
Alternate Energy Based Sizing Method

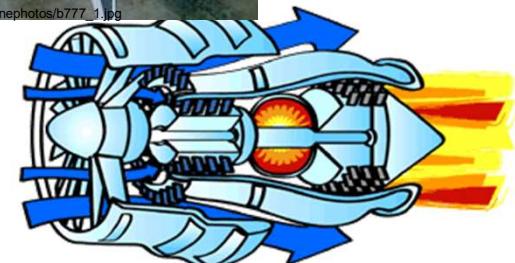
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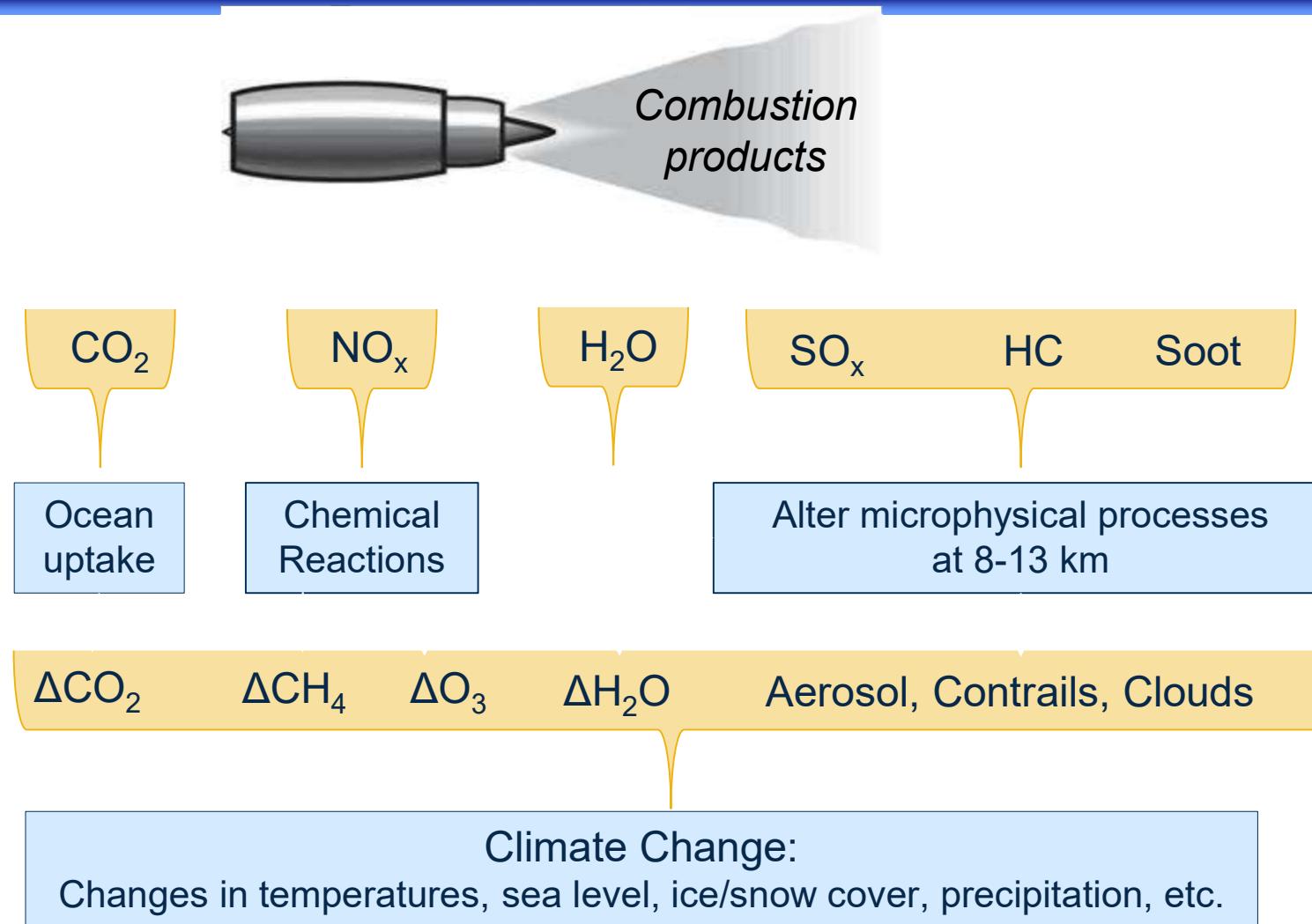
Dr. Gökçin Çınar

After a Century of Efforts

Flying still depends on internal combustion engines



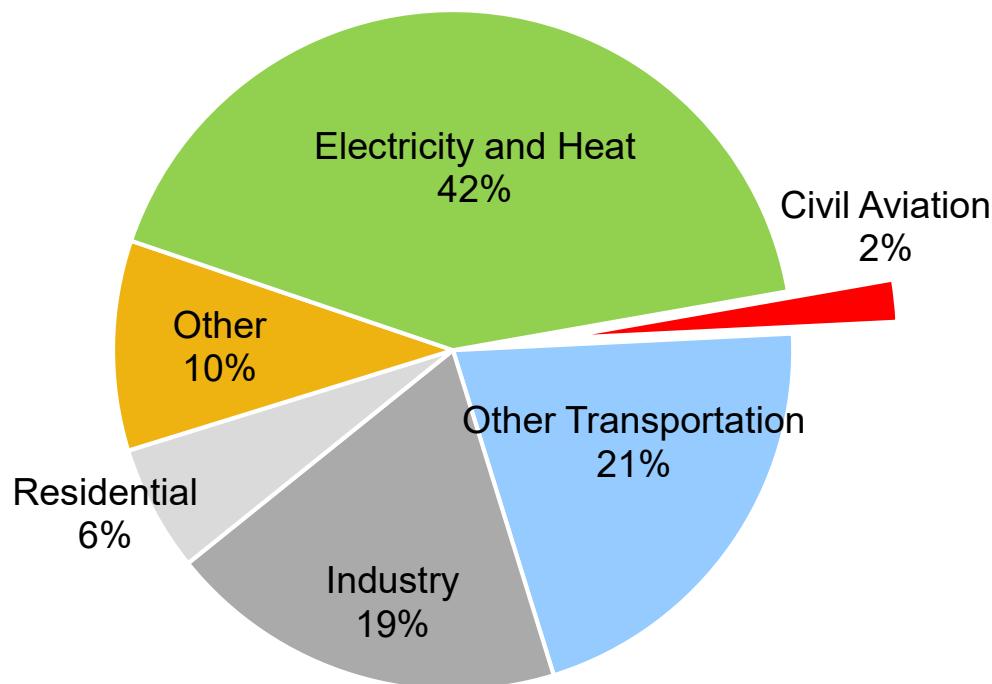
Aviation's Contribution to Climate Change



Schematic adapted from Lee et al., "Aviation and Global Climate Change in the 21st Century," Atmospheric Environment, vol. 43, no. 22-23, 3520-3537, 2009.

Aviation CO₂ Emissions and Future Goals

Global CO₂ Emissions by Sector in 2013 [2]

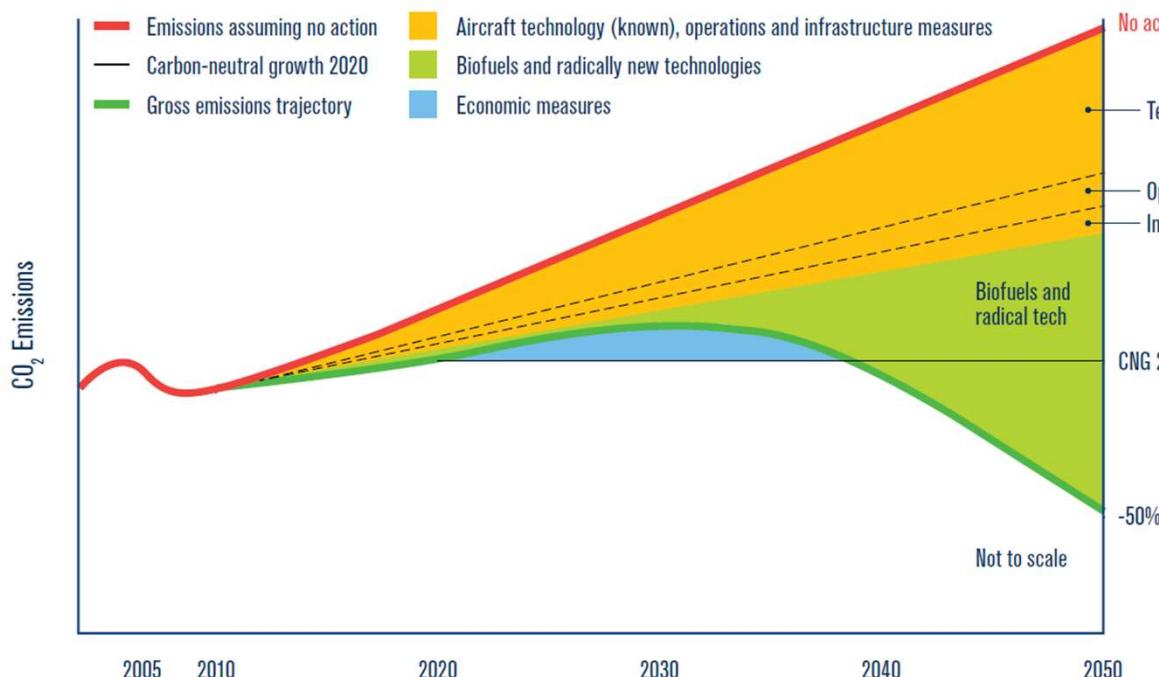


In 2015:

- Total CO₂: 36 billion tons
- Aviation-related CO₂: 781 million tons

- CO₂ emissions are expected to increase as aviation demand increases
- ICAO goals:
 1. 2% annual fuel efficiency improvement through 2050
 - CO₂ emissions are assumed to be proportional to total fuel usage
 2. Keep the net CO₂ emissions at 2020 levels (i.e. Carbon-neutral growth)
 3. Reduce net CO₂ emissions by 50% by 2050 relative to 2005 levels

Future Aircraft Emission Goals



Schematic of CO₂ emissions reduction roadmap by IATA, "IATA Technology Roadmap," 4th Edition, 2013

NASA's primary areas of technical focus:

1. Alternative fuels

- Can lower the carbon use of standard turbofan engines in the near term
- Do not help with the local air quality impact, very long lifetime of CO₂ emissions, or NO_x emissions throughout the upper troposphere and lower stratosphere

2. Hybrid-electric and fully electric propulsion

- Can achieve very low to no carbon emissions

Unconventional Energy/Power Sources

Attracting renewed attention in the past decade

Solar Cell



[http://www.difrc.nasa.gov/Newsroom/
X-Press/images/083101/helios.jpg](http://www.difrc.nasa.gov/Newsroom/X-Press/images/083101/helios.jpg)

Lithium-Polymer Battery



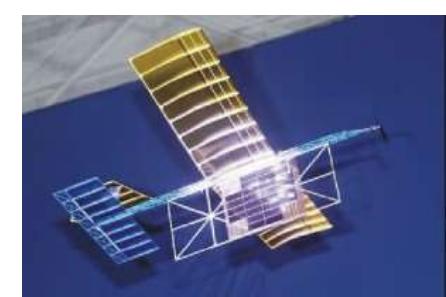
<http://www.aerovironment.com/news/news-archive/local-images/wasp1.jpg6>

Human-Powered



www.difrc.nasa.gov/.../Small/EC87-0014-8.jpg

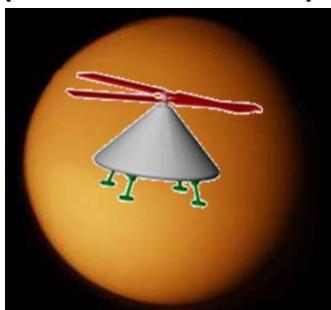
Beam-Powered



Nuclear Battery



Atmosphere (Methane in Titan)



Chemical Muscle



Hydrogen



Hybrid/Electric Aircraft Examples



Uber Elevate
Urban Air Mobility

Image Credit: uber.com



Pipistrel Alpha Electro
Electric General Aviation

Image Credit: pipistrel.si



NASA X-57 Mod IV
Distributed Electric Propulsion

Image Credit: nasa.gov



Bauhaus Luftfahrt Ce-Liner
Electric Transport

Image Credit: bauhaus-luftfahrt.net



Boeing Sugar Volt
Hybrid Electric Transport

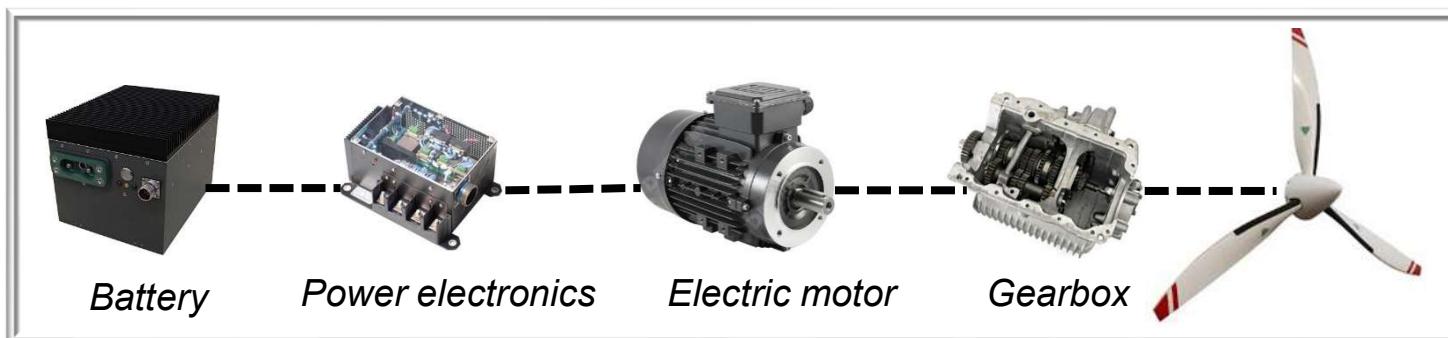
Image Credit: nasa.gov



NASA STARC-ABL
Turboelectric Transport

Image Credit: nasa.gov

Electric Propulsion System



Advantages

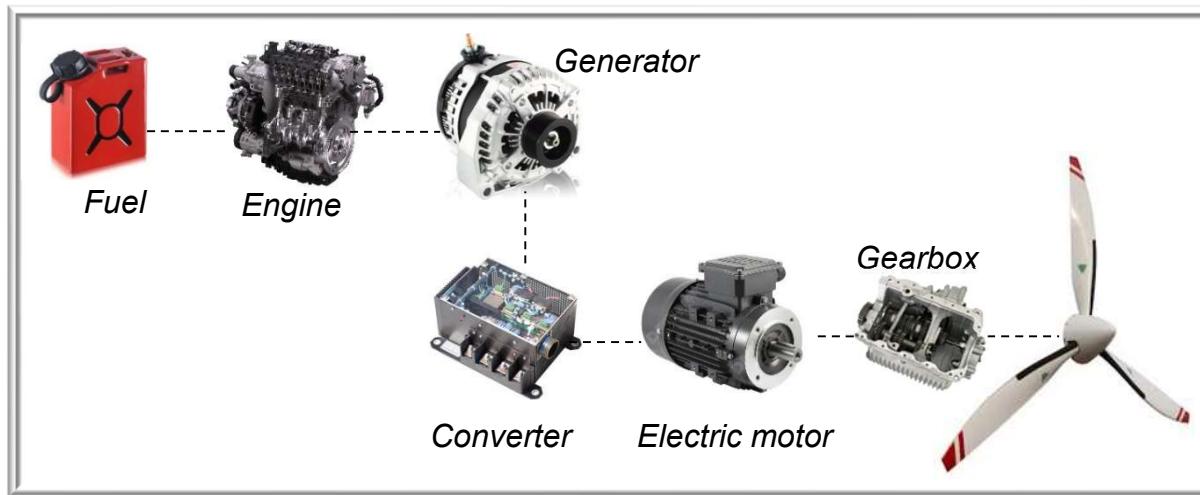
- ✓ Zero CO₂ and NO_x emissions
- ✓ Less atmospheric heat release (less global warming)
- ✓ High efficiency of the electric motor
 - ✓ No power lapse with altitude
 - ✓ Scale-free efficiency and power-to-weight ratio
- ✓ Increased reliability and maintainability
- ✓ Quieter flight

Disadvantages

- Endurance/Range penalty due to the low gravimetric specific energy* of batteries
 - Aviation Gasoline: 12.2 kWh/kg
 - Jet A: 11.9 kWh/kg
 - Lithium Ion Battery: 0.23 kWh/kg
- Increased weight sensitivity

*Gravimetric Specific Energy = ratio of energy to mass of an energy source

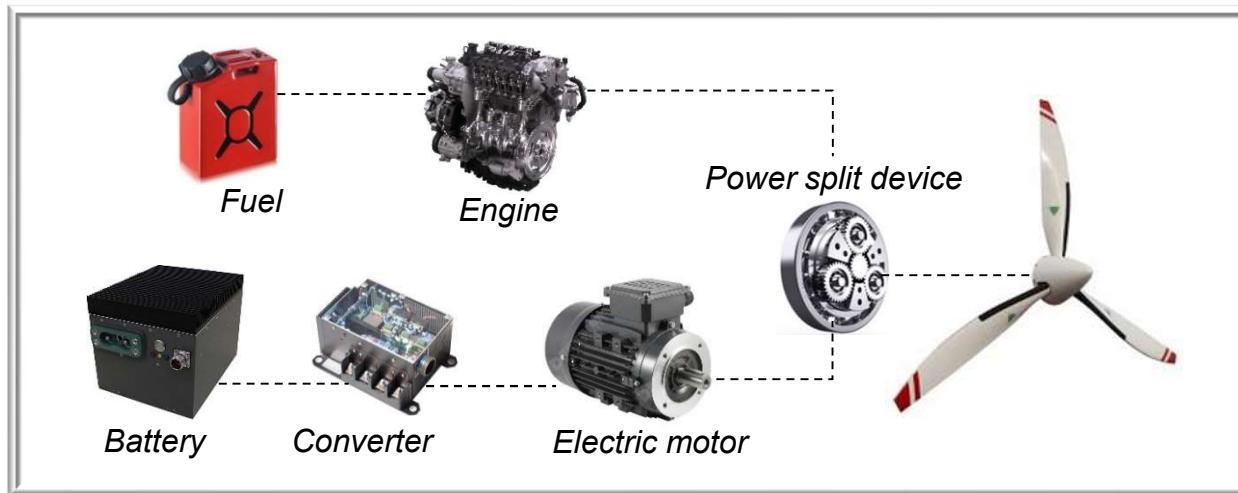
Series Hybrid Electric Propulsion System



Series configuration (Called “turboelectric” if engine is a gas turbine engine)

- ✓ Engine is decoupled from the transmission system; can run at its peak efficiency independent from the RPM of the transmission system
- ✓ Flexibility in terms of the location of engine-generator set
- 3 propulsion devices (engine, motor, and generator) need to be sized for the maximum sustained power for high performance flight
- Increased weight penalty

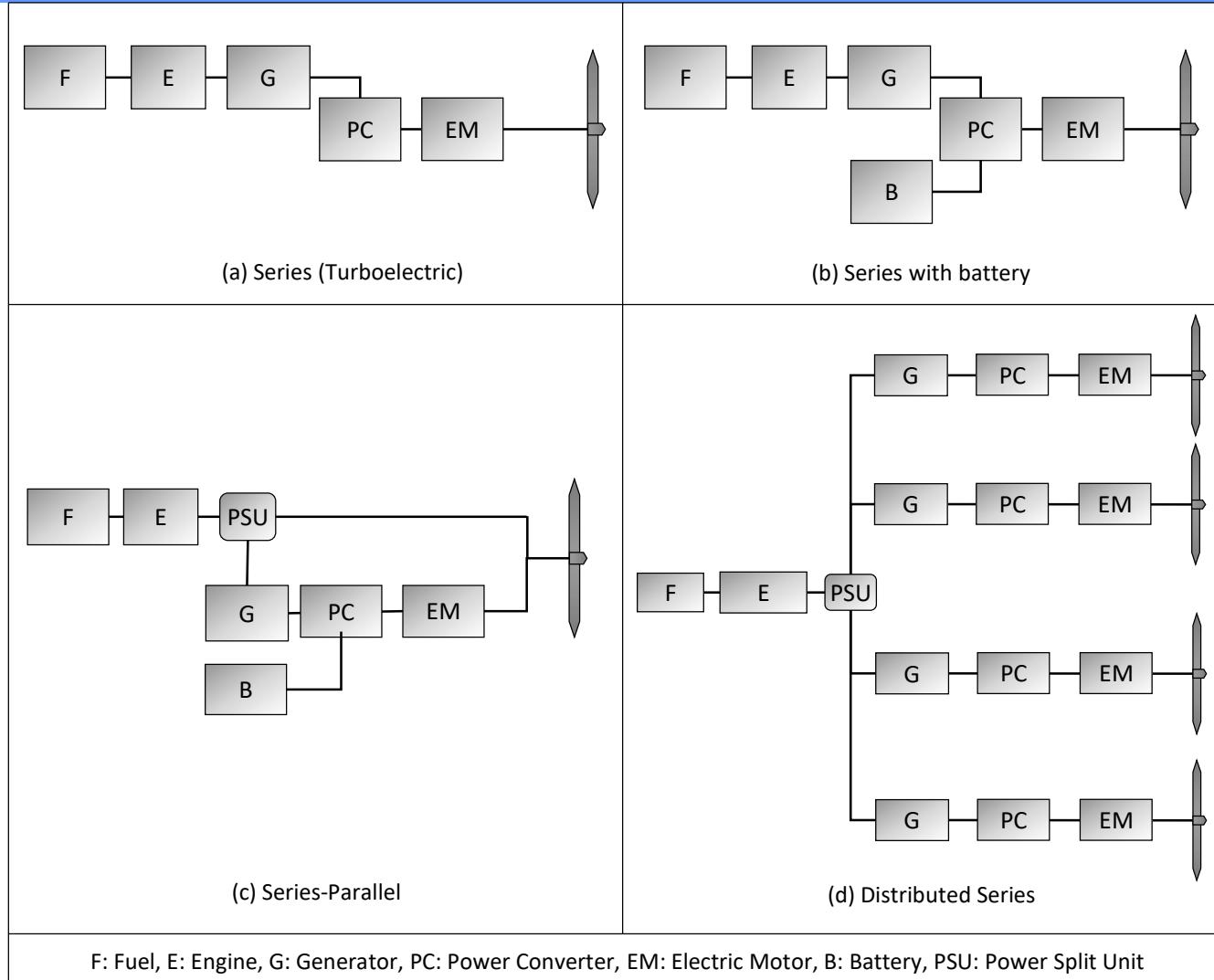
Parallel Hybrid Electric Propulsion System



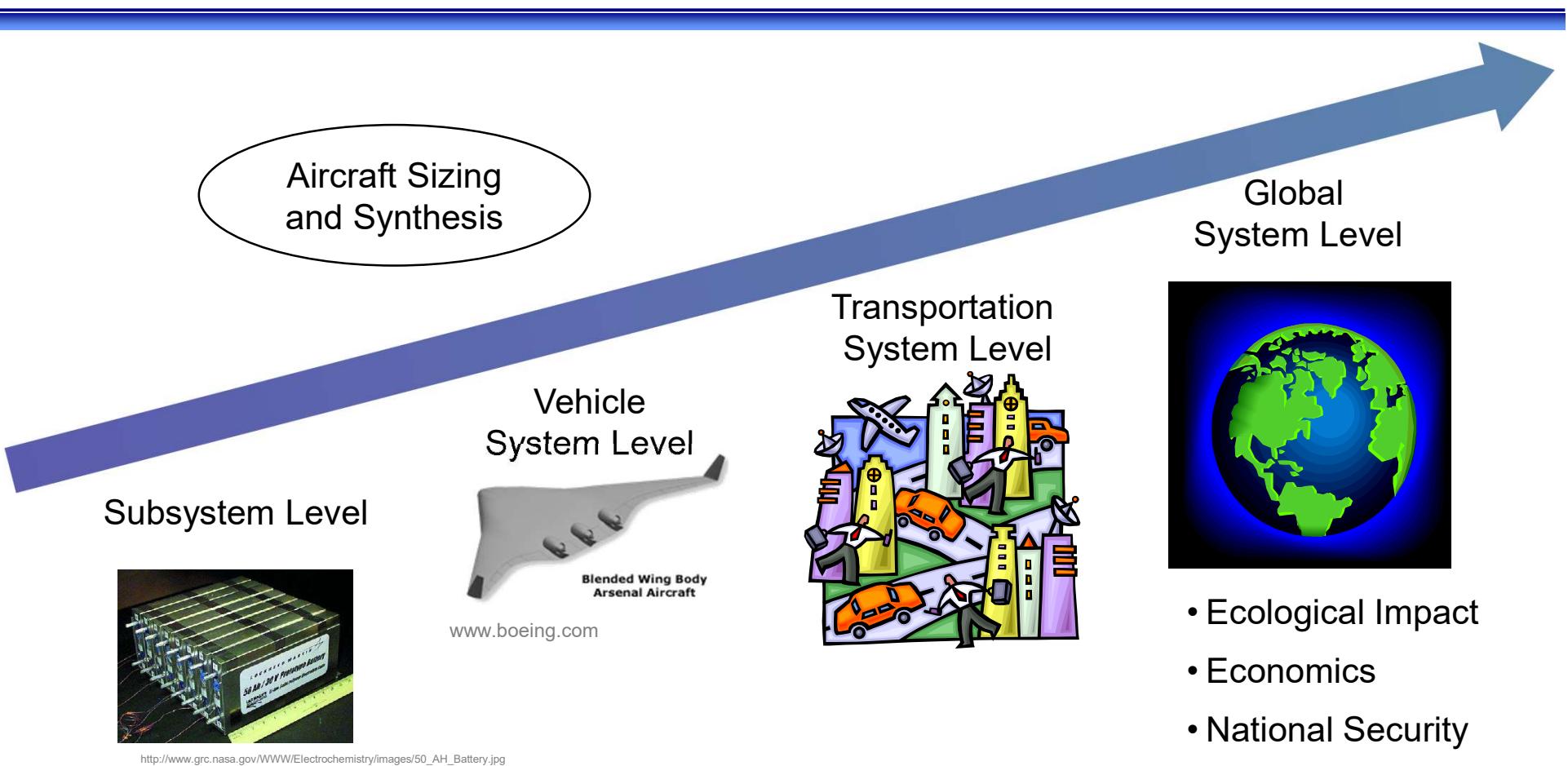
Parallel configuration

- ✓ Engine and motor are coupled to the shaft; either one can be downscaled without any loss in maximum power
- ✓ Power can be delivered by only the engine (conventional propulsion), only the electric motor (fully electric propulsion) or both of them simultaneously (hybrid propulsion)
- ✓ No extra generator (motor can be used as a generator to charge the battery)
- Increased control complexity
- Mechanical couplings
- Requires more complex and expensive transmission system

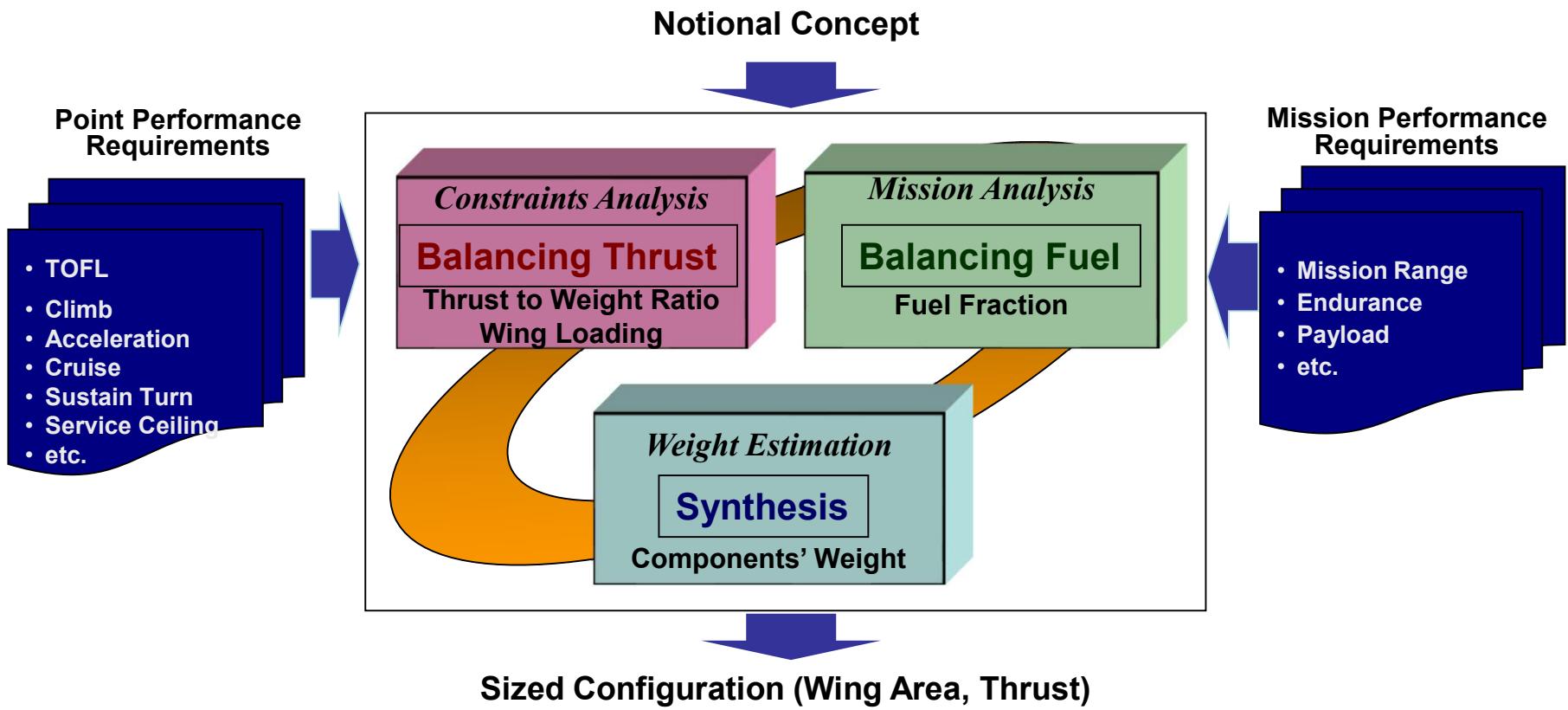
Example Hybrid Electric Propulsion Architectures



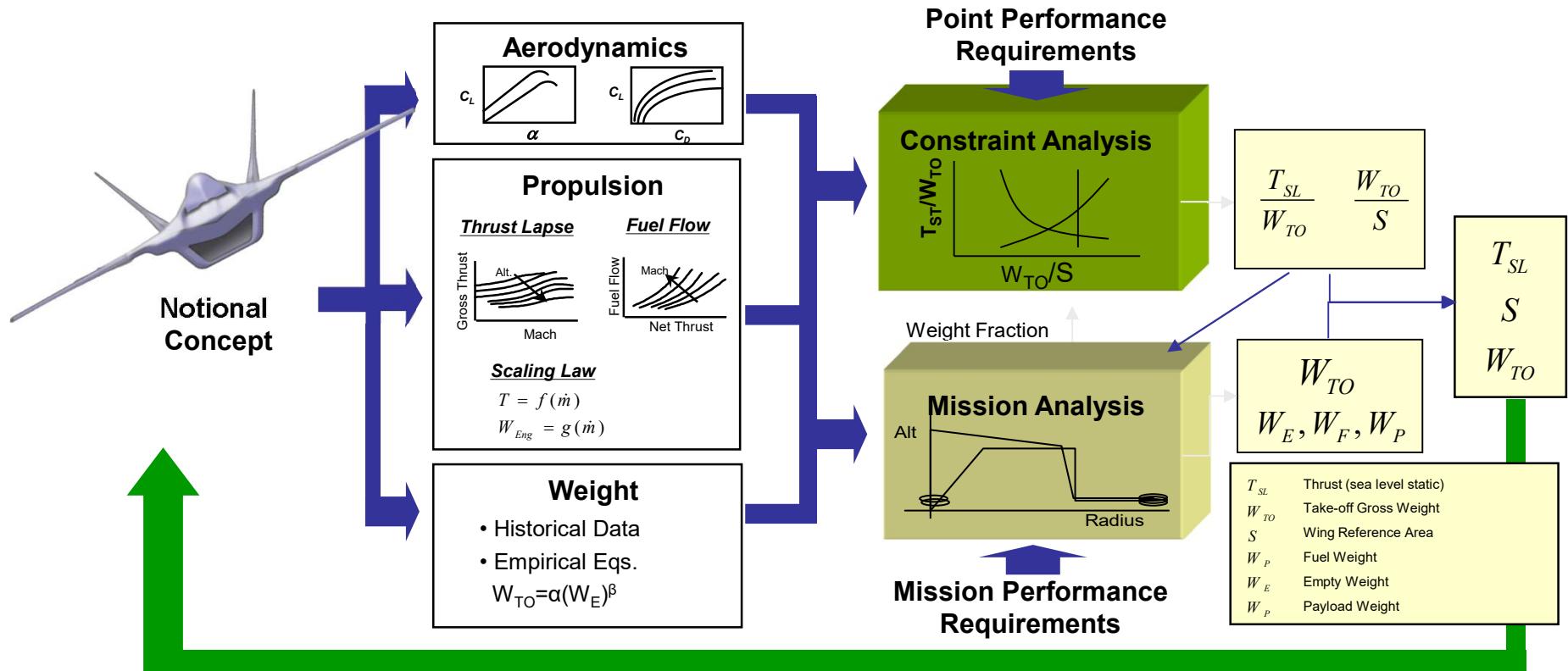
Need for Comprehensive Research



Aircraft Sizing

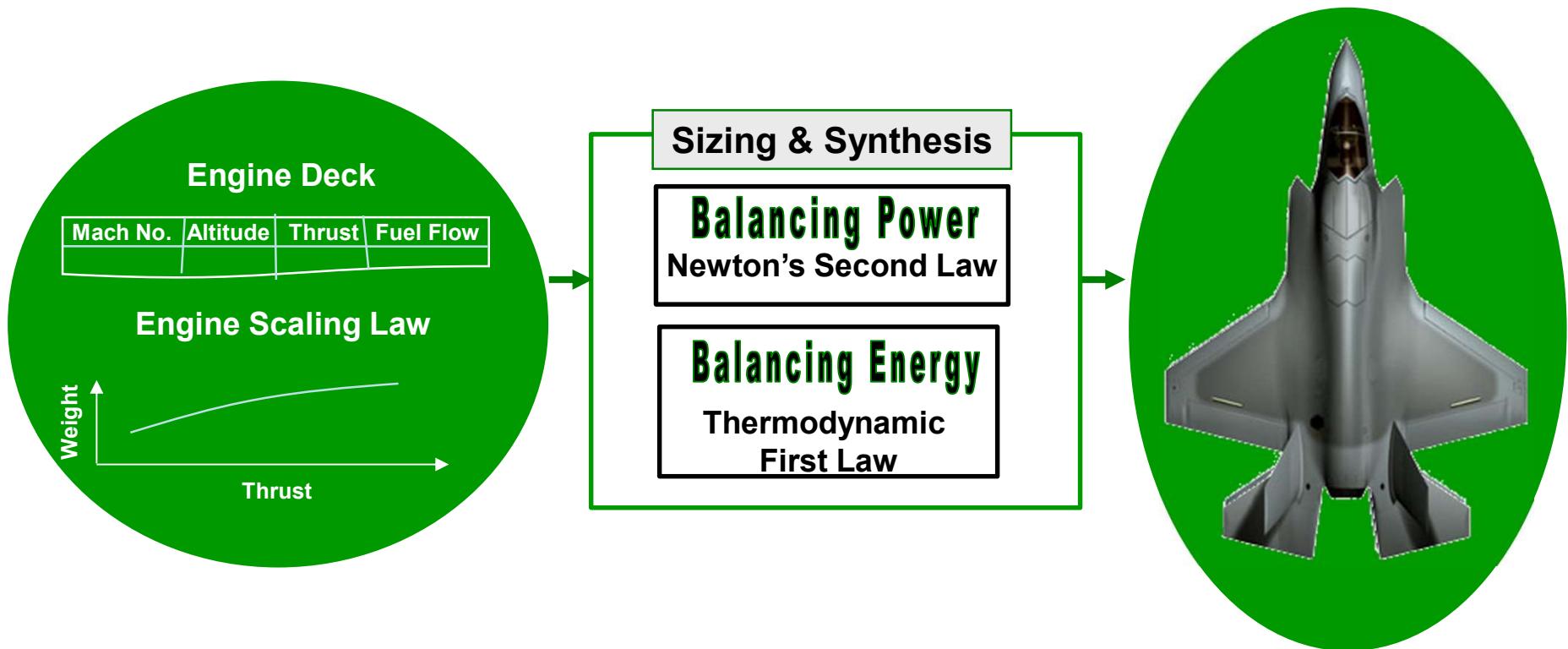


Traditional Aircraft Sizing Process



Propulsion System Integration

Conceptual Sizing



A propulsion system is characterized with numeric data sets,
independent of the airframe design

Propulsion System Integration

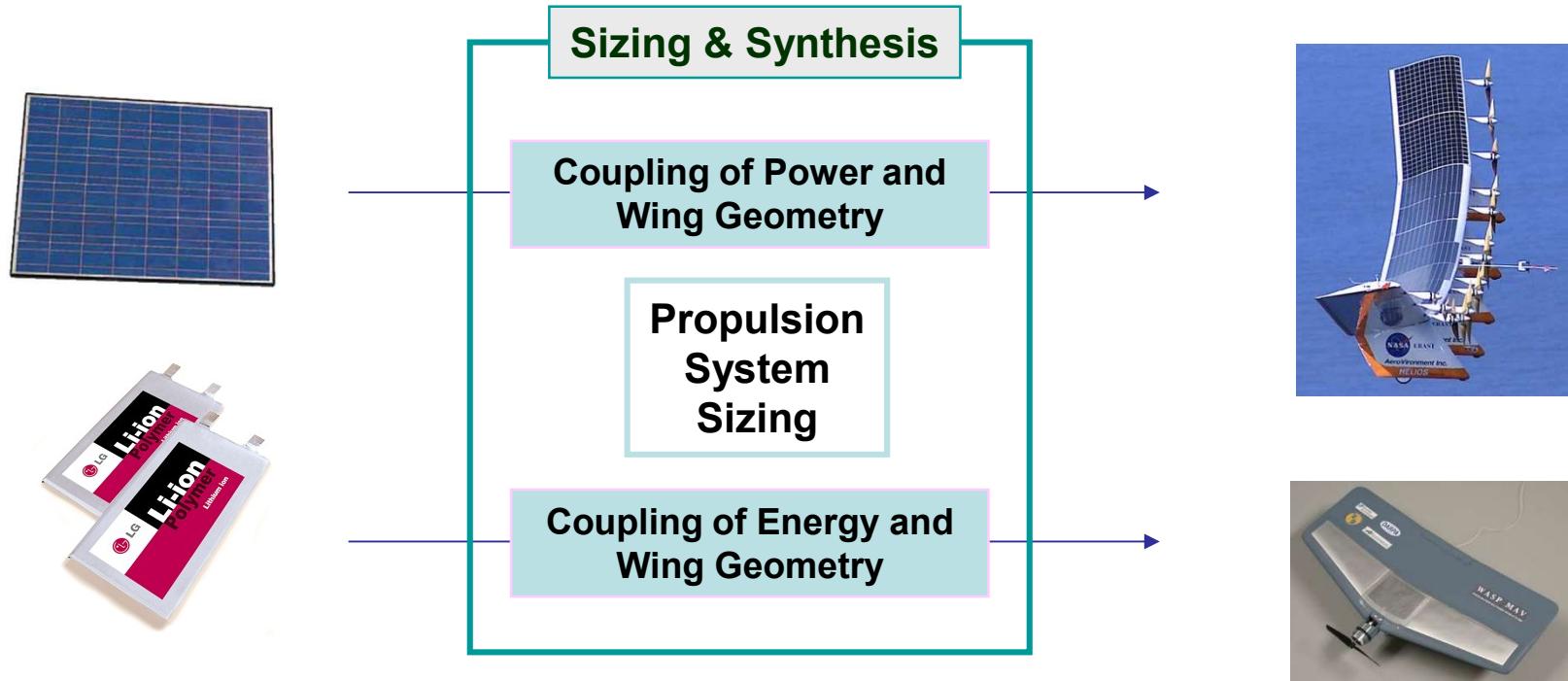
Detail Design
A propulsion system must be tightly integrated with airframe



- Configuration Design:
 - Diffuser design
 - Inlet and forebody integration
- Performance:
 - Thrust and fuel consumption
- Structures:
 - Engine mounting structures
- Subsystem:
 - Engine cooling
 - Accessory gear box (PTO shaft, Bleed air)
 - Secondary power system Integration
- RM&S:
 - Engine install and removal
 - Inspection and maintenance



Propulsion System Integration



Traditional Mission Analysis

Weight Decomposition

A/C weight change equals to fuel weight change.

Fuel weight change (fuel flow) can be expressed as a function of thrust required.

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In addition, thrust-to-weight Ratio can be related to aerodynamic performance.

Breguet Range Equation

$$W_{TO} = W_E + W_P + W_F$$

$$\frac{dW}{dt} = \frac{dW_F}{dt}$$

$$\frac{dW}{dt} = \frac{dW_F}{dt} = -TSFC \times T$$

$$\frac{dW}{W} = -TSFC \frac{T}{W} dt = -TSFC \frac{T}{W} \frac{ds}{V}$$

$$\text{Where, } \frac{T}{W} = \left(\frac{D + R}{\beta W_{TO}} \right) + \frac{1}{V} \frac{d}{dt} \left(h + \frac{V^2}{2g_o} \right)$$

$$\text{Range} = \int ds = \frac{V}{TSFC} \frac{L}{D} \ln \left(\frac{W_{final}}{W_{initial}} \right)$$

$TSFC$	Thrust Specific Fuel Consumption
T	Thrust
s	distance
V	Velocity
D	Basic configuration Drag
R	Additional drag to D
β	Weight fraction
h	Altitude
g_o	Gravity constant
W_{TO}	Take-Off Gross Weight
W_F	Fuel Weight

Traditional Mission Analysis

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This assumption is no longer valid for certain types of alternative propulsion systems
- Zero Emissions Aircraft

$$\frac{dW}{W} = -TSFC \frac{T}{W} dt = -TSFC \frac{T}{W} \frac{ds}{V}$$

Where, $\frac{T}{W} = \left(\frac{D + R}{\beta W_{TO}} \right) + \frac{1}{V} \frac{d}{dt} \left(h + \frac{V^2}{2g_o} \right)$

$$\text{Range} = \int ds = \frac{V}{TSFC} \frac{L}{D} \ln \left(\frac{W_{final}}{W_{initial}} \right)$$

Technical Issues and Approaches

Technical Issues

Coupling between propulsion system sizing and aircraft sizing



Resolution plans

Generalized propulsion system modeling

Limited flexibility to vary “power mix” of hybrid propulsion systems



Concept of multiple power paths

Applicable to only limited types of fuel



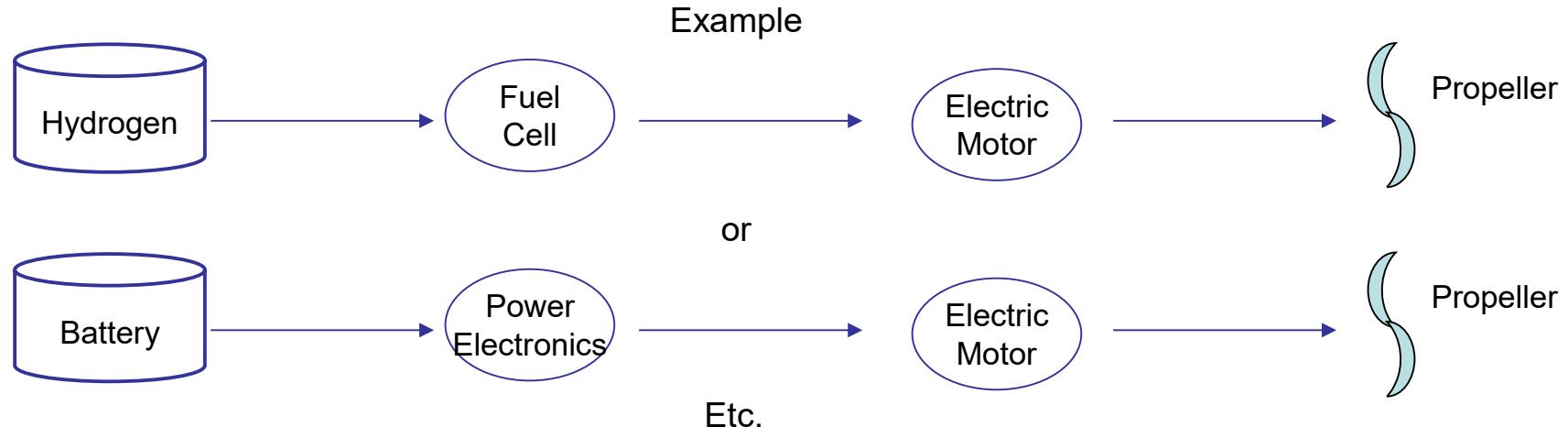
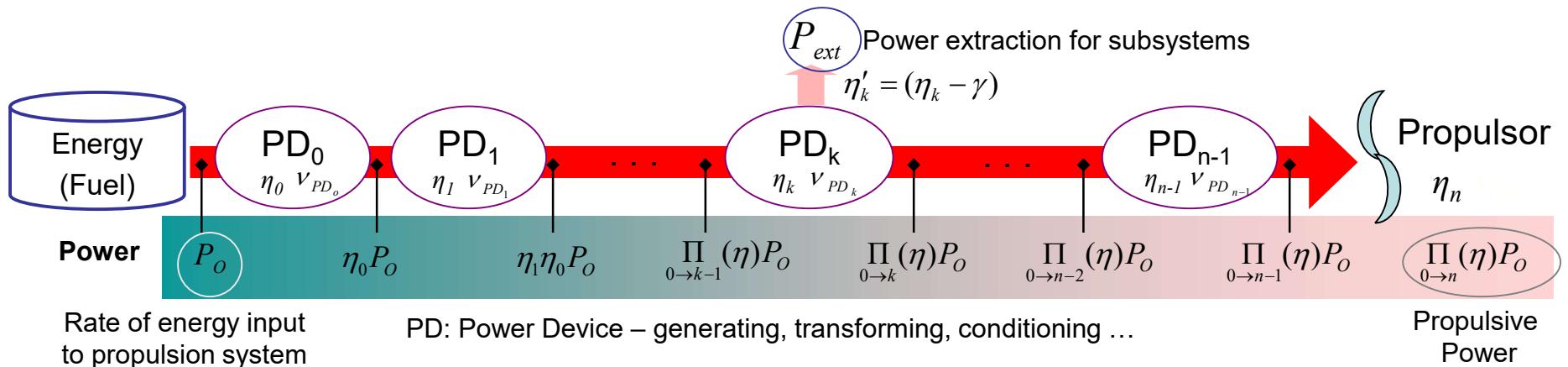
Multiple energy sources
• Consumable energy
• Non-consumable energy

The time rate of change in aircraft weight does NOT necessarily equal fuel flow

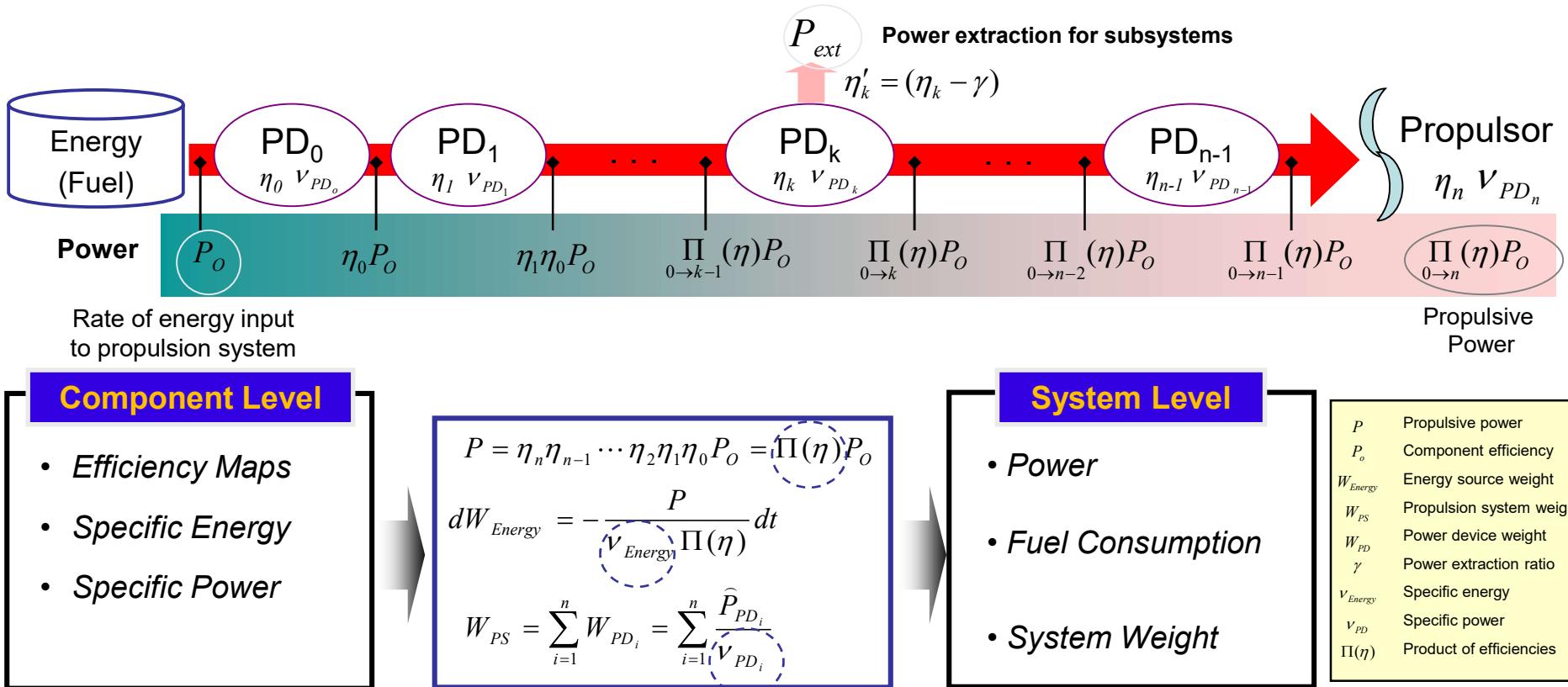


Generalized weight decomposition and weight differential equation

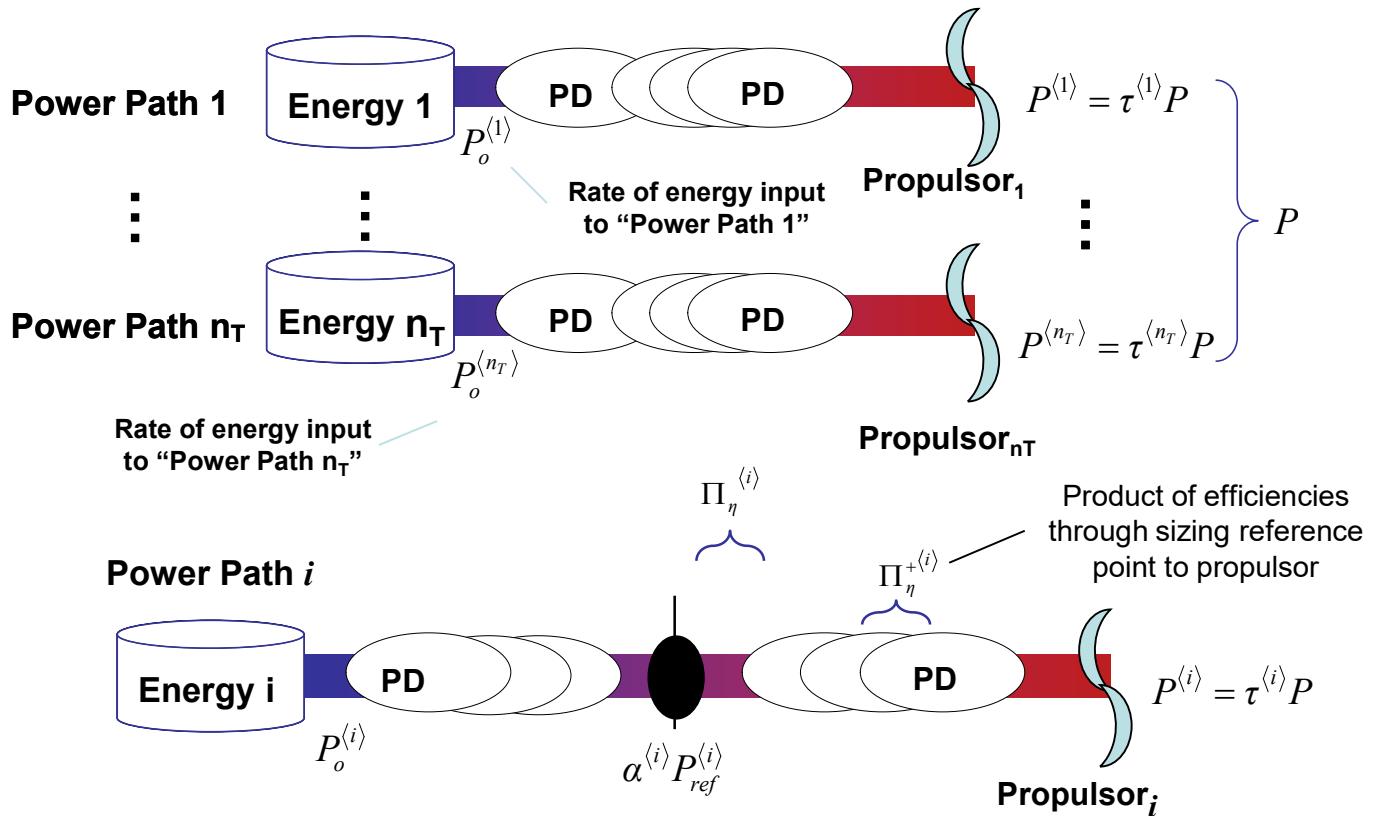
Generalized Propulsion System Modeling



Generalized Propulsion System Modeling



Multiple Power Paths



P Gross propulsive power
 $P^{(i)}$ i-th power path propulsive power
 $\alpha^{(i)}$ Power lapse ratio measured against the sizing reference power
 $\tau^{(i)}$ Power fraction of i-th power path

$$P_{ref}^{(i)} = \frac{\tau^{(i)} P}{\Pi_\eta^{+(i)} \alpha^{(i)}}$$

Sizing reference power for i^{th} power path

Multiple Energy Sources

- Consumable energy

A form of energy that is derived from a source whose weight is reduced during power generation



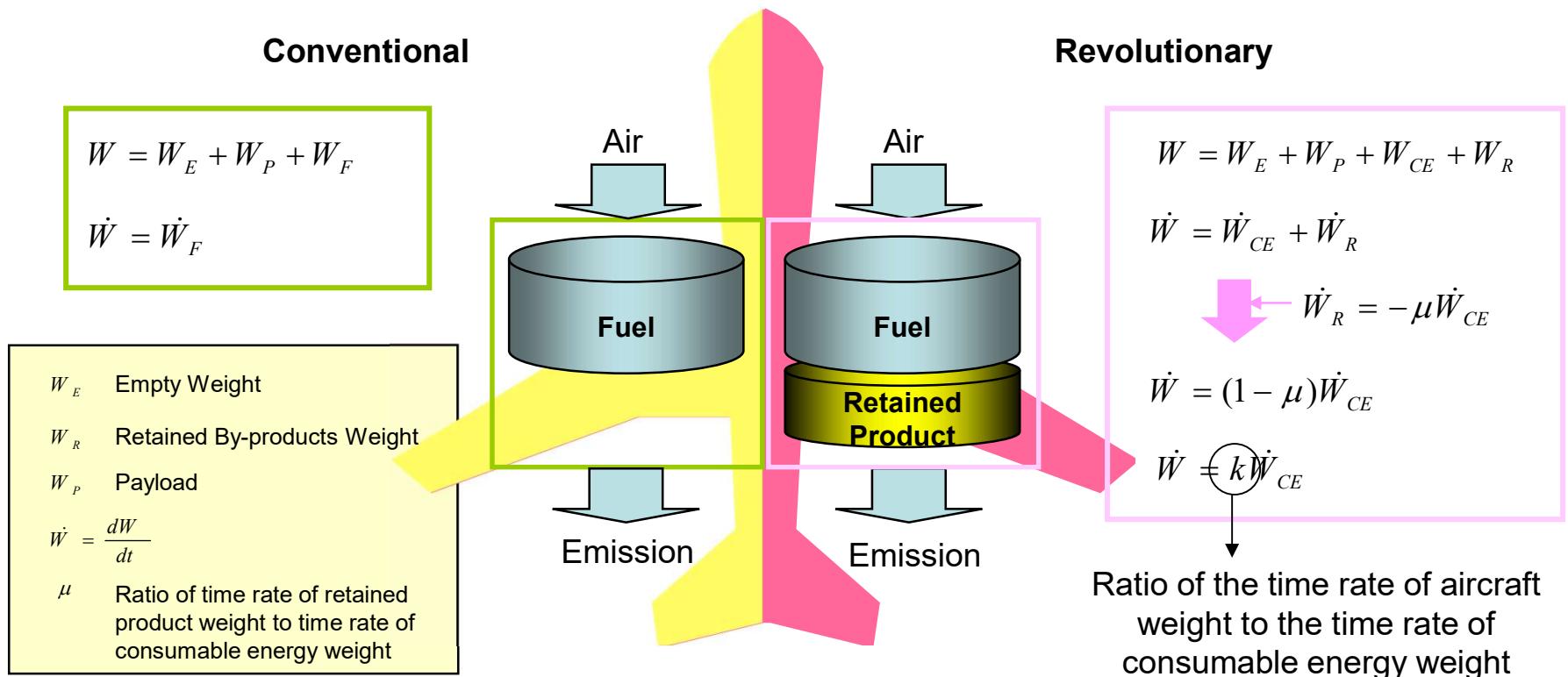
- Non-consumable energy

A form of energy derived from a source whose weight stays constant or changes negligibly during power generation

$$E = \sum_{i=1}^{n_{CE}} E_{CE}^{\langle i \rangle} + \sum_{j=1}^{n_{NE}} E_{NE}^{\langle j \rangle}$$
$$W_{Energy} = \sum_{i=1}^{n_{CE}} W_{CE}^{\langle i \rangle} + \sum_{j=1}^{n_{NE}} W_{NE}^{\langle j \rangle}$$

E_{CE} Amount of consumable onboard energy
 E_{NE} Amount of non-consumable onboard energy
 W_{CE} Consumable energy Weight
 W_{NE} Non-consumable energy Weight

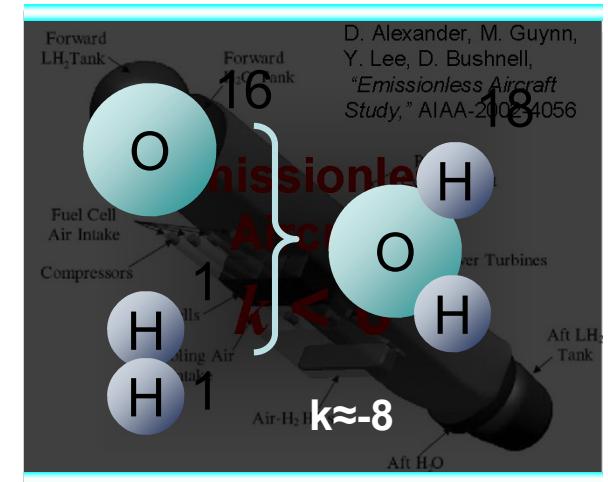
Generalized Weight Equations



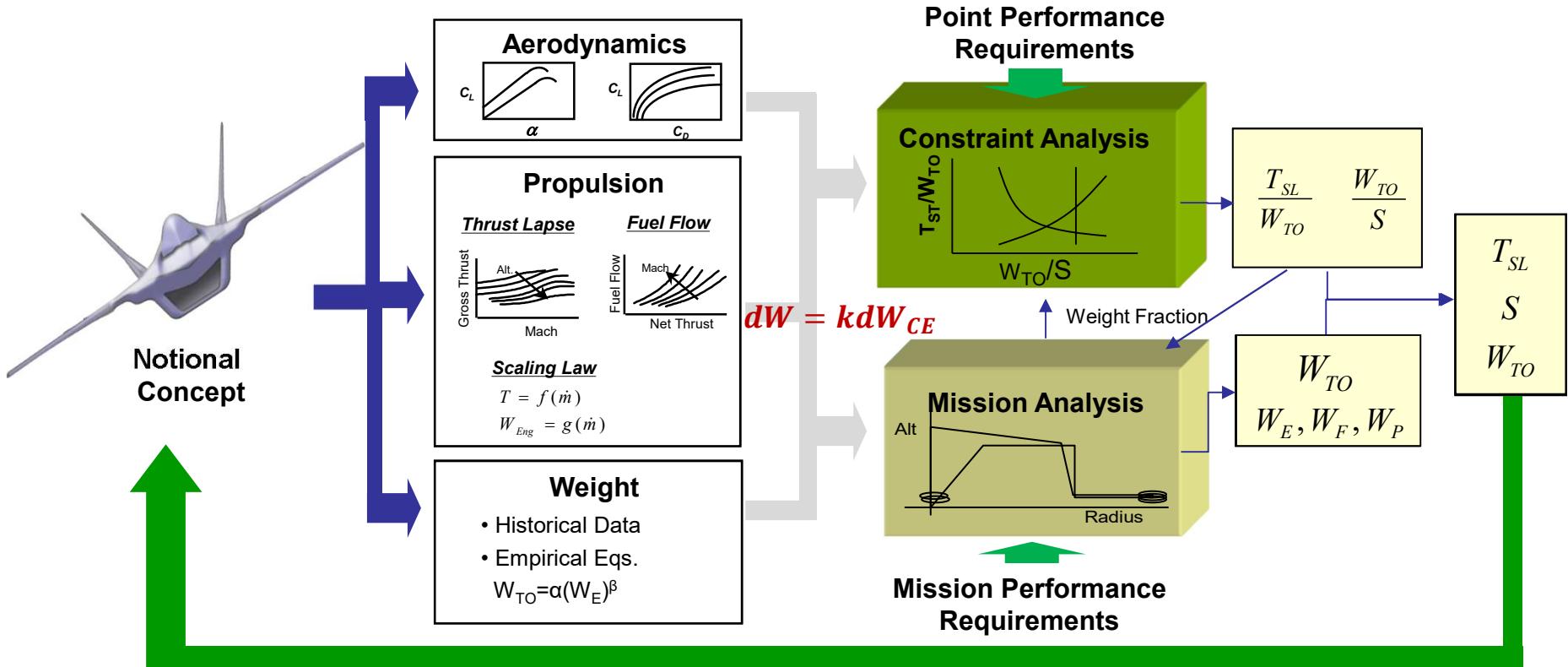
Generic Equation for “k” & Examples

$$k = \frac{\sum_{i=1}^{n_{CE}} \frac{1 - \mu^{\langle i \rangle}}{\tau^{\langle ii \rangle} v_{CE}^{\langle i \rangle} \prod_{\eta}^{\langle i \rangle}}}{\sum_{ii=1}^{n_{CE}} \frac{\tau^{\langle i \rangle} v_{CE}^{\langle ii \rangle} \prod_{\eta}^{\langle ii \rangle}}{\tau^{\langle i \rangle} v_{CE}^{\langle ii \rangle} \prod_{\eta}^{\langle ii \rangle}}}$$

μ Ratio of the time rate of retained product to the time rate of consumable energy weight

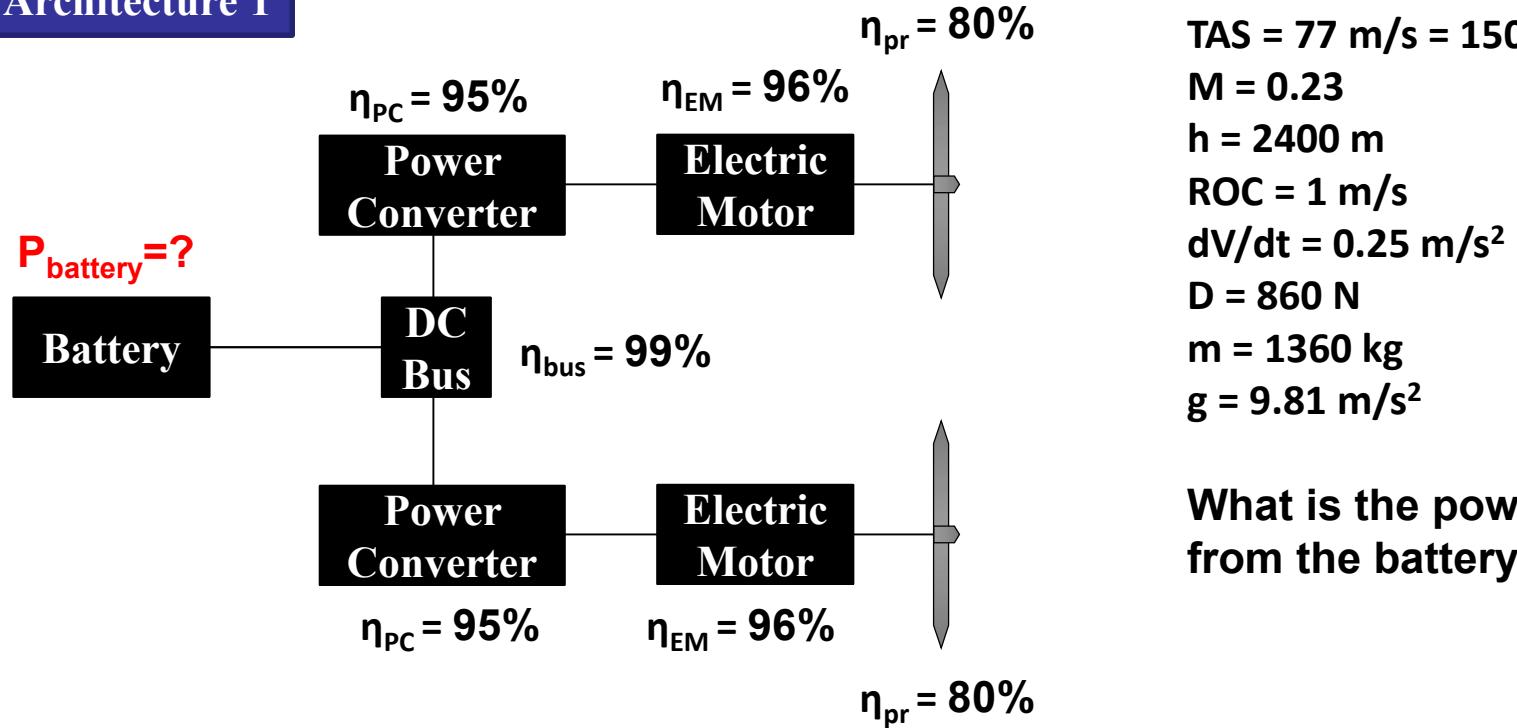


New Aircraft Sizing Process



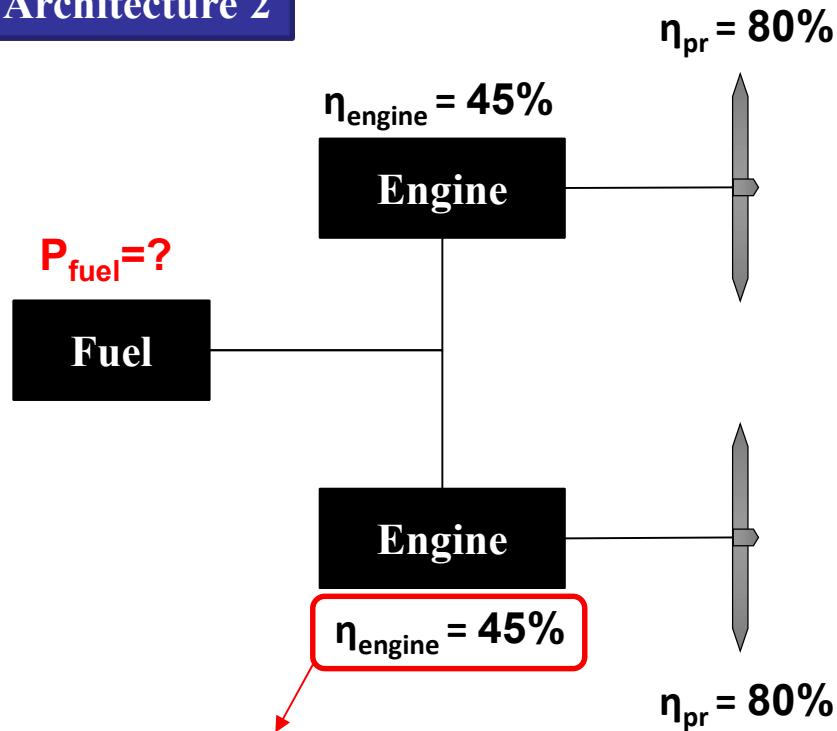
Electric Propulsion Exercise

Architecture 1



Conventional Propulsion Exercise

Architecture 2



$$\text{TAS} = 77 \text{ m/s} = 150 \text{ knots}$$

$$M = 0.23$$

$$h = 2400 \text{ m}$$

$$\text{ROC} = 1 \text{ m/s}$$

$$dV/dt = 0.25 \text{ m/s}^2$$

$$D = 860 \text{ N}$$

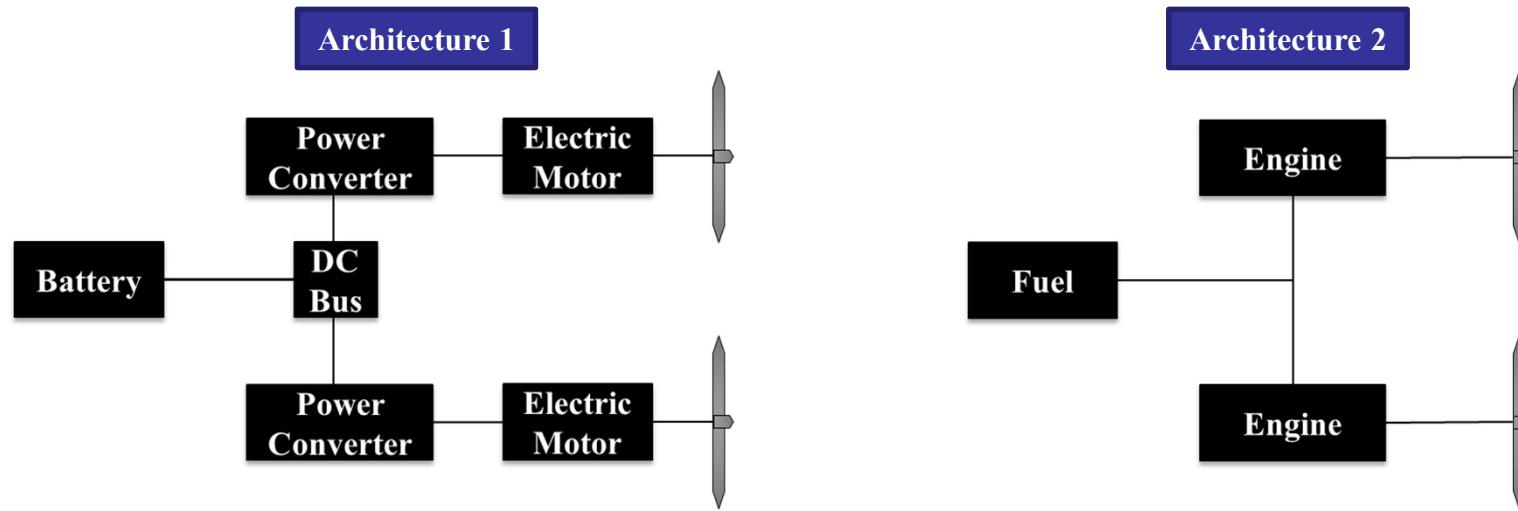
$$m = 1360 \text{ kg}$$

$$g = 9.81 \text{ m/s}^2$$

How does the power requirement from the energy storage change compared to the previous example?

*Notice the efficiency drop
Why?*

Electric to Conventional Comparison



- Assume that:
 - Flight goes on for 1 minute at constant rate of climb and acceleration
 - Battery specific energy = 0.2 kWh/kg
 - Fuel specific energy = 12.2 kWh/kg
- What is the minimum required weight of the two energy sources?
 - Can you calculate the energy source weight with the given information?

Generalized Constraint Analysis Equation

$$\boxed{\text{Rate of Mechanical Energy Input}} = \boxed{\text{Storage Rate Of Potential Energy}} + \boxed{\text{Storage Rate Of Kinetic Energy}}$$

$$\{T - (D + R)\}V = W \frac{dh}{dt} + \frac{W}{g_o} \frac{d}{dt} \left(\frac{V^2}{2} \right)$$



**Mattingly
Constraint
Equation**

$$\frac{T_{SL}}{W_{TO}} = \frac{\beta}{\alpha} \left\{ \frac{qS}{\beta W_{TO}} \left[K_1 \left(\frac{n\beta W_{TO}}{q - S} \right)^2 + K_2 \left(\frac{n\beta W_{TO}}{q - S} \right) + C_{D_o} + \frac{R}{qS} \right] + \frac{1}{V dt} \left(h + \frac{V^2}{2g_o} \right) \right\}$$



**Generalized
Constraint
Equation**

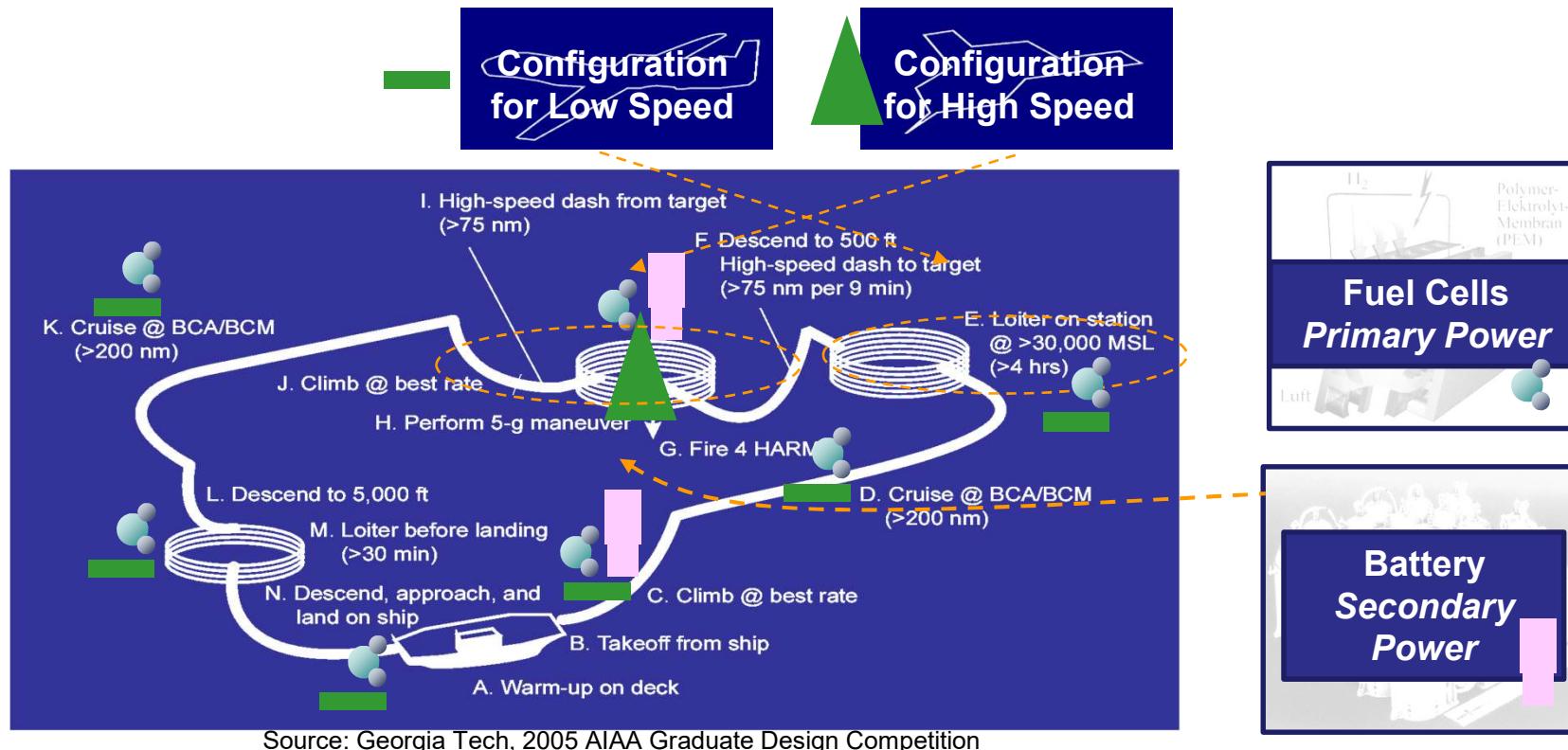
$$\frac{P_{ref}^{(i)}}{W_{TO}} = \frac{\tau^{(i)} \beta}{\prod_{j=1}^{n+1} \alpha^{(j)}} \left\{ \frac{qS}{\beta W_{TO}} \left[K_1 \left(\frac{n\beta W_{TO}}{q - S} \right)^2 + K_2 \left(\frac{n\beta W_{TO}}{q - S} \right) + C_{D_o} + \frac{R}{qS} \right] + \frac{1}{V dt} \left(h + \frac{V^2}{2g_o} \right) \right\} V$$

Constraint Equations

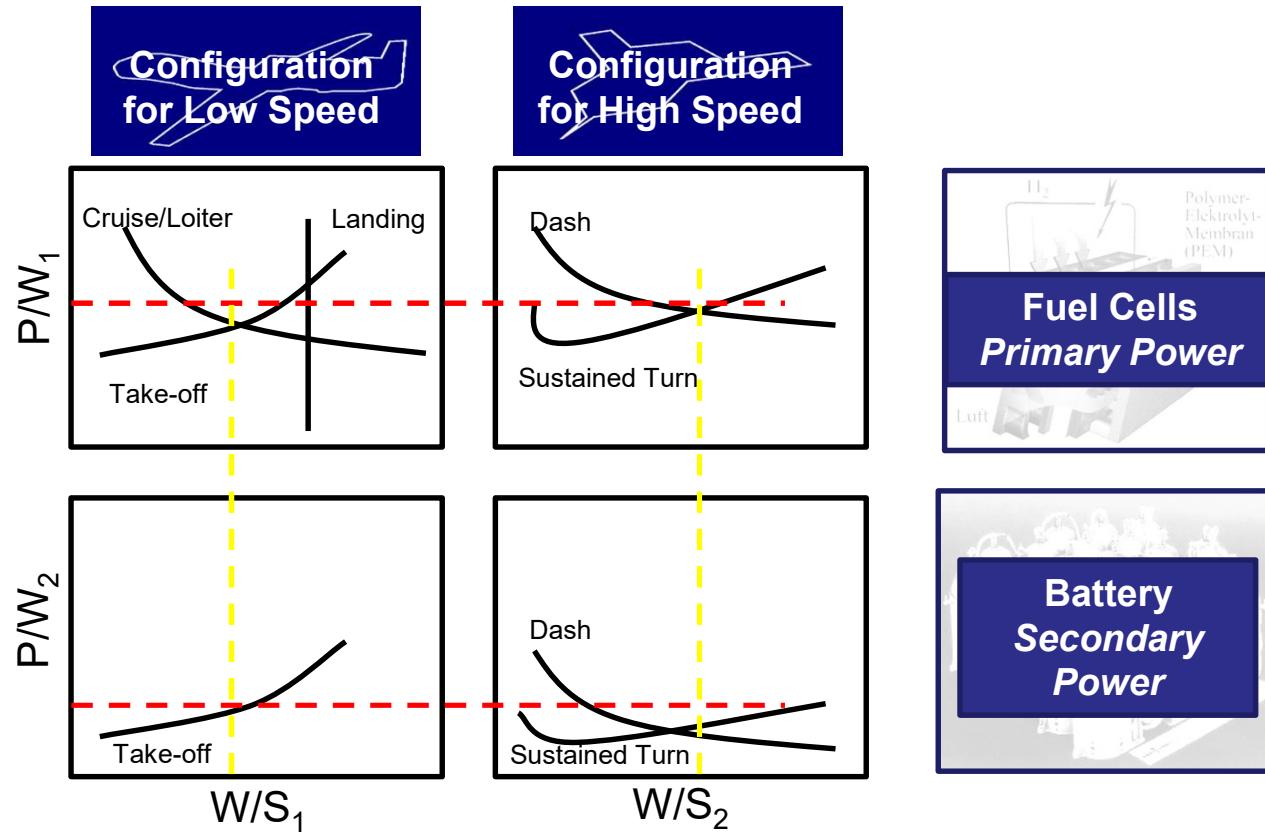
$$\frac{P_{ref}^{(i)}}{W_{TO}} = \frac{\tau^{(i)} \beta}{\Pi_{\eta}^{(i)} \alpha^{(i)}} \left\{ \frac{qS}{\beta W_{TO}} \left[K_1 \left(\frac{n\beta W_{TO}}{q - S} \right)^2 + K_2 \left(\frac{n\beta W_{TO}}{q - S} \right) + C_{D_o} + \frac{R}{qS} \right] + \frac{1}{V} \frac{d}{dt} \left(h + \frac{V^2}{2g_o} \right) \right\} V$$

	Assumption	Constraint Equation
Take-off	$P \gg (D+R)V$ $\frac{dh}{dt} = 0$ $n = 1$ $V_{TO} = k_{TO} V_{STALL}$	
Constant Speed Climb	$\frac{dV}{dt} = 0$ $n \approx 1$	
Cruise	$\frac{dV}{dt} = 0$ $\frac{dh}{dt} = 0$ $n = 1$	
Sustained Turn	$\frac{dV}{dt} = 0$ $\frac{dh}{dt} = 0$ $n = \left\{ 1 + \left(\frac{V}{g_o R_c} \right)^2 \right\}^{\frac{1}{2}}$ $n = \left\{ 1 + \left(\frac{\Omega V}{g_o} \right)^2 \right\}^{\frac{1}{2}}$	<div style="border: 2px solid black; height: 100px;"></div> <div style="border: 2px solid black; height: 100px;"></div>
Service Ceiling	$\frac{dh}{dt} = 100 \text{ ft/min}$ $\frac{dV}{dt} = 0$ $n = 1$	<div style="border: 2px solid black; height: 100px;"></div>

Constraint Analysis Matrix for Morphing Aircraft



Constraint Analysis Matrix for Morphing Aircraft



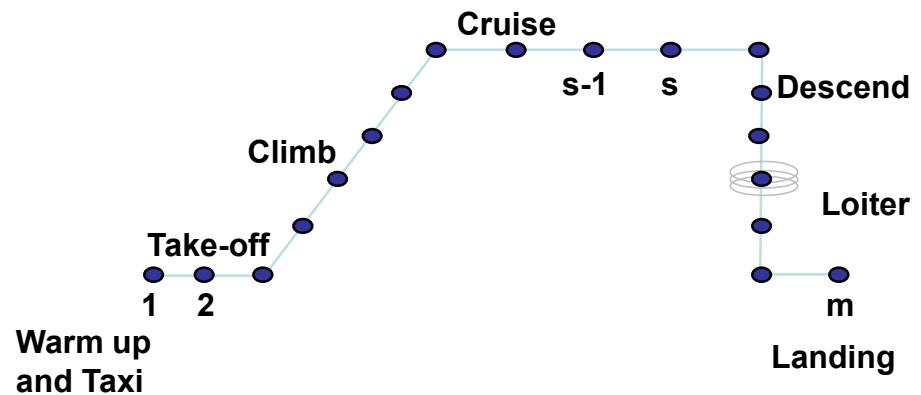
New Mission Analysis

Discretize the Mission Profile

Calculate Energy Consumptions for Each Mission Segment

- ✓ Consumable Energy
 1. *Variable Aircraft Weight ($k \neq 0$)*
 2. *Constant Aircraft Weight ($k = 0$)*

- ✓ Non-consumable Energy
 1. *With Consumable Energy*
 2. *Without Consumable Energy ($k=0$)*



Integrate the Results of All Mission Segments

Summary of Mission Analysis

Consumable Energy

$$\Omega_{CE} = \frac{W_{CE}}{W_{TO}} = (1 + \epsilon_{CE}) \sum_{s=1}^m \frac{W_{CE}^{(s)}}{W_{TO}}$$

Vehicle weight at the end of s-th segment

$$\frac{W_{CE}^{(s)}}{W_{TO}} = \frac{\beta^{(s-1)}}{k} \left(1 - \frac{W^{(s)}}{W^{(s-1)}} \right)$$

- Ω_{CE} Consumable energy weight fraction
- $\epsilon_{CE}^{(s)}$ Overall power-specific fuel consumption at s-th mission segment
- $\gamma^{(s)}$ Weight-specific work down

Non-consumable Energy

$$\Omega_{NE} = \frac{W_{NE}}{W_{TO}} = (1 + \epsilon_{NE}) \sum_{s=1}^m \beta^{(s-1)} \gamma^{(s)} \epsilon_{NE}^{(s)}$$

$$\frac{W^{(s)}}{W^{(s-1)}} = \exp(-k \gamma^{(s)} \epsilon_{CE}^{(s)})$$

$$\frac{W_{CE}^{(s)}}{W_{TO}} = \beta^{(s-1)} \gamma^{(s)} \epsilon_{CE}^{(s)}$$

$$\epsilon_{CE}^{(s)} = \sum_{i=1}^{n_{CE}} \frac{\tau^{(i)}}{\nu_{CE}^{(i)} \eta^{(i)}}$$

$$\gamma^{(s)} = \int_{t^{(s-1)}}^{t^{(s)}} \left(\frac{P}{W} \right) dt$$

Note that $\gamma^{(s)}$ must not be confused with γ , which represents power extraction ratio

Mission Analysis : Consumable Energy Sizing

1. Variable Aircraft Weight ($k \neq 0$)

$$dW = kdW_{CE} \quad dW_{CE_i}^{(i)} = -\frac{\tau^{(i)} P}{v_{CE_i} \prod_{\eta}^{(i)}} dt$$



$$\frac{dW}{W} = -\sum_{i=1}^{n_{CE}} \frac{k \tau^{(i)}}{v_{CE}^{(i)} \prod_{\eta}^{(i)}} \left(\frac{P}{W} \right) dt$$



$$\frac{W^{(s)}}{W^{(s-1)}} = \exp(-k^{(s)} Y^{(s)} \Xi_{CE}^{(s)})$$



$$\frac{W_{CE}^{(s)}}{W_{TO}} = \frac{\beta^{(s-1)}}{k^{(s)}} \left(1 - \frac{W^{(s)}}{W^{(s-1)}} \right)$$

Weight specific work done

$$Y^{(s)} = \int_{t^{(s-1)}}^{t^{(s)}} \frac{P}{W} dt \approx \begin{cases} \frac{\Delta z_e^{(s)}}{1-u} & \text{(Positive excess power)} \\ \left(\frac{D+R}{W} \right) V dt \text{ or } \left(\frac{D+R}{W} \right) ds & \text{(Zero excess power)} \end{cases}$$

Overall power-specific fuel consumption $\Xi_{CE}^{(s)} = \sum_{i=1}^{n_{CE}} \frac{\tau^{(i)}}{v_{CE}^{(i)} \prod_{\eta}^{(i)}}$

Drag to thrust ratio $u = \frac{D+R}{T} = nV \left(\frac{C_D + C_{DR}}{C_L} \right) \left/ \sum_{i=1}^{n_r} \frac{\Pi_{\eta_i} \alpha_i}{\beta} \frac{P_{io SL}}{W_{TO}} \right.$

Energy height $z_e = h + \frac{V^2}{2g_o}$

Weight fraction $\beta^{(s-1)} = \frac{W^{(s-1)}}{W_{TO}}$ (Normal case)
 $= \frac{W^{(s-1)} - W_P^{(s-1)}}{W_{TO}}$ (Payload drop)

Note that $\gamma^{(s)}$ is displayed as $Y^{(s)}$

Mission Analysis : Consumable Energy Sizing

2. Constant Aircraft Weight ($k= 0$)

$$\frac{dW_{CE}}{W} = - \sum_{i=1}^{n_{CE}} \frac{\tau^{\langle i \rangle}}{\nu_{CE_i} \Pi_{\eta}^{\langle i \rangle}} \left(\frac{P}{W} \right) dt$$



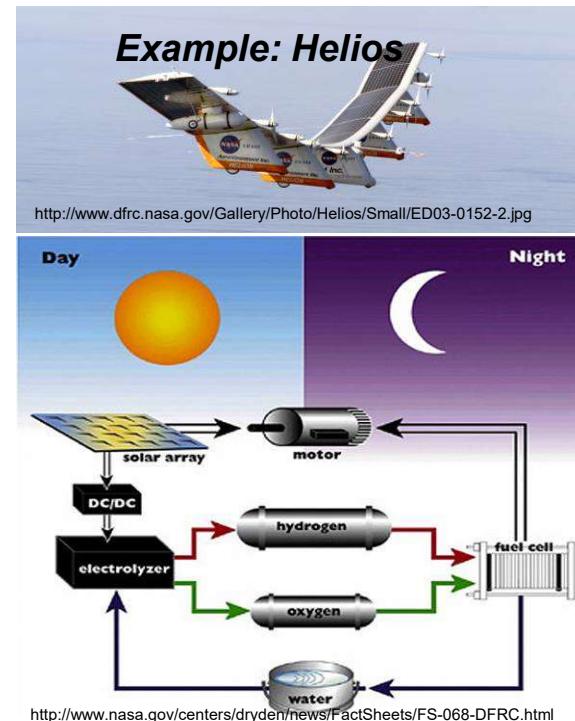
$$\frac{W_{CE}^{(s)}}{W} = \int_{t^{(s)}}^{t^{(s-1)}} \sum_{i=1}^{n_{CE}} \frac{\tau^{\langle i \rangle}}{\nu_{CE_i} \Pi_{\eta}^{\langle i \rangle}} \left(\frac{P}{W} \right) dt$$



$$\frac{W_{CE}^{(s)}}{W_{TO}} = \beta^{(s-1)} Y^{(s)} \Xi_{CE}^{(s)}$$



$$\frac{W_{CE}}{W_{TO}} = \Omega_{CE} = (1 + \varepsilon_{CE}) \sum_{s=1}^m \frac{W_{CE}^{(s)}}{W_{TO}}$$



Note that $\gamma^{(s)}$ is displayed as $Y^{(s)}$

Mission Analysis: Non-consumable Energy Sizing

1. Presence of Consumable Energy

$$dE_{NE}^{(j)} = \frac{\tau^{(j)}}{\tau^{(i)}} \frac{\Pi_\eta^{(i)}}{\Pi_\eta^{(j)}} \nu_{CE}^{(i)} dW_{CE}^{(i)}$$

$$\left(\frac{E_{NE}^{(j)}}{W_{TO}} \right)^{(s-1)} - \left(\frac{E_{NE}^{(j)}}{W_{TO}} \right)^{(s)} = \frac{\tau^{(j)}}{\tau^{(i)}} \frac{\Pi_\eta^{(i)}}{\Pi_\eta^{(j)}} \frac{\nu_{CE}^{(i)} W_{CE}^{(s)}}{W_{TO}}$$

2. Non-consumable Energy Only

$$dE_{NE}^{(j)} = -p_o^{(j)} dt = -\frac{\tau^{(j)} P}{\Pi_\eta^{(j)}} dt \quad \frac{dE_{NE}^{(j)}}{\beta W_{TO}} = -\frac{\tau^{(j)} P}{\Pi_\eta^{(j)} W} dt$$

$$\left(\frac{E_{NE}^{(j)}}{W_{TO}} \right)^{(s-1)} - \left(\frac{E_{NE}^{(j)}}{W_{TO}} \right)^{(s)} = \int_{t^{(s-1)}}^{t^{(s)}} \frac{\beta^{(s-1)} \tau^{(j)}}{\Pi_\eta^{(j)}} \frac{P}{W} dt$$

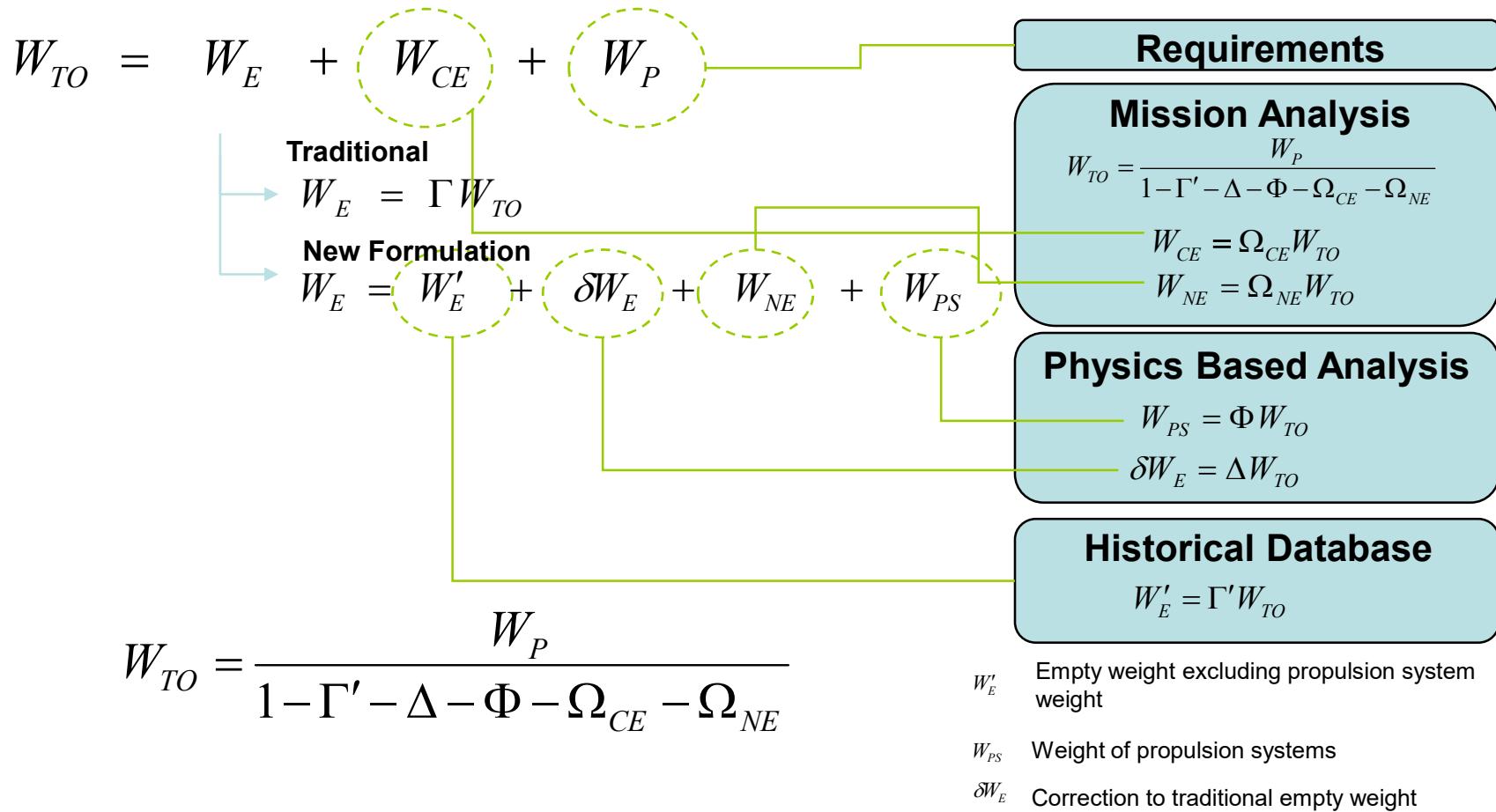
$$\frac{E_{NE}^{(j)}}{W_{TO}} = \sum_{s=1}^m \frac{\beta^{(s-1)} Y^{(s)} \tau^{(j)}}{\Pi_\eta^{(j)}}$$

$$W_{NE} = \sum_{j=1}^{n_{NE}} W_{NE}^{(j)} = \sum_{j=1}^{n_{NE}} \frac{E_{NE}^{(j)}}{\nu_{NE}^{(j)}}$$

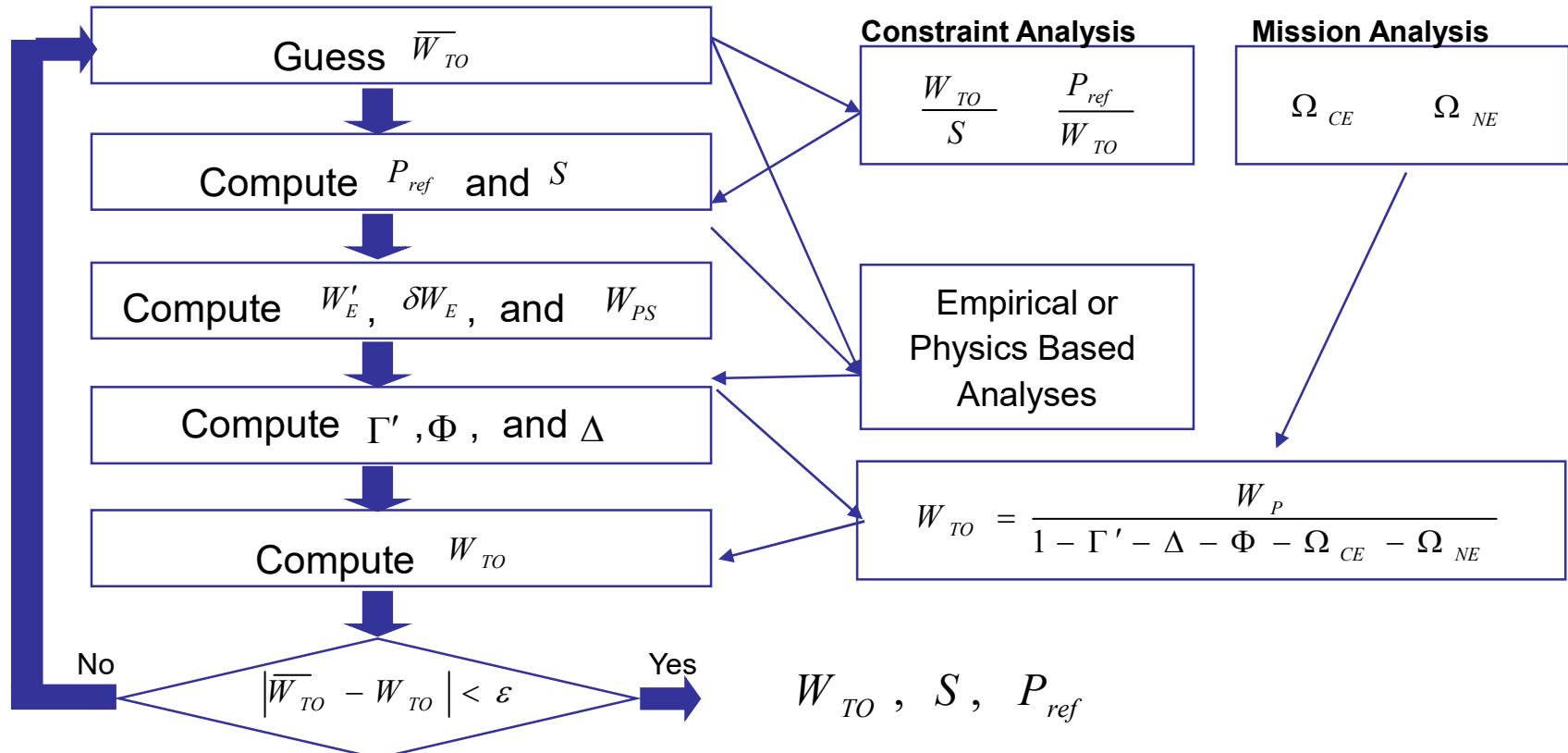
$$\frac{W_{NE}}{W_{TO}} = \Omega_{NE} = (1 + \varepsilon_{CE}) \sum_{s=1}^m \beta^{(s-1)} Y^{(s)} \Xi_{NE}^{(s)}$$

Note that $\gamma^{(s)}$ is displayed as $Y^{(s)}$

Aircraft Weight Estimation



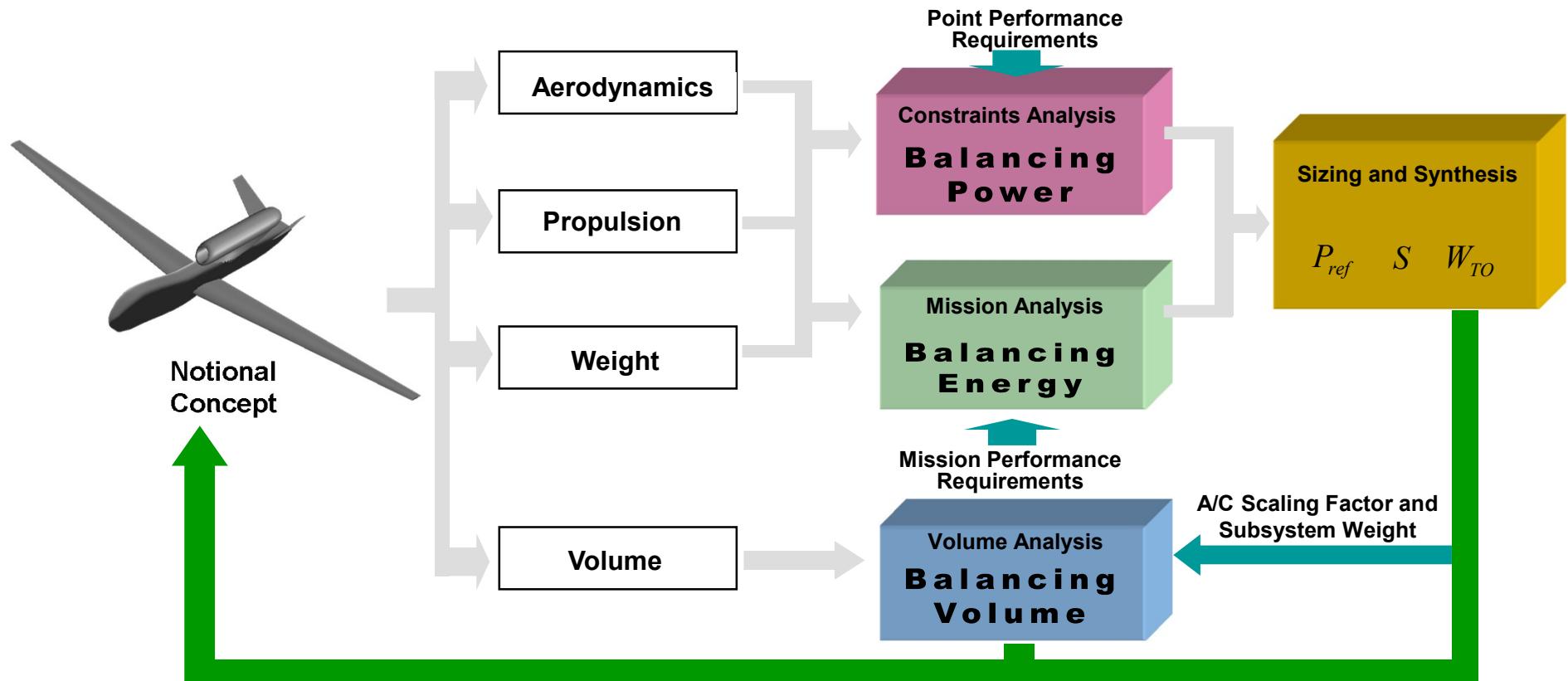
Weight Estimation Process



Comparison

	Old Formulation	New Formulation
Weight Decomposition	$W = W_E + W_F + W_P$	$W = W_E + W_P + W_{CE} + W_R$
Weight Diff. Equation	$dW = dW_F$	$dW = kdW_{CE}$
Onboard Energy Weight	$W_F = (1 + \varepsilon)(1 - \Pi)W_{TO}$	$W_{CE} = \Omega_{CE}W_{TO}$ where $\Omega_{CE} = (1 + \varepsilon_{CE}) \sum_{s=1}^m \frac{W_{CE}^{(s)}}{W_{TO}}$ <i>When $k \neq 0$</i> $\frac{W_{CE}^{(s)}}{W_{TO}} = \frac{\beta^{(s-1)}}{k^{(s)}} \left(1 - \frac{W^{(s)}}{W^{(s-1)}} \right)$ $\frac{W^{(s)}}{W^{(s-1)}} = \exp(-k^{(s)} Y^{(s)} \Xi_{CE}^{(s)})$ <i>When $k = 0$</i> $\frac{W_{CE}^{(s)}}{W} = \beta^{(s-1)} Y^{(s)} \Xi_{CE}^{(s)}$ $W_{NE} = \Omega_{NE}W_{TO}$ where $\Omega_{NE} = (1 + \varepsilon_{NE}) \sum_{s=1}^m \beta^{(s-1)} Y^{(s)} \Xi_{NE}^{(s)}$
Take-Off Gross Weight	$W_{TO} = \frac{W_P}{1 - \Gamma - \frac{W_F}{W_{TO}}}$	$W_{TO} = \frac{W_P}{1 - \Gamma' - \Delta - \Phi - \Omega_{CE} - \Omega_{NE}}$

Comprehensive Aircraft Sizing Method



Generalized Breguet Range Equation (GBRE)

Consumable Energy

When $k \neq 0$

$$R = \frac{\nu_{CE} \eta L}{k D} \ln \left(\frac{1}{1 - k \frac{W_{CE}}{W_{TO}}} \right)$$

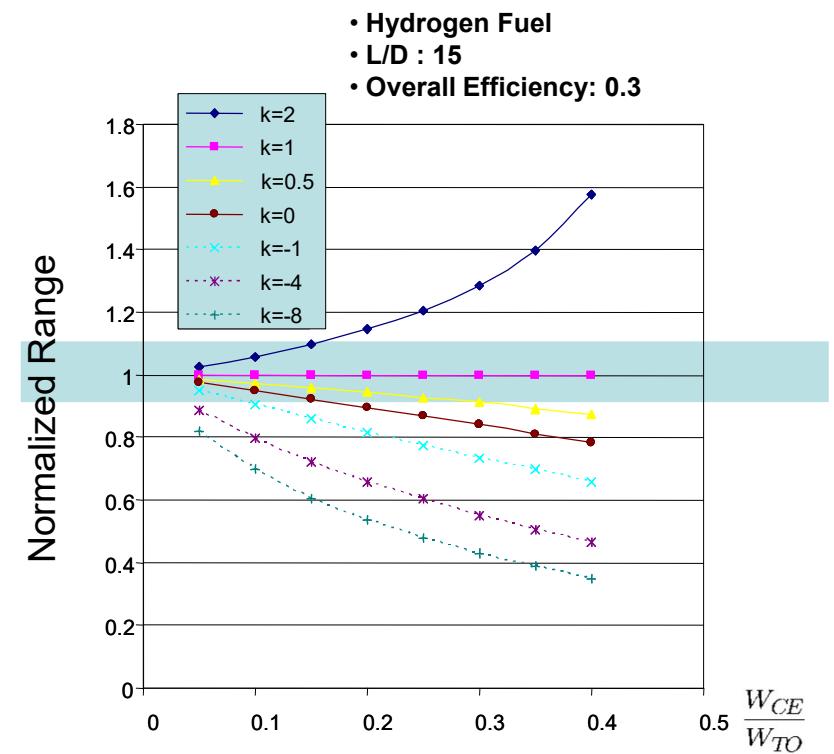
When $k = 0$

$$R = \nu_{CE} \eta \frac{L W_{CE}}{D W_{TO}}$$

Non-consumable Energy

$$R = \nu_{NE} \eta \frac{L W_{NE}}{D W_{TO}}$$

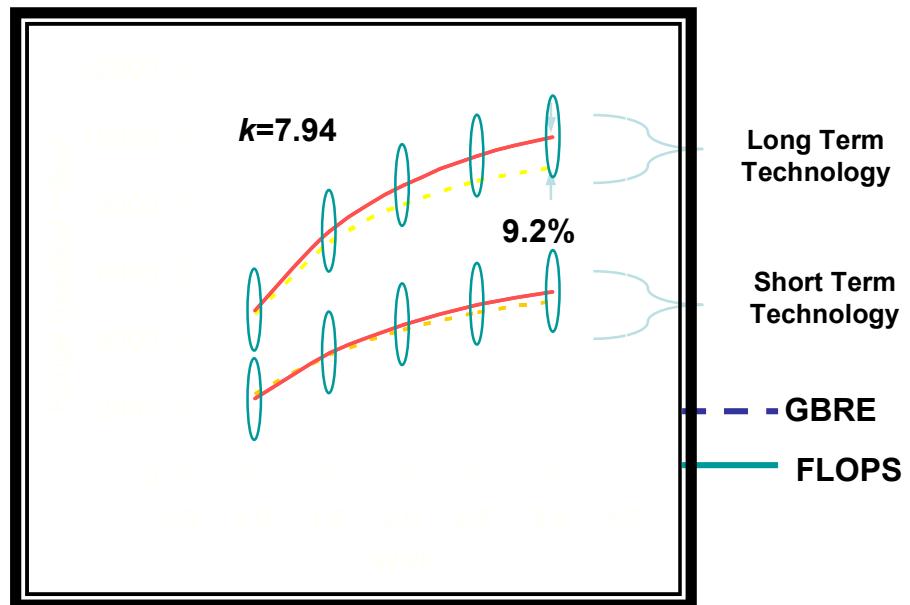
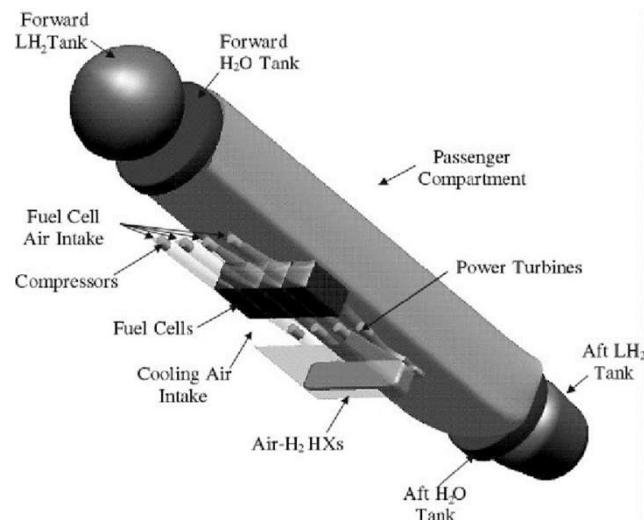
Useful for a first order estimate of range
when limited information is available



Application of GBRE

Zero Emission Aircraft Study Performed by MSE Technology Applications Inc. and NASA LaRC

- 300 PAX subsonic transport fueled by LH₂
- Electric ducted fan engines powered by a PSOFC (planar solid oxide fuel cell) system
- Water vapor is stored in two cylindrical water tanks
- Analyzed by a customized version of FLOPS modified by NASA LaRC



Duality between Energy Source and Propulsion System Weight

$$W_{TO} = W_E + W_{PS} + W_{CE} + \delta W_E + W_{PL}$$

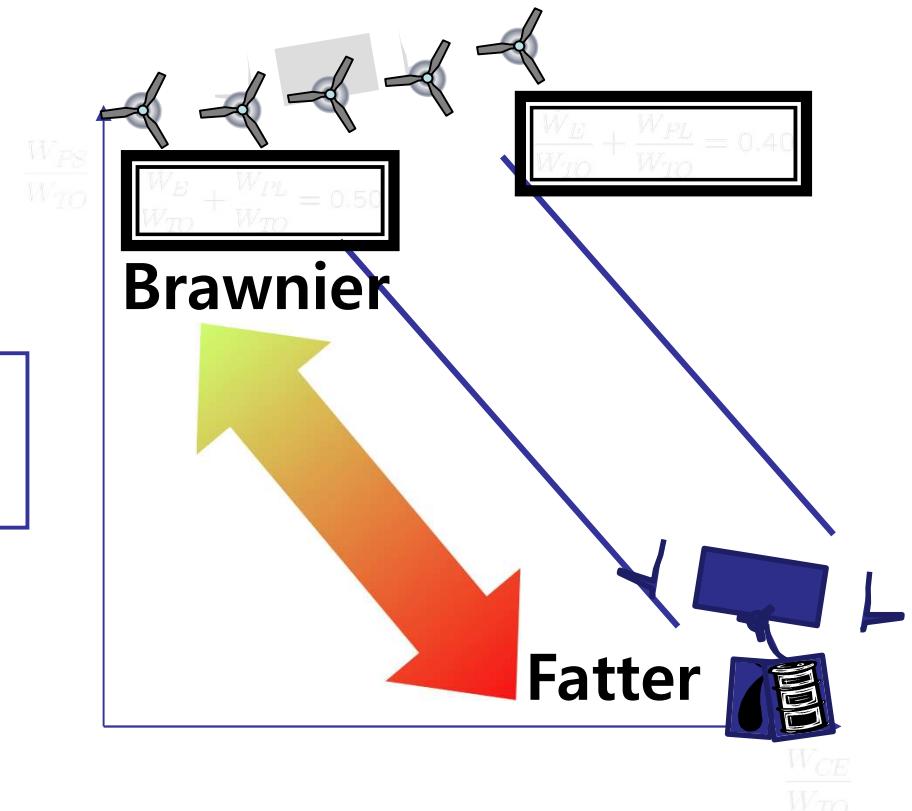
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$$(1 + e_{PS}) \frac{W_{PS}}{W_{TO}} + (1 + e_{CE}) \frac{W_{CE}}{W_{TO}} = 1 - \frac{W_E}{W_{TO}} - \frac{W_{PL}}{W_{TO}}$$

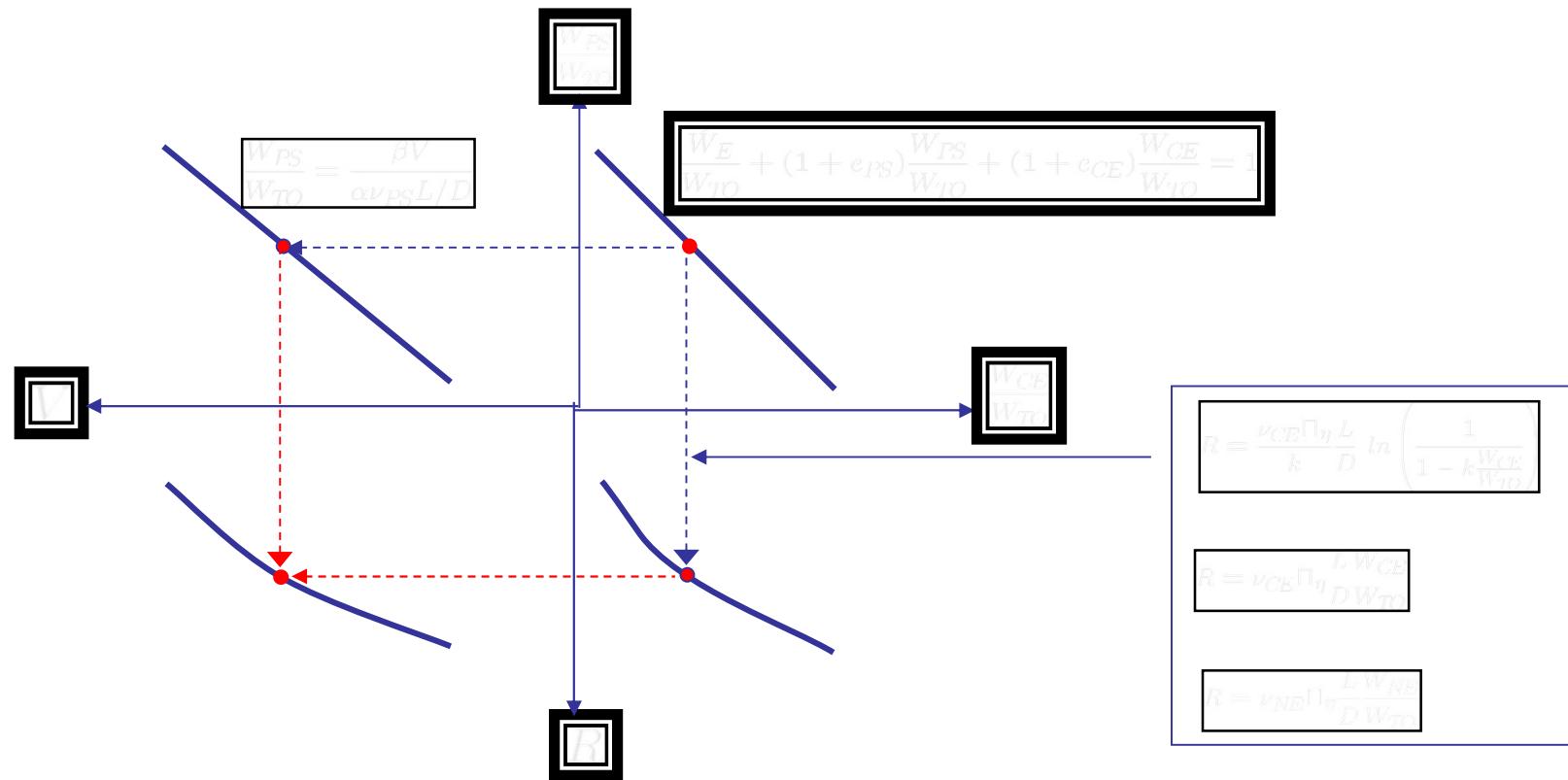
Expresses a set of allowable values for :

- Propulsion system weight fraction
- Energy weight fraction

The impact on the empty weight from integrating an alternative propulsion system and an consumable energy source, all normalized by the take-off gross weight.



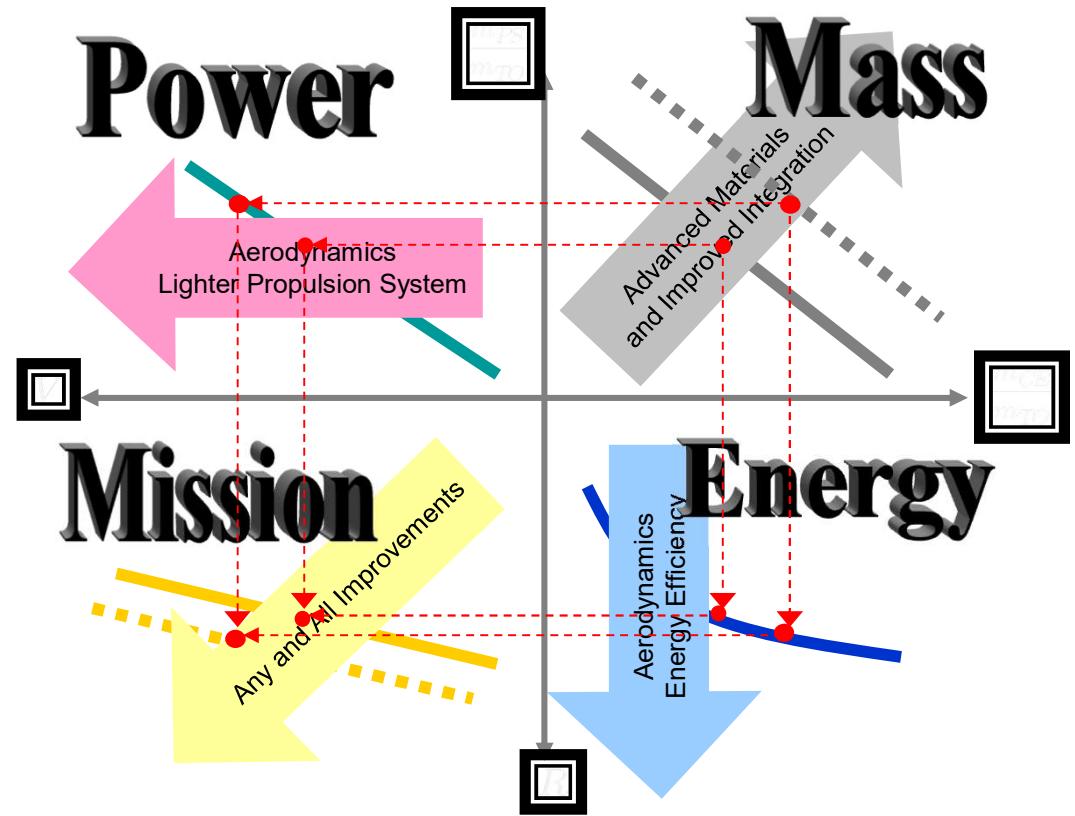
Mapping Weight Fractions to Performance



Non-dimensional Aircraft Mass (NAM) Ratio Diagram

For a given energy-propulsion system architecture, this diagram:

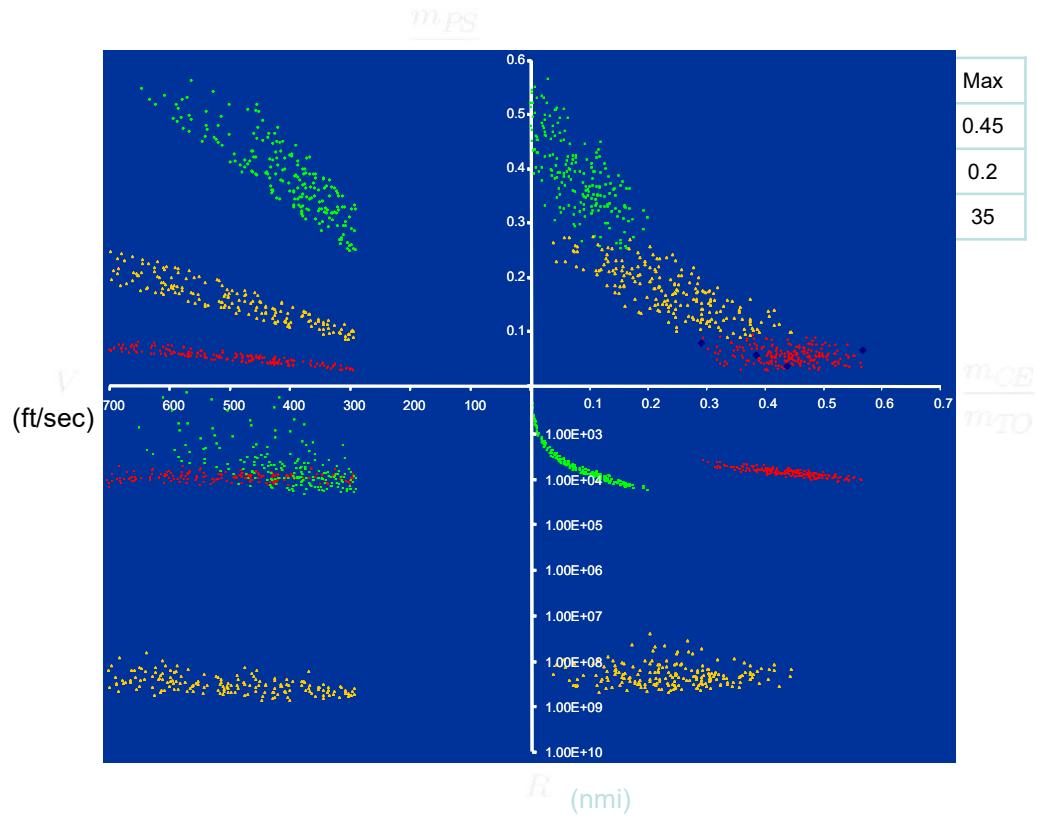
- Develops *the performance frontiers* in terms of range and velocity
- Enables a designer to rapidly examine *a fleet of aircraft designs*
- Identifies *the most appropriate mission*



Example: Comparison of Three Architectures

- **Architecture A:** Conventional turbo prop engine fueled with jet fuel
- **Architecture B:** PEMFC-powered electric propulsion system fueled with liquid hydrogen
- **Architecture C:** Triggered isomer heat exchanger engine (TIHE) fueled isomers of hafnium (^{178}Hf)

Architecture	A	B	C
e_{PS}	0	0	0.51
e_{CE} (e_{NE})	0	0.5	0
Π_η	0.16 - 0.2	0.38 - 0.43	0.35 - 0.5
v_{CE} (v_{NE}) (ft)	1.786×10^7	4.464×10^7	5.653×10^{11}
v_{PS} (ft/sec)	1400	138	421
α	0.27	0.3	0.3



Symbols (1/2)

C_D	Coefficient of clean configuration drag
C_{D_0}	Zero lift drag coefficient
C_{DR}	Coefficient of additional drag
D	Basic configuration drag
E	Amount of stored onboard energy
E_{CB}	Amount of consumable onboard energy
E_{NCB}	Amount of non-consumable onboard energy
g_0	Gravity constant
h	Altitude
\dot{h}	Ratio of the time rate of aircraft weight change to the time rate of consumable energy weight change
K_1	Drag polar coefficient for 2nd order term
K_2	Drag polar coefficient for 1st order term
m	Number of total mission segments
n	Load factor
n_T	Number of total power paths
n_{CP}	Number of consumable power paths
n_{NCP}	Number of non-consumable power paths
n_{PD}	Number of power devices
P	Power available

P_e	Power input from original energy source
P_{ref}	Sizing reference power
p	Dynamic pressure
R	Additional drag to D
s	Travel distance
S	Wing area
S_G	Ground roll
t	Time
T	Thrust
u	Drag to thrust ratio
V	Free stream velocity
V_{stall}	Stall speed
V_{TO}	Take-off speed
W	Instantaneous aircraft weight
W_{CE}	Consumable energy weight
W_{energy}	Total stored energy weight
W_E	Empty weight
W_F	Fuel weight
W_{NE}	Non-consumable energy weight
W_P	Payload weight
W_{PS}	Propulsion system weight
W_{TO}	Take-off gross weight
z	Energy height

Symbols (2/2)

γ	Power lapse ratio
β	Weight fraction
Δ	Weight correction factor
α_{CE}	Consumable energy allowance ratio
α_{NCE}	Non-consumable energy allowance ratio
η	Component efficiency
η_p	Propulsor efficiency
ζ	Empty weight fraction
ξ	Fraction of empty weight excluding propulsion system weight
ρ	Stored product to fuel ratio
ϵ_{CE}	Specific energy of consumable energy
ϵ_{NCE}	Specific energy of non-consumable energy
ϵ_{PD}	Specific power of power devices

ω_{CE}	Consumable energy weight fraction
ω_{NCE}	Non-consumable energy weight fraction
ϕ	Power devices weight fraction
Π_η	Overall efficiency of individual power path
ρ	Free-stream air density
τ	Power fraction of individual power path
T	Weight-specific mechanical energy of aircraft
Ξ_{CE}	Overall power specific fuel consumption

Superscript

(i)	ID number of a power path powered by consumable energy sources
(j)	ID number of a power path powered by non-consumable energy sources
(s)	Mission segment number

 $\Pi_\eta^{+ \langle i \rangle}$

**Product of efficiencies
from sizing reference point to propulsor**