

**EXPERIMENT III CIRCUIT ANALYSIS TECHNIQUES, PRACTICAL SUPPLIES and MAXIMUM POWER TRANSFER**

**EQUIPMENT LIST:**

DC Power Supply

Multimeter

Resistors (100Ω, 2 x 1kΩ, 2.2kΩ, 3.3kΩ, 6.8kΩ, 8.2kΩ, 1k pot)

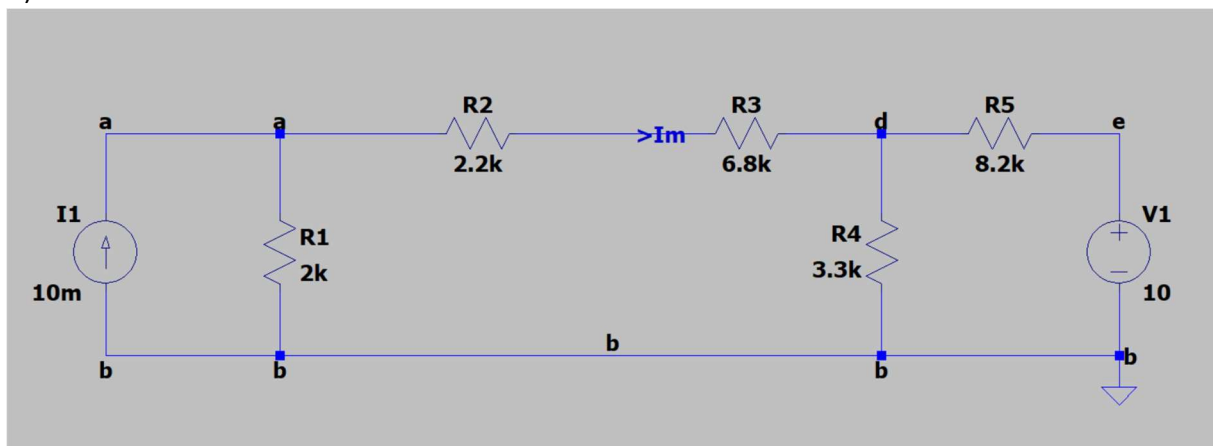
**PRELIMINARY WORK:**

**Introduction:**

In this prework we will study the nodal analysis in circuits, Thevenin and Norton Equivalents, practical(real) sources and maximum power transfer.

QUESTION 1. Node voltage, Thevenin and Norton transformation techniques:

A)



Applying KLC at node a we get:

$$-I_1 + (V_a/R_1) + [(V_a - V_d)/(R_2 + R_3)] = 0$$

$$10\text{mA} = (V_a/2) + (V_a - V_d)/9$$

$$10\text{mA} = (9V_a + 2V_a - 2V_d)/18$$

$$10\text{mA} \cdot 18 = 180\text{A} = 11V_a - 2V_d$$

Applying KLC at node d we get:

$$[(V_a - V_d)/R_2 + R_3] + [(V_1 - V_d)/R_5] - V_d/R_4 = 0$$

$$V_d/3.3 = (V_a - V_d)/9 + (10 - V_d)/8.2$$

$$73.8V_d = (27.06V_a - 27.06V_d) + (297 - 29.7V_d)$$

$$130.56V_d - 27.06V_a = 297$$

By solving the 2 equations:

$$130.56V_d - 27.06V_a = 297$$

$$11V_a - 2V_d = 180 \rightarrow 718.08V_a - 130.56V_d = 11750.4$$

$$691.02V_a = 12047.4$$

$$V_a = 17.43 \text{ V}$$

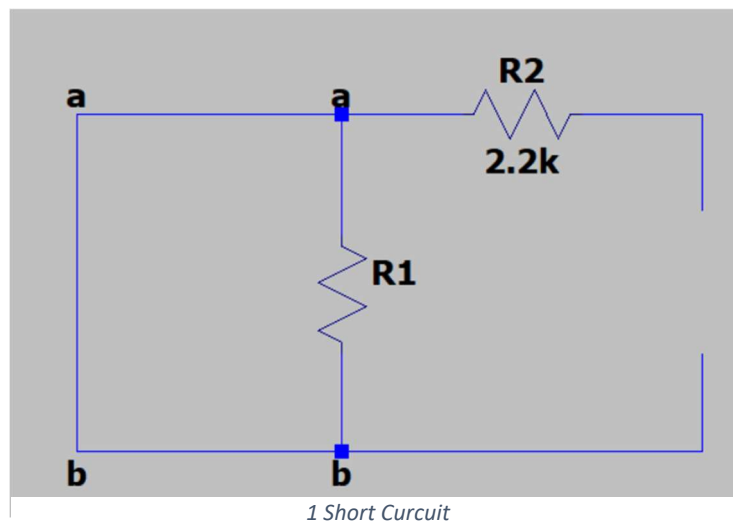
By putting  $V_a$  in the first equation:  $V_d = 5.865 \text{ V}$

$$\text{Then } I_m = (V_a - V_d) / (R_2 + R_3)$$

$$I_m = (17.43 - 5.865) / 9 = 11.565 / 9 = 1.285 \text{ A}$$

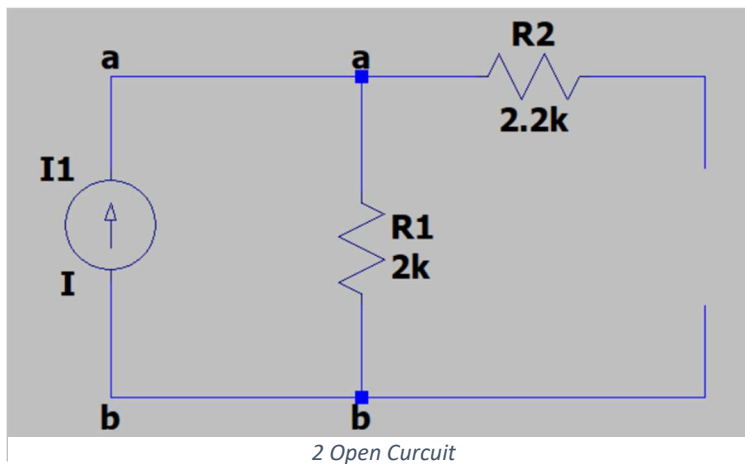
$$V_m = V_a - I_m * R_2 = 17.43 - (2.2 * 1.285) = 14.603 \text{ V}$$

**B)** To derive the thevenin equivalent for the portion of the circuit to the left of  $v_m$  terminals we need  $R_{th}$  and  $V_{th}$ .



By killing the source and making the circuit as a short circuit we found the  $R_{eq}$ :

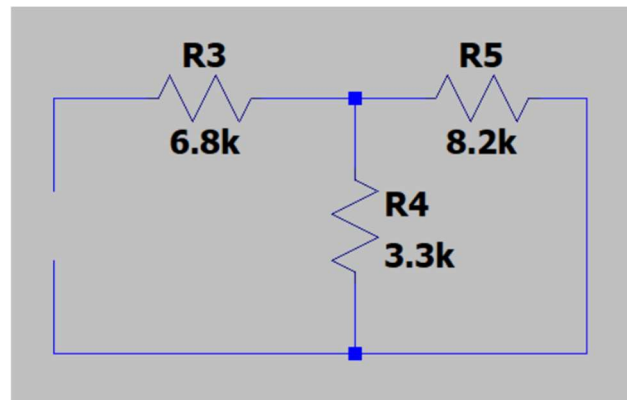
$$R_{eq} = 2.2 \text{ k}\Omega = R_{th}$$



By making the circuit as an open circuit we found the  $V_{th}$ :

$$V_{th} = I_1 * R_1 = 10 \text{ mA} * 2 \text{ k}\Omega = 20 \text{ V}$$

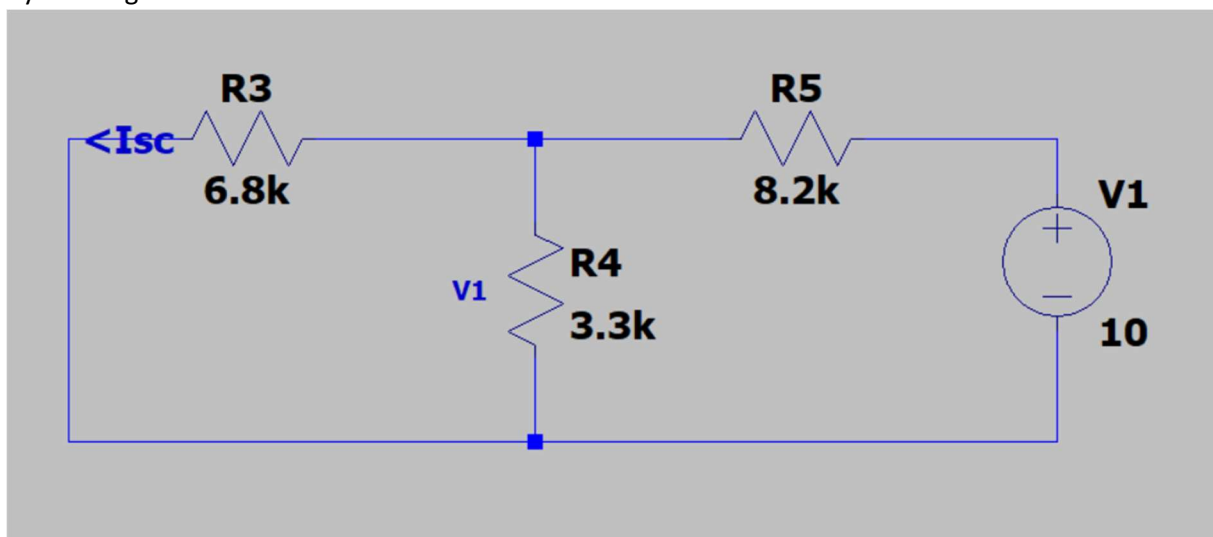
**C)** To derive the Norton equivalent  $I_n$  for the portion of the circuit that is to the right of  $v_m$  terminals we need  $R_n$  and  $I_n$ .



By killing the source we found  $R_n$ :

$$R_n = R_3 + (R_5 \parallel R_4) = 6.8 + \left[ \frac{(8.2 \times 3.3)}{(8.2 + 3.3)} \right] = 6.8 + 2.35 = 9.15 \text{ k}\Omega$$

By creating a short circuit:



$$R_{eq} = (R_3 \parallel R_4) + R_5 = \left[ \frac{(6.8 \times 3.3)}{(6.8 + 3.3)} \right] + 8.2 = 2.22 + 8.2 = 10.42$$

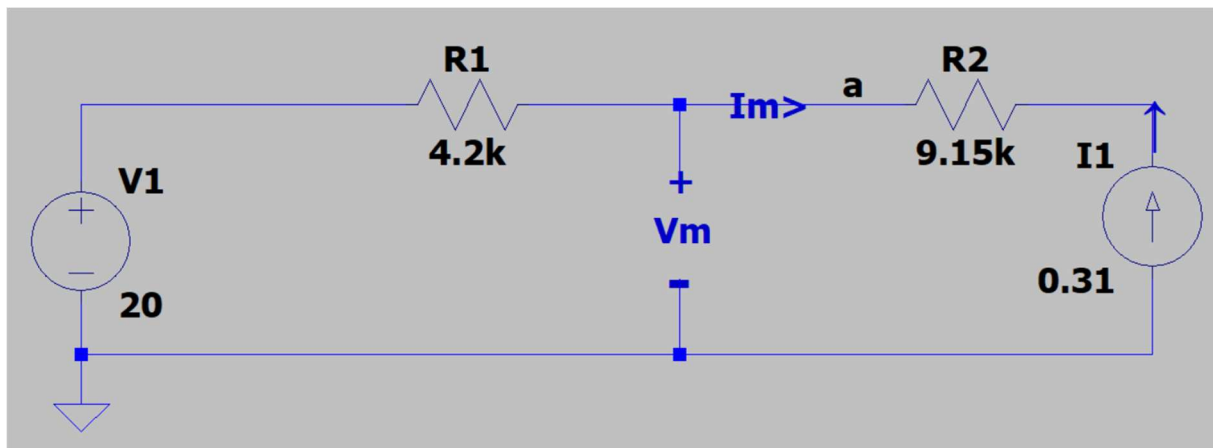
$$V = I \cdot R_{eq} \rightarrow 10 = I \cdot 10.42$$

$$I = 0.96 \text{ A}$$

$$I_{sc} = I_n = I \cdot \frac{3.3}{(6.8 + 3.3)} = (0.96) \cdot \frac{(3.3)}{(10.1)} = 0.31 \text{ A}$$

$$R_{th} = V_{oc} / I_{sc} = 20 / 0.31 = 64.5$$

D)



E)

$$V_1 = 20 \text{ V}$$

$$V = I * R ; V = 0.31 * 9.15 = 2.84 \text{ V (for right side)}$$

$$I_m = (V_1 - 2.84) / R_1 = (20 - 2.84) / 4.2 = 1.29 \text{ A}$$

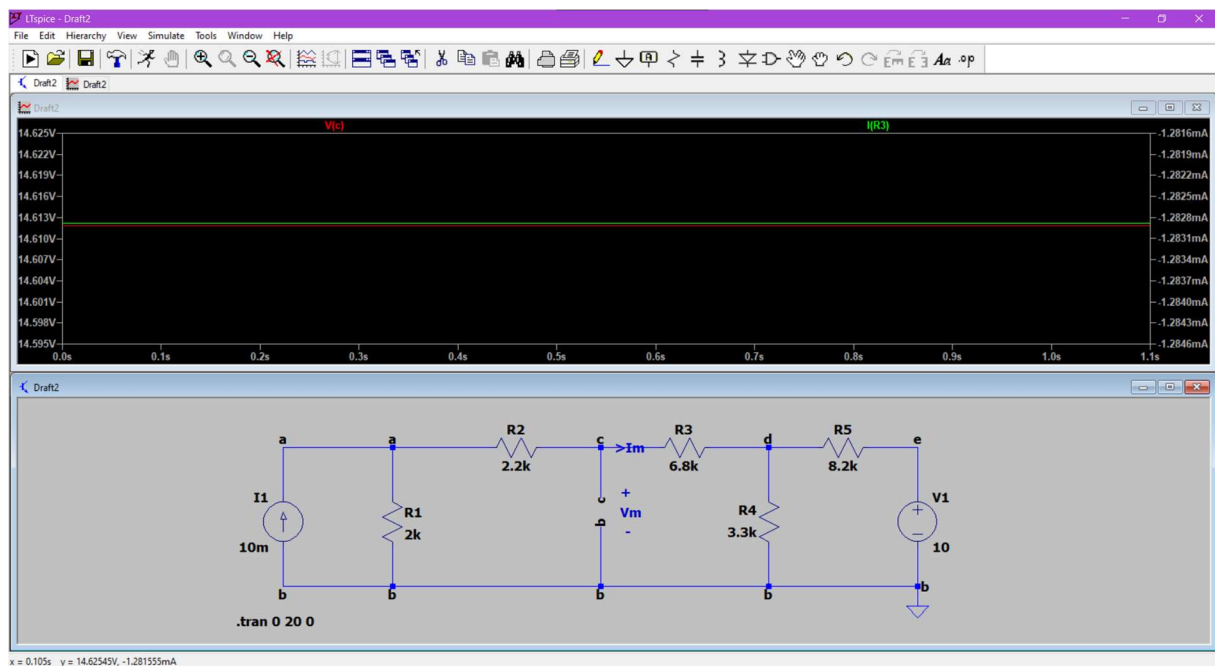
$$\text{For } V_m: (20 - V_m) / 4.2 = 1.29$$

$$20 - V_m = 1.29 * 4.2$$

$$V_m = 14.582 \text{ V}$$

These values are consistent with the values we found at (a). We simplify the circuit by applying Thevenin and Norton transformation techniques and calculate the unknowns. Since we didn't change the circuit the founded values didn't change at the end.

F)



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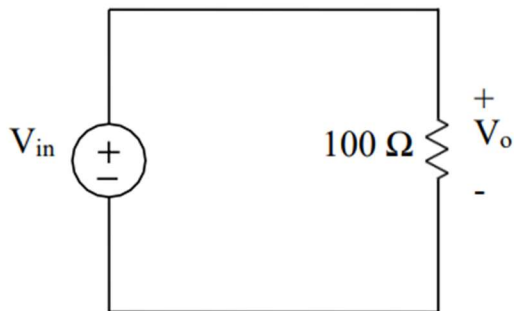
--- Operating Point ---

V(a) :      17.4342      voltage
V(c) :      14.6119      voltage
V(d) :       5.88825     voltage
V(n001) :    10         voltage
I(I1) :      0.01        device_current
I(R1) :      0.00871711  device_current
I(R2) :     -0.00128289  device_current
I(R3) :     -0.00128289  device_current
I(R4) :     -0.00178432  device_current
I(R5) :     -0.000501433 device_current
I(V1) :     -0.000501433 device_current

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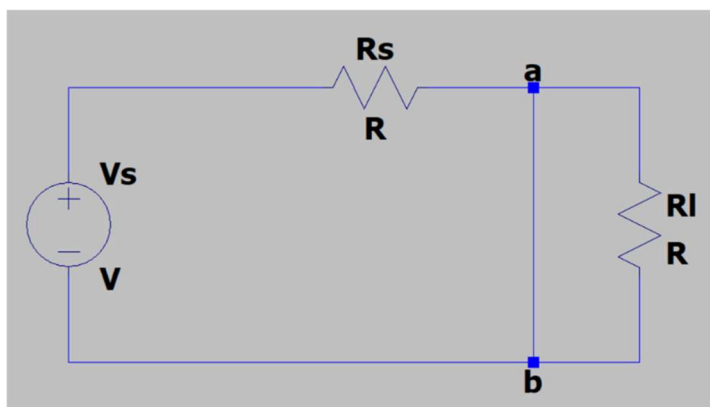
QUESTION 2. Real (practical) power supplies and maximum power transfer

A)

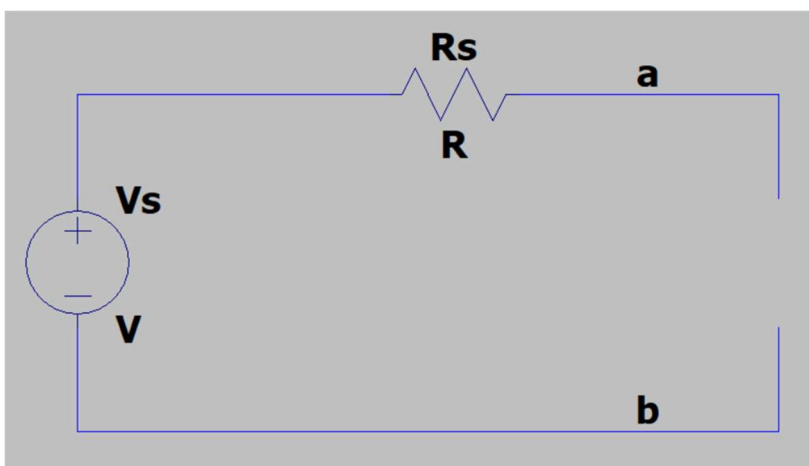


No,  $V_{in}$  and  $V_o$  don't have same value. Because in reality there are always resistive drops due to voltage resistance and cable resistance.

**B)** When a-b connected with a wire, we create a short circuit. And by the information we know that the current measured between node a and b is 50 mA. This value is equal to  $I_s$ .



When  $R_L$  is disconnected from the circuit we create an open-circuit. And by the information we know that between a and b the voltage is 5V. This voltage equal to  $V_s$ . Therefore  $V_s = 5V$



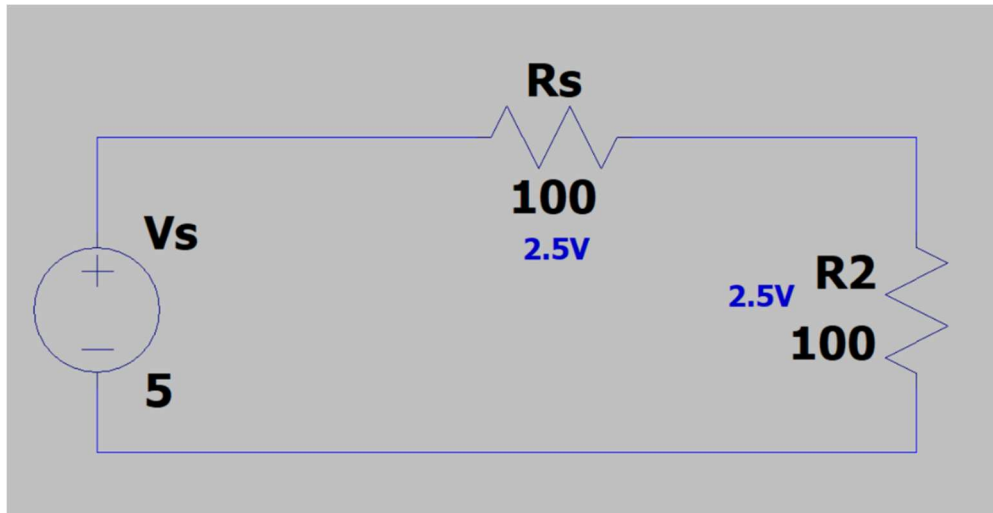
Also,  $R_s = V_s / I_s = 5 / 0.05 = 100\ \text{ohm}$

B)

When max power transfered:  $R(\text{Load}) = R_s$ , therefore

$R(\text{Load}) = 100 \text{ ohm}$

c)

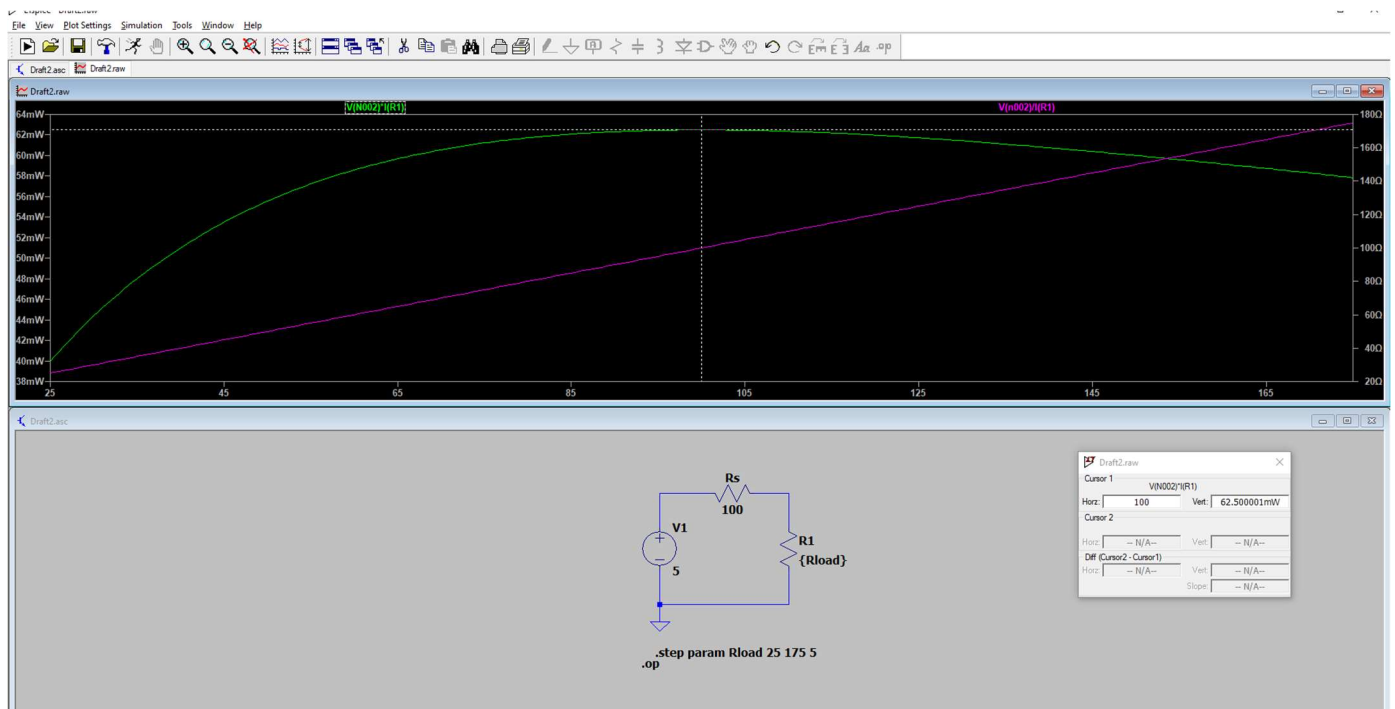


$$V = I * R$$

$$5 = I * (100 + 100)$$

$$P = [(2.5)^2] / 100 = 0.0625 \text{ W}$$

D)



**Conclusion:**

We studied the nodal analysis in circuits and find the unknown values by KVL and KCL equations for each reference nodes.

We used Thevenin and Norton Equivalents to simplify the circuit and calculate the same unknowns by KVL and KCL. They initially have the same values because the circuit remains the same.

We studied the differences between practical and theoretical sources and understand that with the same circuit the values differentiate due to voltage resistance and cable resistance.

We used LTSpice to find when circuit uses max. power.