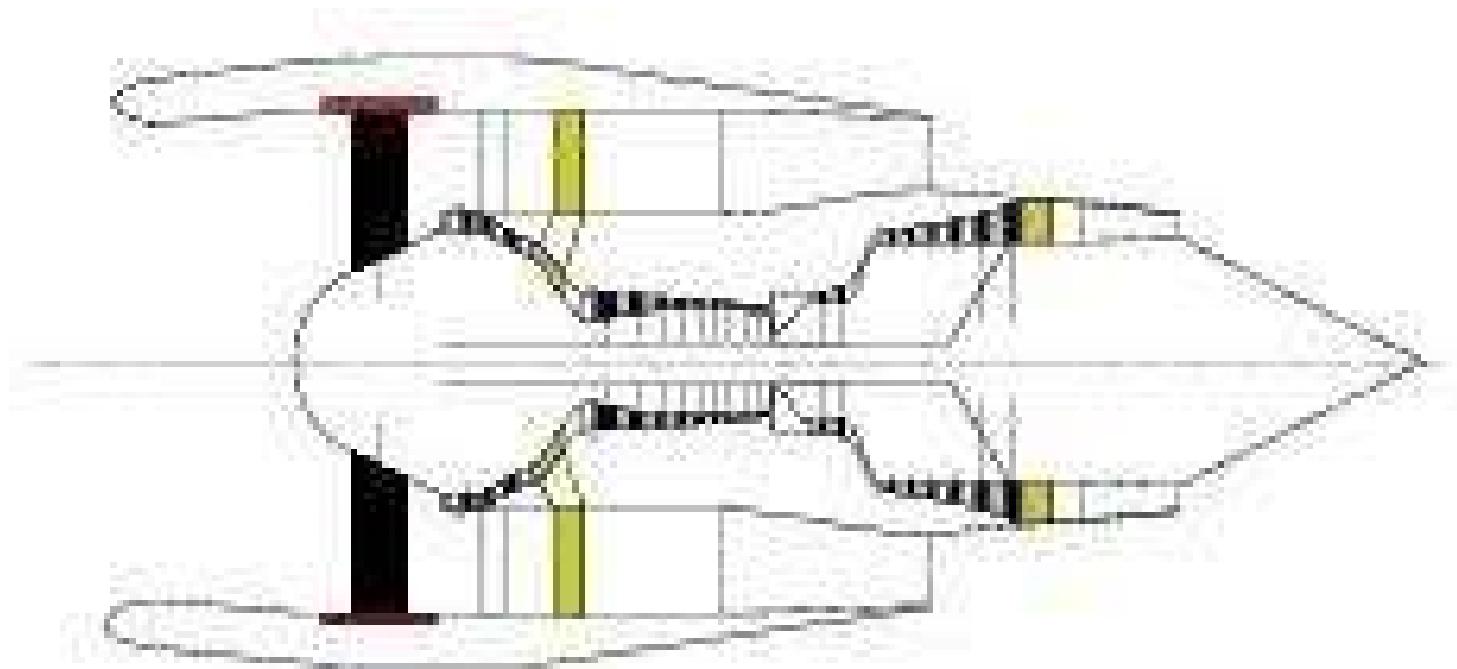


# Two Shafts Connect Engine Hardware

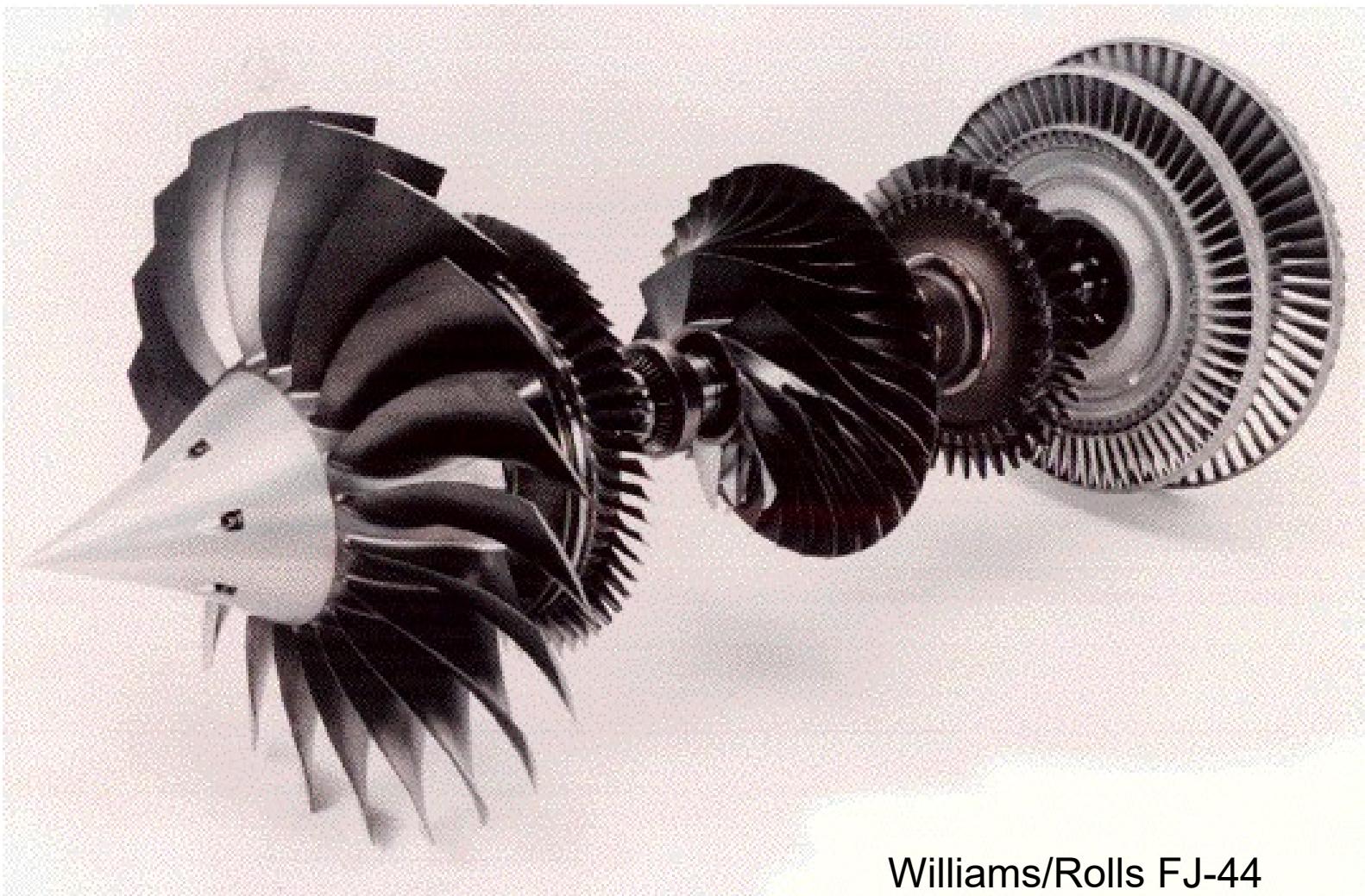


# Example: 300 PAX

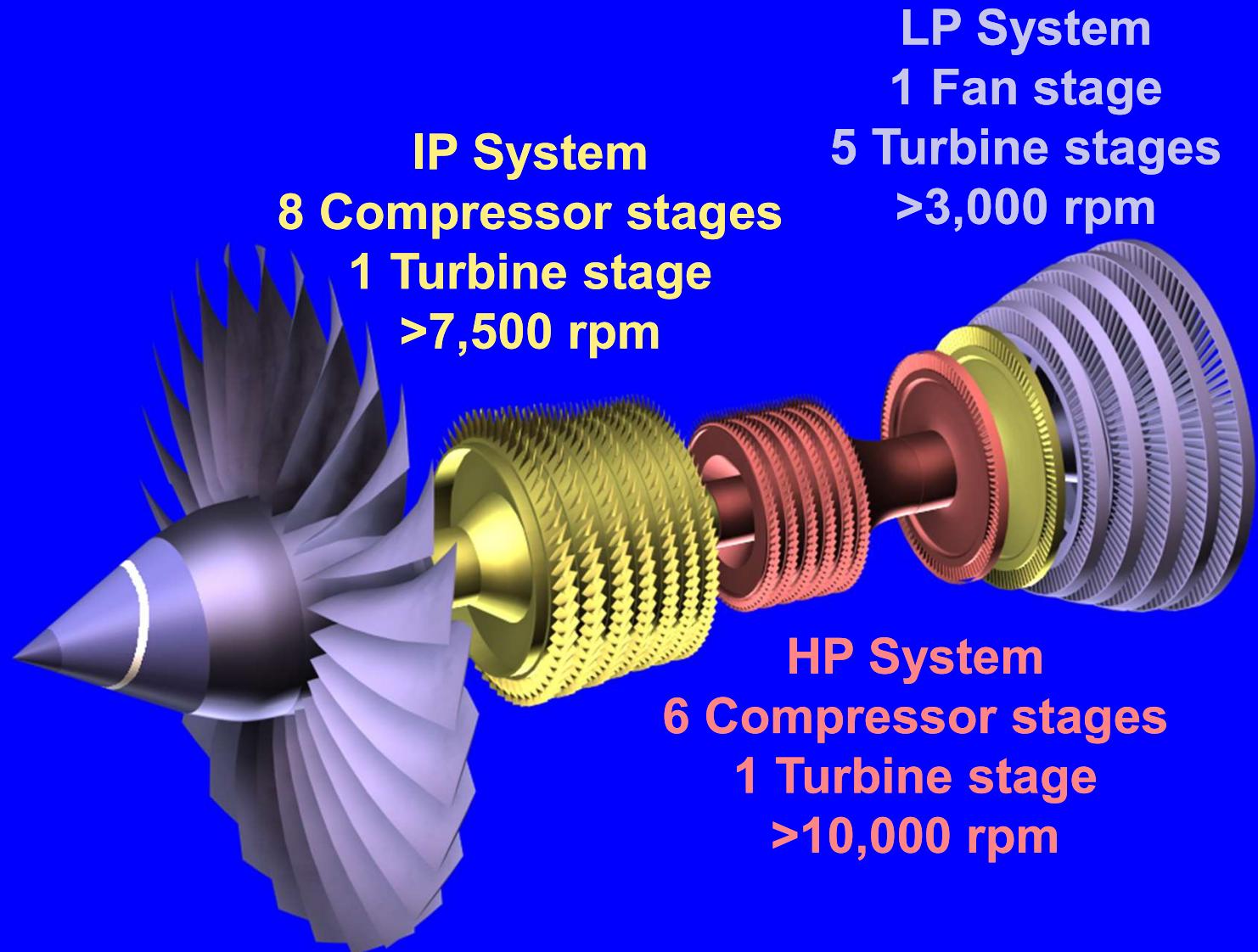
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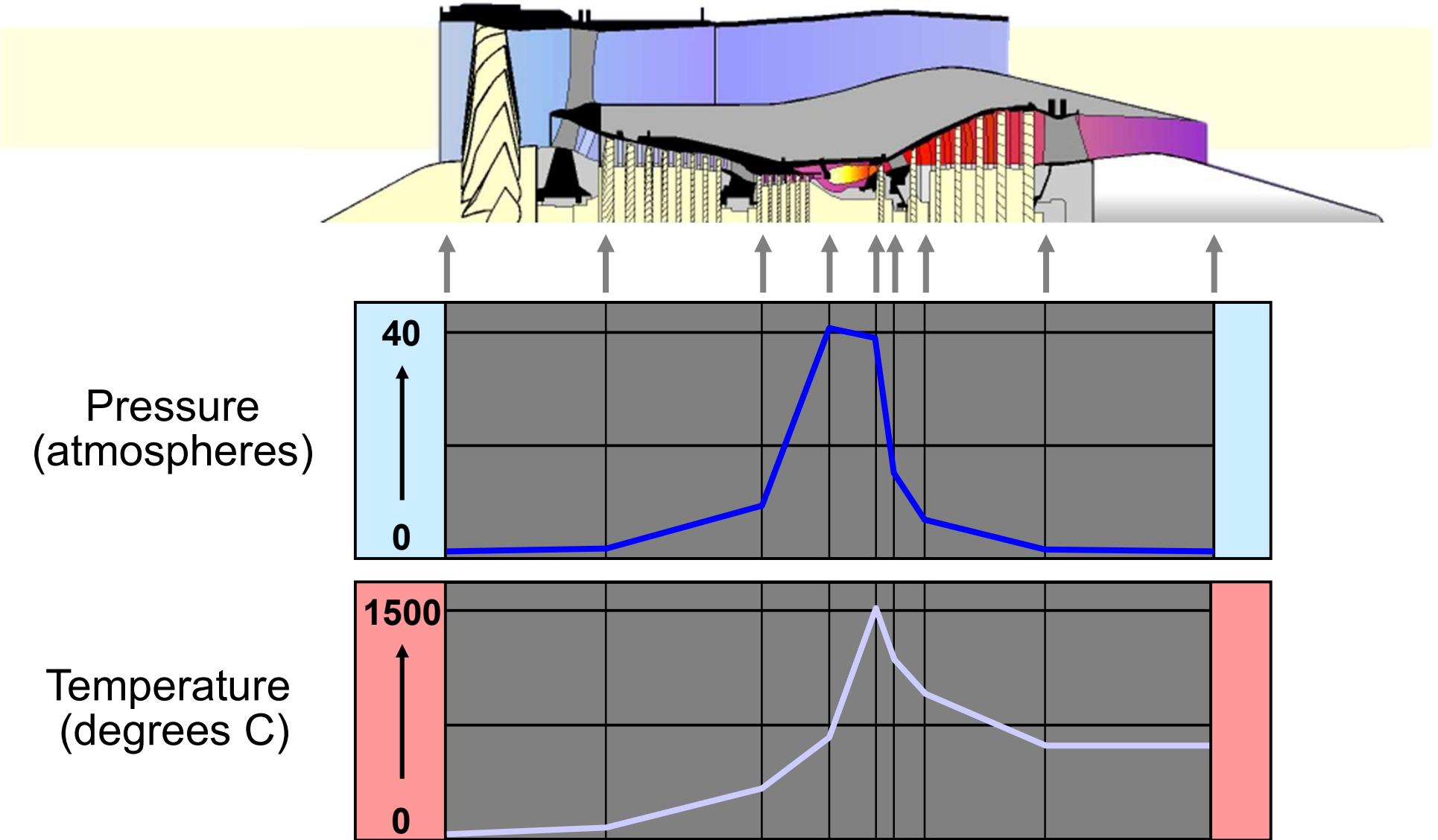
# Rotating Machinery



Williams/Rolls FJ-44



# Pressure and Temperature



# Fan

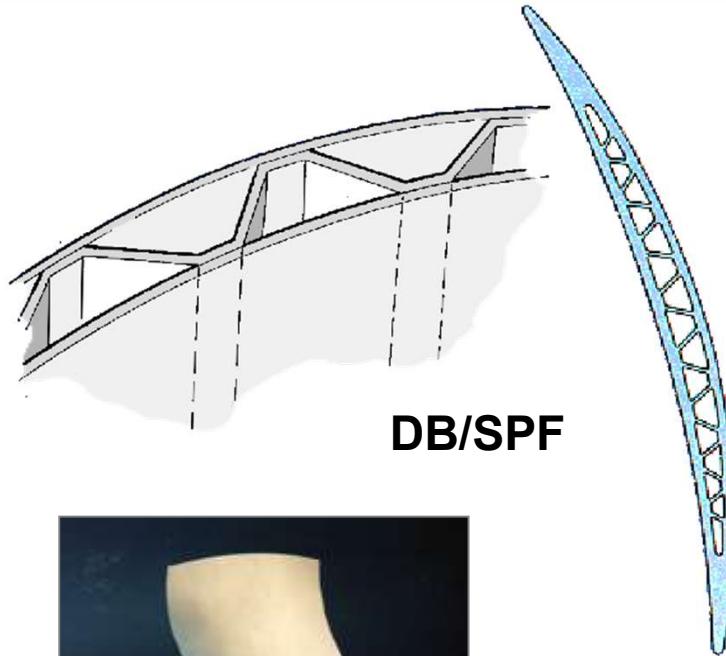
- The fan is the first component of the turbofan engine.  
It behaves like a propeller

$$F = \dot{m}_e v_e - \dot{m}_0 v_0 + (p_e - p_0) A_e$$

- Thrust is proportional to mass flow and velocity
  - Increasing velocity (turbojet) is noisy
  - Increasing mass flow (turbofan) means a big heavy fan is needed
- Turbofans push more air through the engine, but at a slower velocity

# Fan

- Usually 1 or 2 stages
- Blades are very large
- Blades are sometimes hollow
- Root stress on each blade is like having a 747 hanging from the disc!!!



DB/SPF



Wide  
Chord  
Blade

# Swept Fan Blades



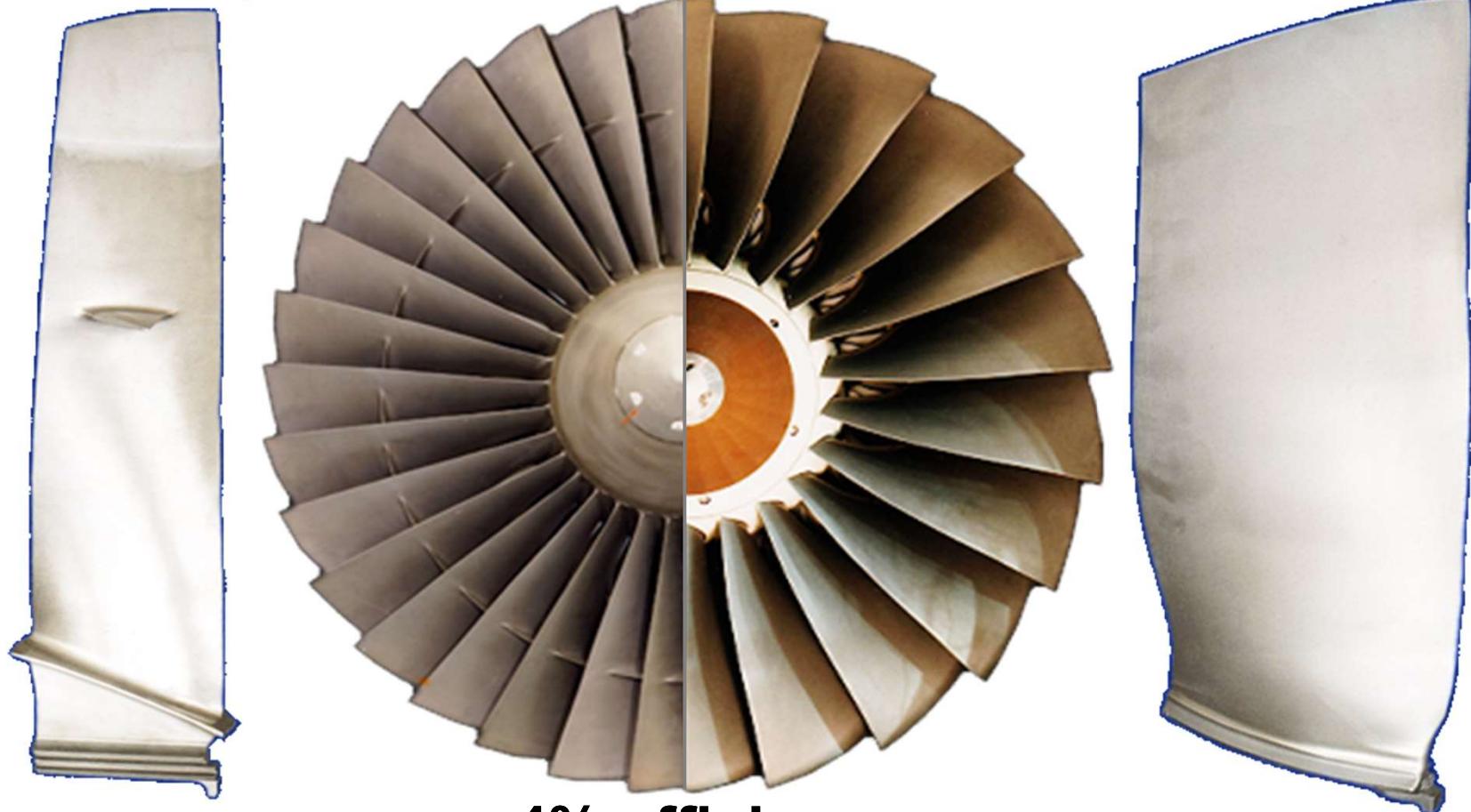
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Georgia Institute of Technology  
*Aerospace Systems Design Laboratory*

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**ASDL**

# Fan Blade Technology



**Clapped**

+ 4% efficiency

**Wide-chord fan**

# Compressor

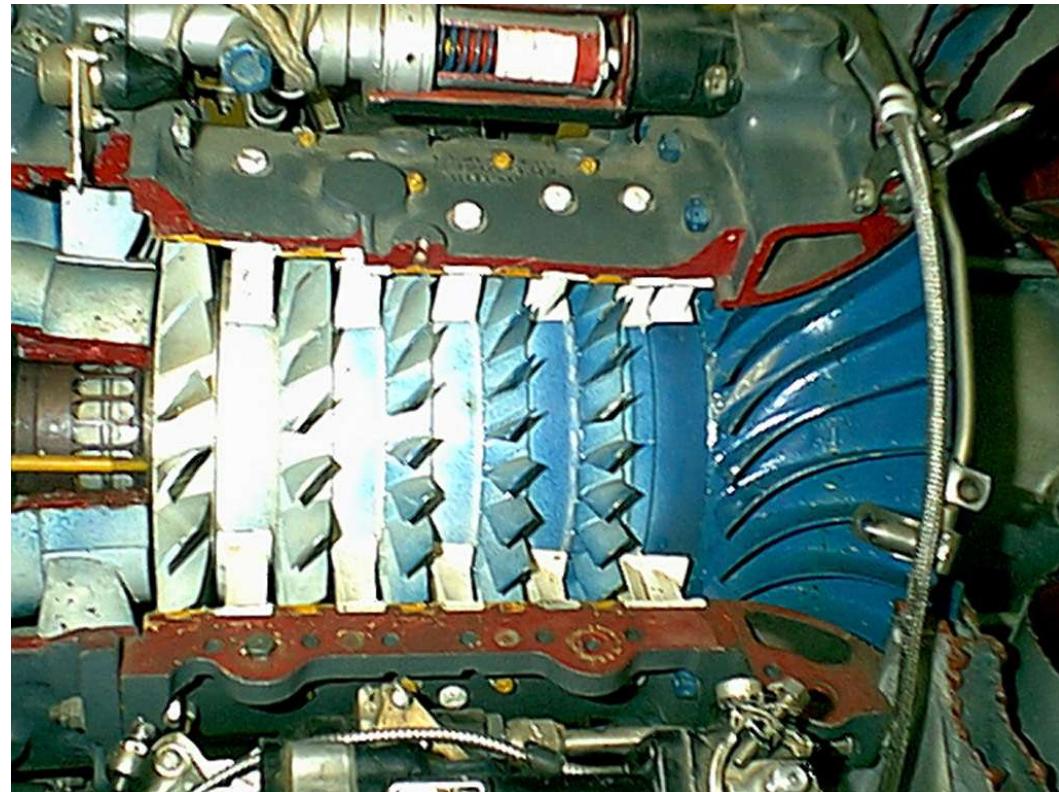
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- The compressor is made up of many small airfoils called blades.
  - These are attached to discs or “wheels”
  - The discs are attached to shafts which rotate
- There are vanes between each row of blades
  - Spinning metal gives air high vorticity
  - Efficiency is increased by using vanes to “straighten” the flow out
- Compressors are usually the heaviest and most expensive component in an engine

# Compressor



Small Compressor  
Disc with Blades

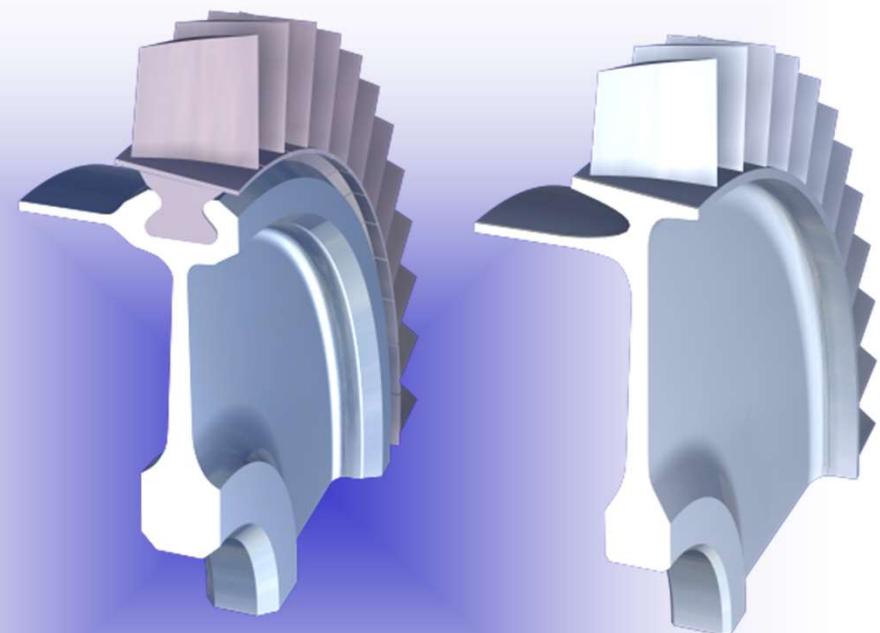
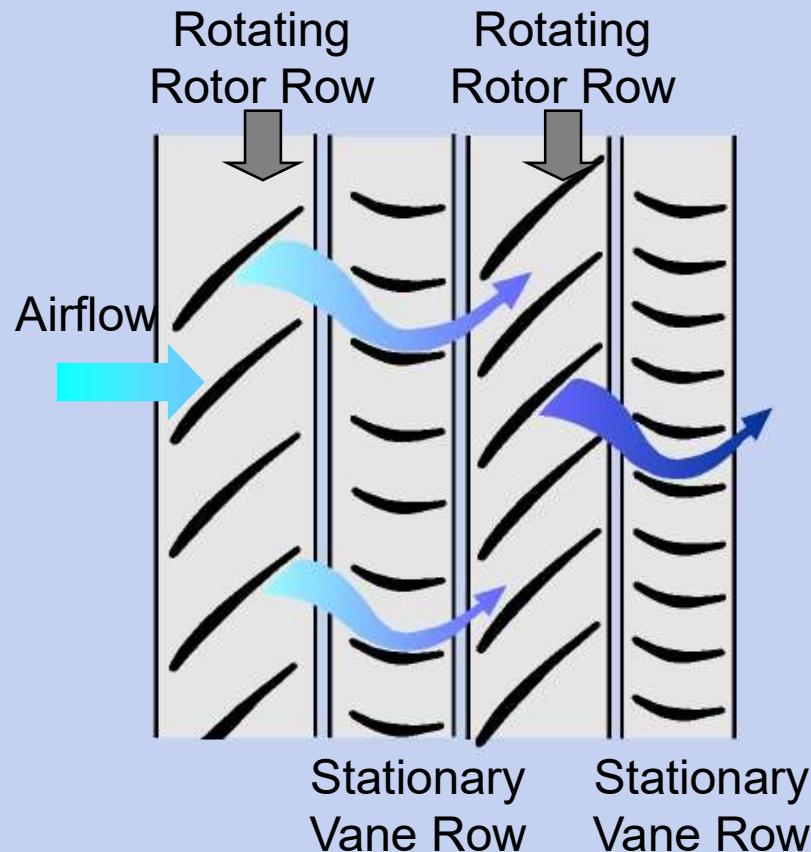


Axial Compressor

Centrifugal  
Compressor

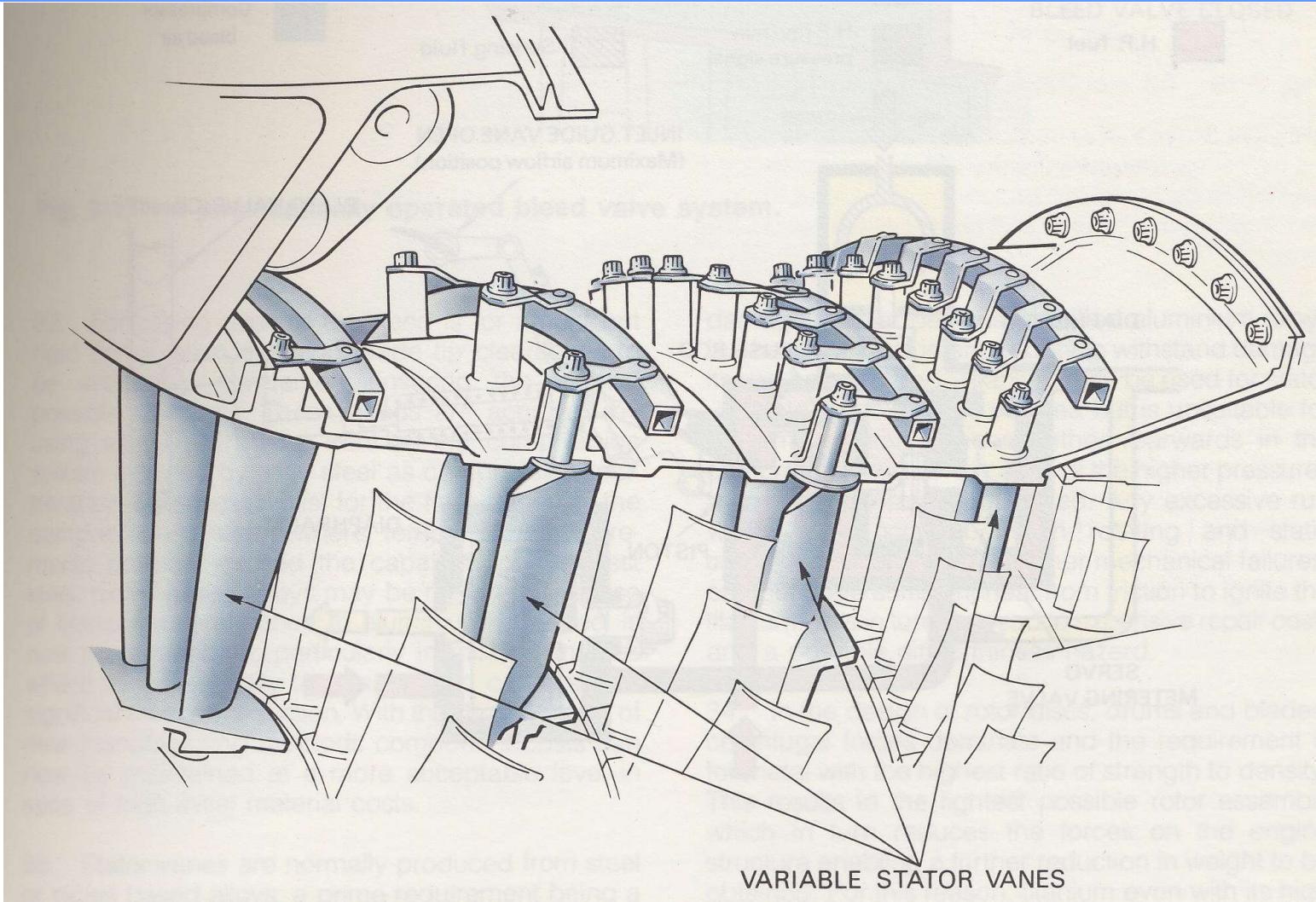
# Compressor

## Compressor Stages

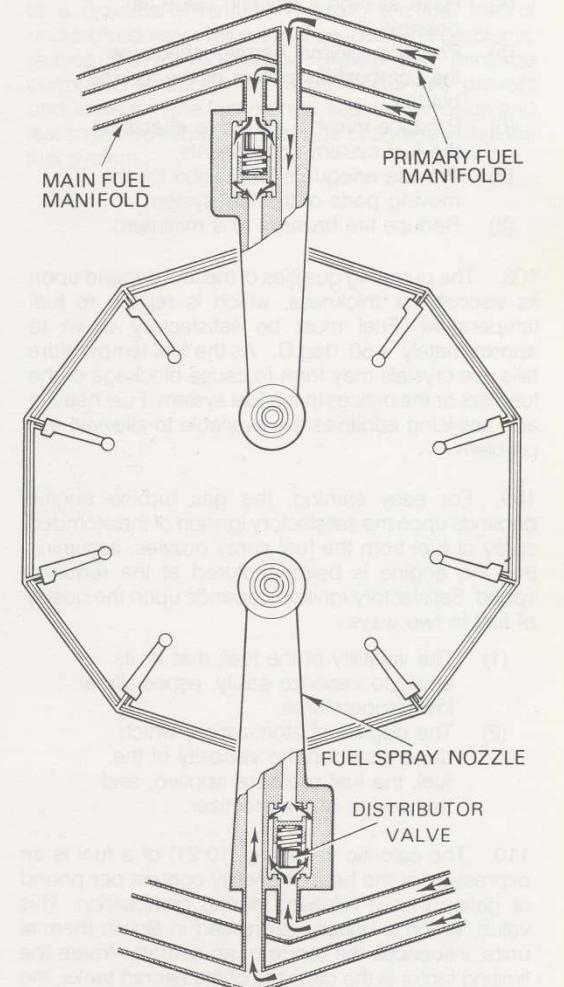
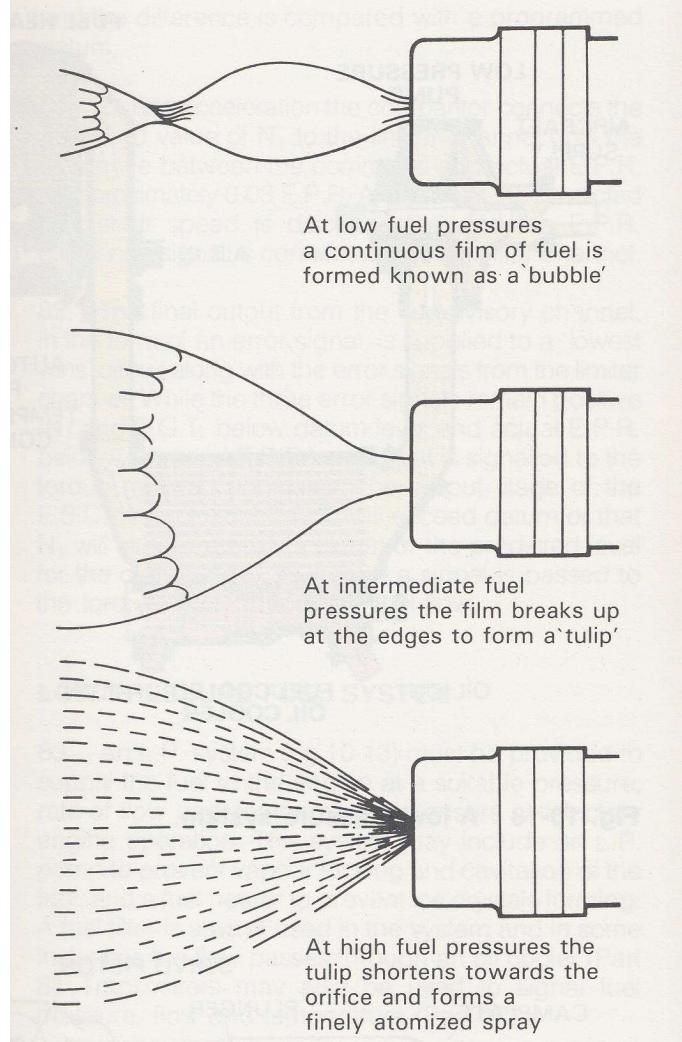


c/o Rolls-Royce

# Stators in a Compressor

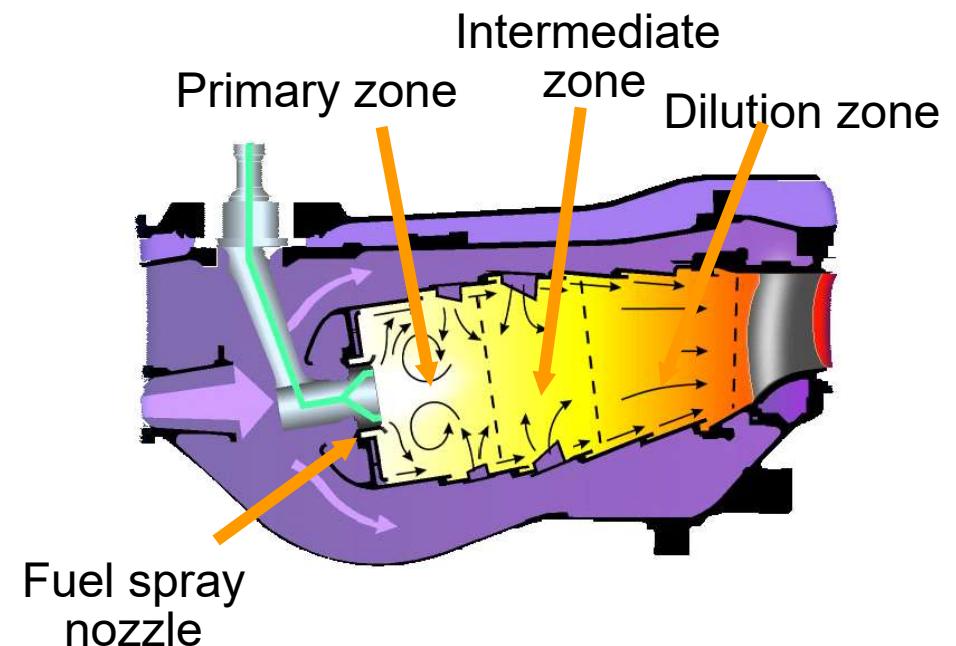


# Fuel Injection



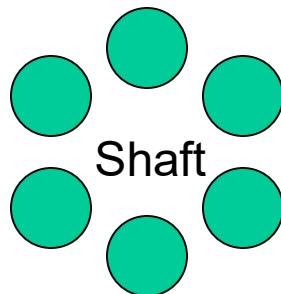
# Combustor

- Fuel nozzles are like perfume atomizers
- Burn pattern is designed for a certain engine
- Temperature very high. Keep it away from the metal surface.



c/o Rolls-Royce

# Combustors



NASA's CMC Combustor Liner  
2200 F for 9,000 hours



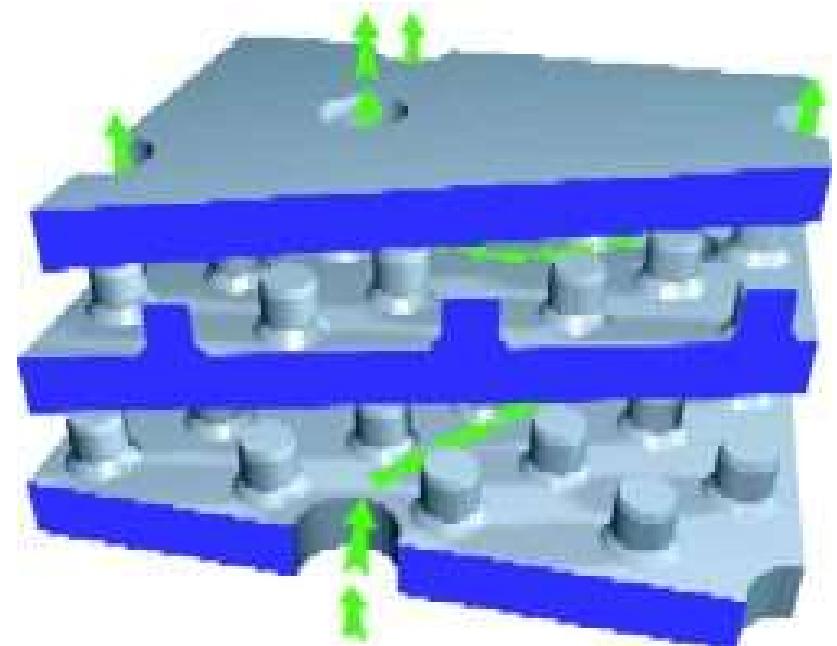
Holes shown are for Cooling Air

Combustion Liner by AADC  
Uses "Lamilloy" cooling.

This is an annular combustor.  
One large ring. Shaft in the  
Middle of it.

# Afterburner/Nozzle

- Lamilloy® is a quasi-transpiration cooling material
- Uses sandwich panels to divert cooling air

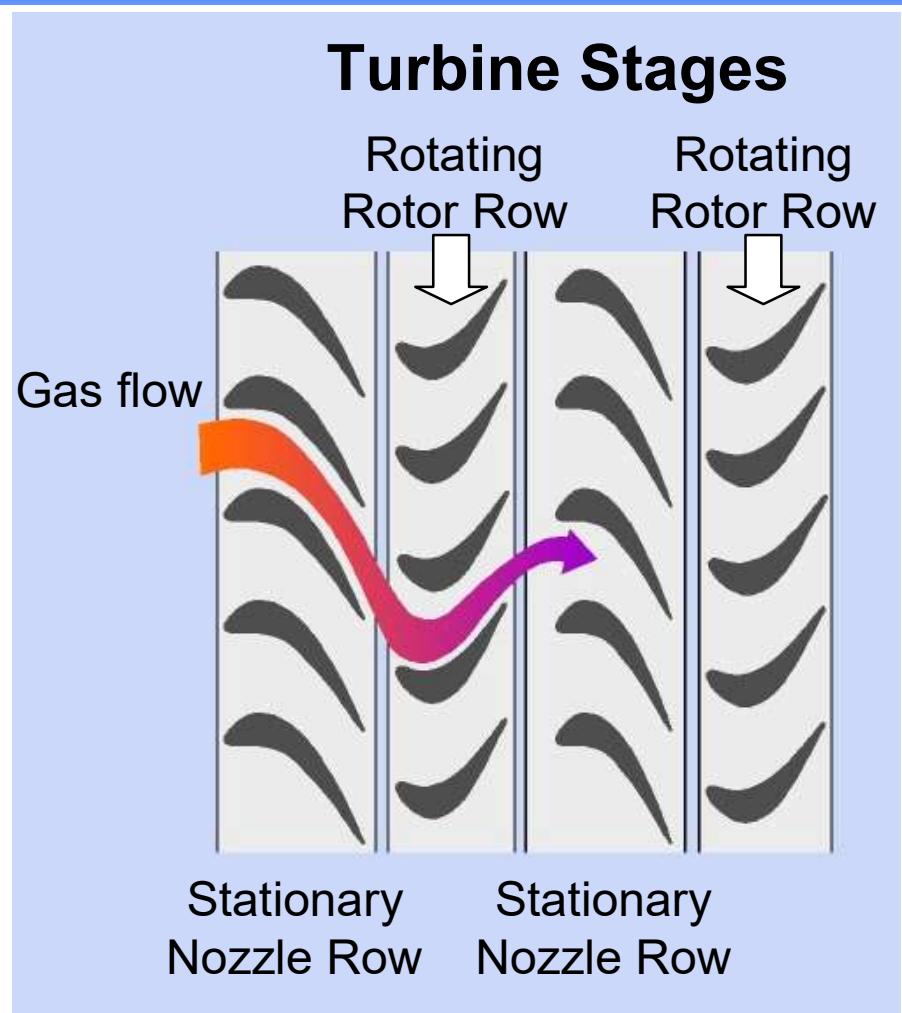


**Lamilloy® Sandwich Panels**

c/o Rolls-Royce

# HP/LP Turbine

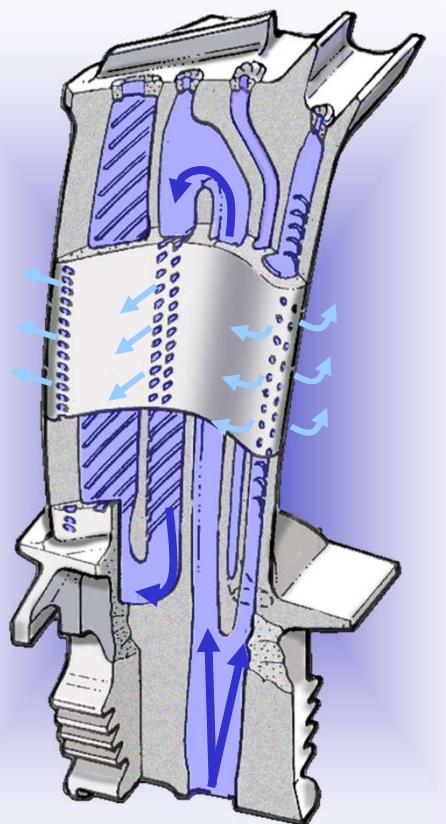
- HPT
  - Sometimes Single Stage
  - Efficiency: 90.5%
  - RIT: 2500-3000°F
  - Cooled blades
- LPT
  - Usually Multiple Stages
  - Sometimes uncooled



c/o Rolls-Royce

# KT40 Turbine Technology

**Multi-pass  
Cooling**

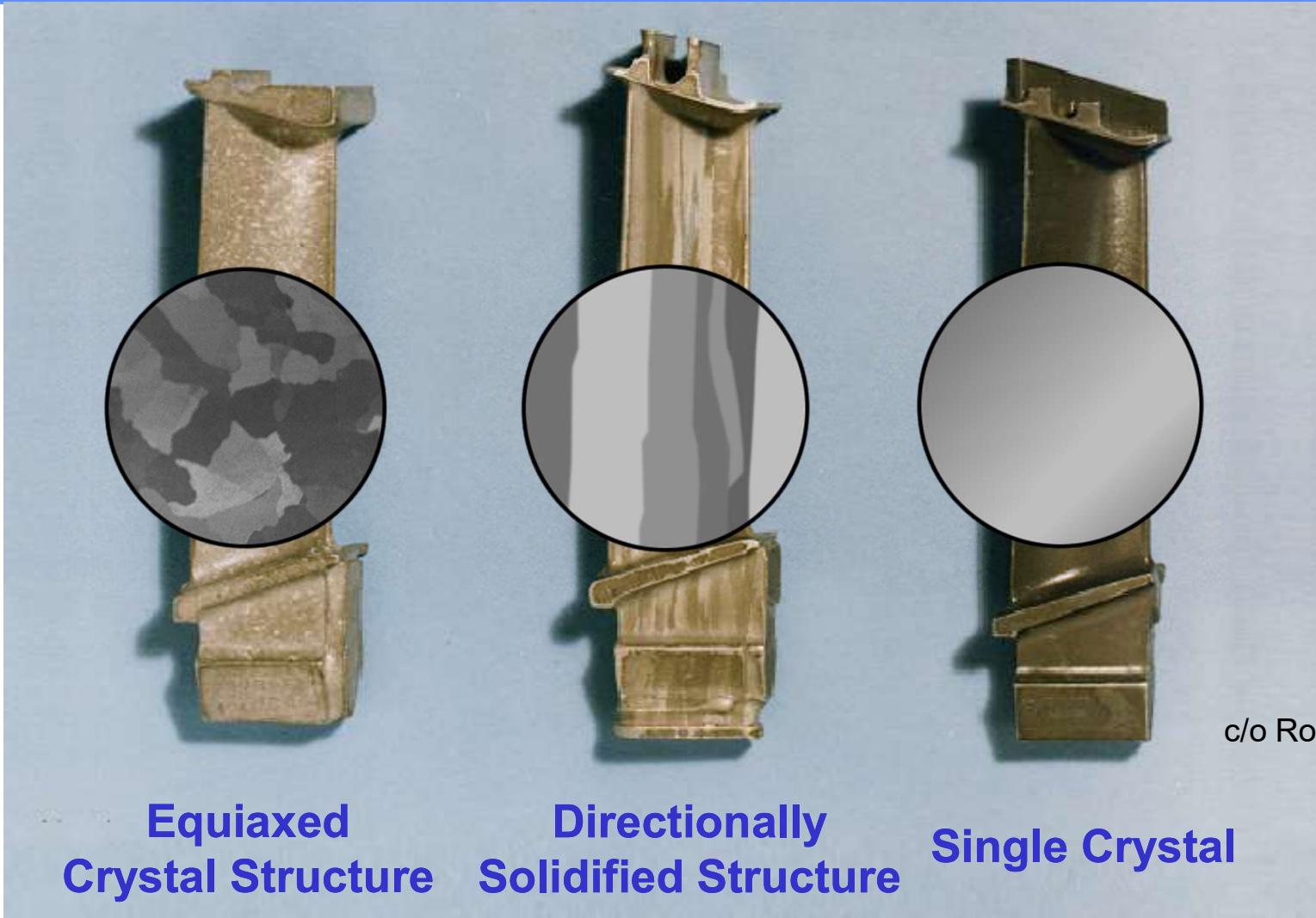


**Cooling air**

**Thermal Barrier  
Coating**



# KT40 Turbine Technology



Equiaxed  
Crystal Structure

Directionally  
Solidified Structure

Single Crystal

# Engine Performance



AE6343 Fall 2020



# Engine Performance

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- The thermodynamic cycle of the engine can be calculated and used to evaluate the performance of that engine
- This can be easily done by hand, using some given information or assumptions at the beginning of the process

# Key Terms

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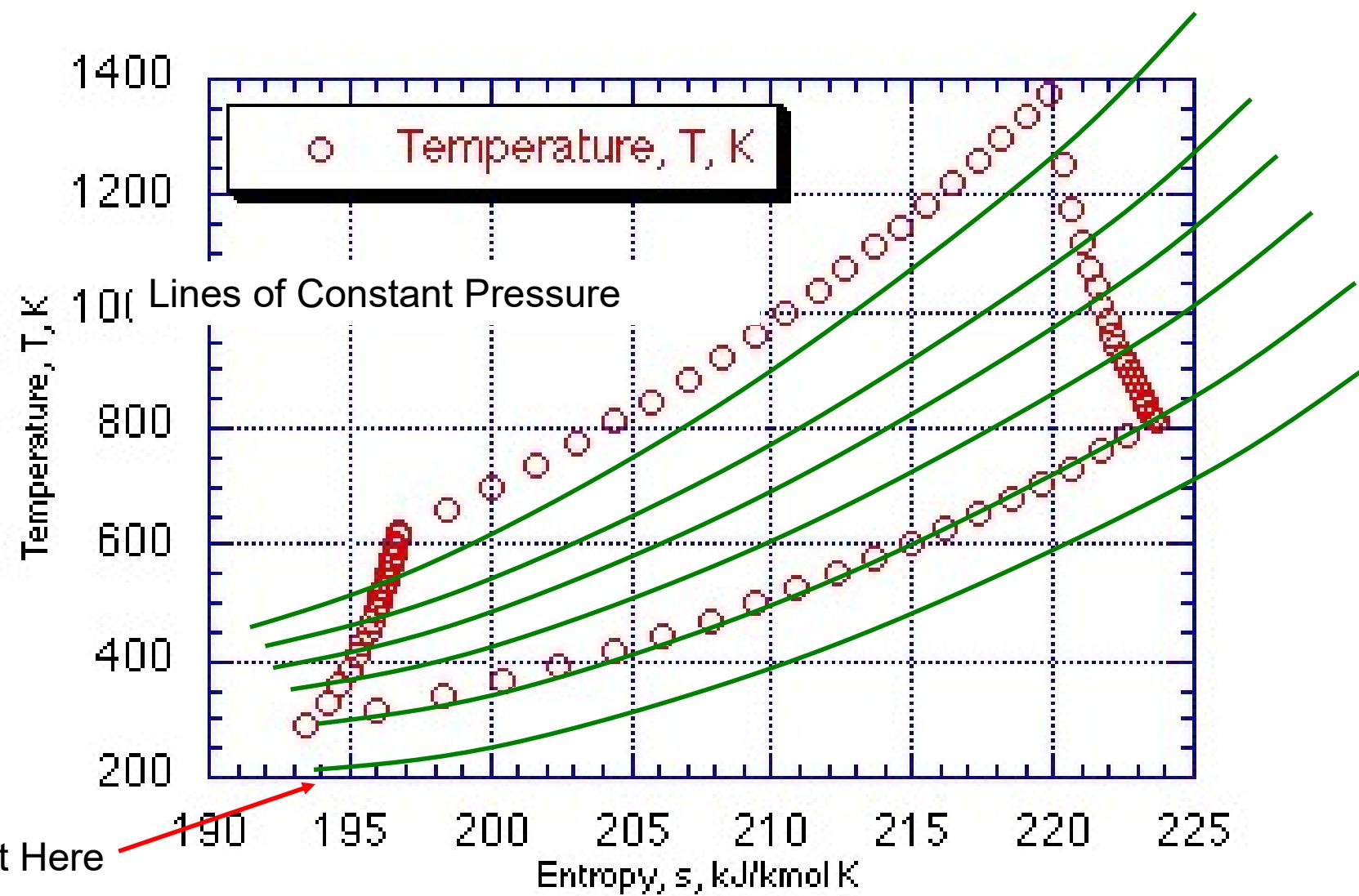
- Adiabatic = no heat loss
- Reversible Process = reactions proceed in either direction
- Isentropic = no increase in entropy
  - If something is isentropic it means it is adiabatic and reversible
- Sometimes, these terms are used interchangeably. Engines usually use the term “adiabatic” to mean no heat losses.

# Brayton Cycle

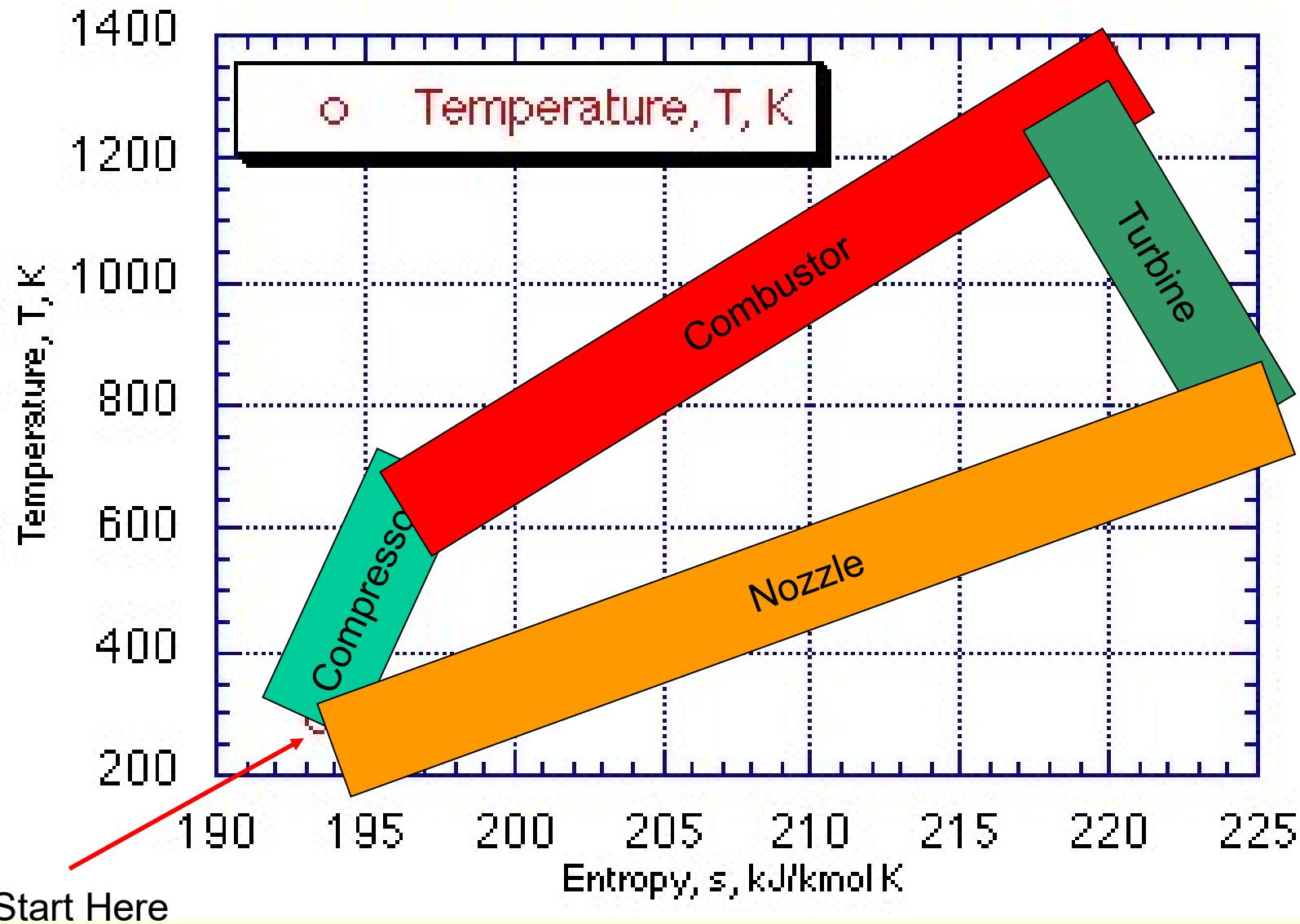
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- Four Steps:
  - Compressor working fluid
    - Use a compressor. Adiabatic compression.
  - Heat Added to Fluid
  - Extract Work from Fluid
  - Cool the Fluid

# Brayton Cycle Using Constant Specific Heats



# Brayton Cycle Using Constant Specific Heats

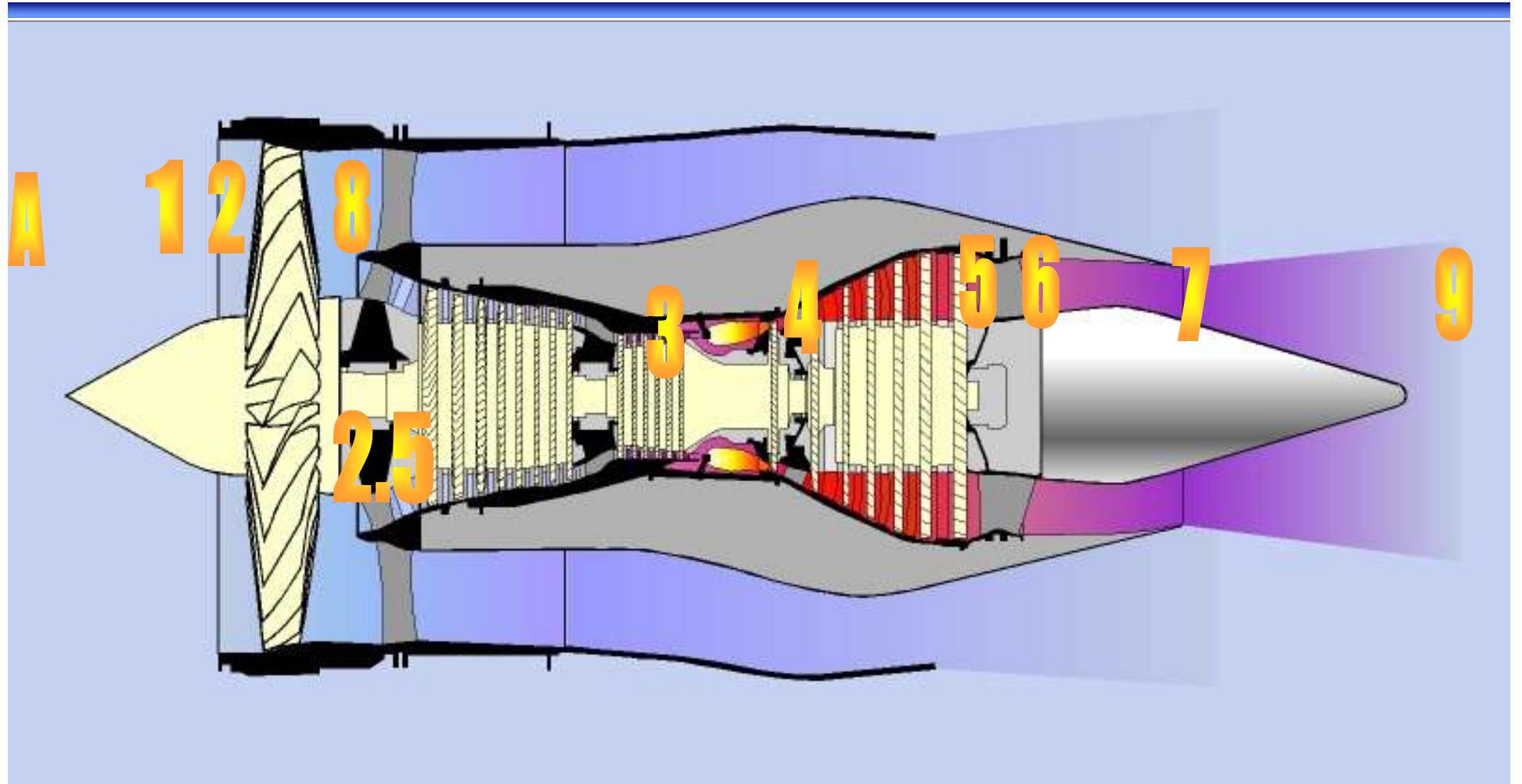


## What This Tells Us:

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- Want to combust at high pressure (higher efficiency)
  - Therefore, need to raise the pressure. Also we raise the temperature when we do this.
- We also want to combust at constant pressure
- We then take pressure or work out using a turbine
- Finally, we blow what is left out the nozzle and try to return to the starting point in a perfect cycle

# Station Numbering



# Given Information

- Bypass Ratio:  $BPR = 1.5$ 
  - Turbojet  $BPR = 0$
  - Low  $BPR = 0\text{-}2$  or  $3$
  - High  $BPR = >4$  or  $5$
  - Ultra High  $BPR = 10$  or  $12$ .
    - These are for a blended wing body or tip driven fan. Not for 777-ish engines.
    - Why? The fan would hit the ground!!!

$$BPR = \frac{\bullet}{\bullet}$$
$$m_{cold} \\ m_{hot}$$

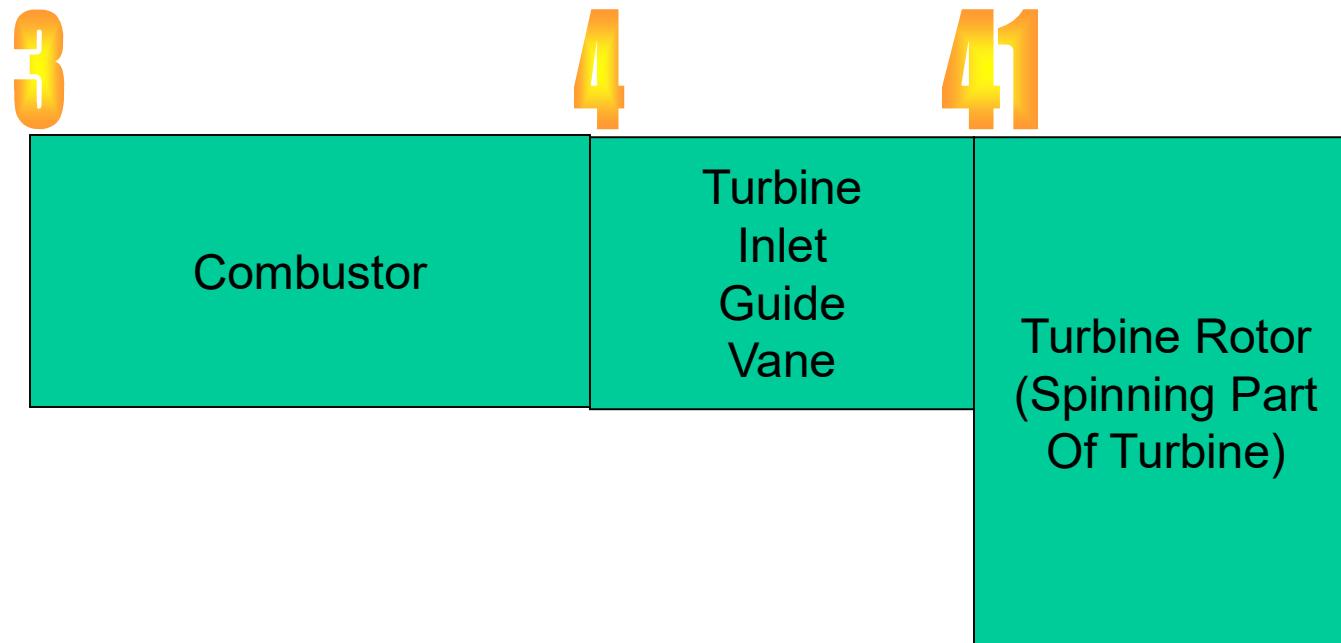
# Given Information

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- Pressure Ratio = How much does the stagnation pressure increase as work is added?
- Compressor (CPR),  $\pi_c=10$  (typically 10-35)
- Fan (FPR),  $\pi_f=2.0$  (typically 1.2 – 2.5)
- Fuel Heating Value ( $q_r=44,194,000 \text{ J/kg}$ )
  - This is about right for JP-4 jet fuel
  - This is a measure of how much heat is released (energy, J) for each kg of fuel burned

# Given Information

- RIT =  $2000^{\circ}\text{K}$ 
  - This is the rotor inlet temperature
  - This is sometimes called “T41”



# Given Information- Efficiencies

---

- Not all components can be 100% efficient
  - In fact, some are not even close!!!
- Efficiencies,  $\eta$ 
  - Fan,  $\eta_f = 91\%$
  - Compressor,  $\eta_c = 88\%$
  - Combustor,  $\eta_b$  ( $b$  is for burner) = 98%
    - This can be as high as 99.9%. Often very high.
  - Turbine,  $\eta_t = 98\%$
  - Nozzle,  $\eta_n = 100\%$

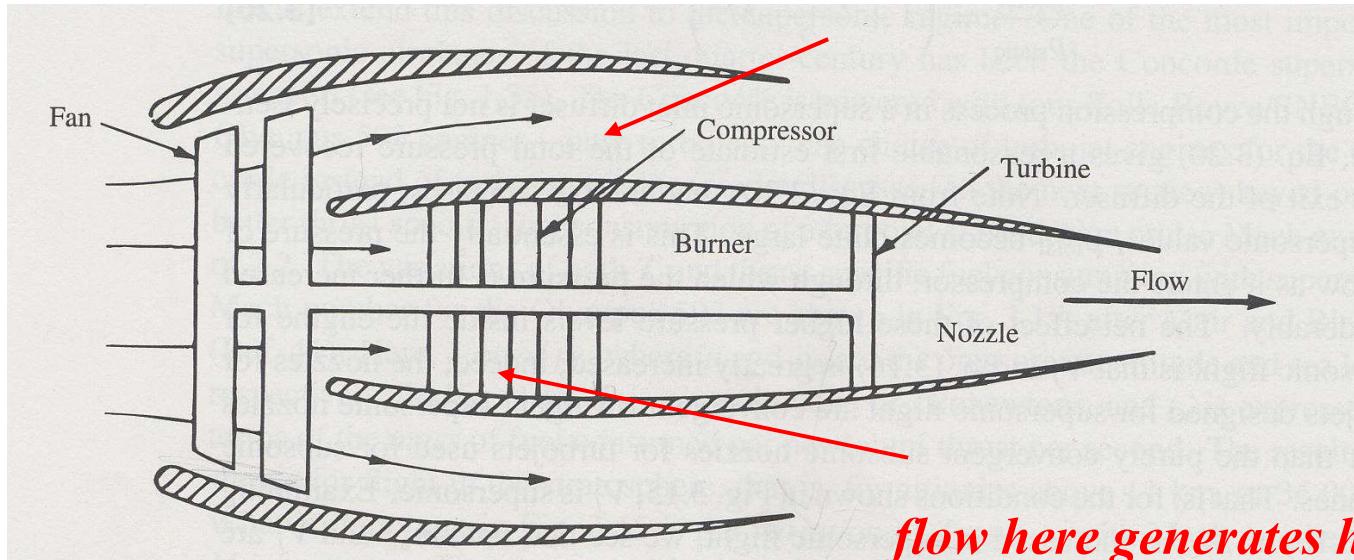
# Stagnation Pressure Loss

- As we travel through the engine, we will lose some of the starting stagnation pressure.
- Stagnation pressure translates to work. Taking it away is like throwing away our ability to do work.
- This is also called “pressure recovery,  $r$ ”
  - Inlet pressure recovery,  $r_i = 90\%$
  - Burner Pressure Recovery,  $r_b=95\%$
  - The second one is worse because the pressure in the burner is MUCH higher than the inlet pressure!!!

# Turbofan Engine

Strives to combine the high thrust of a turbojet with the high efficiency of a propeller

*flow here takes advantage of the propeller*



*flow here generates high thrust*

Core of turbofan is a turbojet. However, the turbine drives not only the compressor but a large external fan

# Bypass Ratio

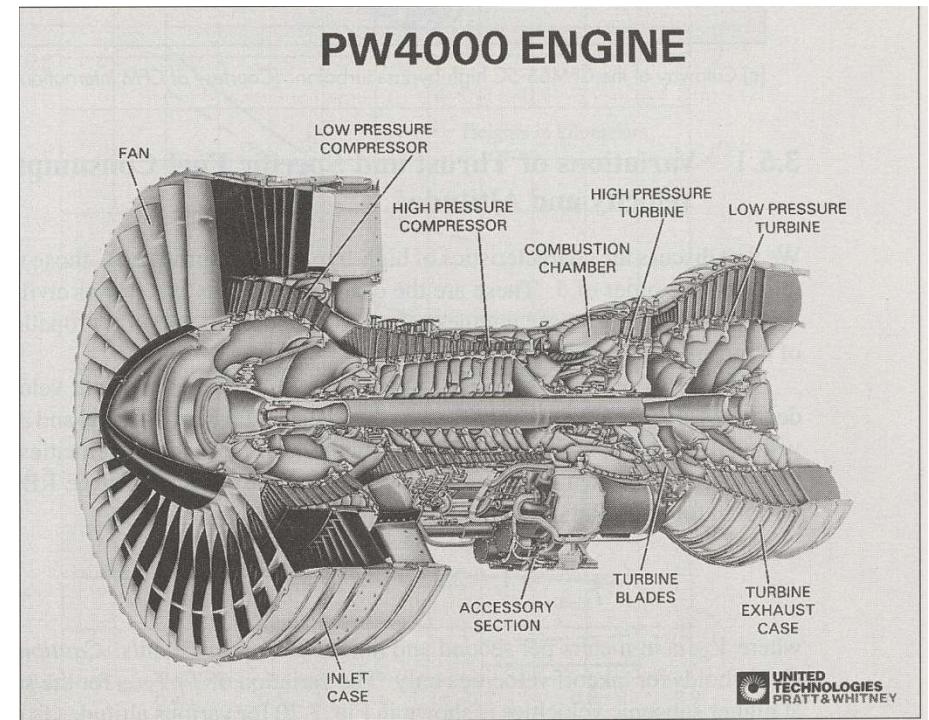
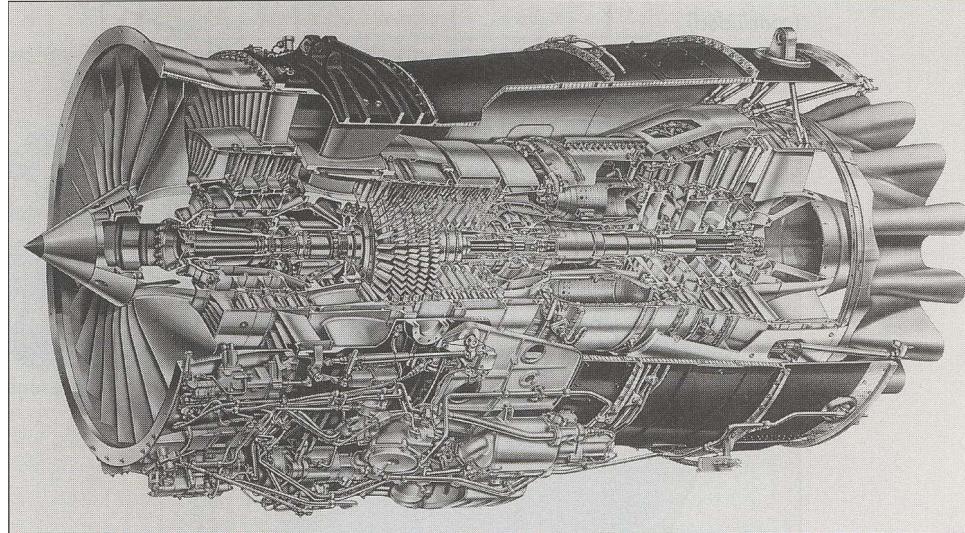
$$\text{Bypass ratio} = \frac{\text{mass flow through the fan}}{\text{mass flow through the core}}$$

The higher the bypass ratio, the higher the propulsive efficiency

Typical bypass ratios are on the order of 5.

Typical values of TSFC are **0.6  $\frac{\text{lb}}{\text{Hr}^* \text{ h}}$**  (almost half of a conventional turbojet)

# Typical High Bypass Turbofan

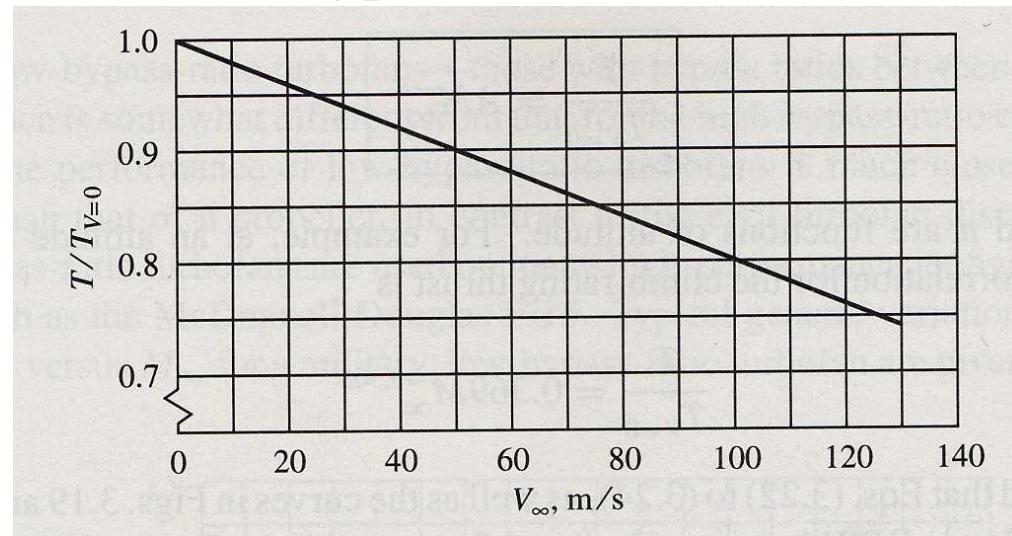


# Variation of Thrust with Velocity and Altitude

$T \downarrow$  as  $V_\infty \uparrow$

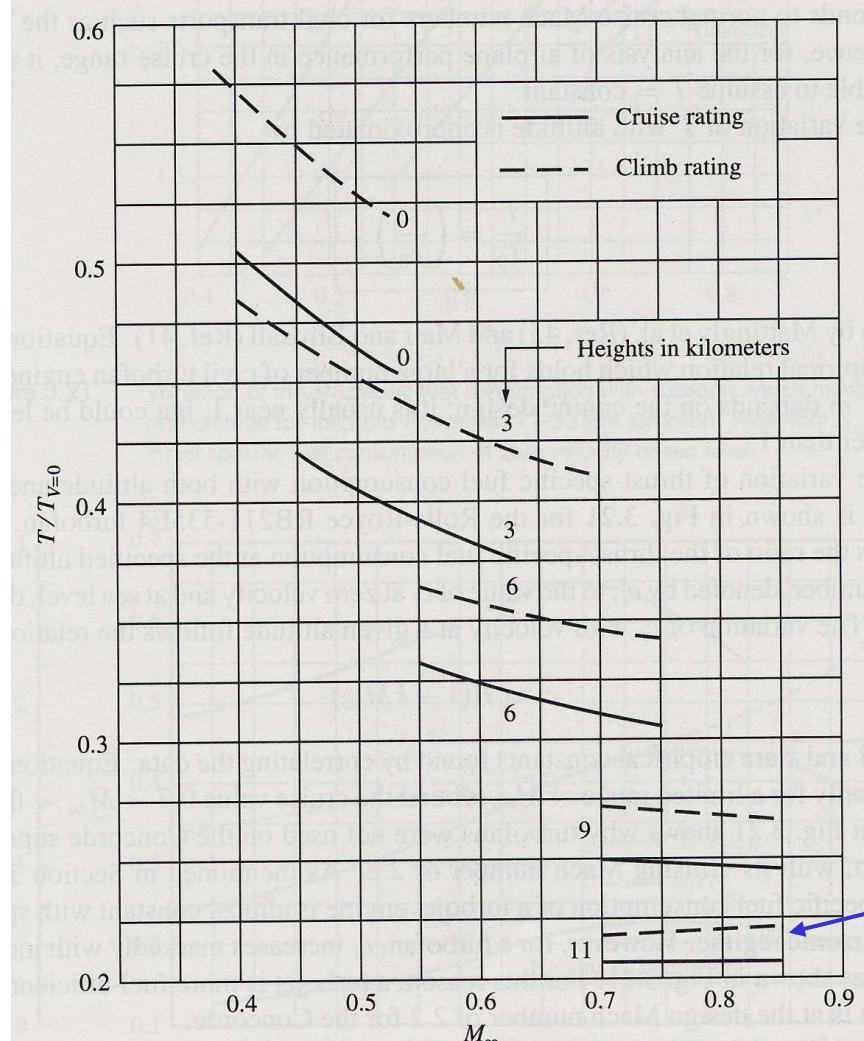
Thrust has strong variation with velocity

Civil Transport Turbofans: bypass ratios of 5+. This is considered “high”



Max Takeoff Thrust as a function of velocity at sea level  
Rolls Royce RB211-535E4 Turbofan

# Variation of Thrust with Velocity and Altitude



Empirical Relationship for variation of  $T$  with altitude:

$$\frac{T}{T_0} = \left( \frac{\rho}{\rho_0} \right)^m$$

( $m$  is function of engine design, usually 1)



Note relatively flat curve at higher altitudes for  $M=0.70$  to  $M=0.85$ .

This corresponds to normal cruise Mach numbers, so  $T$  can be assumed constant in the cruise range.

# TSFC varying with Velocity and Altitude

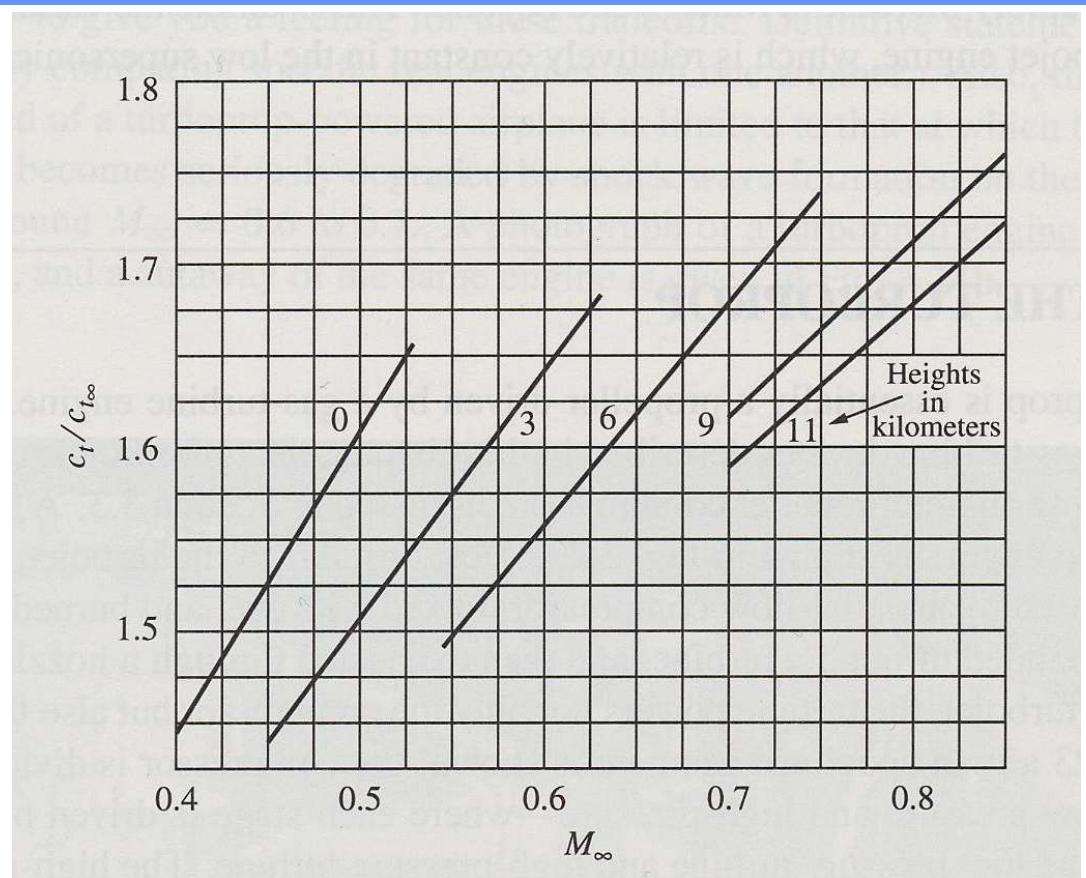
$$c_t \quad \text{as} \quad V_{\infty}$$

Follows the relation:

$$c_t = B (1 + kM_{\infty})$$

where  $B$  and  $k$  are empirical constants found from correlating engine data

$c_t$  is near constant with altitude



Remember: for a turbojet, TSFC was near constant with speed in supersonic regime. Therefore, turbojet is more **efficient** choice for supersonic cruise aircraft than turbofan.

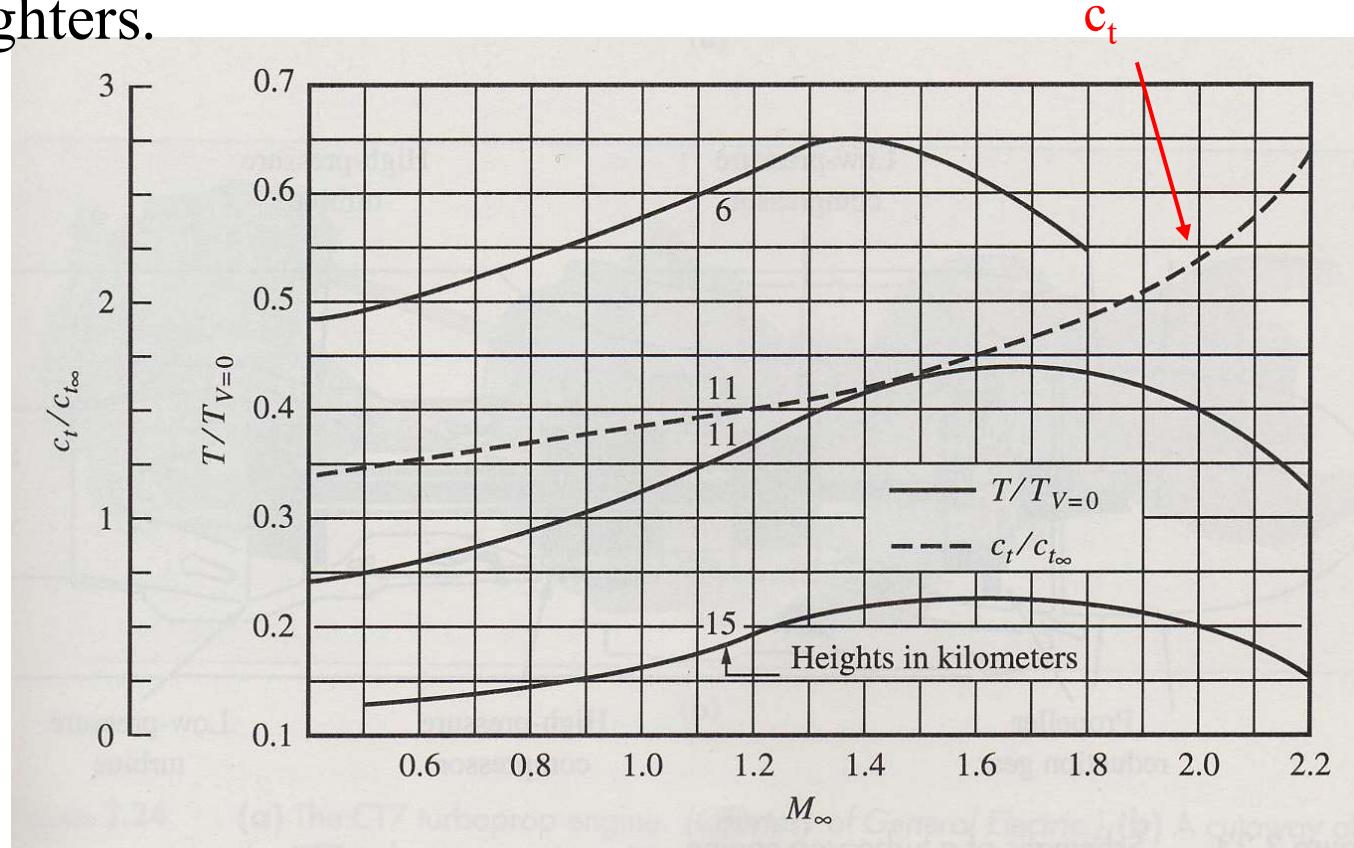
# Low Bypass Ratio variations

For low bypass turbofans (between 0 and 1), the performance more closely models a turbojet than a propeller. Generally used on high performance fighters.

$T \uparrow$  as  $M \uparrow$

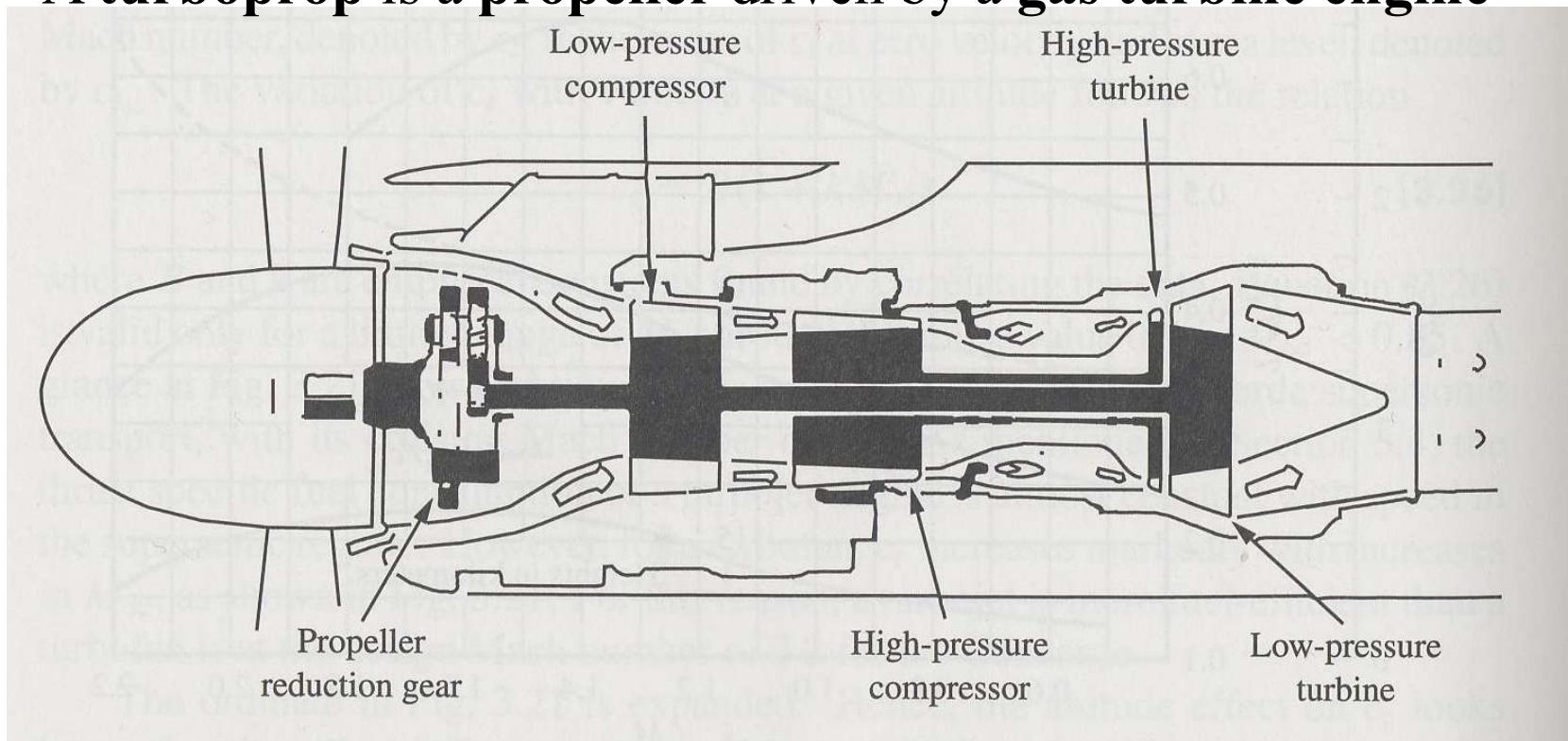
(at higher  $M$ )

$c_t \uparrow$  as  $M \uparrow$



# Turboprop Engines

A turboprop is a propeller driven by a gas turbine engine



The turbine powers both the compressor and the propeller

Most available work is extracted by the turbines, leaving little available for jet thrust. Only ~5% of total thrust is through jet exhaust.

# Characteristics of a Turboprop

---

- Turboprops generate **more thrust** than a reciprocating/propeller combination
- Turboprops generate **less thrust** than turbofans or turbojets
- Turboprops have **higher SFC** than reciprocating/propeller but **lower** than turbofans or turbojets
- Maximum flight speed of turboprop is limited by shock waves (usually  $M=0.6$  to  $0.7$ )

# Turboprop Equations

Thrust is sum of propeller thrust and jet thrust. Power available at  $V_\infty$  is

$$P_A = (T_p + T_j)V_\infty$$

$T_p$  is propeller thrust  
 $T_j$  is jet thrust

Due to the propeller aspect of the turboprop, performance is often in terms of **power**

$$P_A = \eta_{pr} P_S + T_j V_\infty$$

$P_S$  is shaft power

Equivalent shaft power,  $P_{es}$ , includes the effect of jet thrust

$$P_A = \eta_{pr} P_{es}$$

This relationship defines  $P_{es}$

# Turboprop Equations

Combining above two equations,

$$P_{es} = P_s + \frac{T_j V_\infty}{\eta_{pr}}$$

*This relates equivalent shaft power to actual shaft power and jet thrust.*

TSFC is defined as

$$c_t = \frac{\dot{\omega}_{fuel}}{T}$$

*We don't use power because it could be confusing as to which power we are referring to:*

$$\begin{aligned} P_s \\ P_{es} \\ P_A \end{aligned}$$

Useful approximation: at static conditions (engine operating with airplane at zero velocity on the ground), a turboprop produces 2.5 lb/shp

# Variations of Power with Velocity/Altitude for Turboprops

Recall:

$$P_A = T_A V_\infty$$

At  $M > \sim 0.7$ ,  $T_A \downarrow$

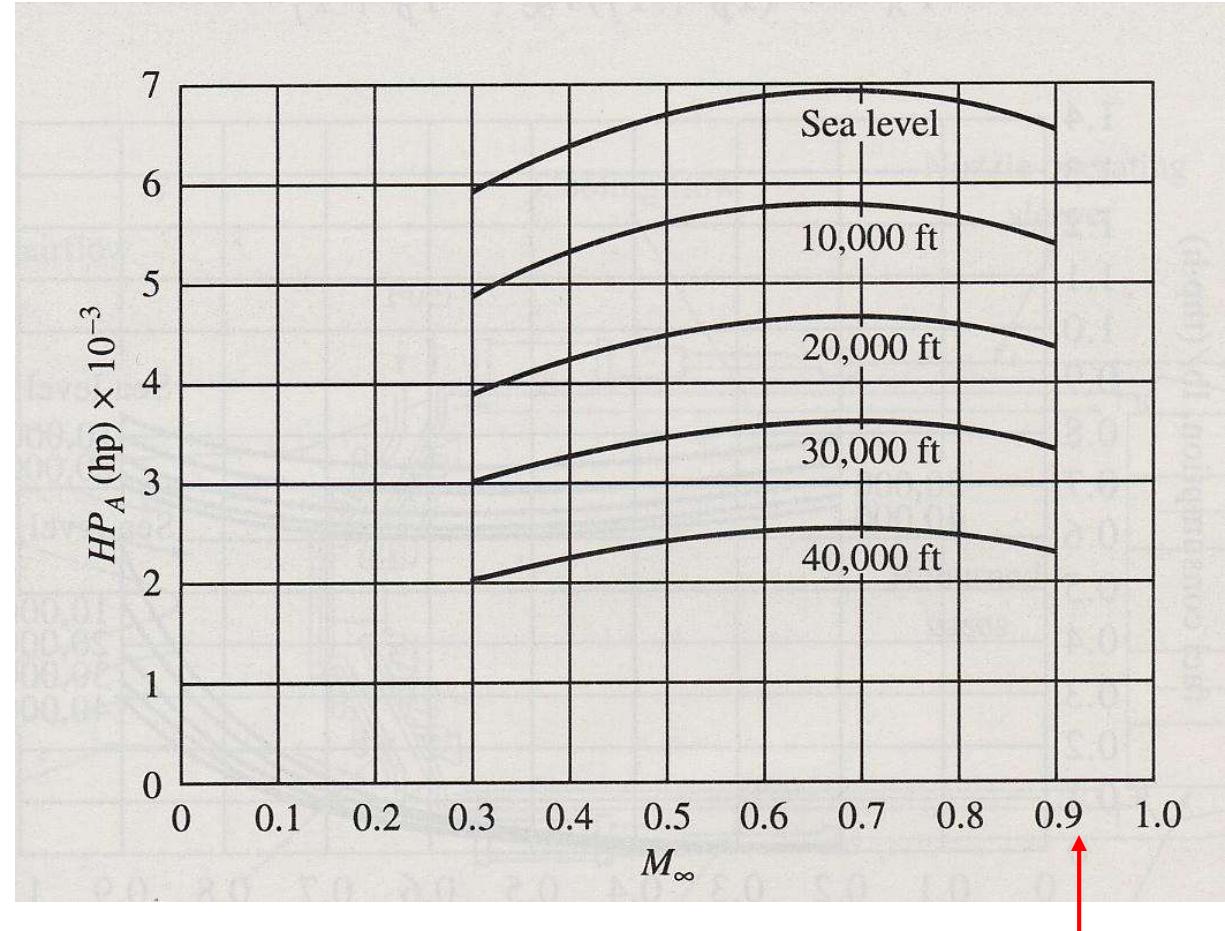
Combined effect of  $V_\infty$  and  $T_A$  results in

$P_A$  is constant with  $M_\infty$

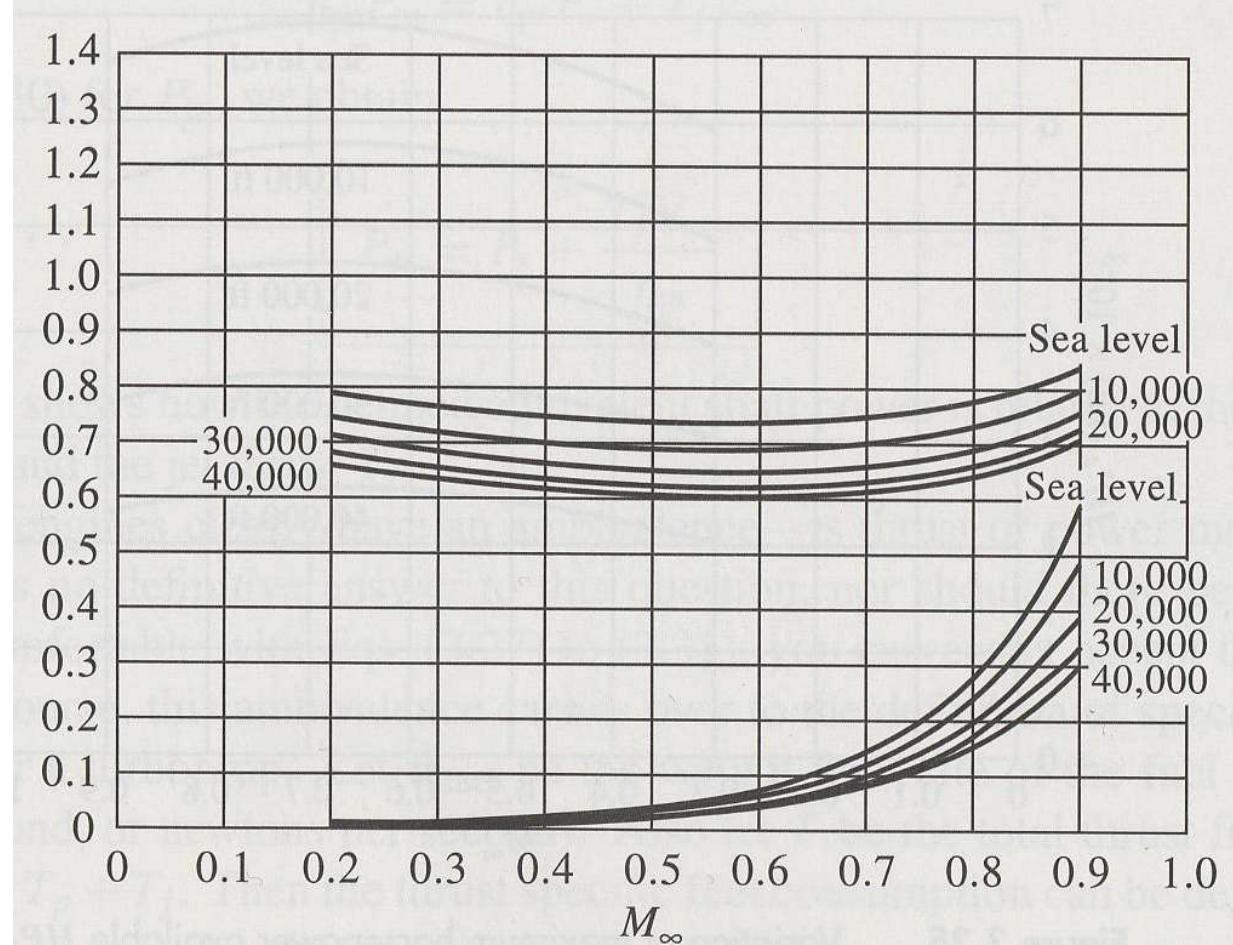
For altitude, use

$$\frac{P_A}{P_{A,0}} = \left(\frac{\rho}{\rho_0}\right)^n$$

$n = \text{depends on engine, use 0.7 for unknown}$



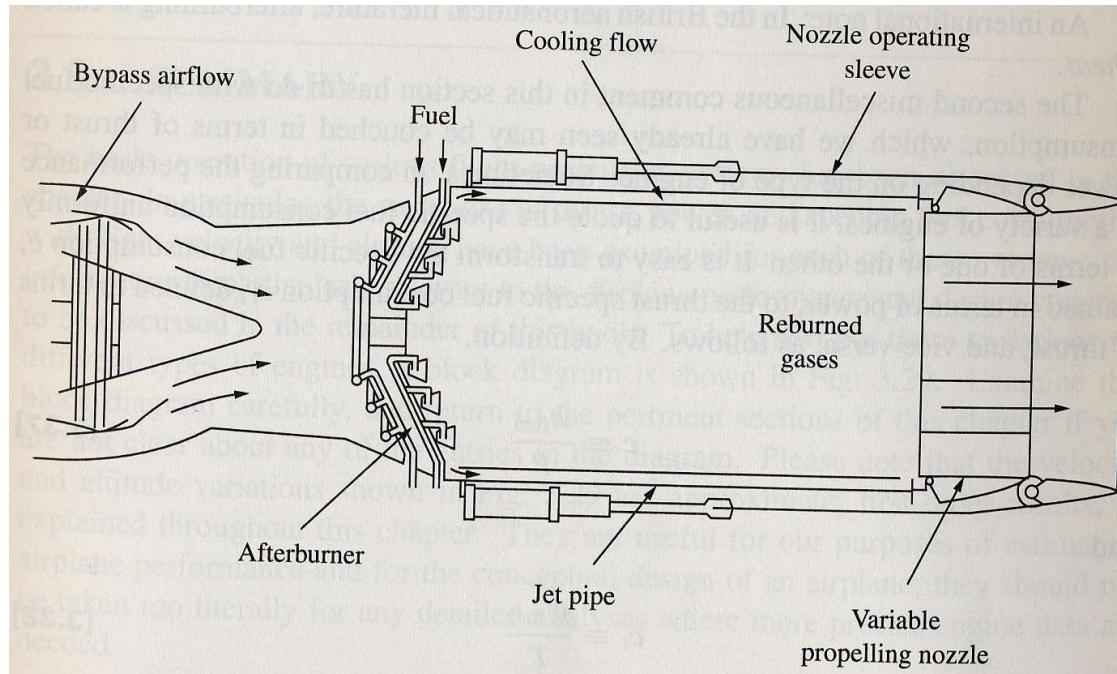
# Variations of SFC with Velocity/Altitude for Turboprops



SFC can be assumed constant with velocity and altitude

# Afterburners

For a turbojet or turbofan, the fuel-air mixture in the combustion chamber is lean (more oxygen than fuel). Extra fuel is injected into the oxygen-rich exhaust gas and then ignited downstream of the turbine. This is called **afterburning**.

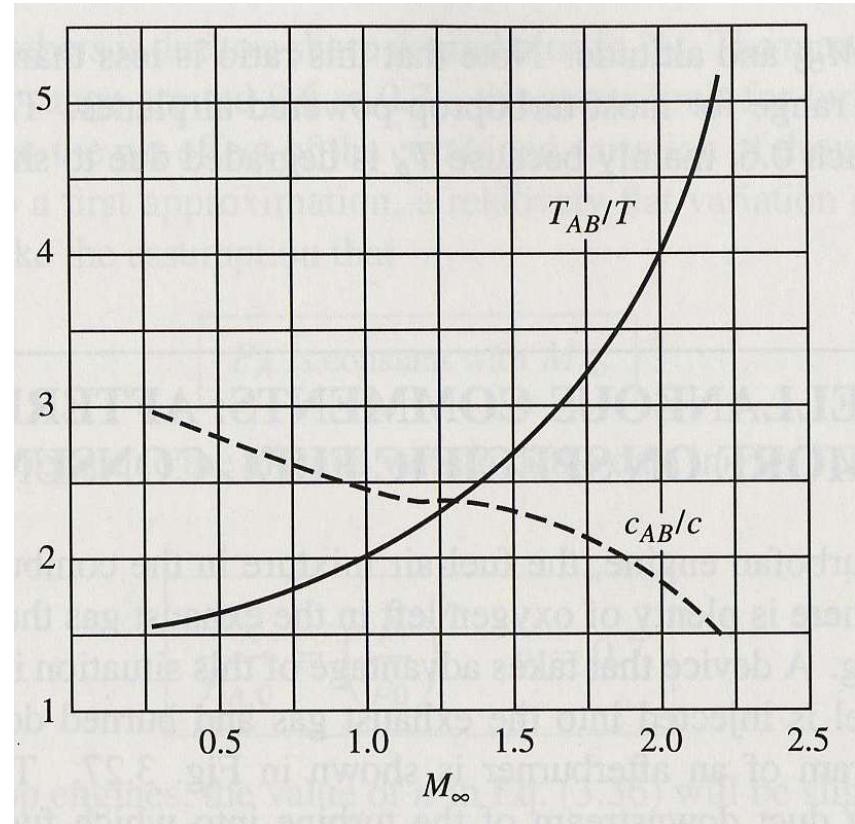


Afterburners are used for short periods of greatly increased thrust, but burns much fuel, so must be used carefully.

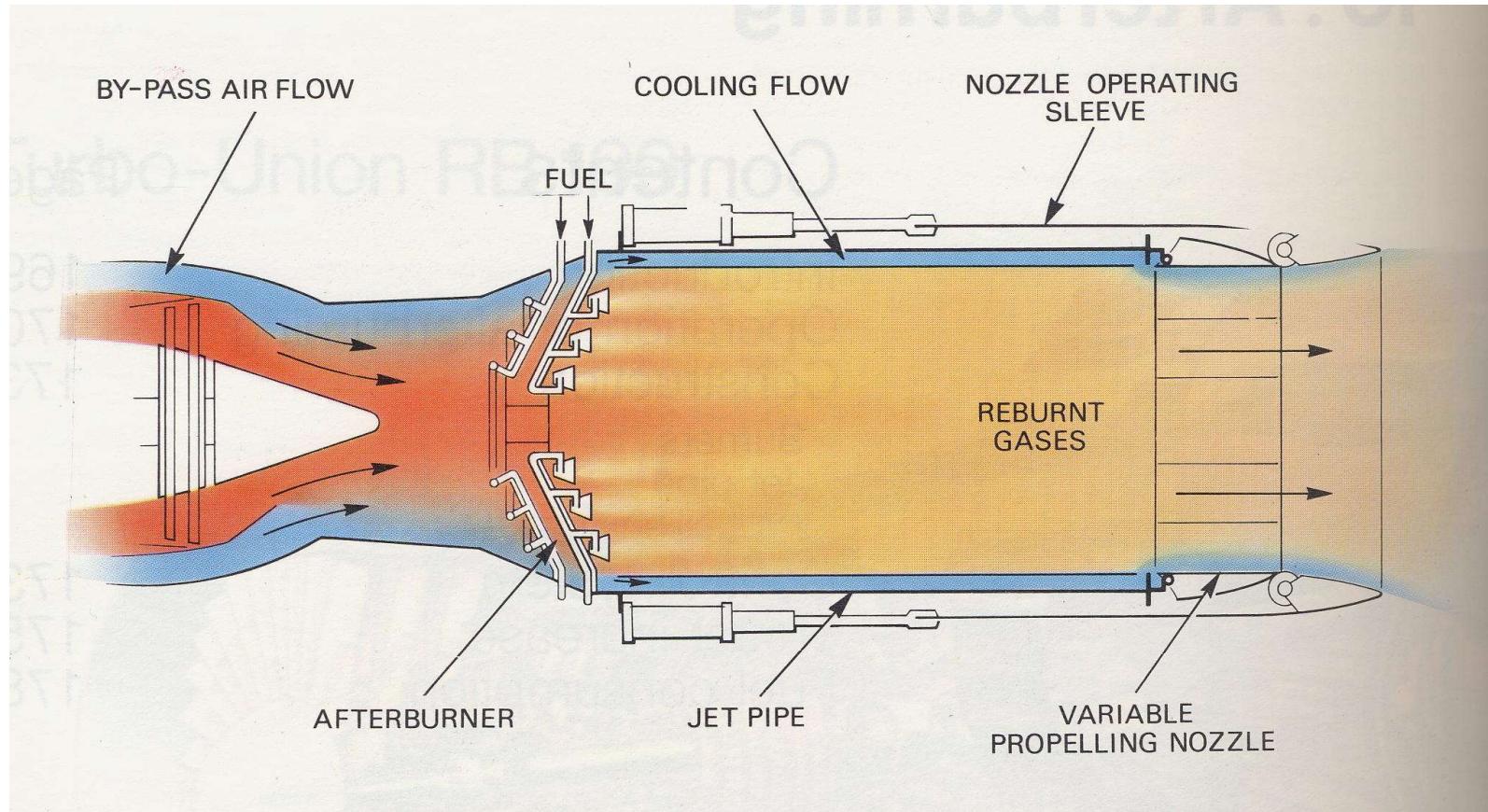
# Performance of Afterburner

The Concorde uses afterburning for rapid climb and acceleration.

The British call afterburning *reheat*.



# Afterburner



# Transforming Fuel Consumptions

It is useful to be able to transform specific fuel consumption,  $c$ , (which is in terms of power) to thrust specific fuel consumption,  $c_t$ , (which is in terms of thrust).

$$c = \frac{\dot{\omega}_{\text{fuel}}}{P} \quad \text{and} \quad c = \frac{\dot{\omega}_{\text{fuel}}}{T} \quad \text{combine to give}$$

$$c_t = \frac{cP}{T}$$

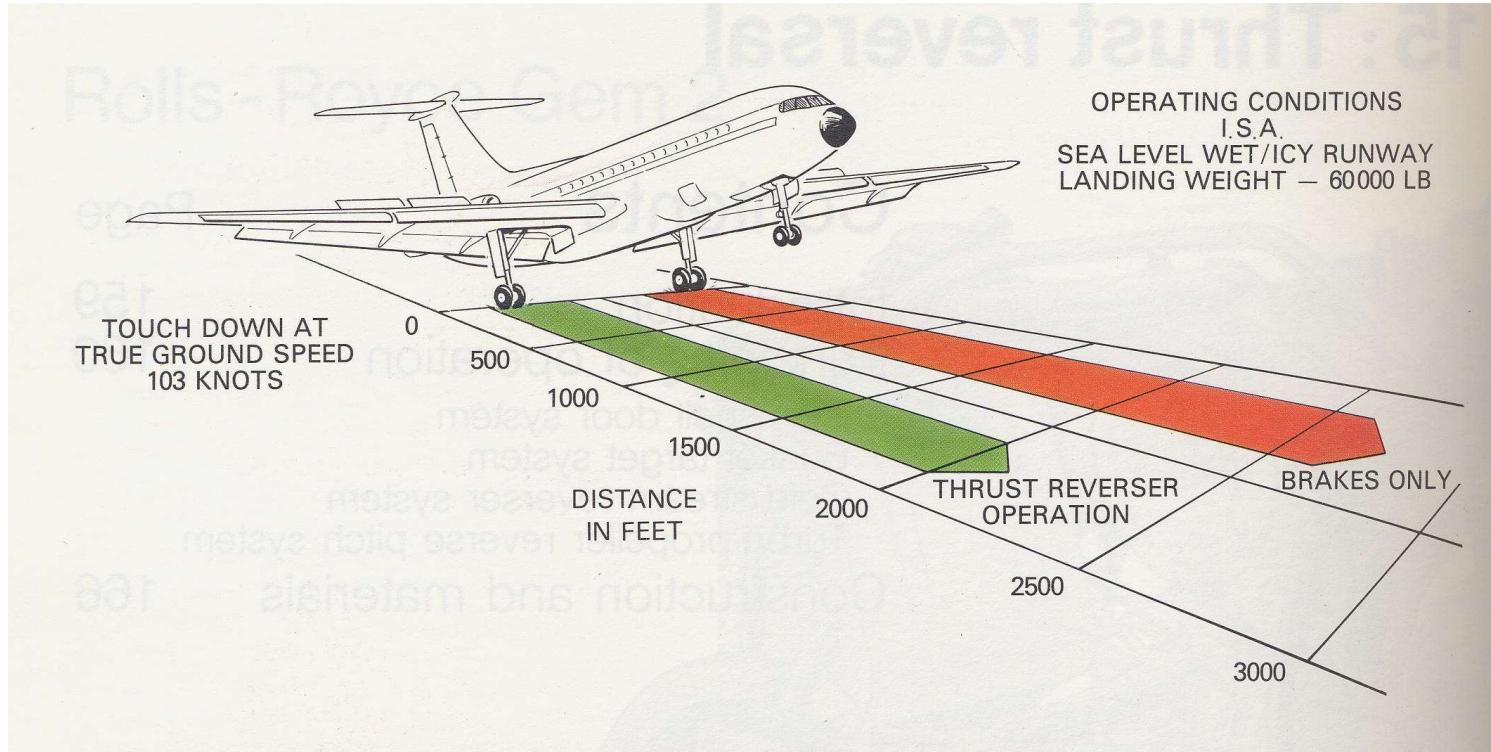
$$P = \frac{P_A}{\eta_{\text{pr}}} \quad \text{and} \quad P_A = TV_\infty \quad \text{combine to give}$$

$$P = \frac{TV_\infty}{\eta_{\text{pr}}}$$

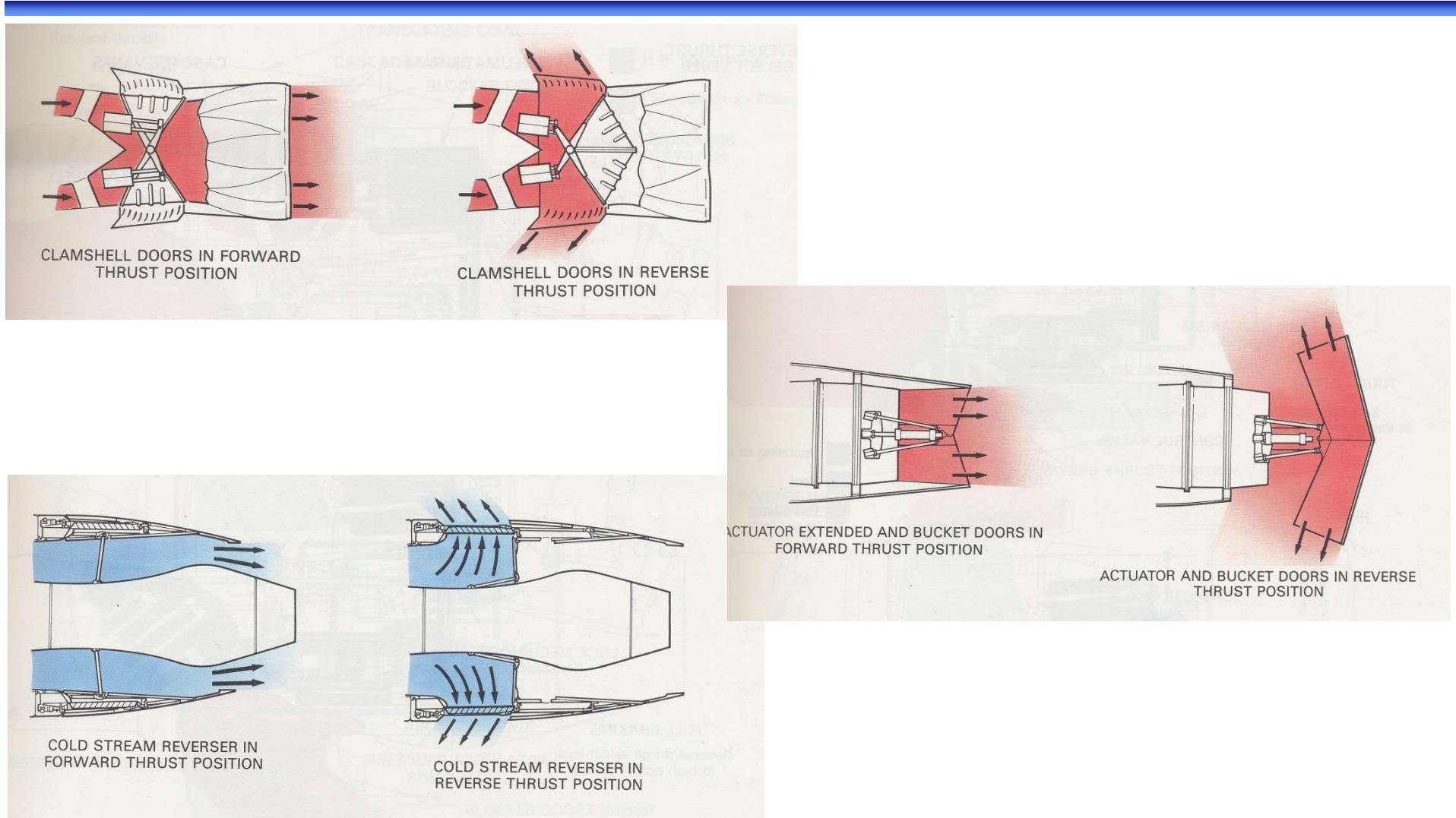
Substituting two boxed equations gives:

$$c_t = \frac{cV_\infty}{\eta_{\text{pr}}}$$

# Thrust Reversers



# Thrust Reversers

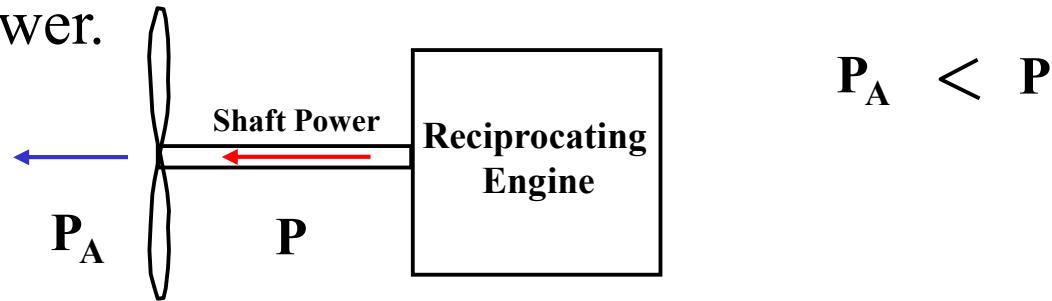


# Thrust Reversers



# The Propeller

- Realize, like Wilbur Wright did in 1902, that a propeller is nothing more than a twisted wing.
- Like a wing, a propeller produces friction drag, form drag, induced drag, and wave drag. Thus, it is a **loss mechanism** and the power output of the engine/propeller combination will always be less than the shaft power.



Propeller efficiency is defined as:

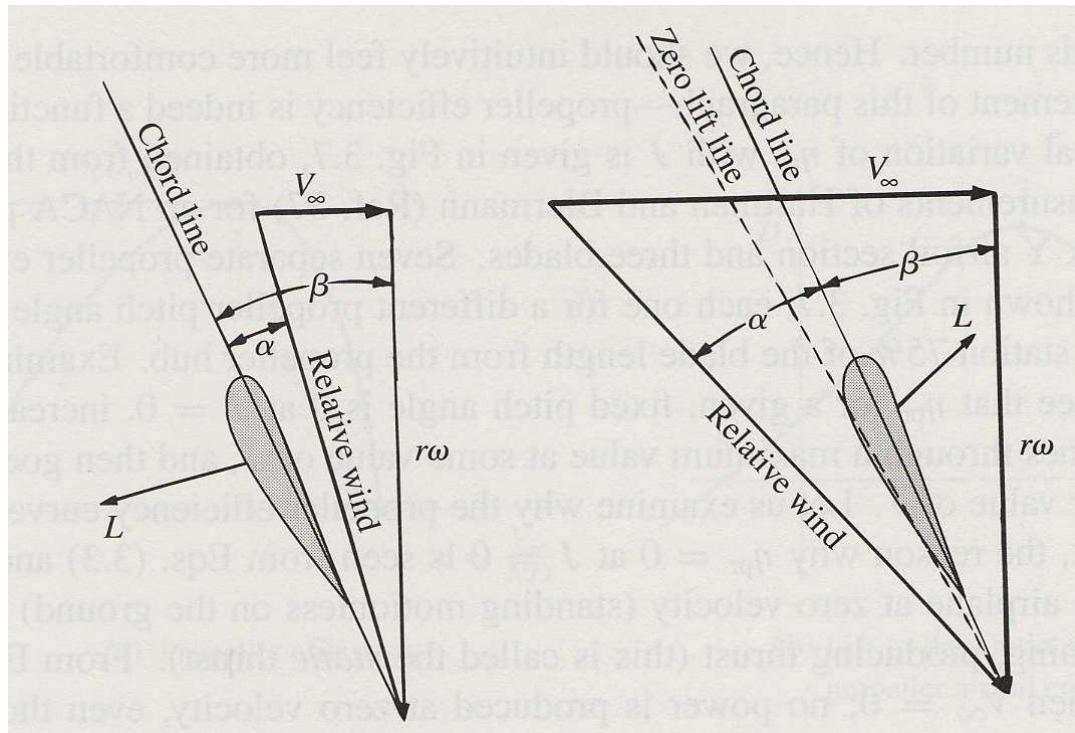
$$P_A = \eta_{pr} P$$

$$\eta_{pr} < 1$$

Propeller  
efficiency is a  
function of the  
*Advance Ratio*

# Advance Ratio, $J$

Local relative wind is the vector sum of  $V_\infty$  and the translational motion of the propeller section due to propeller rotation,  $r\omega$ .



***pitch angle,  $\beta$ ,  
between airfoil  
chord line and  
plane of rotation***

The ratio  $\frac{V_\infty}{r\omega}$  sets the direction of the local relative wind

# Advance Ratio, J

$$\frac{V_\infty}{r\omega} = \frac{V_\infty}{r(2\pi N)}$$

*N is number of propeller revolutions per second*

Evaluated at propeller tip:

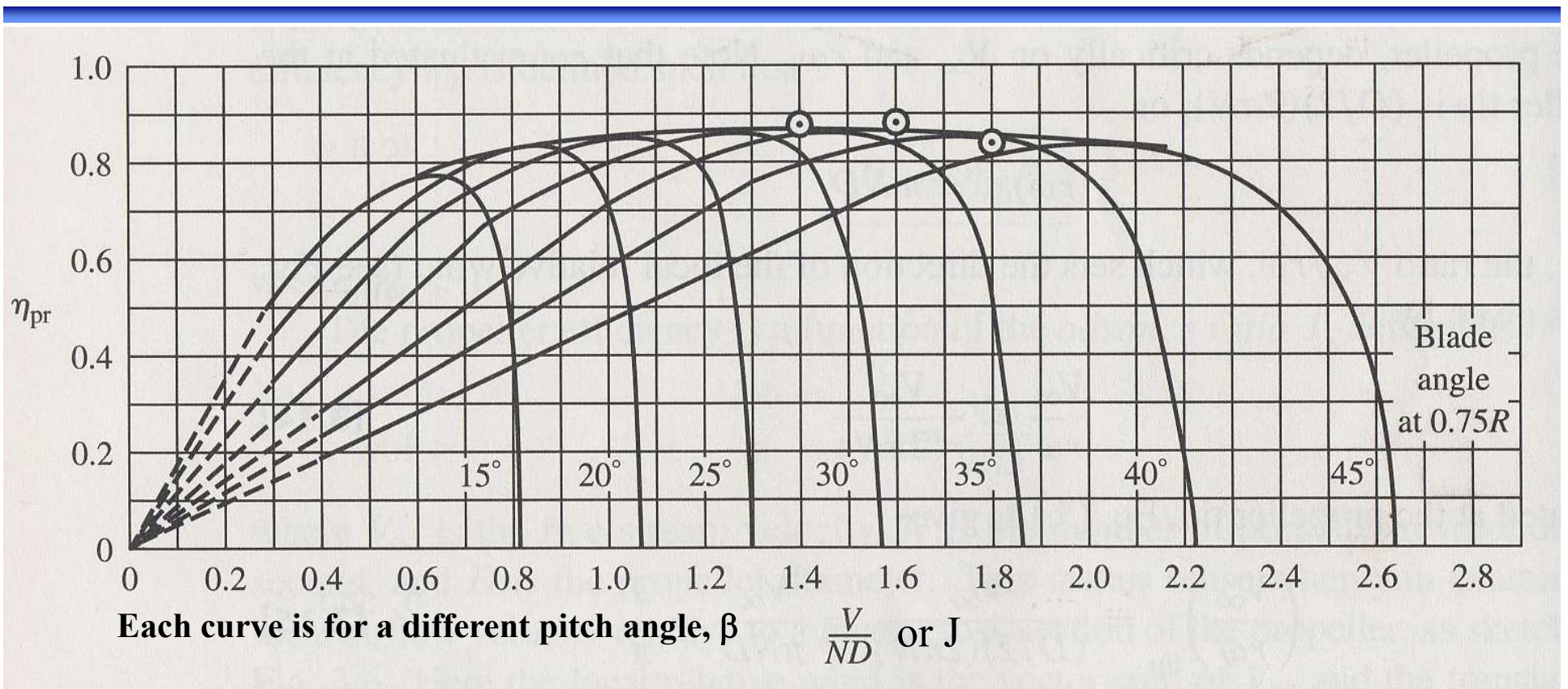
$$\left[ \frac{V_\infty}{r\omega} \right]_{\text{tip}} = \frac{V_\infty}{(D/2)(2\pi N)} = \frac{V_\infty}{\pi ND} = \frac{J}{\pi}$$

$$J = \frac{V_\infty}{ND}$$

propeller efficiency is a function of J, the advance ratio

J is a similarity parameter for propeller performance, similar to Mach number and Reynolds number

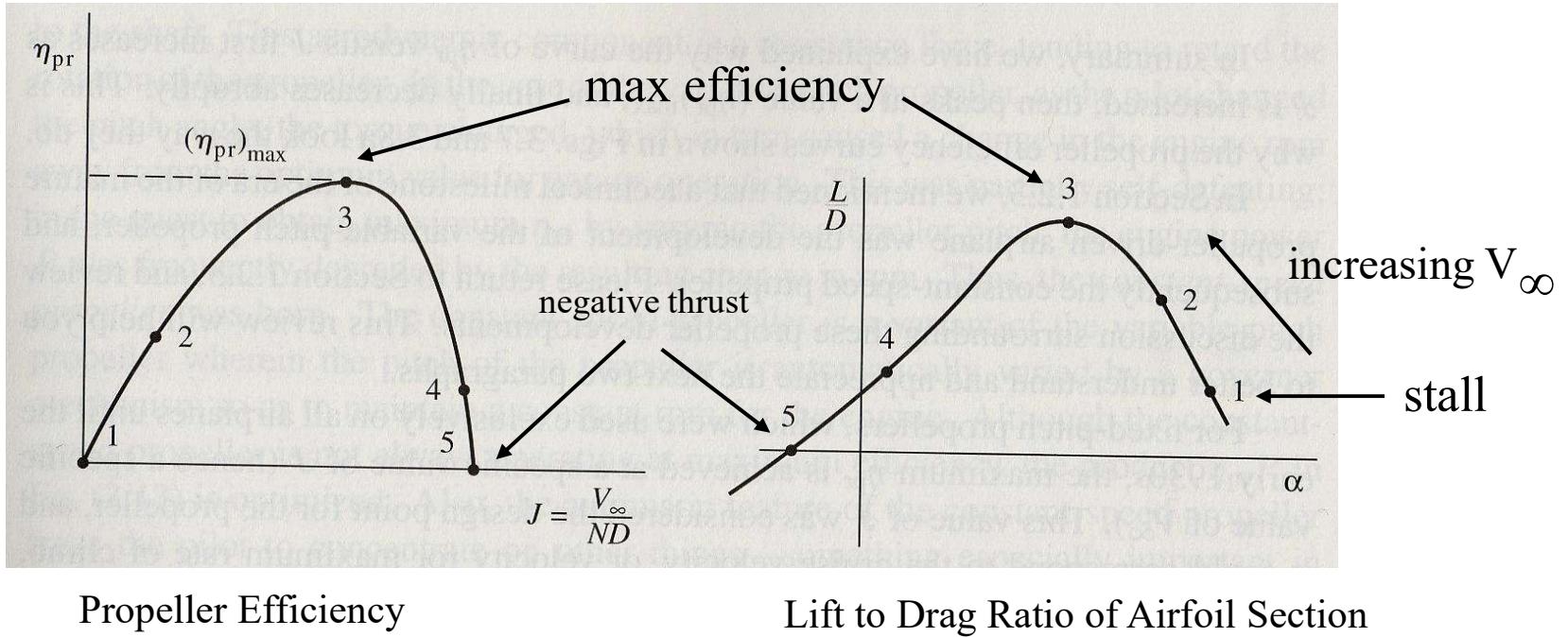
# Propeller Efficiency and J



**Remember:**

$$P_A = T V_\infty = \eta_{pr} P \quad \text{so when } J = 0, \eta_{pr} = 0$$

# Shape of Propeller Efficiency Curve



For a fixed pitch propeller,  $\beta$  is constant at any given  $r$ . Also, for a given  $N$ ,  $r\omega$  is constant

However, as  $V_\infty$  changes, the angle of attack will change, as will the efficiency.

# Feathering

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- A propeller is feathered when its pitch is adjusted so that the drag is minimized, and there is little chance of autorotation when the engine is turned off but the aircraft is still moving (the windmill effect).
- Feather the prop when there is an engine failure in midflight, or sometimes on a multi-engine aircraft when one or more engines is turned off and the others are used for taxi.

# Rate of Climb and Propellers

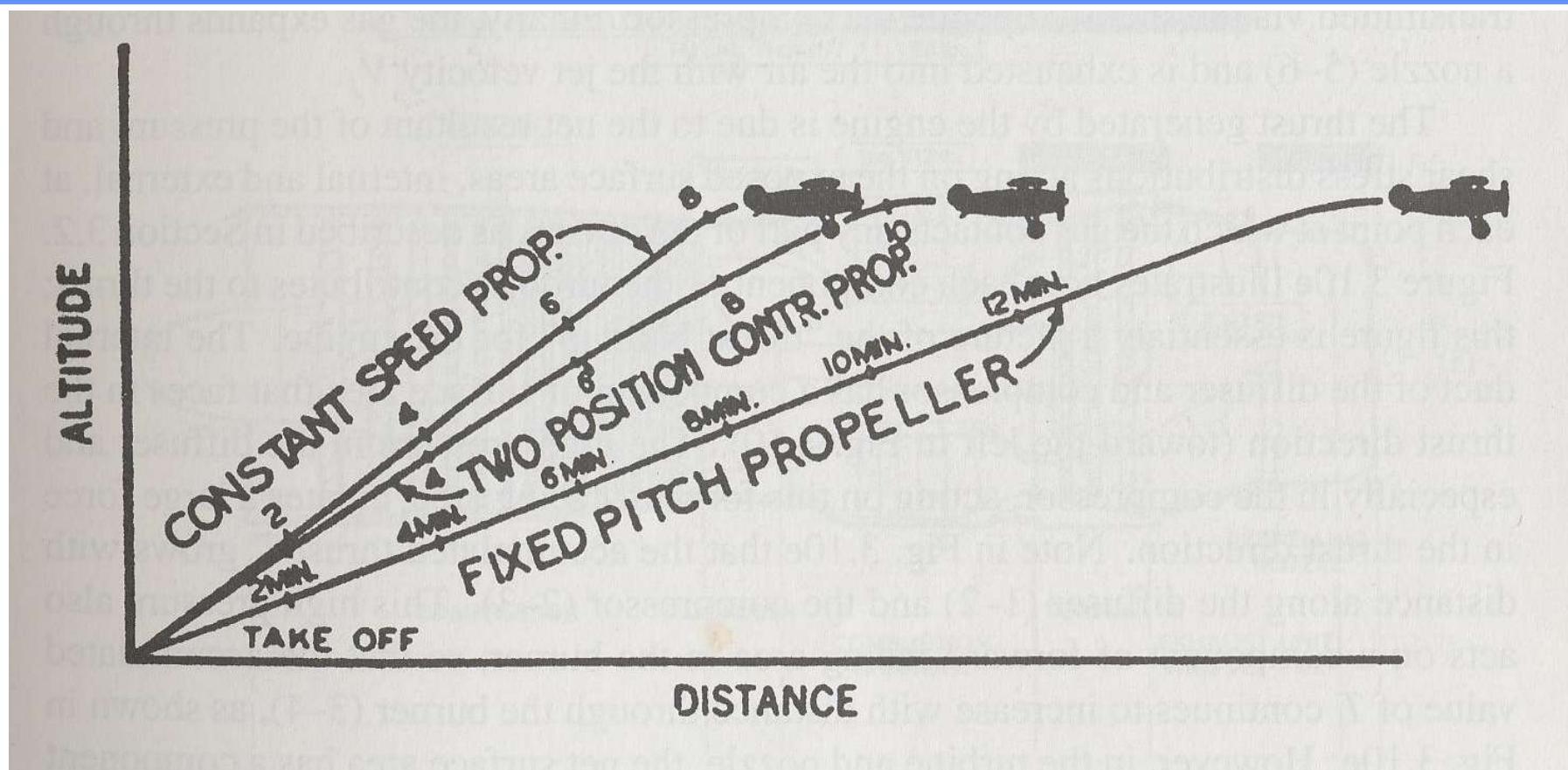


Chart from 1940, the beginning of the mature propeller-driven airplane era