

# Stream Reasoning with Cycles\*

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<sup>3</sup>University of Piraeus, Greece

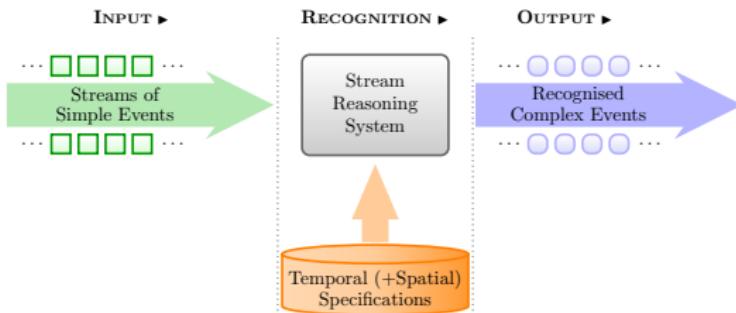
<sup>4</sup>University of Liverpool, UK

<http://cer.iit.demokritos.gr/>

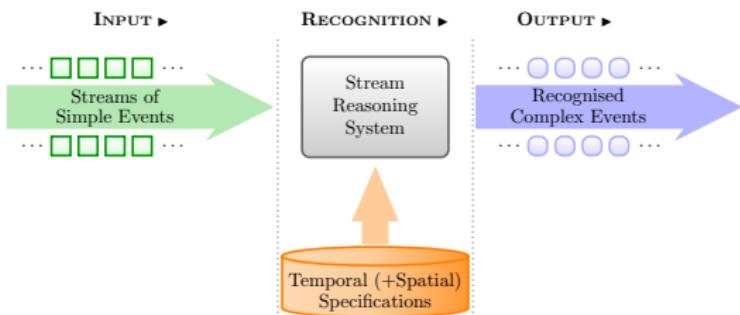
\*Originally presented at KR 2022.



# Stream Reasoning



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[https://cer.iit.demokritos.gr \(maritime\)](https://cer.iit.demokritos.gr (maritime))

# Event Calculus

- A logic programming language for representing and reasoning about events and their effects.
- Key components:
  - event (typically instantaneous).
  - fluent: a property that may have different values at different points in time.

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- A logic programming language for representing and reasoning about events and their effects.
- Key components:
  - event (typically instantaneous).
  - fluent: a property that may have different values at different points in time.
- Built-in representation of inertia:
  - $F = V$  holds at a particular time-point if  $F = V$  has been *initiated* by an event at some earlier time-point, and not *terminated* by another event in the meantime.

## Run-Time Event Calculus

Time in RTEC is a **linear** and **discrete** structure.

Predicate	Meaning
<b>happensAt</b> ( $E, T$ )	Event $E$ occurs at time $T$
<b>initiatedAt</b> ( $F = V, T$ )	At time $T$ a period of time for which $F = V$ is initiated
<b>terminatedAt</b> ( $F = V, T$ )	At time $T$ a period of time for which $F = V$ is terminated
<b>holdsFor</b> ( $F = V, I$ )	$I$ is the list of the maximal intervals for which $F = V$ holds continuously
<b>holdsAt</b> ( $F = V, T$ )	The value of fluent $F$ is $V$ at time $T$

# Fluent-Value Pair Specification

Definition:

**initiatedAt**( $F = V$ ,  $T$ )  $\leftarrow$   
**happensAt**( $E_{In_1}$ ,  $T$ ),  
[conditions]

...

**initiatedAt**( $F = V$ ,  $T$ )  $\leftarrow$   
**happensAt**( $E_{In_i}$ ,  $T$ ),  
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**terminatedAt**( $F = V$ ,  $T$ )  $\leftarrow$   
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[conditions]

...

**terminatedAt**( $F = V$ ,  $T$ )  $\leftarrow$   
**happensAt**( $E_{T_j}$ ,  $T$ ),  
[conditions]

where

conditions:       $^{0-K}$  [not] **happensAt**( $E_k$ ,  $T$ ),  
 $^{0-M}$  [not] **holdsAt**( $F_m = V_m$ ,  $T$ ),  
 $^{0-N}$  atemporal-constraint<sub>n</sub>

# Fluent-Value Pair Computation

Definition:

**initiatedAt**( $F = V, T$ )  $\leftarrow$   
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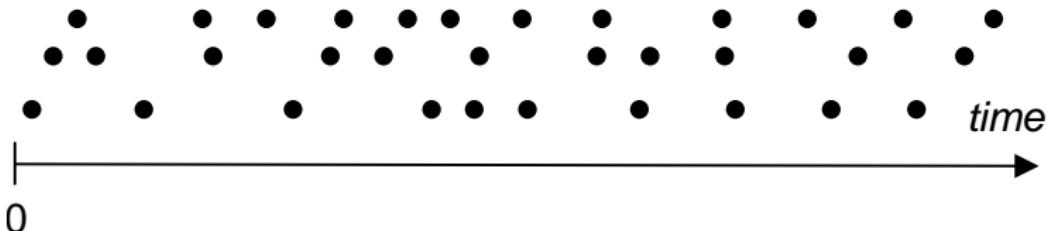
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Reasoning:



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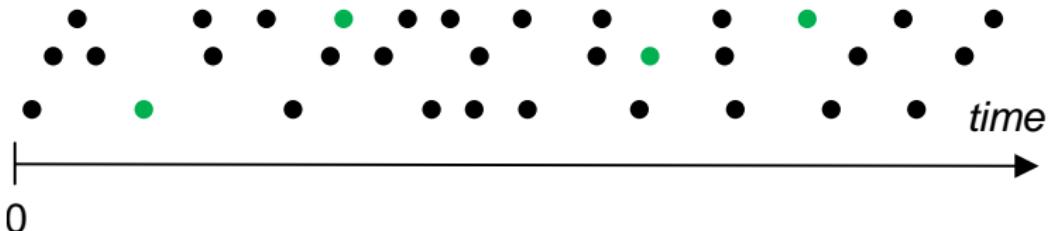
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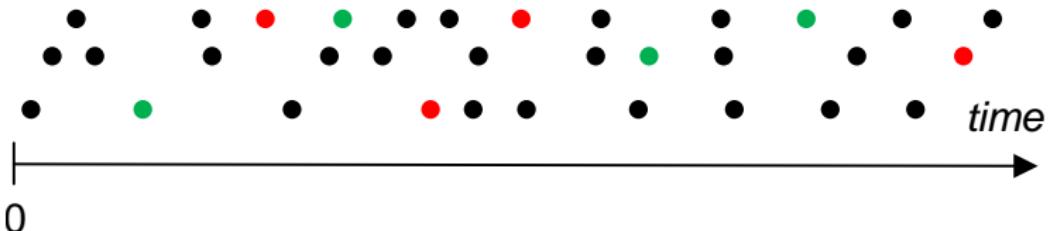
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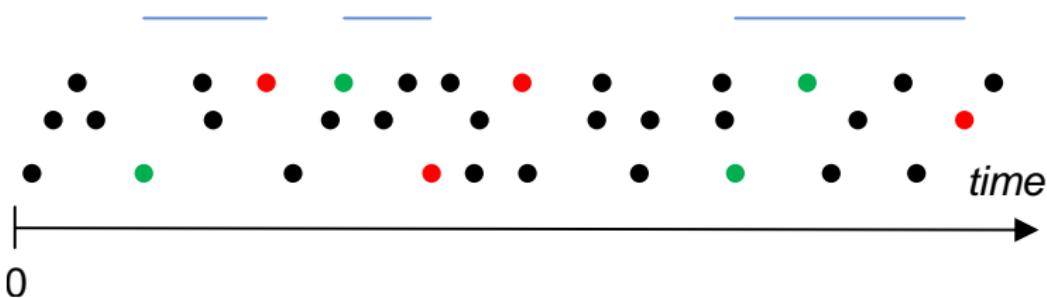
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[conditions]

Reasoning: **holdsFor**( $F = V, I)$



# Stratification

## Definition

A logic program  $P$  is called stratified when it is made up of several distinct strata  $P_i$  i.e.,

$$P = P_0 \cup P_1 \dots P_n$$

where:

- $P_0$  contains only definite clauses and,
- for  $i > 0$  any clauses with negative literals in  $P_i$  may only refer to predicates of  $P_j$  where  $j < i$ .

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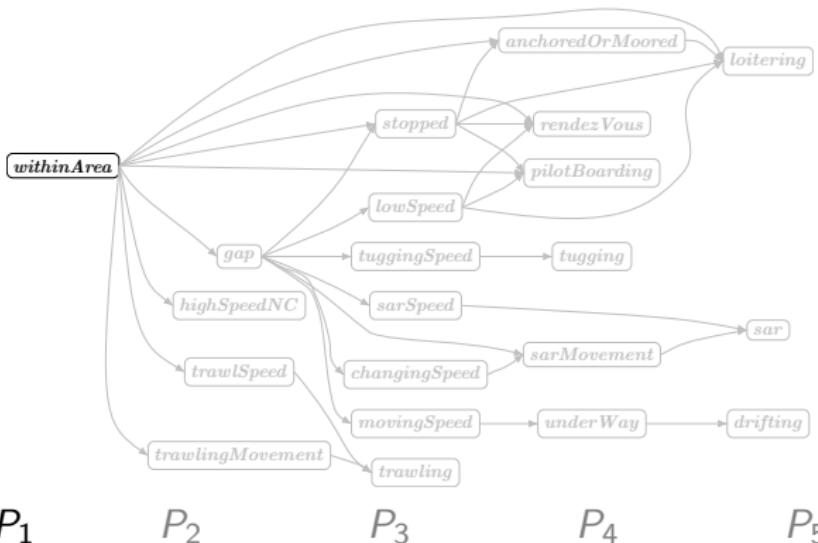
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An acyclic event description in RTEC is a **locally stratified logic program**.

# Stratification in RTEC



$P_1$

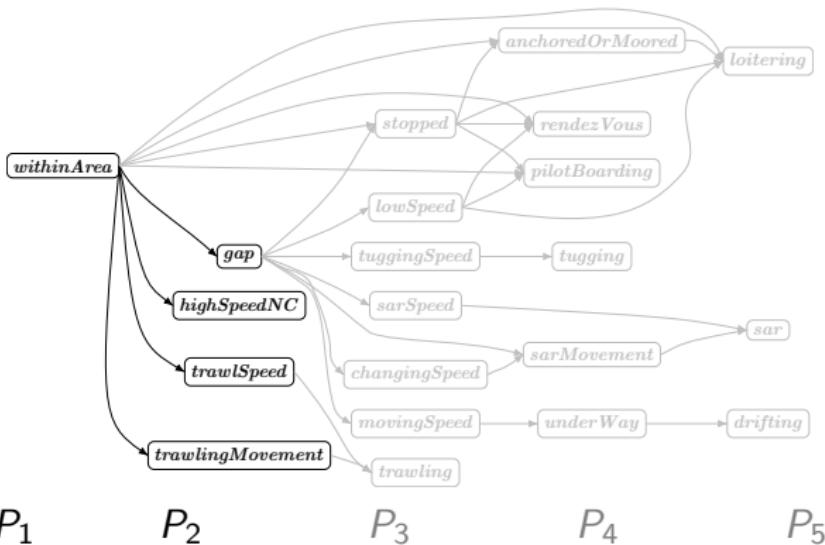
$P_2$

$P_3$

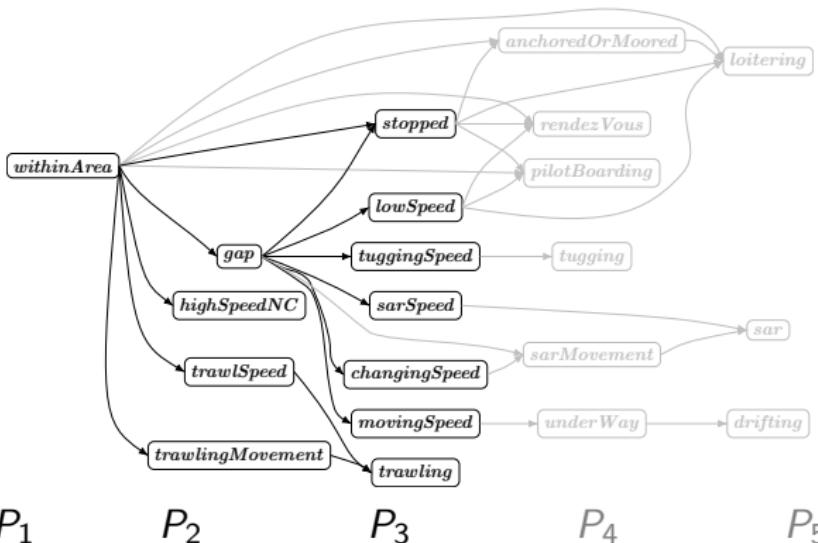
$P_4$

$P_5$

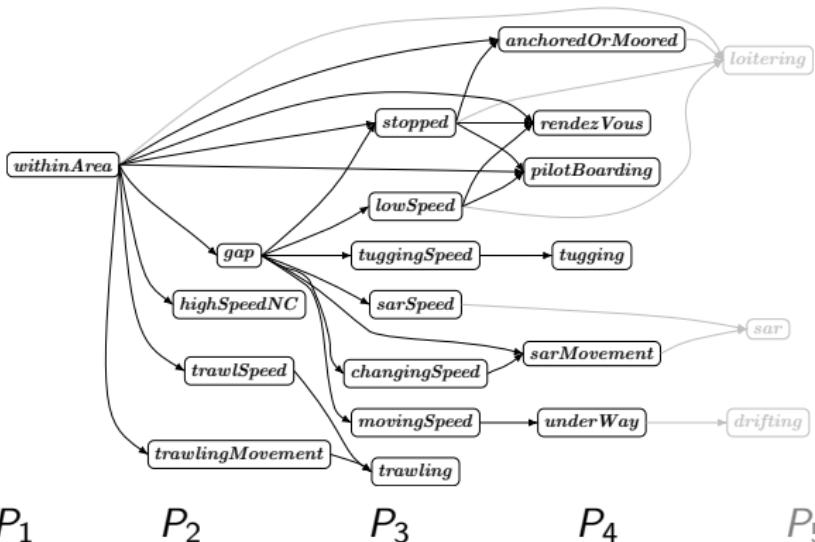
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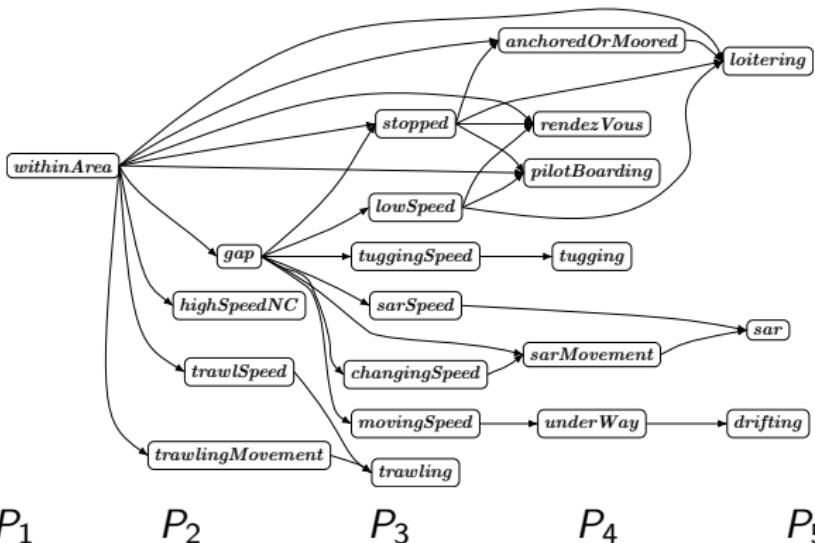
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# Cyclic Dependencies in Temporal Specifications

```
initiatedAt(status( $M$ ) = proposed,  $T$ ) ←  
  happensAt(propose( $P$ ,  $M$ ),  $T$ ),  
  holdsAt(status( $M$ ) = null,  $T$ ).
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initiatedAt(status( $M$ ) = proposed,  $T$ ) ←  
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initiatedAt(status( $M$ ) = voting,  $T$ ) ←  
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  holdsAt(status( $M$ ) = proposed,  $T$ ).  
  
initiatedAt(status( $M$ ) = voted,  $T$ ) ←  
  happensAt(close_ballot( $C, M$ ),  $T$ ),  
  holdsAt(status( $M$ ) = voting,  $T$ ).
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# Cyclic Dependencies in Temporal Specifications

**initiatedAt**( $status(M) = proposed, T$ )  $\leftarrow$   
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**initiatedAt**( $status(M) = voted, T$ )  $\leftarrow$   
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**initiatedAt**( $status(M) = null, T$ )  $\leftarrow$   
**happensAt**( $declare(C, M, Res), T$ ),  
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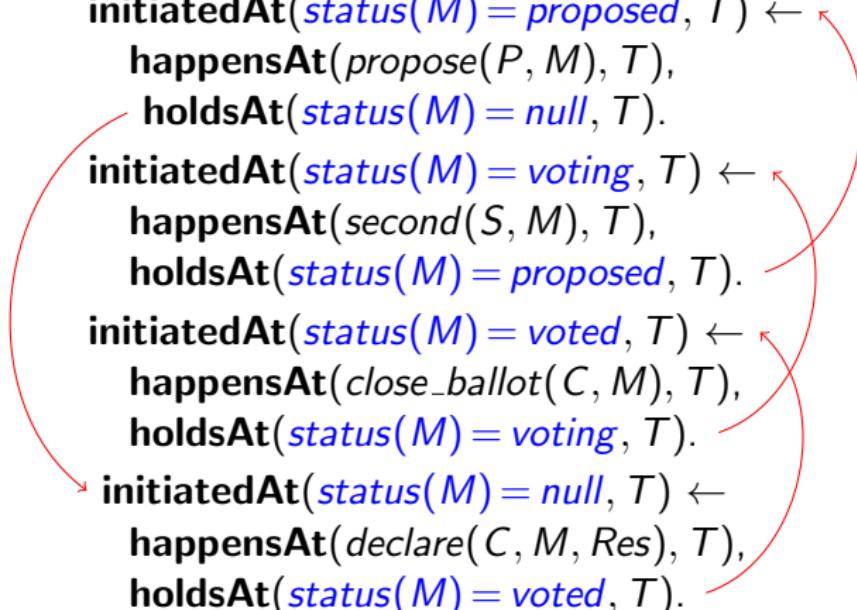
# Cyclic Dependencies in Temporal Specifications

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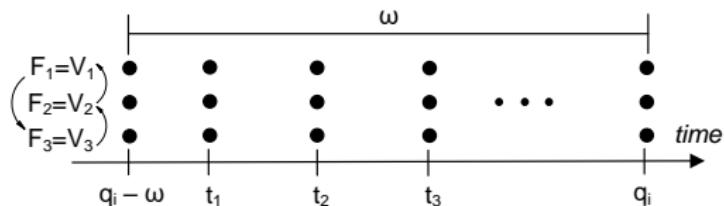
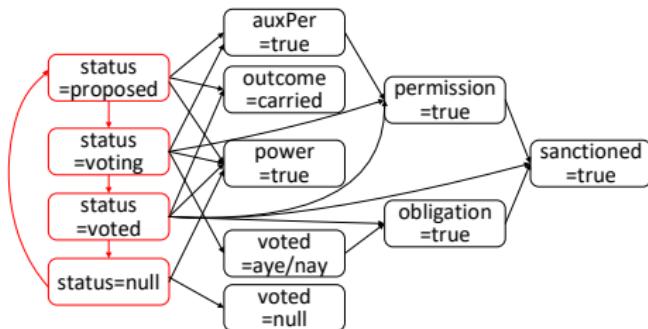


# RTEC<sub>o</sub>: Run-Time Event Calculus for Cyclic Dependencies

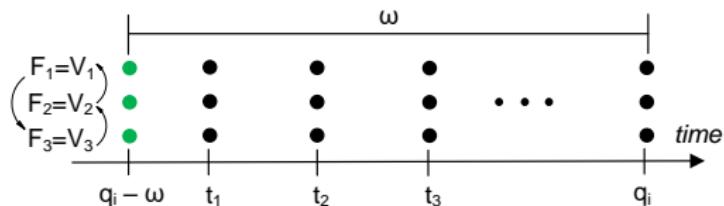
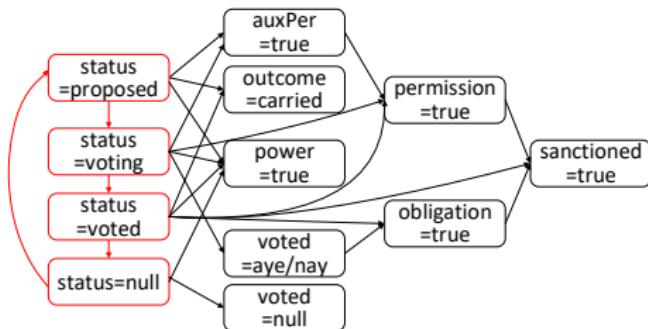
RTEC<sub>o</sub>: an extension of RTEC for efficient reasoning over specifications with **cyclic dependencies**

- Formal & open-source computational framework
- Locally stratified specifications
- Incremental caching of intermediate computations
- Scalable in large, real-world data streams

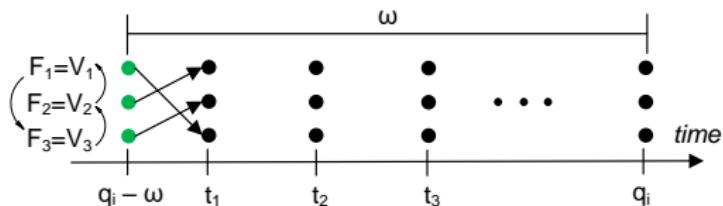
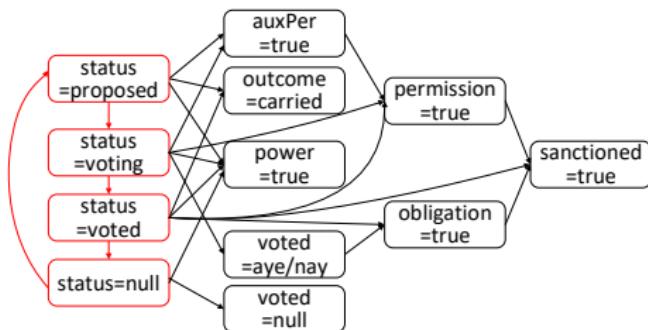
# Stratification in RTEC.



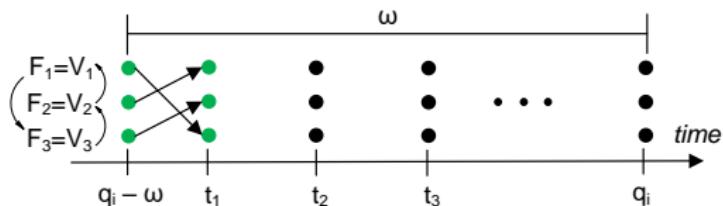
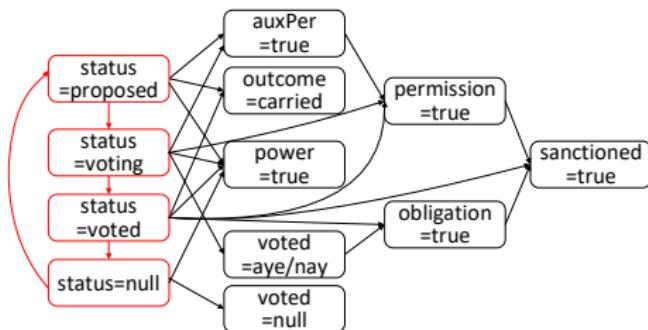
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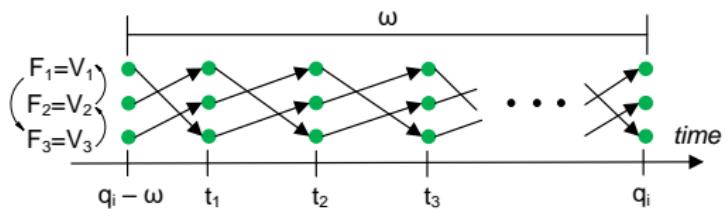
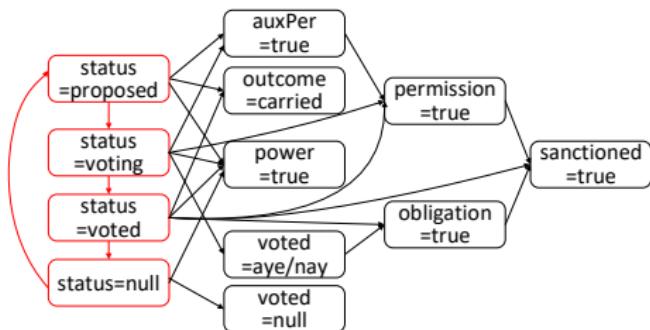
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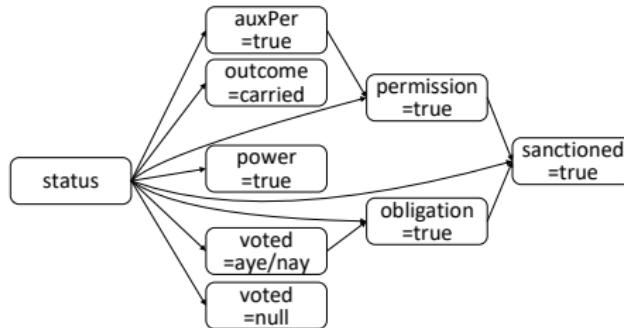
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# Stratification in RTEC<sub>o</sub>



## Stratification in RTEC<sub>o</sub>



$P_1$

$P_2$

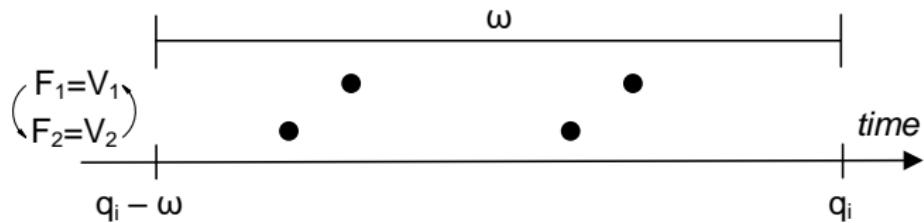
$P_3$

$P_4$

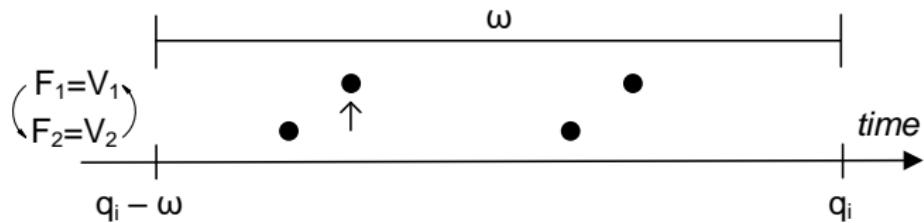
$$P_1 = P_{q_i-\omega} \cdots P_{q_i}$$

An event description of RTEC<sub>o</sub> is a locally stratified logic program.

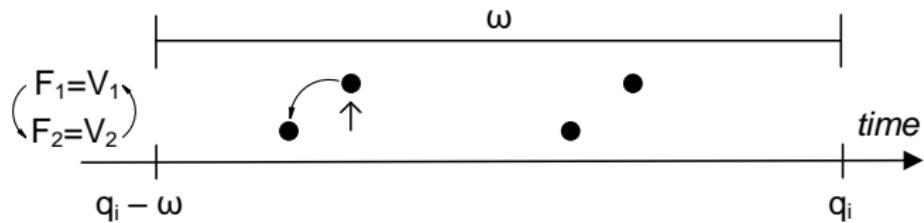
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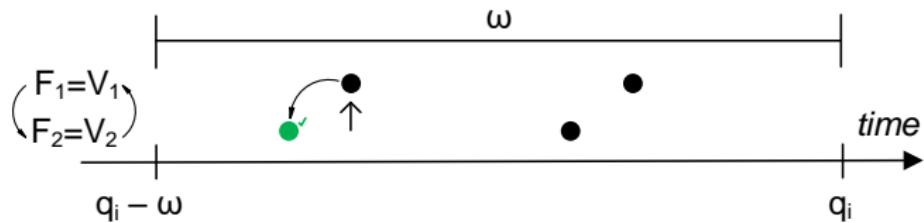
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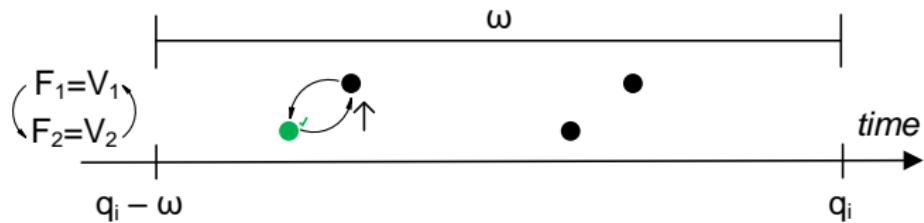
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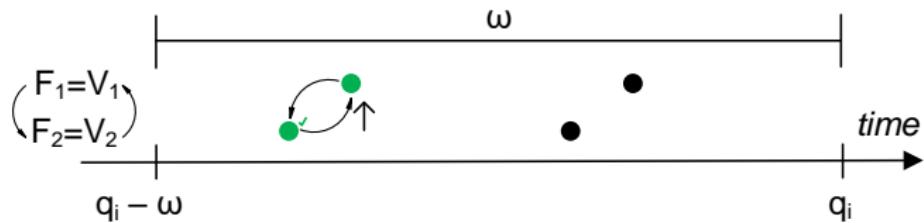
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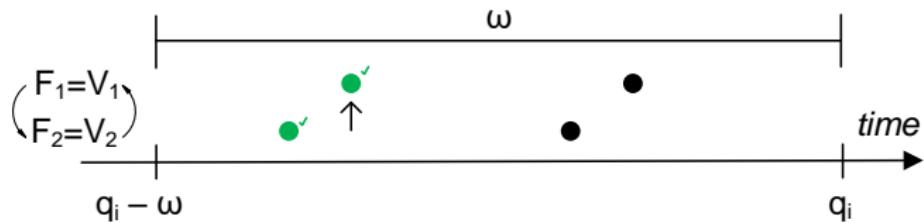
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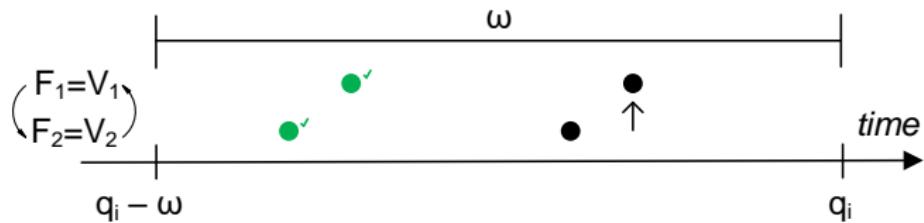
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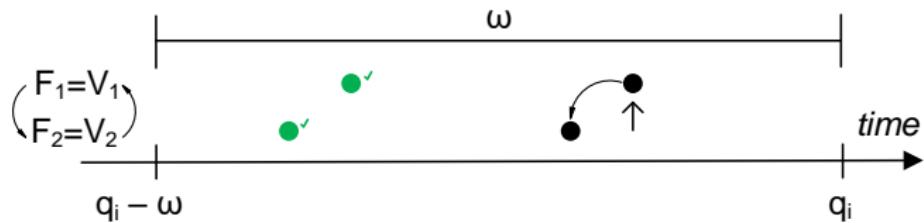
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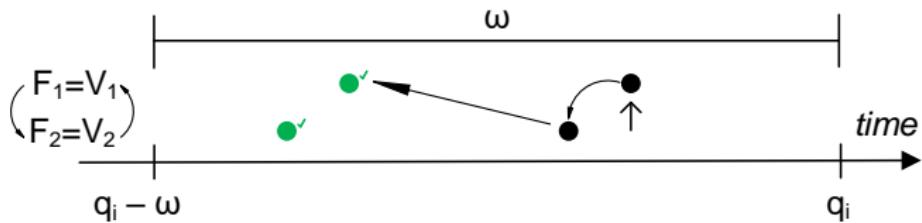
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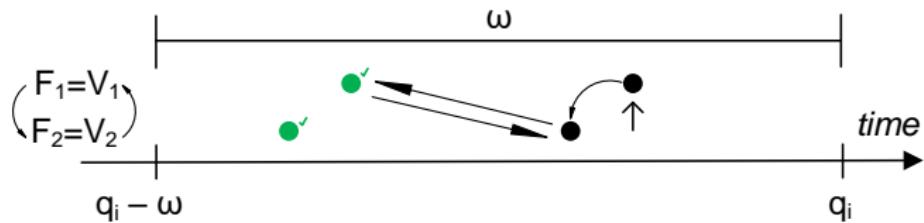
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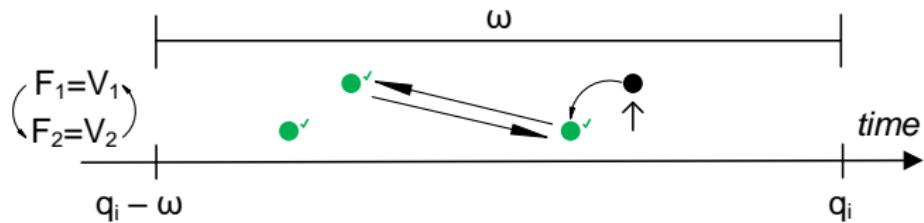
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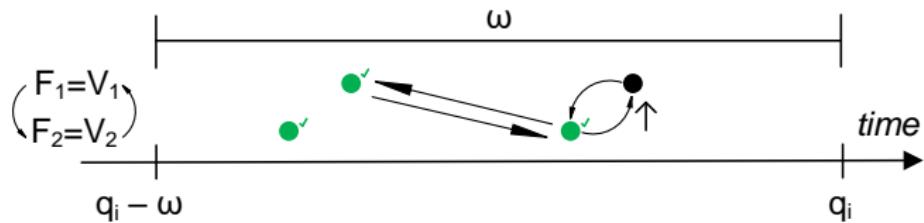
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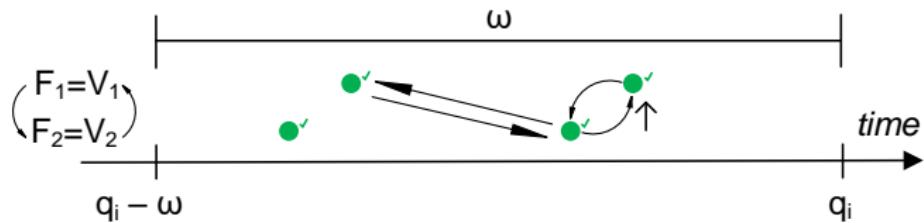
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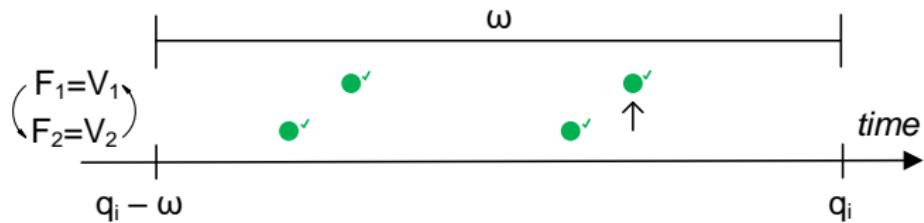
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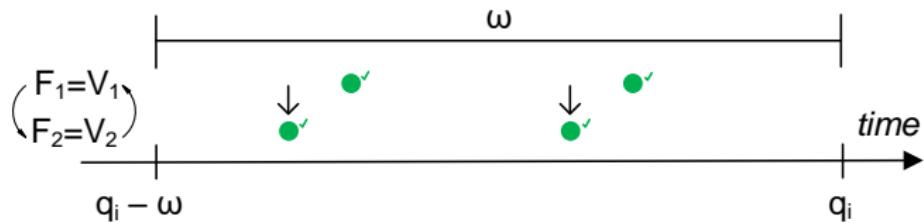
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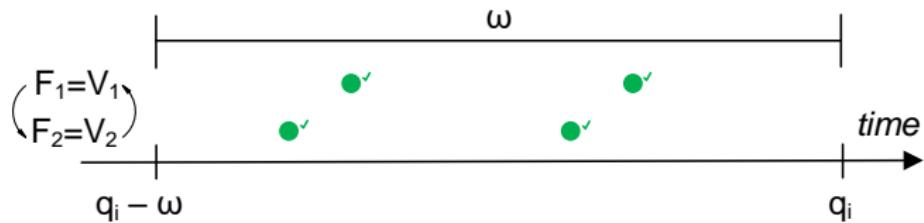
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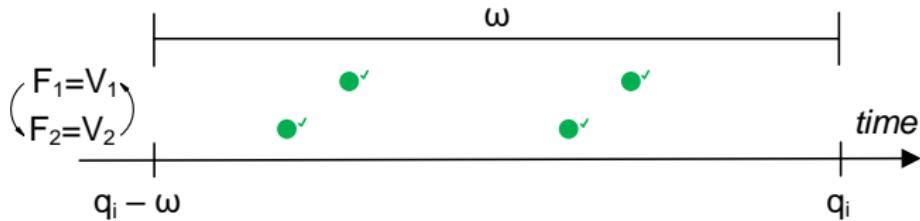


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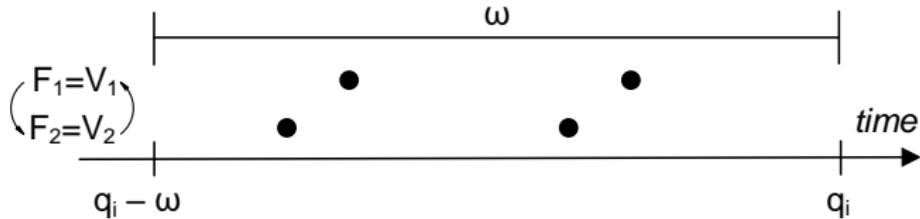


# Handling Cyclic Dependencies

RTEC<sub>o</sub>

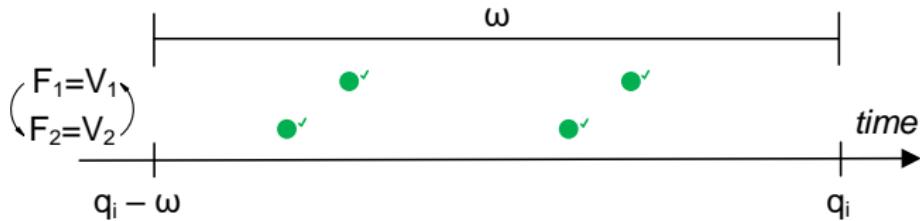


Event Calculus

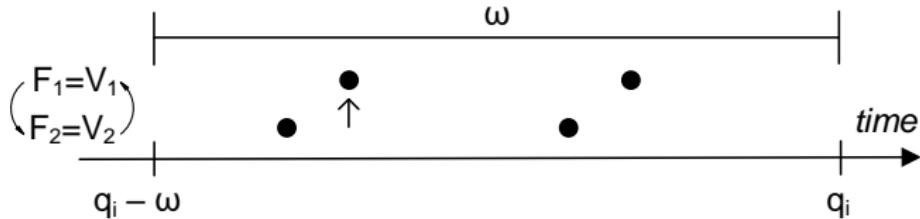


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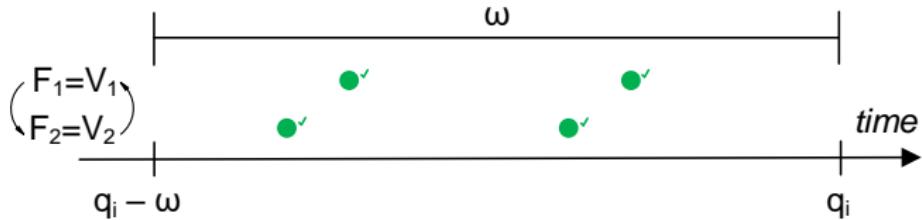


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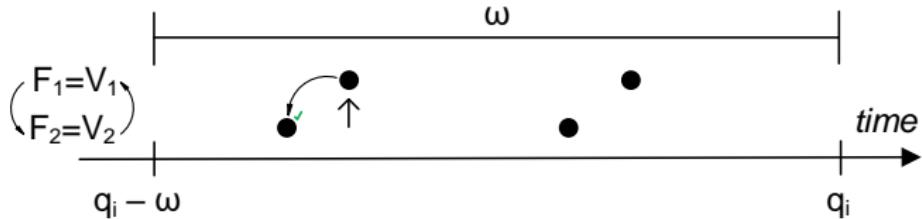


# Handling Cyclic Dependencies

RTEC<sub>o</sub>

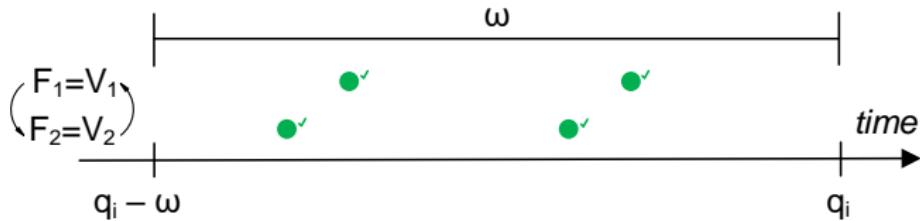


Event Calculus

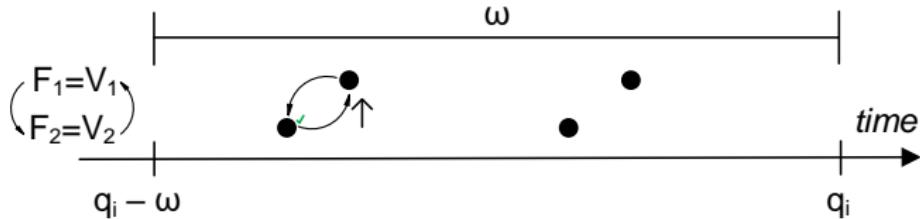


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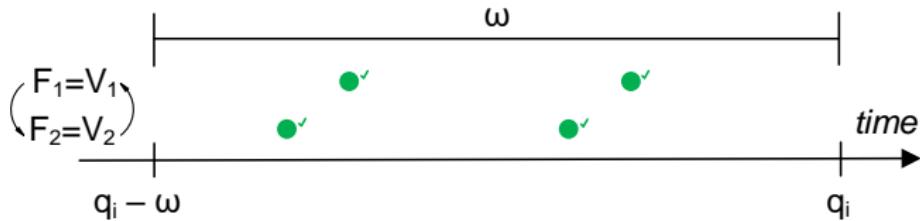


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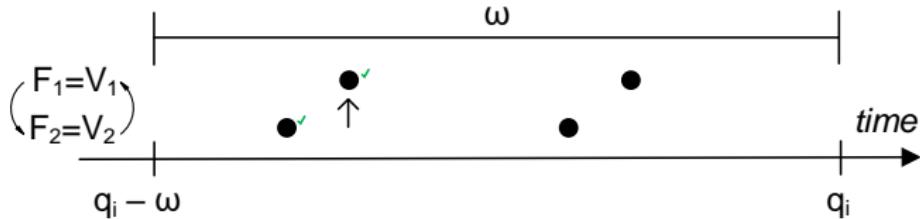


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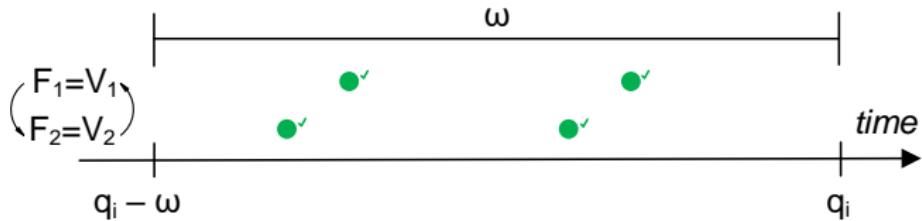


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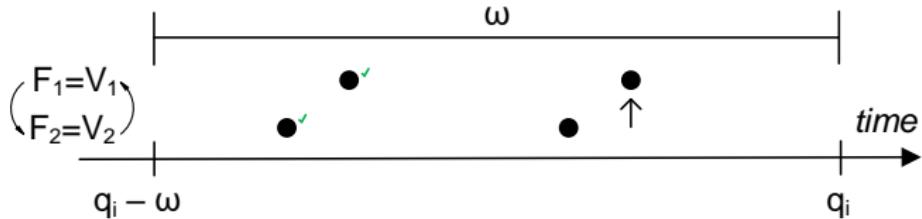


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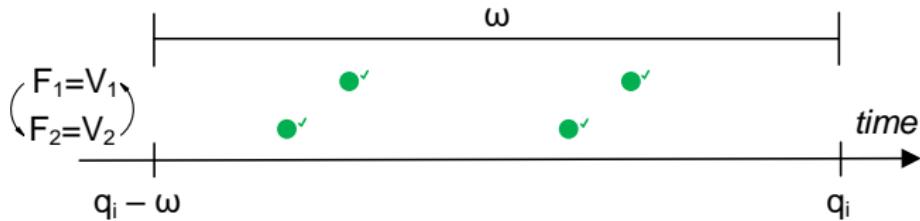


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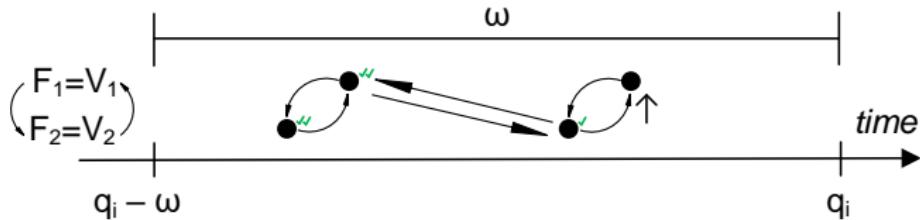


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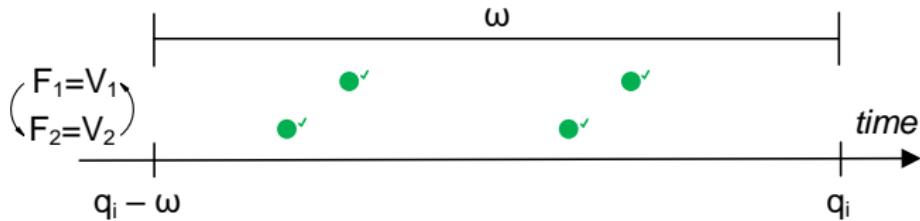


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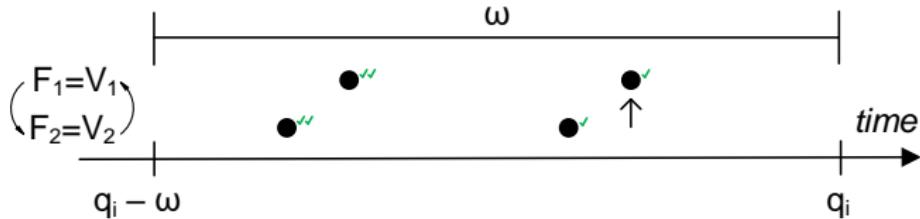


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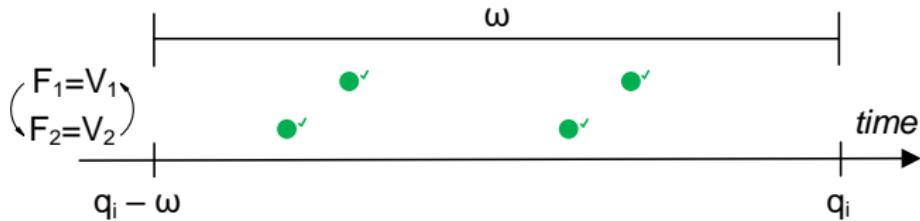


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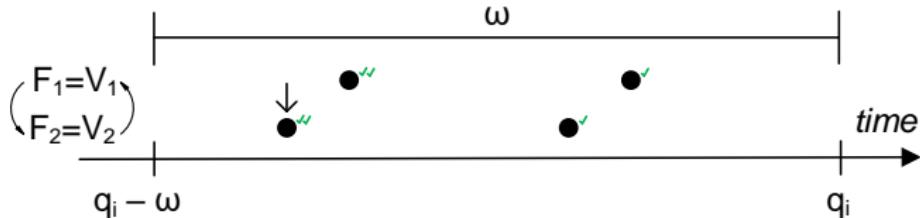


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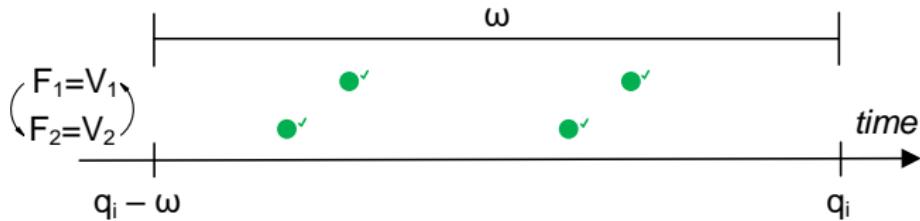


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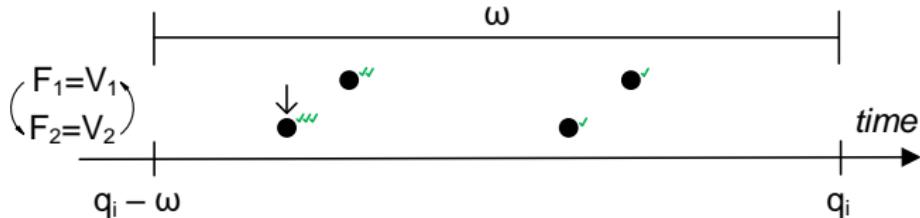


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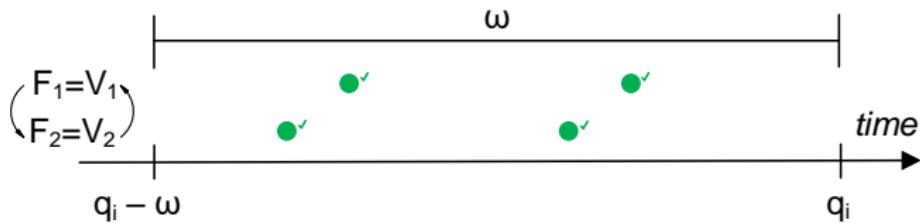


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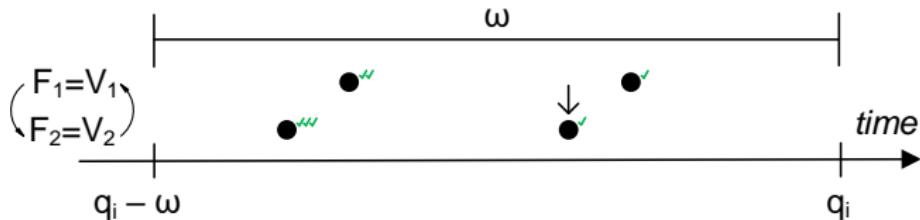


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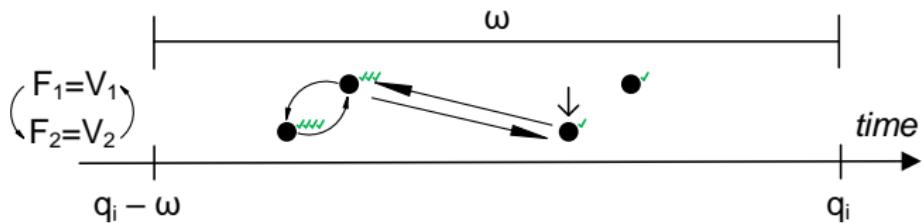


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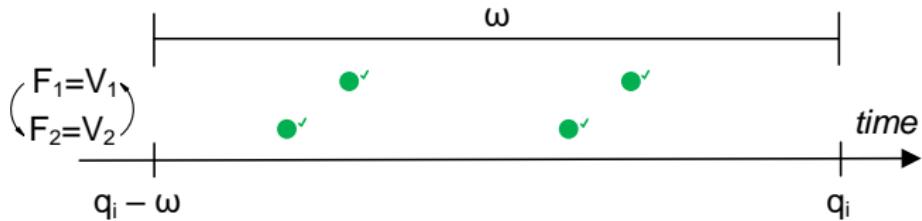


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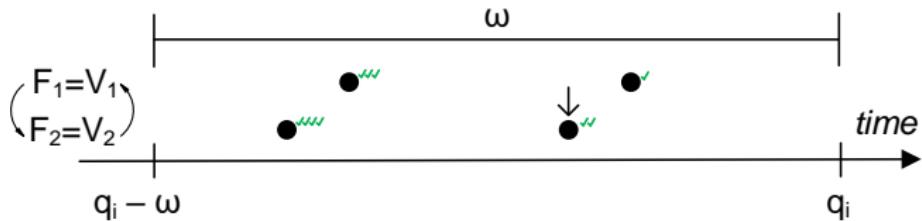


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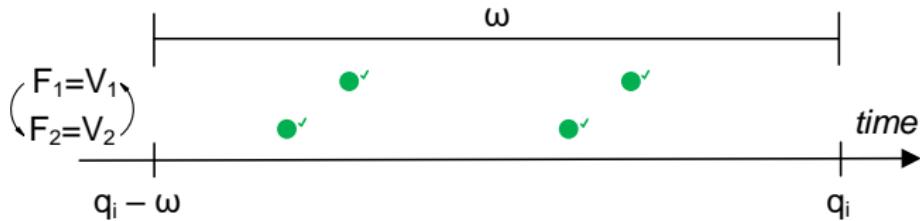


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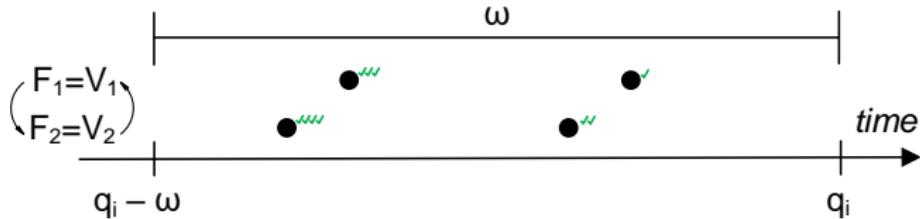


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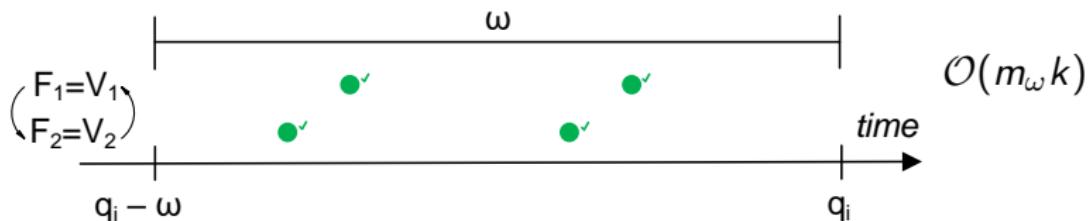


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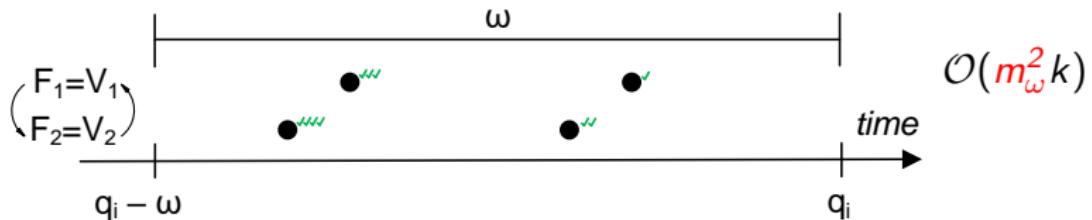


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## Experimental Setup

### Multi-Agent Systems: Voting & NetBill

- Compute, e.g., normative positions of agents.

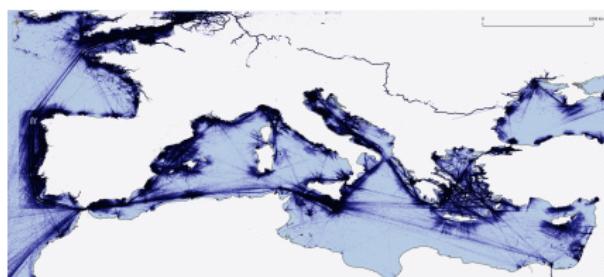
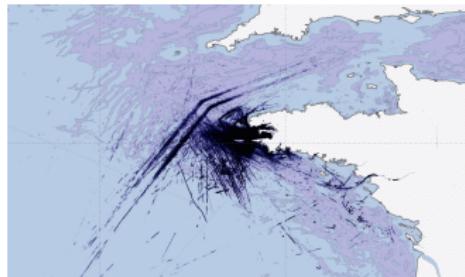
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## Maritime Situational Awareness

- Recognise dangerous, illegal and suspicious vessel activity.



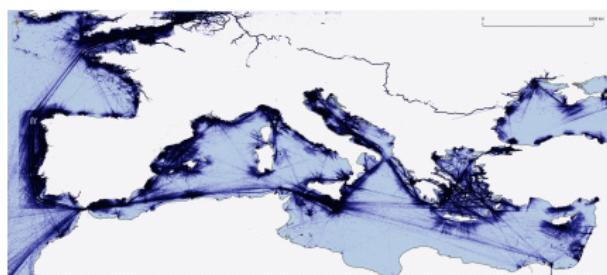
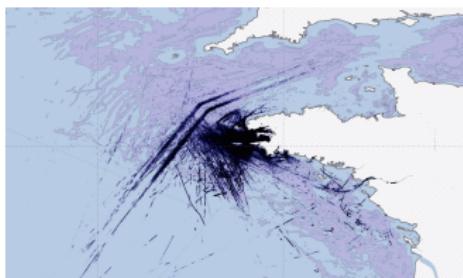
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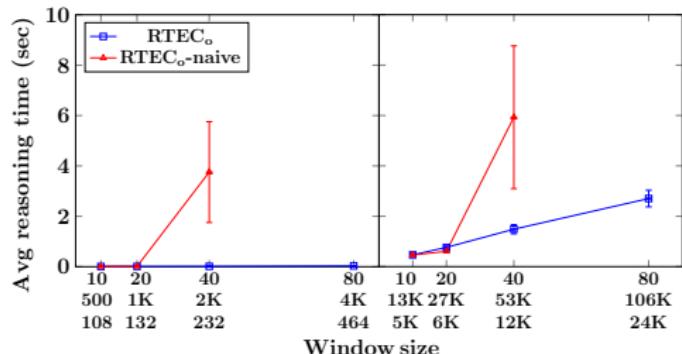


## Code, Data & Temporal Specifications

<https://github.com/aartikis/RTEC>

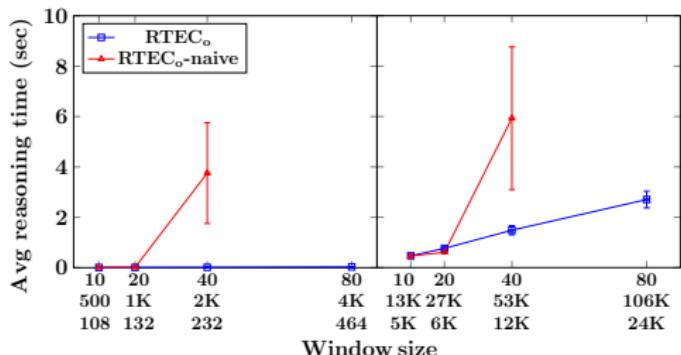
# Experimental Results

## Voting & NetBill

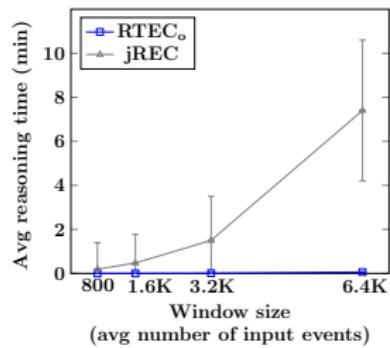


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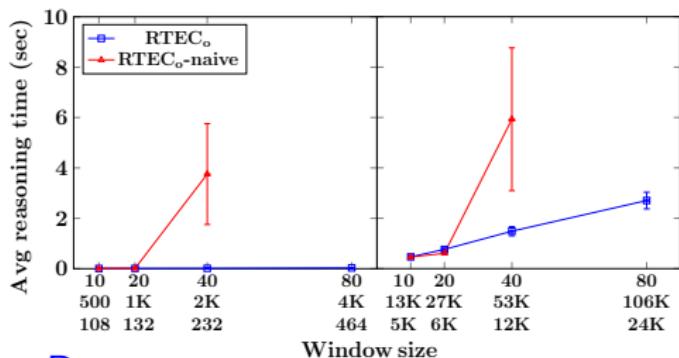


## Voting: *status* fluent

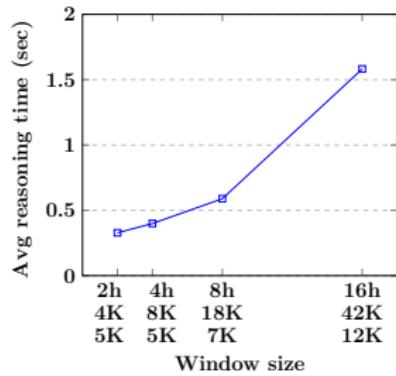


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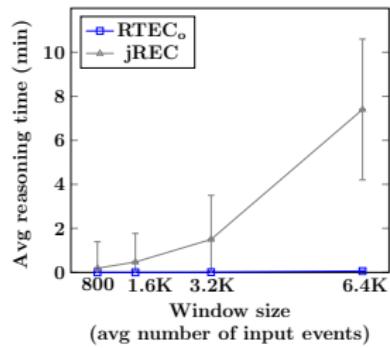
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Brest

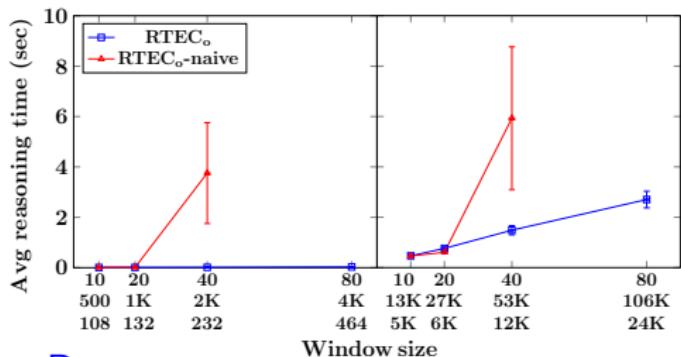


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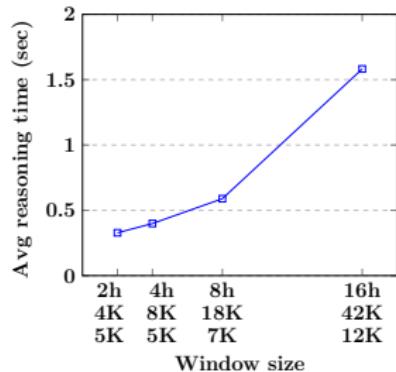


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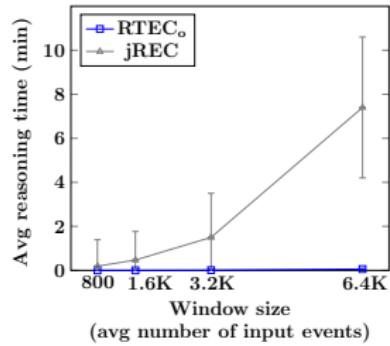
## Voting & NetBill



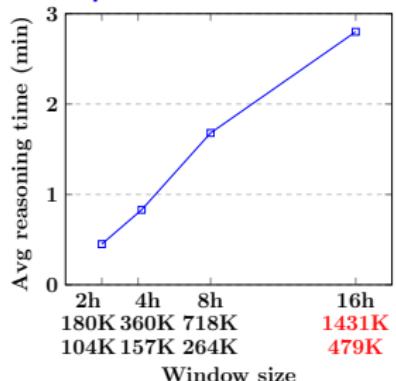
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## European seas



## Summary & Further Work

### RTEC<sub>o</sub>

- A formal, open-source stream reasoning system
- Efficient treatment of *cyclic dependencies*
- Locally stratified specifications
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### Resources

<https://cer.iit.demokritos.gr/>

Thank you!