Running head: TITLE

The title

Karolina Muszyńska  $^1~\&~XXX^2$ 

<sup>1</sup> University of Warsaw, Faculty of Psychology

<sup>2</sup> Stanford University

Author Note

- Add complete departmental affiliations for each author here. Each new line herein
- 7 must be indented, like this line.
- Enter author note here.

2

5

- The authors made the following contributions. Karolina Muszyńska:
- 10 Conceptualization, Writing Original Draft Preparation, Writing Review & Editing;
- 11 XXX: Writing Review & Editing, Supervision.
- 12 Correspondence concerning this article should be addressed to Karolina Muszyńska,
- University of Warsaw, Faculty of Psychology, ul. Stefana Banacha 2D, 02-097 Warsaw,
- Poland. E-mail: karolina.muszynska@psych.uw.edu.pl

Abstract

One or two sentences providing a basic introduction to the field, comprehensible to a scientist in any discipline. Two to three sentences of more detailed background, comprehensible to scientists in related disciplines. One sentence clearly stating the general problem being addressed by this particular study. One sentence summarizing the main result (with the words "here we show" or their equivalent). Two or three sentences explaining what the main result reveals in direct comparison to what was thought to be the case previously, or how the main result adds to previous knowledge. One or two sentences to put the results into a more general context. Two or three sentences to provide a broader perspective, readily comprehensible to a scientist in any discipline.

25 Keywords: keywords

26 Word count: X

The title 27 Methods 28 (to paste from google doc) 29 **Participants** (to paste from google doc) Mention the bilinguals and multilinguals 31 Material (to paste from google doc) 33 Procedure (to paste from google doc) 35 Data analysis Results 37 Psychometric properties of the two CAT-CDIs Our first aim was to examine whether CAT-CDIs in American English and Polish 39 demonstrate comparable psychometric properties. To that end, we revisit the psychometric properties reported for the American English CAT-CDI (word production) in Kachergis et 41 al. (2022) and compare those to the data from Polish CAT-CDI (Words and Sentences). We found similarly strong correlations in the two languages between the abilities 43 estimated from CDI-CAT and full CDI scores (American English and Polish: r = .86), the

abilities estimated from the CDI-CAT and abilities estimated from full CDI (American

- English and Polish: r = .92), and the abilities estimated from the full CDI and the full
- <sup>47</sup> CDI scores (American English: r = .95, Polish: r = 0.94). The abilities estimated from the
- 48 CDI-CAT and the full CDI scores were also strongly correlated within individual age
- 49 groups (see Table 2).

Table 1

American English: Correlations between ability estimated by CAT-CDI and ability estimated from full CDI by children's age

	[15,18)	[18,21)	[21,24)	[24,27)	[27,30)	[30,33)	[33,36]
r ability CAT vs full CDI	0.95	0.85	0.82	0.83	0.59	0.84	0.86
N	26	22	26	30	28	24	48

Table 2

Polish: Correlations between ability estimated by CAT-CDI and ability estimated from full CDI by children's age

	[18,21)	[21,24)	[24,27)	[27,30)	[30,33)	[33,36]
r ability CAT vs full CDI	0.8	0.94	0.91	0.89	0.95	NA
N	29	22	16	23	22	1

- The Polish validation study included 28 data from bi- and multilingual families.
- Though it is a small group, we decided to explore their correlation coefficients
- 52 (non-parametric Spearman's rho) and found these were similar to those found for Polish
- monolingual children (see Table 3 in Supplementary Materials).

Table 3
Supplementary Material: Table S1 - Spearman's correlations for monolingual and multilingual children in the Polish dataset

lang_group	r	n	correlation
monolingual	0.92	85	Ability from CDI-CAT $\sim$ full CDI score
multilingual	0.90	28	Ability from CDI-CAT $\sim$ full CDI score
monolingual	0.92	85	Ability from CDI-CAT $\sim$ ability from full CDI
multilingual	0.90	28	Ability from CDI-CAT $\sim$ ability from full CDI
monolingual	1.00	85	Ability from full CDI $\sim$ full CDI score
multilingual	1.00	28	Ability from full CDI $\sim$ full CDI score

We also looked at the mean squared error between the abilities as estimated by 54 CAT-CDI and from the full CDI. The mean squared error in English was 0.55 (Mdn =0.17, SD = 1), and in Polish it was 0.19 (Mdn = 0.08, SD = 0.45). We also looked at the children for whom the estimates from the CAT-CDI and full CDI diverged extremely, i.e. their difference between the errors was 1.5 SD from the mean. There were 15 such cases (7.35%) in the English dataset and 4 cases (1.96%) in the Polish dataset. All participants in both datasets showed higher ability estimates on the CDI-CAT compared to the full CDI. If the full CDI is considered the baseline, this suggests that parents may have overestimated their child's vocabulary on the CDI-CAT, potentially responding "yes – produces" to more items than expected based on full CDI estimates (as suggested by Kachergis, et al. 2022). An alternative explanation is that, for these participants, the full CDI may have underestimated the child's true ability. Notably, all Polish participants with large discrepancies completed the full CDI in unusually short times (their completion times were among the shortest 5% in the sample) suggesting their responses may have been 67 rushed or less attentive. This could have led to lower ability estimates from the full CDI.

<sup>69</sup> Supporting this interpretation, their CDI-CAT scores had acceptable measurement errors

- 70 (below or equal to 0.1 for Polish), indicating reliable ability estimation by the CDI-CAT, in
- contrast to the full CDI. However, this pattern did not appear in the English dataset,
- $^{72}$  where only 2 participants who showed extreme discrepancy also showed very short
- <sup>73</sup> administrations of the full CDI.

Table 4

Table 4										TITLE
production	sex_full	age_full	order	fullTheta	fullTheta_SE	catTheta	catTheta_SE	sq_err	full_cat_diff	extreme_discre
97.00	Female	27.00	full_first	-0.14	0.04	1.20	0.17	1.81	-1.34	yes
8.00	Male	17.00	cat_first	-1.58	0.16	-0.23	0.16	1.82	-1.35	yes
158.00	Male	35.00	$full_first$	0.14	0.04	1.62	0.16	2.17	-1.47	yes
0.00	Male	34.00	$full_first$	-2.90	0.43	-1.48	0.38	2.01	-1.42	yes
132.00	Female	21.00	cat_first	0.02	0.04	1.75	0.17	2.99	-1.73	yes
165.00	Male	20.00	full_first	0.18	0.04	1.48	0.17	1.71	-1.31	yes
47.00	Female	28.00	$full_first$	-0.57	90.0	1.86	0.17	5.90	-2.43	yes
14.00	Male	20.00	$full\_first$	-1.27	0.12	0.01	0.16	1.64	-1.28	yes
124.00	Female	28.00	$\operatorname{cat}$ _first	0.00	0.04	1.30	0.17	1.68	-1.30	yes
210.00	Female	26.00	$\operatorname{cat}$ _first	0.33	0.03	1.85	0.17	2.31	-1.52	yes
5.00	Female	26.00	$\operatorname{cat}$ _first	-1.79	0.19	-0.42	0.19	1.87	-1.37	yes
177.00	Male	28.00	$full_first$	0.22	0.03	1.62	0.18	1.98	-1.41	yes
470.00	Male	36.00	$full\_first$	1.14	0.03	2.82	0.35	2.83	-1.68	yes
253.00	Male	35.00	cat_first	0.48	0.03	1.83	0.16	1.83	-1.35	yes
287.00	Male	23.00	full_first	0.58	0.03	1.91	0.16	1.78	-1.33	yes

We also re-calculated the mean squared error without the cases of extreme discrepancy, which yielded a MSE of 0.44 (Mdn = 0.29, SD = 0.44) in English and MSE of 0.12 (Mdn = 0.07, SD = 0.14) in Polish.

## 7 Item properties in the two CAT-CDIs

Our second aim was to analyze similarities and differences in IRT item properties and item selection in CAT in English and Polish.

There are 679 items in the English CAT-CDI and 666 items in the Polish CAT-CDI. 80 For both sets of items, the items' difficulty and discrimination parameters were calculated 81 using IRT 2 parameter model (these included separate samples, see Kachergis et al. 2022) 82 and Krajewski et al. (in preparation)). An item's difficulty indicates the ability level at 83 which there is a 50% probability that a participant will respond correctly. It includes negative and positive values, with 0 indicating medium difficulty, thus reflecting the range 85 of values of ability, i.e. theta. An item's discrimination indicates how well it distinguishes between individuals with slightly different ability levels—especially those near that difficulty 87 point. Of these two parameters, item difficulty is of greater interest to the present paper as 88 it is directly linked to ability and as discrimination power is more about how good the item is at measuring, rather than what it is measuring.

English items are more difficult than the Polish items,  $\Delta M = -1.87, 95\%$  CI [-2.06, -1.69], t(1227.61) = -20.09, p < .001 (English: min = -7.16, max = 4.45, M = -2.19, Mdn = -2.21, SD = 1.98; Polish: min = -4.34, max = 4.41, M = -0.32, Mdn = -0.43, SD = 1.41). Notably, this was true even for a subset of 390 items common to both languages - these items still proved to be more difficult in English than in Polish:  $M_D = -1.68, 95\%$  CI [-1.82, -1.54], t(389) = -23.11, p < .001. This difference in mean difficulty may be influenced by the characteristics of the samples used to estimate the IRT models. In English, item difficulty was calculated based on a broader sample of children

aged 12–36 months (spanning the CDI:WG, CDI:WS, and CDI-III), whereas the Polish data came from a sample of narrower age range of 18–36 months, corresponding to the CDI:WS. As a result, item difficulty in English was estimated using a relatively younger sample, for whom certain items may have been more challenging—thus appearing more difficult—compared to the older Polish sample. Still the item difficulty for common items in the two languages was positively and moderately correlated: r = .65, 95% CI [.58, .70], t(388) = 16.68, p < .001.

Table 5

category_pl	rho	n
quantifiers	0.11	10
clothing	0.22	19
connecting_words	0.23	8
locations	0.31	6
pronouns_demonstrative	0.32	4
places	0.32	7
vehicles	0.45	9
furniture_rooms	0.47	17
action_words	0.50	75
body_parts	0.52	17
prepositions	0.55	10
games_routines	0.57	12
time_words	0.57	8
household	0.57	30
outside	0.58	20
sounds	0.60	6
$food\_drink$	0.61	39
descriptive_words (adjectives)	0.62	19
people	0.67	16
animals	0.68	29
toys	0.74	15
descriptive_words (adverbs)	0.80	4
question_words	0.91	10

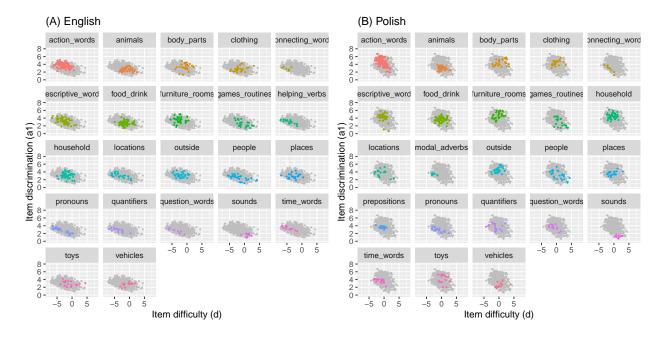


Figure 1. The relative positioning of the items by semantic category (colored) plotted in the context of the full item pool (grey): (A) English, (B) Polish.

We also wanted to do check whether items in particular CDI semantic categories 106 show related parameter values across the two languages. We performed a series of 107 Spearman's rank correlations (on the items common to CDI-CATs in Polish and English) 108 for each CDI semantic category (see Table @ref(tab:d by cdi category tab)). The rank 109 correlations coefficients vary by category, but for half of the categories the correlations are 110 moderate to strong (0.52 to 0.91). Figure 1 shows the relative positioning of the items by 111 semantic category (colored) plotted in the context of the full item pool (grey) in the two 112 languages. It can be seen from the figure that many categories (e.g., sounds) show a similar 113 distribution of items relative to the whole item pool across Polish and English.

## 15 Item selection in the two CAT-CDIs

It is to be expected that a CDI-CAT will not need to administer all the items in the item bank. In fact, in the validation study the English CAT-CDI used 251 items (36.91%) and similarly, the Polish CAT-CDI used 258 items (38.74%). Figure 2 shows how often a

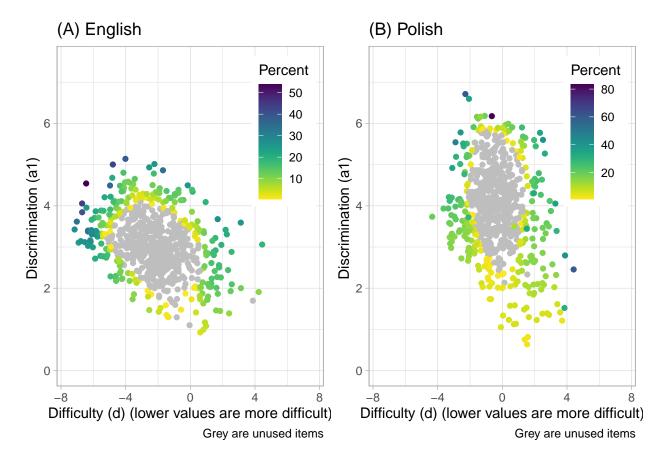


Figure 2. How often a given item was used in CAT-CDI administrations in the validation study in (A) English and (B) Polish. The items (points) are colored by the percentage of their appearance in the CAT-CDI administrations. Items colored in grey are items never used in any of the CAT-CDI administrations.

given item was used in CAT-CDI administrations in the validation study in English and
Polish. By design, a CDI-CAT selects items that are most informative for each participant.
This means it draws from a subset of available items—typically those matched to the
participant's current ability estimate in terms of difficulty, and with high discrimination,
meaning they effectively distinguish between individuals with abilities close to that
estimate.

Discussion

1. Correlations strong in both languages (overall and in age-bins; in PL: multi and mono correlations similar and strong).

- 2. MSE after removing cases with extreme discrepancies.
- 3. Extreme discrepancies mixed results?

128

References

```
<sup>131</sup> Auguie, B. (2017). gridExtra: Miscellaneous functions for "grid" graphics. Retrieved from
```

- https://CRAN.R-project.org/package=gridExtra
- <sup>133</sup> Aust, F., & Barth, M. (2024). papaja: Prepare reproducible APA journal articles with R
- 134 Markdown. https://doi.org/10.32614/CRAN.package.papaja
- Barth, M. (2023). tinylabels: Lightweight variable labels. Retrieved from
- 136 https://cran.r-project.org/package=tinylabels
- <sup>137</sup> Chalmers, R. P. (2012). mirt: A multidimensional item response theory package for the R
- environment. Journal of Statistical Software, 48(6), 1–29.
- https://doi.org/10.18637/jss.v048.i06
- <sup>140</sup> Chalmers, R. P. (2016). Generating adaptive and non-adaptive test interfaces for
- multidimensional item response theory applications. Journal of Statistical Software,
- 71(5), 1–39. https://doi.org/10.18637/jss.v071.i05
- Chang, W., Cheng, J., Allaire, J., Sievert, C., Schloerke, B., Xie, Y., ... Borges, B. (2024).
- Shiny: Web application framework for r. Retrieved from
- https://CRAN.R-project.org/package=shiny
- Garnier, Simon, Ross, Noam, Rudis, Robert, ... Cédric. (2023). viridis(Lite) -
- colorblind-friendly color maps for r. https://doi.org/10.5281/zenodo.4678327
- Garnier, Simon, Ross, Noam, Rudis, Robert, ... Cédric. (2024). viridis(Lite) -
- colorblind-friendly color maps for r. https://doi.org/10.5281/zenodo.4679423
- Grolemund, G., & Wickham, H. (2011). Dates and times made easy with lubridate.
- Journal of Statistical Software, 40(3), 1–25. Retrieved from
- https://www.jstatsoft.org/v40/i03/
- Kassambara, A. (2023). Ggpubr: 'ggplot2' based publication ready plots. Retrieved from
- https://CRAN.R-project.org/package=ggpubr
- 155 Krajewski, G. (2025). Multilada: MultiLADA's little helpers. Retrieved from
- https://github.com/gkrajewski/Multilada

- Müller, K. (2020). Here: A simpler way to find your files. Retrieved from
- https://CRAN.R-project.org/package=here
- <sup>159</sup> Müller, K., & Wickham, H. (2025). Tibble: Simple data frames. Retrieved from
- https://CRAN.R-project.org/package=tibble
- R Core Team. (2025). R: A language and environment for statistical computing. Vienna,
- Austria: R Foundation for Statistical Computing. Retrieved from
- https://www.R-project.org/
- Sarkar, D. (2008). Lattice: Multivariate data visualization with r. New York: Springer.
- Retrieved from http://lmdvr.r-forge.r-project.org
- Slowikowski, K. (2024). Ggrepel: Automatically position non-overlapping text labels with
- 'ggplot2'. Retrieved from https://CRAN.R-project.org/package=ggrepel
- Wickham, H. (2016). ggplot2: Elegant graphics for data analysis. Springer-Verlag New
- York. Retrieved from https://ggplot2.tidyverse.org
- Wickham, H. (2023a). Forcats: Tools for working with categorical variables (factors).
- Retrieved from https://CRAN.R-project.org/package=forcats
- Wickham, H. (2023b). Stringr: Simple, consistent wrappers for common string operations.
- 173 Retrieved from https://CRAN.R-project.org/package=stringr
- Wickham, H., Averick, M., Bryan, J., Chang, W., McGowan, L. D., François, R., ...
- Yutani, H. (2019). Welcome to the tidyverse. Journal of Open Source Software, 4(43),
- 1686. https://doi.org/10.21105/joss.01686
- Wickham, H., François, R., Henry, L., Müller, K., & Vaughan, D. (2023). Dplyr: A
- grammar of data manipulation. Retrieved from
- https://CRAN.R-project.org/package=dplyr
- Wickham, H., & Henry, L. (2025). Purrr: Functional programming tools. Retrieved from
- https://CRAN.R-project.org/package=purrr
- Wickham, H., Hester, J., & Bryan, J. (2024). Readr: Read rectangular text data. Retrieved
- from https://CRAN.R-project.org/package=readr

Wickham, H., Vaughan, D., & Girlich, M. (2024). *Tidyr: Tidy messy data*. Retrieved from https://CRAN.R-project.org/package=tidyr

R (Version 4.4.3; R Core Team, 2025) and the R-packages dplyr (Version 1.1.4; 186 Wickham, François, Henry, Müller, & Vaughan, 2023), forcats (Version 1.0.0; Wickham, 187 2023a), ggplot2 (Version 3.5.2; Wickham, 2016), ggpubr (Version 0.6.0; Kassambara, 2023), 188 ggrepel (Version 0.9.6; Slowikowski, 2024), gridExtra (Version 2.3; Auguie, 2017), here 189 (Version 1.0.1; Müller, 2020), lattice (Version 0.22.7; Sarkar, 2008), lubridate (Version 1.9.4; 190 Grolemund & Wickham, 2011), mirt (Version 1.44.0; Chalmers, 2012, 2016), mirtCAT 191 (Version 1.14; Chalmers, 2016), Multilada (Version 0.7.0; Krajewski, 2025), papaja (Version 192 0.1.3; Aust & Barth, 2024), purr (Version 1.0.4; Wickham & Henry, 2025), readr (Version 193 2.1.5; Wickham, Hester, & Bryan, 2024), shiny (Version 1.10.0; Chang et al., 2024), stringr 194 (Version 1.5.1; Wickham, 2023b), tibble (Version 3.3.0; Müller & Wickham, 2025), tidyr 195 (Version 1.3.1; Wickham, Vaughan, & Girlich, 2024), tidyverse (Version 2.0.0; Wickham et 196 al., 2019), tinylabels (Version 0.2.5; Barth, 2023), viridis (Garnier et al., 2023; Version 197 0.6.5; Garnier et al., 2024) and viridisLite (Version 0.4.2; Garnier et al., 2023) 198