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Author Note

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12 Abstract

Abstract here

14 Keywords: keywords

Word count: X

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17 Methods

# 18 Participants

In the American English validation study, the participants were 204 parents of 19 children aged 15 to 36 months (M = 26.21, Mdn = 26, SD = 6.37). There were 103 girls in 20 the sample (50.49%). The sample was ethnically diverse, including White, Black, 21 Latino/Hispanic, Asian, Native American, and other races/ethnicities. None of the children 22 were reported to hear other languages apart from English. The average number of years of education attained by the primary caregiver was 15.82 (SD = 2.27). In the Polish validation study, the participants were 113 parents of children aged 18 25 to 34 months (M = 24.73, Mdn = 24, SD = 4.47). There were 49 girls in the sample 26 (43.36%). The sample was White (reflecting the limited ethnic diversity within the Polish population). However, there were 28 children multilingual with Polish (as their home language) and some other (majority) language. [todo: add info on parental edu]. Notably, the two validation samples differed slightly (but significantly) in mean age, 30  $\Delta M = -1.49, 95\%$  CI [-2.69, -0.28], t(297.82) = -2.42, p = .016, which may affect the 31 outcomes of direct comparisons between them, as age could be a contributing factor. We 32 present one such comparison-standard error of CAT ability-where this difference is 33 explicitly indicated. NOTE: You can also view/comment on this on GitHub Issue #7 linked here.

#### 36 Materials

The data was gathered with CAT-CDIs in American English and Polish. The
American English CAT-CDI was created from the items that were common to three CDIs:
Words and Gestures, Words and Sentences and CDI-III. With these items, two CAT-CDIs

were created, one for word production and another for word comprehension (see Kachergis et al. 2022 for more details). The Polish CAT-CDIs were created following a largely similar procedure as the ones in American English, but there was a separate CDI-CAT developed for each CDI version (CDI: Words and Gestures and CDI: Words and Sentences) and for each CDI:WG subscale (word production, word comprehension, gesture use) (Krajewski et al. in preparation). Here we show data from the validation study of American English CAT-CDI word production (i.e. 679 items) and Polish CAT-CDI version of WS: Words and Sentences (i.e. 666 items). There are 395 words that appear in both CDI-CAT language versions.

#### 49 Procedure

Though in both validation studies the parents were asked to fill in both the full CDI and the CAT-CDI, the procedure differed between the two validation studies. In the validation of American English CDI-CAT, parents were given both CDIs in one sitting, but the order of the CDI versions was counterbalanced. In the Polish validation study, the order of the CDIs was fixed, with the full CDI always first, and then, after 1–30 days (M = 8.31, Mdn = 8, SD = 4.90) parents were asked to fill in the CAT-CDI. Both studies were done fully online and obtained the approval of adequate ethics committees.

57 Results

## Psychometric properties of the two CAT-CDIs

Our first aim was to examine whether CAT-CDIs in American English and Polish
demonstrate comparable psychometric properties. To that end, we revisit the psychometric
properties reported for the American English CAT-CDI (word production) in Kachergis et
al. (2022) and compare those to the data from Polish CAT-CDI (Words and Sentences).

We found similarly strong correlations in the two languages between the abilities estimated from CDI-CAT and full CDI scores (American English and Polish: r=.86), the abilities estimated from the CDI-CAT and abilities estimated from full CDI (American English and Polish: r=.92), and the abilities estimated from the full CDI and the full CDI scores (American English: r=.95, Polish: r=0.94). The abilities estimated from the CDI-CAT and the full CDI scores were also strongly correlated within individual age

Table 1

American English: Correlations between ability estimated by CAT-CDI and ability estimated from full CDI by children's age

groups (see Table 2).

	[15,18)	[18,21)	[21,24)	[24,27)	[27,30)	[30,33)	[33,36]
r ability CAT vs full CDI	0.95	0.85	0.82	0.83	0.59	0.84	0.86
N	26	22	26	30	28	24	48

Table 2

Polish: Correlations between ability estimated by CAT-CDI and ability estimated from full CDI by children's age

	[18,21)	[21,24)	[24,27)	[27,30)	[30,33)	[33,36]
r ability CAT vs full CDI	0.8	0.94	0.91	0.89	0.95	NA
N	29	22	16	23	22	1

The Polish validation study included 28 data from bi- and multilingual families.

<sup>71</sup> Though it is a small group, we decided to explore their correlation coefficients

<sup>(</sup>non-parametric Spearman's rho) and found these were similar to those found for Polish

monolingual children (see Table 3 in Supplementary Materials). *NOTE*: Here is an Issue for commenting on Supplementary Materials.

Table 3
Supplementary Material: Table S1 - Spearman's correlations for monolingual and multilingual children in the Polish dataset

lang_group	r	n	correlation
monolingual	0.92	85	Ability from CDI-CAT $\sim$ full CDI score
multilingual	0.90	28	Ability from CDI-CAT $\sim$ full CDI score
monolingual	0.92	85	Ability from CDI-CAT $\sim$ ability from full CDI
multilingual	0.90	28	Ability from CDI-CAT $\sim$ ability from full CDI
monolingual	1.00	85	Ability from full CDI $\sim$ full CDI score
multilingual	1.00	28	Ability from full CDI $\sim$ full CDI score

We also looked at the mean squared error between the abilities as estimated by 75 CAT-CDI and from the full CDI. The mean squared error in English was 0.55 (Mdn = 0.17, SD = 1), and in Polish it was 0.19 (Mdn = 0.08, SD = 0.45). We then zoomed in on 77 children for whom the estimates from the CAT-CDI and full CDI diverged extremely, i.e. their difference between the errors was 1.5 SD from the mean. There were 15 such cases (7.35%) in the English dataset and 4 cases (1.96%) in the Polish dataset. All participants in both datasets showed higher ability estimates on the CDI-CAT compared to the full 81 CDI. If the full CDI is considered the baseline, this suggests that parents may have overestimated their child's vocabulary on the CDI-CAT, potentially responding "yes – produces" to more items than expected based on full CDI estimates (as suggested by Kachergis, et al. 2022). An alternative explanation is that, for these participants, the full CDI may have underestimated the child's true ability. Notably, all Polish participants with large discrepancies completed the full CDI in unusually short times (their completion times

were among the shortest 5% in the sample) suggesting their responses may have been rushed or less attentive. This could have led to lower ability estimates from the full CDI and larger discrepancies between estimates from full and CAT CDI. Supporting this interpretation, their CDI-CAT scores had acceptable measurement errors (below or equal to 0.1 for Polish), indicating reliable ability estimation by the CDI-CAT, in contrast to the full CDI. This was partially true for the American sample - though only 2 participants had similarly short full CDIs, all but two showed relatively low measurement errors (more on measurement error in Section XX).

We also re-calculated the mean squared error without the cases of extreme discrepancy, which yielded a MSE of 0.44 (Mdn = 0.29, SD = 0.44) in English and MSE of 0.12 (Mdn = 0.07, SD = 0.14) in Polish.

### 99 Item properties in the two CAT-CDIs

Our second aim was to analyze similarities and differences in IRT item properties and item selection in CAT in English and Polish.

There are 679 items in the English CAT-CDI and 666 items in the Polish CAT-CDI. 102 For both sets of items, the items' difficulty and discrimination parameters were calculated 103 using IRT 2 parameter model (these included separate samples, see Kachergis et al. 2022) 104 and Krajewski et al. (in preparation)). An item's difficulty indicates the ability level at 105 which there is a 50% probability that a participant will respond correctly. NOTE: See 106 GitHub Issue 1. It is on the same scale as ability with negative values indicating difficult items, values around 0 indicating medium difficulty, and positive values indicating easy items. An item's discrimination indicates how well it distinguishes between individuals 109 with slightly different ability levels—especially those near that difficulty point. Of these two 110 parameters, item difficulty is of greater interest to the present paper as it is directly linked 111 to ability and as discrimination power is more about how good the item is at measuring, 112

rather than what it is measuring.

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English items are more difficult than the Polish items, \Delta M = -1.87, 95\% CI
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   [-2.06, -1.69], t(1227.61) = -20.09, p < .001 (English: min = -7.16, max = 4.45, M = -20.09, p < .001)
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   -2.19, Mdn = -2.21, SD = 1.98; Polish: min = -4.34, max = 4.41, M = -0.32, Mdn = -0.43,
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    SD = 1.41). Notably, this was true even for a subset of 390 items common to both
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   languages - these items still proved to be more difficult in English than in Polish:
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   M_D = -1.68, 95\% CI [-1.82, -1.54], t(389) = -23.11, p < .001. This difference in mean
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   difficulty may be influenced by the characteristics of the samples used to estimate the IRT
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   models. In English, item difficulty was calculated based on a broader sample of children
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   aged 12–36 months (spanning the CDI:WG, CDI:WS, and CDI-III), whereas the Polish
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   data came from a sample of narrower age range of 18–36 months, corresponding to the
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    CDI:WS. As a result, item difficulty in English was estimated using a relatively younger
   sample, for whom certain items may have been more challenging—thus appearing more
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   difficult—compared to the older Polish sample. Still the item difficulty for common items
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   in the two languages was positively and moderately correlated: r = .65, 95\% CI [.58, .70],
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   t(388) = 16.68, p < .001.
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Table 4

category_pl	rho	n
quantifiers	0.11	10
clothing	0.22	19
connecting_words	0.23	8
locations	0.31	6
$pronouns\_demonstrative$	0.32	4
places	0.32	7
vehicles	0.45	9
$furniture\_rooms$	0.47	17
action_words	0.50	75
body_parts	0.52	17
prepositions	0.55	10
games_routines	0.57	12
time_words	0.57	8
household	0.57	30
outside	0.58	20
sounds	0.60	6
food_drink	0.61	39
descriptive_words (adjectives)	0.62	19
people	0.67	16
animals	0.68	29
toys	0.74	15
descriptive_words (adverbs)	0.80	4
question_words	0.91	10

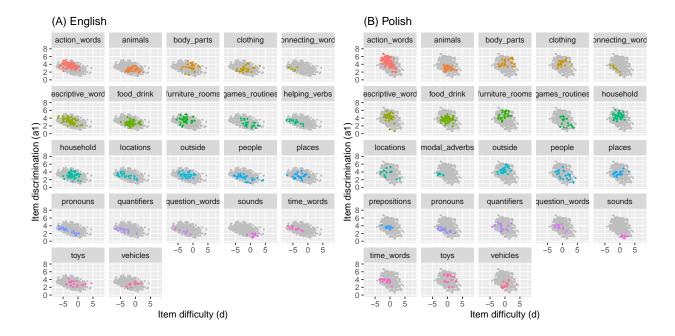


Figure 1. The relative positioning of the items by semantic category (colored) plotted in the context of the full item pool (grey): (A) English, (B) Polish.

We also wanted to do check whether items in particular CDI semantic categories show 129 related difficulty values across the two languages. We performed a series of Spearman's 130 rank correlations (on the difficulty of items common to CDI-CATs in Polish and English) 131 for each CDI semantic category (see Table @ref(tab:d by cdi category tab)). The rank 132 correlations coefficients vary by category, but for half of the categories the correlations are 133 moderate to strong (0.52 to 0.91). Figure 1 shows the relative positioning of the items by 134 semantic category (colored) plotted in the context of the full item pool (grey) in the two 135 languages. It can be seen from the figure that many categories (e.g., sounds) show a similar 136 distribution of items relative to the whole item pool across Polish and English. 137

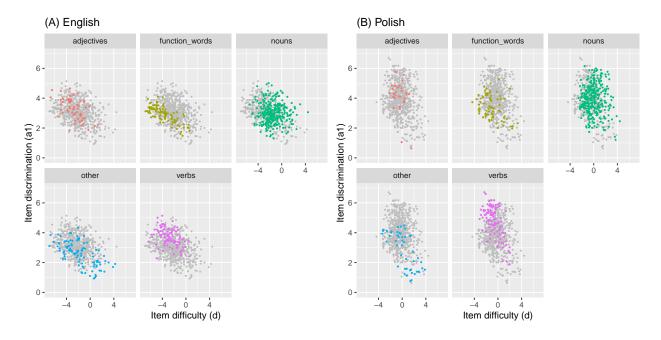


Figure 2. The relative positioning of the items by lexical class (colored) plotted in the context of the full item pool (grey): (A) English, (B) Polish.

Table 5

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lexical class en	rho	n
function_words	0.40	50
verbs	0.49	71
adjectives	0.53	25
nouns	0.59	194
other	0.75	50

Last, we investigated whether particular lexical categories show related difficulty values across the two languages. Again, we performed a series of Spearman's rank correlations (on the difficulty of items common to CDI-CATs in Polish and English) for each lexical class (see Table @ref(tab:d\_by\_lexical\_class\_tab), Figure 2). The lowest

correlation was for function words (0.40), then verbs (0.47), adjectives (0.53), nouns (0.6), other, i.e. mostly sounds and words relating to routines (e.g. "hello", "yes", "thank you") and time (e.g. "tommorow", "day") (0.75).

#### 145 Item selection in the two CAT-CDIs

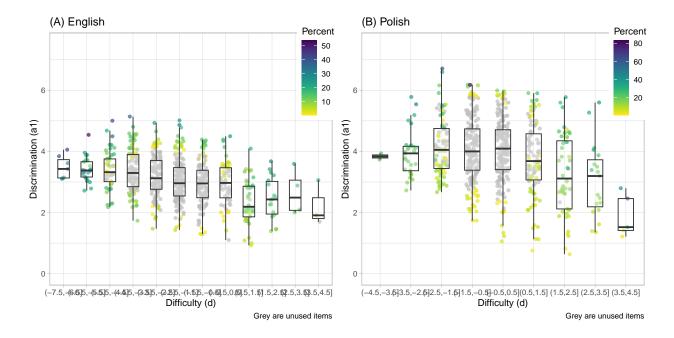


Figure 3. How often a given item was used in CAT-CDI administrations in the validation study in (A) English and (B) Polish. The items (points) are colored by the percentage of their appearance in the CAT-CDI administrations. Items colored in grey are items never used in any of the CAT-CDI administrations.

It is to be expected that a CDI-CAT will not need to administer all the items in the item bank. In fact, in the validation study the English CAT-CDI used 251 items (36.91%) and similarly, the Polish CAT-CDI used 258 items (38.74%). By design, a CDI-CAT selects items that are most informative for each participant. This means it draws from a subset of available items—typically those matched to the participant's current ability estimate in terms of difficulty, and with high discrimination, meaning they effectively distinguish between individuals with abilities close to that estimate. Figure 3 plots the items by their

difficulty and discrimination parameters and colors the items (points) by how often they 153 were used in CAT-CDI administrations in English and Polish. A few findings are of note 154 here. First, both CAT-CDIs used items of very low discrimination (i.e, items that do no 155 discriminate well between ability levels). Often that was because for a given difficulty level 156 there were not enough items and CAT-CDI had to use all the items available (this is 157 particularly true of the items on the two ends of difficulty). However, more surprisingly, it 158 is also true of items of medium difficulty, where items of higher discrimination were 159 available (but were not chosen by the CAT algorithm). NOTE: See Issue 2 here. 160

Finally, some items keep being shown in many CAT administrations. In English, 3 161 items appear in more than half of administrations - "long" in 64% of administrations, 162 "make" in 54% of administrations, and "last" in 53% of administrations. They are also 163 high discrimination items in their difficulty bins. "Long" is additionally one of the starting 164 items, i.e. a first item shown to the parent, chosen so that there is high probability the 165 parent can respond positively. In Polish, 3 items appear in more than half of 166 administrations - "szukać" (to look for) appearing in 83% of administrations, "znaleźć" (to 167 find) appearing in 61% of administrations, and "babcia" (grandmother) appearing in 60% 168 of administrations. All three items show very high discrimination. "Szukać" (to look for) and "znaleźć" (to find) are also in top 5 discrimination items in general. "Babcia" (grandmother) is one of the starting items. 171

To check whether the CDI items common in both languages may show similar frequencies in CAT-CDI administrations, we ran Spearman's rank correlation and found that the items frequencies in administrations were weakly correlated,  $r_{\rm s}=.37$ ,  $S=6,420,909.29,\ p<.001$ . However, the two CAT-CDIs differed in their potential length, as the English CAT-CDI was set to administer 25–50 items and the Polish CAT-CDI could administer up to 75 items (no minimum was set, but in practice the minimum items administered were 13). As an item is more likely to appear in longer tests (simply due to test length), then frequency of the Polish items could be inflated. *NOTE*:Could it be that,

as an item is more likely to appear in longer tests (simply due to test length), frequency of 180 the Polish items could be inflated? Could it influence the item's rank? I could probably 181 recalculate item frequency not per total number of administrations, but per total number 182 of items administered? SEE ISSUE #3 183

One of the key metrics for CAT-CDI's usefulness is whether it can shorten the CDI

#### CAT-CDIs' usefullness in research and practice 184

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administration compared to the full CDI, but still obtain a reliable estimate of child's lexical ability. We have found that CAT-CDIs were significantly shorter to administer: the 187 English CAT-CDI median time was 342s (~5.7 minutes) (median full CDI time was 1466s 188  $(\sim 24.43 \text{ minutes})$ ) and the Polish CAT-CDI median time was 117s  $(\sim 1.95 \text{ minutes})$  (median 189 full CDI time was 1240s (~20.67 minutes)). Even though the CAT-CDI in Polish seemed shorter (compared to English CAT-CDI), the number of items administered in the two 191 language versions of CAT-CDI was comparable: English M=31.42, Mdn=25 (25–50 192 items), Polish M = 34.71, Mdn = 23 (13–75 items). 193 The two CAT-CDIs differed in their settings as to when to finish the administration. 194 Specifically, the Polish CAT-CDI was set so that the SEM as low as 0.1 be reached (with as 195 few items as possible), and if the SEM could not be lowered to or below 0.1, the CAT-CDI 196 stopped after administering a maximum of 75 items. The English CAT-CDI on the other 197 hand was set to administer a maximum of 50 items, but the administration could be 198 stopped earlier if the SEM of 0.15 or lower was reached. In other words, the Polish CAT-CDI prioritized as low SEM as possible, while the English CAT-CDI prioritized shorter test length. This difference resulted in slightly lower mean SEM in Polish CAT-CDI, compared to English CAT-CDI  $\Delta M = 0.06, 95\%$  CI [0.05, 0.07], 202 t(257.25) = 11.36, p < .001 but comparable mean number of items administered, 203  $\Delta M = -3.29, 95\%$  CI [-7.74, 1.16], t(137.00) = -1.46, p = .147. However, it should be 204 noted that the Polish and American validation samples differed slightly in age

 $\Delta M = -1.49, 95\%$  CI [-2.69, -0.28], t(297.82) = -2.42, p = .016, and as age is weakly correlated with SEM (r = .18, 95% CI [.04, .31], t(202) = 2.60, p = .010), this slight difference in age could feed the SEM difference in the two validation samples. *NOTE*: We could consider matching kids from the two samples one-to-one on age, to even out this potential effect of age difference on SEM, see Issue #8.

In both CAT-CDIs, we have been able to reliably estimate lexical ability for majority of children. Taking as the cut-off Makransky's suggestion to consider a SEM below 0.2 as acceptable, so defined reliable CAT estimate was gathered for 96.5 of the American participants, and 92.6 of the Polish participants. The remaining participants, i.e. those with higher standard errors of measurement (in other words, lower reliability of ability estimates) were typically those at the extremes of the ability scale—children with either relatively low or relatively high lexical skills (see Figure 4).

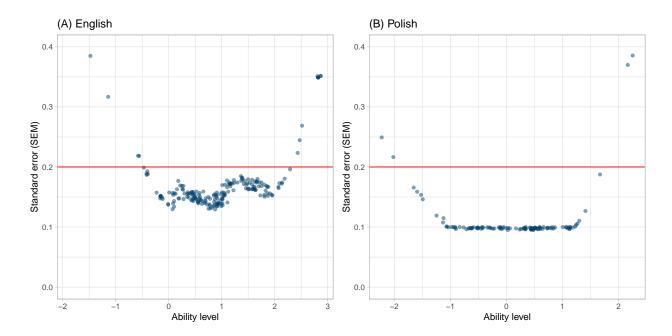


Figure 4. Standard Error of Measurement (SEM) by ability estimate in (A) English and (B) Polish. The red line marks the SE of 0.2.

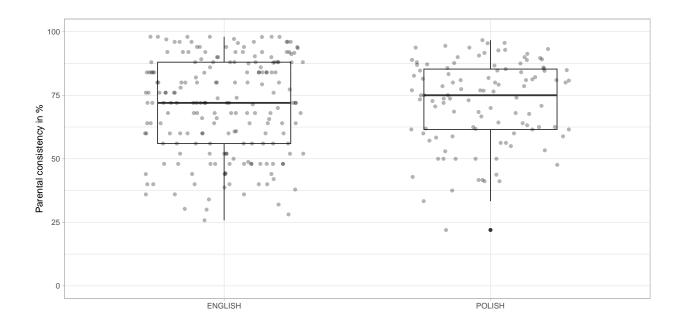


Figure 5. Percentage of parents' consistency in responding to items in the two CDI versions in the same way (in the English and in the Polish dataset).

### Parental consistency in responses

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We compared the parental consistency in their responses in the full and CAT version of CDI in two ways - using a percentage of agreement and by calculating Cohen's Kappa, which additionally factors in chance agreement. When calculating the percentage agreement, for each parent we calculated the number of items to which they responded in the same way in both CDI versions against the whole number of items asked in both CDI versions. We found though the Median consistency was relatively high: 72% for English and 75% for Polish, it varied largely across parents in both samples (see Figure 5).

We also calculated Cohen's kappa per each parent, considering their observed agreement (between responses to the same items in full and CAT CDI) and expected agreement by chance. The kappa values indicated fair (or close to fair) agreement: English M=0.40, Mdn=0.37, Polish M=0.39, Mdn=0.34. NOTE: There's an Issue for that here

Discussion 231

In points for now:

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1. Strong correlations with full CDI.

The CAT-CDIs were strongly correlated with the full CDI versions in both languages, 234 which supports the overall validity of the CAT approach. These correlations held for 235 both monolingual and multilingual participants. However, the Polish sample was 236 small, so further research is needed—and planned—to confirm these findings. 237

2. Cases of extreme divergence.

CAT-CDI scores diverged notably from full CDI estimates for only a small number of children in both language groups. In the Polish sample all divergent cases had low SEM, and their full CDIs were unusually short—maybe the full form underestimated their ability? In the English sample, their full CDIs were not very short, but SEM was relatively low, which is good.

3. Item paramteres across languages.

Item parameters (i.e., difficulty and discrimination) showed moderate correlations across languages. These likely stem from variations in the calibration samples. Still, some semantic categories showed consistent patterns across languages, suggesting underlying structural similarities in lexical development.

4. Item selection.

Each CAT version used c.a. half of the full CDI item pool. Few items were overused 250 (mostly those with highest discrimination in the item pool or starting items). But we also saw items being chosen for CAT that wouldn't be considered very informative 252 (i.e., of low discrimination). That's something to explore further, I wrote to Phil 253 Chalmers (author of mirt and mirtCAT), maybe he'll be able to help? 254

5. Efficiency and Reliability.

CAT-CDIs were significantly shorter than the full CDIs while maintaining high reliability for most children. The few less reliable estimates were for children at the ends of the ability range (children with either very low or very high lexical skills). Comparing Polish and English samples, the ability ranges with low SEM differed (see Figure 3) - this again might be a result of the calibration samples and item parameters? This is a good place to stress the importance of well-balanced, diverse calibration datasets. Also, while the CAT-CDI is efficient and useful for screening or initial identification ("pomiar przesiewowy" in Polish), it may be less suited for diagnostic purposes where high precision is needed across the full ability range.

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