# CAS 741: Module Interface Specification

Dynamical Systems: Multi-Pendulum Simulation

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# 1 Revision History

Date	Version	Notes
November 26, 2018	1.0	First full draft for submission

# 2 Symbols, Abbreviations and Acronyms

See SRS Documentation at CAS-741-Pendula SRS [give url —SS] [Also add any additional symbols, abbreviations or acronyms —SS] The symbols are listed in alphabetical order.

symbol	description
A	Assumption
DD	Data Definition
GD	General Definition
GS	Goal Statement
IM	Instance Model
LC	Likely Change
NF	Non-Functional Requirement
MIS	Module Interface Specification
PS	Physical System Description
R	Requirement
SRS	Software Requirements Specification
Τ	Theoretical Model

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# 3 Introduction

The following document details the Module Interface Specifications for the Multi-Pendulum Simulation project [Fill in your project name and description —SS]

Complementary documents include the System Requirement Specifications and Module Guide. The full documentation and implementation can be found at:

https://github.com/karolserkis/CAS-741-Pendula. [provide the url for your repo —SS]

# 4 Notation

[You should describe your notation. You can use what is below as a starting point. —SS]

The structure of the MIS for modules comes from ?[HoffmanAndStrooper1995 —SS], with the addition that template modules have been adapted from ?[GhezziEtAl2003 —SS]. The mathematical notation comes from Chapter 3 of ?[HoffmanAndStrooper1995 —SS]. For instance, the symbol := is used for a multiple assignment statement and conditional rules follow the form  $(c_1 \Rightarrow r_1|c_2 \Rightarrow r_2|...|c_n \Rightarrow r_n)$ .

(Karol) I am also using this link for now.

The following table summarizes the primitive data types used by Multi-Pendulum Simulation and the symbols used in this document. The choice of symbols was made to be consistent with calculus, ordinary differentials (ODE), the Lagrangian, kinematics etc. The standard mathematical spaces are used (e.g.  $\mathbb{N}$ ,  $\mathbb{Z}$ ,  $\mathbb{R}$ , etc.)

Data Type	Notation	Description
character	char	a single symbol or digit
integer	$\mathbb{Z}$	a number without a fractional component in $(-\infty, \infty)$
natural number	N	a number without a fractional component in $[1, \infty)$
real	$\mathbb{R}$	any number in $(-\infty, \infty)$

The specification of Multi-Pendulum Simulation uses some derived data types: sequences, strings, and tuples. Sequences are lists filled with elements of the same data type. Strings are sequences of characters. Tuples contain a list of values, potentially of different types. In addition, Multi-Pendulum Simulation uses functions, which are defined by the data types of their inputs and outputs. Local functions are described by giving their type signature followed by their specification.

# 5 Module Decomposition

The following table is taken directly from the Module Guide document for this project.

Level 1	Level 2
Hardware-Hiding	
	Multi-Pendulum Simulation Control Module
	Multi-Pendulum Simulation GUI Module
	User Input Parameters Module
Behaviour-Hiding	Data Structure Module
	Generic Trajectory Simulation GUI Module
Software Decision	Generic GUI/Plot Module
	Lagrangian Module
	Hamiltonian Module

Table 1: Module Hierarchy

# 6 MIS of Multi-Pendulum Simulation Control Module (M2)

[You can reference SRS labels, such as R??.—SS]
[It is also possible to use LATEX for hypperlinks to external documents.—SS]

Execution flow of Multi-Pendulum Simulation . Calls the different modules in the appropriate order. The general steps of the module are:

- 1. Read in and verify mps\_input.
- 2. Calculate Lagrangian module, iterate over the whole time frame (use data structure).
- 3. Calculate Hamiltonian module, iterate over the whole time frame (use data structure).
- 4. Generate a Plot and Poincaré map
- 5. Return the trajectory plot output as per the output/simulation module specifications.

# 6.1 Module

mps\_control

# 6.2 Uses

```
mps_gui (M3, Section 7)
mps_input (M4, Section 8)
```

Processing modules:

```
mps_lagrang (M5, Section 9), mps_hamil (M6, Section 10)
mps_datastruct (M7, Section 11)
generic_plot (M8, Section 12), mps_trajplotsim (M9, Section 13)
```

# 6.3 Syntax

# 6.3.1 Exported Constants

None

# 6.3.2 Exported Access Programs

Name	In	Out	Exceptions
run_mps	int, str	None	None

# 6.4 Semantics

The Multi-Pendulum Simulation is designed to have the input and initialization controlled by the user directly through the GUI. The Multi-Pendulum Simulation Control Module uses the events in the Multi-Pendulum Simulation GUI to use the processing modules in order.

# 6.4.1 State Variables

• mps\_input\_init : init (see Section 8)

• mps\_datastruct\_init : init (see Section 11)

• mps\_lagrang : calc (see Section 9)

• mps\_hamil : calc (see Section 10)

#### 6.4.2 Environment Variables

[This section is not necessary for all modules. Its purpose is to capture when the module has external interaction with the environment, such as for a device driver, screen interface, keyboard, file, etc. —SS]

# 6.4.3 Assumptions

[Try to minimize assumptions and anticipate programmer errors via exceptions, but for practical purposes assumptions are sometimes appropriate. —SS]

#### 6.4.4 Access Routine Semantics

run\_mps(mps\_input):

- transition: The Multi Pendulum Simulation is initialized and the data structure through the modules for calculation (Lagrangian & Hamilonian). The result is then passed to the plot/simulation/output modules.
- output: None [if appropriate —SS]
- exception: None [if appropriate—SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[As appropriate—SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope.—SS]

# 7 MIS of Multi-Pendulum Simulation GUI (M3)

```
[Use labels for cross-referencing —SS]
[You can reference SRS labels, such as R??. —SS]
[It is also possible to use LATEX for hypperlinks to external documents. —SS]
```

Methods to interact with user to make run Multi-Pendulum Simulation . Serves as interface between the user and the software through the hardware by outputting calculation results and collecting user information (user inputs) for the calculation modules.

# 7.1 Module

mps\_gui

# 7.2 Uses

mps\_datastruct (M7, Section 11) generic\_plot (M8, Section 12), mps\_trajplotsim (M9, Section 13)

# 7.3 Syntax

# 7.3.1 Exported Constants

None

# 7.3.2 Exported Access Programs

Name	In	Out	Exceptions
mps_input	int, str	-	-
$gui\_trajsim$	-	GUI object	-
$gui\_plot$	-	GUI object (Poincaré)	-

# 7.4 Semantics

The Multi-Pendulum Simulation process flow is initialized buy user through the GUI. The user triggeres the events that start the selected processing step.

#### 7.4.1 State Variables

None

# 7.4.2 Environment Variables

Plot\_TrajSim: GUI object button\_Input: GUI object button\_TrajSim: GUI object button\_Poincaré: GUI object

[This section is not necessary for all modules. Its purpose is to capture when the module has external interaction with the environment, such as for a device driver, screen interface, keyboard, file, etc. —SS]

# 7.4.3 Assumptions

[Try to minimize assumptions and anticipate programmer errors via exceptions, but for practical purposes assumptions are sometimes appropriate. —SS]

#### 7.4.4 Access Routine Semantics

mps\_input():

- transition: Trigger mps\_input when button\_Input pressed.
- output: [if appropriate —SS]
- exception: WarnOutOfBounds (warn when mps\_input are invalid) [if appropriate—SS] gui\_trajsim():
  - transition: Trigger gui\_trajsim when button\_TrajSim pressed.
  - output: [if appropriate —SS]
  - exception: [if appropriate —SS]

gui\_plot():

- transition: Trigger gui\_plot when button\_Poincaré pressed.
- output: [if appropriate —SS]
- exception: [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[As appropriate—SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope.—SS]

# 8 MIS of User Input Module (M4)

```
[Use labels for cross-referencing —SS]
[You can reference SRS labels, such as R??. —SS]
[It is also possible to use LATEX for hypperlinks to external documents. —SS]
```

The format and structure of the input data. Loads, verifies and stores the input data into the appropriate data and object structure.

# 8.1 Module

mps\_input

# 8.2 Uses

mps\_gui (M3, Section 7) mps\_datastruct (M7, Section 11)

# 8.3 Syntax

# 8.3.1 Exported Constants

None

# 8.3.2 Exported Access Programs

Name	In	Out	Exceptions
verify_Input	int, str	-	-
$data\_struct$	int, str	-	-
$gui\_trajsim$	-	GUI object	-
$gui\_plot$	-	GUI object (Poincaré)	-

# 8.4 Semantics

# 8.4.1 State Variables

data: object

# 8.4.2 Environment Variables

Plot\_TrajSim: GUI object

[This section is not necessary for all modules. Its purpose is to capture when the module has external interaction with the environment, such as for a device driver, screen interface, keyboard, file, etc. —SS]

# 8.4.3 Assumptions

[Try to minimize assumptions and anticipate programmer errors via exceptions, but for practical purposes assumptions are sometimes appropriate. —SS]

# 8.4.4 Access Routine Semantics

verify\_Input():

- transition: [if appropriate —SS]
- output: [if appropriate —SS]
- exception: Check of int or str value out of bounds:  $(\exists \mathbb{I} : I_{\text{calc}} \notin \mathbb{R}) \& \Rightarrow \text{NotReal}$  [if appropriate —SS]

data\_struct(mps\_input):

- transition: mps\_input is the user input that is entered into the GUI. The input is used to initialize the data structure.
- output: [if appropriate —SS]
- exception: [if appropriate —SS]

gui\_trajsim(mps\_datastruct, mps\_input):

- transition: mps\_datastruct is a module that takes the mps\_input and thus the program gui\_trajsim will be prepared for the lagrangian and hamiltonian calculations done by their coresponding modules.
- output: [if appropriate —SS]
- exception: [if appropriate —SS]

gui\_plot(mps\_datastruct, mps\_input):

- transition: mps\_datastruct is a module that takes the mps\_input and thus the program gui\_plot will be prepared for the lagrangian and hamiltonian calculations done by their coresponding modules.
- output: [if appropriate —SS]

• exception: [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

#### 8.4.5 Local Functions

[As appropriate—SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope. —SS]

# 9 MIS of Lagrangian Module (M5)

```
[Use labels for cross-referencing —SS]
[You can reference SRS labels, such as R??. —SS]
[It is also possible to use LATEX for hypperlinks to external documents. —SS]
```

Lagrangian calculation/algorithm. Calculates the variation of Lagrangian for each pendulum in the chain (each element of the array).

# 9.1 Module

mps\_lagrang

# 9.2 Uses

mps\_input (M4, Section 8)

Processing modules: mps\_lagrang (M5, Section 9) mps\_datastruct (M7, Section 11)

# 9.3 Syntax

# 9.3.1 Exported Constants

None

# 9.3.2 Exported Access Programs

Name	In	Out	Exceptions
mps_input	int, str	-	_
$\operatorname{calc\_lagrang}$	int, str	long, str	-

# 9.4 Semantics

# 9.4.1 State Variables

#### 9.4.2 Environment Variables

[This section is not necessary for all modules. Its purpose is to capture when the module has external interaction with the environment, such as for a device driver, screen interface, keyboard, file, etc. —SS]

# 9.4.3 Assumptions

[Try to minimize assumptions and anticipate programmer errors via exceptions, but for practical purposes assumptions are sometimes appropriate. —SS]

# 9.4.4 Access Routine Semantics

mps\_input():

- transition: mps\_input passed to calc\_lagrang (which in turn the module utilizes mps\_datastruct).
- output: [if appropriate —SS]
- exception: WarnOutOfBounds (warn when mps\_input are invalid) [if appropriate—SS]

calc\_lagrang(mps\_input):

- transition: Utilizing the mps\_datastruct the mps\_input is calculated and passed to the gui\_trajsim and gui\_plot [if appropriate —SS]
- output: To gui\_trajsim and gui\_plot [if appropriate —SS]
- exception: WarnOutOfBounds (warn when mps\_input are invalid) [if appropriate—SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[As appropriate—SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope.—SS]

# 10 MIS of Hamiltonian Module (M6)

```
[Use labels for cross-referencing —SS]
[You can reference SRS labels, such as R??. —SS]
[It is also possible to use LATEX for hypperlinks to external documents. —SS]
```

Hamiltonian calculation/algorithm. Calculates the variation of Hamiltonian for each pendulum in the chain (each element of the array).

# 10.1 Module

 $mps\_hamil$ 

# 10.2 Uses

mps\_input (M4, Section 8)

Processing modules:

mps\_lagrang (M5, Section 9), mps\_hamil (M6, Section 10) mps\_datastruct (M7, Section 11)

# 10.3 Syntax

# 10.3.1 Exported Constants

None

# 10.3.2 Exported Access Programs

Name	In	Out	Exceptions
mps_input	int, str	-	-
calc_lagrang	int, str	long, str	-
$calc\_hamil$	long, str	long, str	-

# 10.4 Semantics

# 10.4.1 State Variables

#### 10.4.2 Environment Variables

[This section is not necessary for all modules. Its purpose is to capture when the module has external interaction with the environment, such as for a device driver, screen interface, keyboard, file, etc. —SS]

# 10.4.3 Assumptions

[Try to minimize assumptions and anticipate programmer errors via exceptions, but for practical purposes assumptions are sometimes appropriate. —SS]

#### 10.4.4 Access Routine Semantics

mps\_input():

- transition: mps\_input passed to calc\_lagrang (which in turn the module utilizes mps\_datastruct).
- output: [if appropriate —SS]
- exception: WarnOutOfBounds (warn when mps\_input are invalid) [if appropriate—SS] calc\_lagrang(mps\_input):
  - transition: Utilizing the mps\_datastruct the mps\_input is calculated and passed to the gui\_trajsim and gui\_plot [if appropriate —SS]
  - output: To gui\_trajsim and gui\_plot [if appropriate—SS]
- exception: WarnOutOfBounds (warn when mps\_input are invalid) [if appropriate—SS] calc\_hamil(mps\_input):
  - transition: Utilizing the mps\_datastruct the mps\_input is calculated and passed to the gui\_trajsim and gui\_plot [if appropriate —SS]
  - output: To gui\_trajsim and gui\_plot [if appropriate—SS]
  - exception: WarnOutOfBounds (warn when mps\_input are invalid) [if appropriate—SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[As appropriate—SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope.—SS]

# 11 MIS of Data Structure Module (M7)

```
[Use labels for cross-referencing —SS]
[You can reference SRS labels, such as R??. —SS]
[It is also possible to use LATEX for hypperlinks to external documents. —SS]
```

Data format for an image. Provides convenient format to store, read and manipulate all elements (pixel) from an image.

# 11.1 Module

mps\_datastruct

# 11.2 Uses

```
mps_gui (M3, Section 7)
mps_input (M4, Section 8)
```

Processing modules:

mps\_lagrang (M5, Section 9), mps\_hamil (M6, Section 10) mps\_datastruct (M7, Section 11)

# 11.3 Syntax

# 11.3.1 Exported Constants

None

# 11.3.2 Exported Access Programs

$\mathbf{Name}$	In	Out	Exceptions
calc_lagrang	; int, str	long, str	-
$calc\_hamil$	long, str	long, str	-
mps_gui	GUI object	-	

# 11.4 Semantics

# 11.4.1 State Variables

#### 11.4.2 Environment Variables

Plot\_TrajSim: GUI object Plot\_Poincaré: GUI object

[This section is not necessary for all modules. Its purpose is to capture when the module has external interaction with the environment, such as for a device driver, screen interface, keyboard, file, etc. —SS]

# 11.4.3 Assumptions

[Try to minimize assumptions and anticipate programmer errors via exceptions, but for practical purposes assumptions are sometimes appropriate. —SS]

# 11.4.4 Access Routine Semantics

calc\_lagrang(mps\_input):

- transition: Utilizing the mps\_datastruct the mps\_input is calculated and passed to the gui\_trajsim and gui\_plot [if appropriate —SS]
- output: To gui\_trajsim and gui\_plot [if appropriate —SS]
- exception: WarnOutOfBounds (warn when mps\_input are invalid) [if appropriate—SS] calc\_hamil(mps\_input):
  - transition: Utilizing the mps\_datastruct the mps\_input is calculated and passed to the gui\_trajsim and gui\_plot [if appropriate —SS]
  - output: To gui\_trajsim and gui\_plot [if appropriate —SS]
- exception: WarnOutOfBounds (warn when mps\_input are invalid) [if appropriate—SS] mps\_gui(mps\_datastruct, gui\_trajsim, gui\_plot):
  - transition: Utilizing the mps\_datastruct the mps\_input is calculated and passed to the gui\_trajsim and gui\_plot and thus the program gui\_trajsim will be prepared for the lagrangian and hamiltonian calculations done by their coresponding modules.
  - output: To gui\_trajsim and gui\_plot [if appropriate —SS]
  - exception: WarnOutOfBounds (warn when mps\_input are invalid) [if appropriate—SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

# 11.4.5 Local Functions

[As appropriate—SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope.—SS]

# 12 MIS of Generic GUI/Plot Module (M8)

[Use labels for cross-referencing —SS]

[You can reference SRS labels, such as R??.—SS]

It is also possible to use LaTeXfor hypperlinks to external documents. —SS

Generic methods to interact with the user. Provides the generic interface methods such as buttons, windows, plotting, entry fields to interact with a user.

# 12.1 Module

generic\_plot

# 12.2 Uses

Hardware-Hiding (M1)

# 12.3 Syntax

# 12.3.1 Exported Constants

None

# 12.3.2 Exported Access Programs

$\mathbf{Name}$	In	Out	Exceptions
gui_trajsim	GUI object	GUI object	_
gui_plot	GUI object	GUI object	_

# 12.4 Semantics

# 12.4.1 State Variables

#### 12.4.2 Environment Variables

Plot\_TrajSim: GUI object Plot\_Poincaré: GUI object

[This section is not necessary for all modules. Its purpose is to capture when the module has external interaction with the environment, such as for a device driver, screen interface, keyboard, file, etc. —SS]

# 12.4.3 Assumptions

[Try to minimize assumptions and anticipate programmer errors via exceptions, but for practical purposes assumptions are sometimes appropriate. —SS]

# 12.4.4 Access Routine Semantics

gui\_trajsim():

- transition: [if appropriate —SS]
- output: To mps\_gui(mps\_datastruct, gui\_trajsim, gui\_plot) or the generic\_plot module [if appropriate —SS]
- exception: WarnOutOfBounds (warn when gui\_trajsim are invalid) [if appropriate SS]

gui\_plot(mps\_datastruct, mps\_input):

- transition: mps\_datastruct is a module that takes the mps\_input and thus the program gui\_plot will be prepared for the lagrangian and hamiltonian calculations done by their coresponding modules.
- output: [if appropriate —SS]
- exception: [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[As appropriate—SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope.—SS]

# 13 MIS of Trajectory Simulation Module (M9)

```
[Use labels for cross-referencing —SS]
[You can reference SRS labels, such as R??. —SS]
[It is also possible to use LATEX for hypperlinks to external documents. —SS]
```

Algorithm to simulate the plot trajectory of the chain of pendula. Simulates the chain of pendula in space using the Lagrangian and the Hamiltonian.

# 13.1 Module

mps\_trajplotsim

# 13.2 Uses

```
mps_gui (M3, Section 7)
mps_input (M4, Section 8)
```

Processing modules:

mps\_lagrang (M5, Section 9), mps\_hamil (M6, Section 10)

# 13.3 Syntax

# 13.3.1 Exported Constants

None

# 13.3.2 Exported Access Programs

Name	In	Out	Exceptions
MPS_trajsii	m GUI object	GUI object	WarnOutOfBounds

# 13.4 Semantics

#### 13.4.1 State Variables

data: object

# 13.4.2 Environment Variables

Plot\_TrajSim: GUI object

[This section is not necessary for all modules. Its purpose is to capture when the module has external interaction with the environment, such as for a device driver, screen interface, keyboard, file, etc. —SS]

# 13.4.3 Assumptions

[Try to minimize assumptions and anticipate programmer errors via exceptions, but for practical purposes assumptions are sometimes appropriate. —SS]

# 13.4.4 Access Routine Semantics

MPS\_trajsim():

- transition:
  - 1. Read in and verify mps\_input.
  - 2. Calculate Lagrangian module calc\_lagrang, iterate over the whole time frame (use data structure).
  - 3. Calculate Hamiltonian module calc\_hamil, iterate over the whole time frame (use data structure).
  - 4. Return the trajectory plot output as per the output/simulation module specifications.
- output: [if appropriate —SS]
- exception: WarnOutOfBounds (warn when mps\_input or calculations of the data structure are invalid) [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

#### 13.4.5 Local Functions

[As appropriate—SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope.—SS]

# References

[You shouldn't do this manually, especially since you use BibTeX in the next section. The new references can be added to your .bib file and everything will be generated automatically. —SS]

- [1] Dynamics of multiple pendula http://wmii.uwm.edu.pl/~doliwa/IS-2012/Szuminski-2012-Olsztyn.pdf
- [2] Pendulum https://en.wikipedia.org/wiki/Pendulum
- [3] Pendulum (mathematics) https://en.wikipedia.org/wiki/Pendulum\_(mathematics)
- [4] Double Pendulum https://en.wikipedia.org/wiki/Double\_pendulum
- [4] Differential-Algebraic Equations by Taylor Series http://www.cas.mcmaster.ca/~nedialk/daets/
- [5] Multi-body Lagrangian Simulations https://www.youtube.com/channel/UCCuLchOxOWOyoNE9KOCY1VQ
- [6] The double pendulum: Lagrangian formulation https://diego.assencio.com/?index=1500c66ae7ab27bb0106467c68feebc6
- [7] Poincaré map https://en.wikipedia.org/wiki/Poincar%C3%A9\_map
- [8] D. L. Parnas, "On the criteria to be used in decomposing systems into modules", Comm. ACM, vol. 15, pp. 1053-1058, December 1972.
- [9] D. Parnas, P. Clement, and D. M. Weiss, "The modular structure of complex systems", in International Conference on Software Engineering, pp. 408-419, 1984.
- [10] D. L. Parnas, "Designing software for ease of extension and contraction," in ICSE '78: Proceedings of the 3rd international conference on Software engineering, (Piscataway, NJ, USA), pp. 264-277, IEEE Press, 1978.
- [11] Smith and Lai(2005); Smith et al. (2007). See bib file that doesn't work for me for full citation.

# 14 Appendix

 $[{\bf Extra~information~if~required~--SS}]$