

CAS 741: Module Interface Specification

Dynamical Systems: Multi-Pendulum Simulation

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November 28, 2018

1 Revision History

Date	Version	Notes
November 26, 2018	1.0	First full draft for submission

2 Symbols, Abbreviations and Acronyms

See SRS Documentation at [CAS-741-Pendula SRS](#) [give url —SS]

[Also add any additional symbols, abbreviations or acronyms —SS]

The symbols are listed in alphabetical order.

symbol	description
A	Assumption
DD	Data Definition
GD	General Definition
GS	Goal Statement
IM	Instance Model
LC	Likely Change
NF	Non-Functional Requirement
MIS	Module Interface Specification
PS	Physical System Description
R	Requirement
SRS	Software Requirements Specification
T	Theoretical Model

Contents

1	Revision History	i
2	Symbols, Abbreviations and Acronyms	ii
3	Introduction	1
4	Notation	1
5	Module Decomposition	2
6	MIS of Multi-Pendulum Simulation Control Module (M2)	3
6.1	Module	3
6.2	Uses	3
6.3	Syntax	3
6.3.1	Exported Constants	3
6.3.2	Exported Access Programs	3
6.4	Semantics	4
6.4.1	State Variables	4
6.4.2	Environment Variables	4
6.4.3	Assumptions	4
6.4.4	Access Routine Semantics	4
6.4.5	Local Functions	5
7	MIS of Multi-Pendulum Simulation GUI (M3)	5
7.1	Module	5
7.2	Uses	5
7.3	Syntax	5
7.3.1	Exported Constants	5
7.3.2	Exported Access Programs	5
7.4	Semantics	5
7.4.1	State Variables	6
7.4.2	Environment Variables	6
7.4.3	Assumptions	6
7.4.4	Access Routine Semantics	6
7.4.5	Local Functions	7
8	MIS of User Input Module (M4)	7
8.1	Module	7
8.2	Uses	7
8.3	Syntax	7
8.3.1	Exported Constants	7
8.3.2	Exported Access Programs	7

8.4	Semantics	7
8.4.1	State Variables	7
8.4.2	Environment Variables	8
8.4.3	Assumptions	8
8.4.4	Access Routine Semantics	8
8.4.5	Local Functions	9
9	MIS of Lagrangian Module (M5)	9
9.1	Module	9
9.2	Uses	9
9.3	Syntax	9
9.3.1	Exported Constants	9
9.3.2	Exported Access Programs	10
9.4	Semantics	10
9.4.1	State Variables	10
9.4.2	Environment Variables	10
9.4.3	Assumptions	10
9.4.4	Access Routine Semantics	10
9.4.5	Local Functions	10
10	MIS of Hamiltonian Module (M6)	11
10.1	Module	11
10.2	Uses	11
10.3	Syntax	11
10.3.1	Exported Constants	11
10.3.2	Exported Access Programs	11
10.4	Semantics	11
10.4.1	State Variables	11
10.4.2	Environment Variables	11
10.4.3	Assumptions	12
10.4.4	Access Routine Semantics	12
10.4.5	Local Functions	12
11	MIS of Data Structure Module (M7)	12
11.1	Module	12
11.2	Uses	13
11.3	Syntax	13
11.3.1	Exported Constants	13
11.3.2	Exported Access Programs	13
11.4	Semantics	13
11.4.1	State Variables	13
11.4.2	Environment Variables	13
11.4.3	Assumptions	13

11.4.4	Access Routine Semantics	13
11.4.5	Local Functions	14
12	MIS of Generic GUI/Plot Module (M8)	14
12.1	Module	14
12.2	Uses	14
12.3	Syntax	14
12.3.1	Exported Constants	14
12.3.2	Exported Access Programs	15
12.4	Semantics	15
12.4.1	State Variables	15
12.4.2	Environment Variables	15
12.4.3	Assumptions	15
12.4.4	Access Routine Semantics	15
12.4.5	Local Functions	15
13	MIS of Trajectory Simulation Module (M9)	16
13.1	Module	16
13.2	Uses	16
13.3	Syntax	16
13.3.1	Exported Constants	16
13.3.2	Exported Access Programs	16
13.4	Semantics	16
13.4.1	State Variables	16
13.4.2	Environment Variables	16
13.4.3	Assumptions	17
13.4.4	Access Routine Semantics	17
13.4.5	Local Functions	17
14	Appendix	19

3 Introduction

The following document details the Module Interface Specifications for the Multi-Pendulum Simulation project [\[Fill in your project name and description —SS\]](#)

Complementary documents include the System Requirement Specifications and Module Guide. The full documentation and implementation can be found at:
<https://github.com/karolserkis/CAS-741-Pendula>. [\[provide the url for your repo —SS\]](#)

4 Notation

[\[You should describe your notation. You can use what is below as a starting point. —SS\]](#)

The structure of the MIS for modules comes from [?\[HoffmanAndStrooper1995 —SS\]](#), with the addition that template modules have been adapted from [?\[GhezziEtAl2003 —SS\]](#). The mathematical notation comes from Chapter 3 of [?\[HoffmanAndStrooper1995 —SS\]](#). For instance, the symbol $:=$ is used for a multiple assignment statement and conditional rules follow the form $(c_1 \Rightarrow r_1 | c_2 \Rightarrow r_2 | \dots | c_n \Rightarrow r_n)$.

(Karol) I am also using [this link](#) for now.

The following table summarizes the primitive data types used by Multi-Pendulum Simulation and the symbols used in this document. The choice of symbols was made to be consistent with calculus, ordinary differentials (ODE), the Lagrangian, kinematics etc. The standard mathematical spaces are used (e.g. \mathbb{N} , \mathbb{Z} , \mathbb{R} , etc.)

Data Type	Notation	Description
character	char	a single symbol or digit
integer	\mathbb{Z}	a number without a fractional component in $(-\infty, \infty)$
natural number	\mathbb{N}	a number without a fractional component in $[1, \infty)$
real	\mathbb{R}	any number in $(-\infty, \infty)$

The specification of Multi-Pendulum Simulation uses some derived data types: sequences, strings, and tuples. Sequences are lists filled with elements of the same data type. Strings are sequences of characters. Tuples contain a list of values, potentially of different types. In addition, Multi-Pendulum Simulation uses functions, which are defined by the data types of their inputs and outputs. Local functions are described by giving their type signature followed by their specification.

5 Module Decomposition

The following table is taken directly from the Module Guide document for this project.

Level 1	Level 2
Hardware-Hiding	
	Multi-Pendulum Simulation Control Module
	Multi-Pendulum Simulation GUI Module
	User Input Parameters Module
Behaviour-Hiding	Data Structure Module
Software Decision	Generic Trajectory Simulation GUI Module
	Generic GUI/Plot Module
	Lagrangian Module
	Hamiltonian Module

Table 1: Module Hierarchy

6 MIS of Multi-Pendulum Simulation Control Module (M2)

[You can reference SRS labels, such as R??. —SS]

[It is also possible to use L^AT_EX for hypperlinks to external documents. —SS]

Execution flow of Multi-Pendulum Simulation . Calls the different modules in the appropriate order. The general steps of the module are:

1. Read in and verify mps_input.
2. Calculate Lagrangian module, iterate over the whole time frame (use data structure).
3. Calculate Hamiltonian module, iterate over the whole time frame (use data structure).
4. Generate a Plot and Poincaré map
5. Return the trajectory plot output as per the output/simulation module specifications.

6.1 Module

mps_control

6.2 Uses

mps_gui (M3, Section 7)

mps_input (M4, Section 8)

Processing modules:

mps_lagrang (M5, Section 9), mps_hamil (M6, Section 10)

mps_datastruct (M7, Section 11)

generic_plot (M8, Section 12), mps_trajplotsim (M9, Section 13)

6.3 Syntax

6.3.1 Exported Constants

None

6.3.2 Exported Access Programs

Name	In	Out	Exceptions
run_mps	int, str	None	None

6.4 Semantics

The Multi-Pendulum Simulation is designed to have the input and initialization controlled by the user directly through the GUI. The Multi-Pendulum Simulation Control Module uses the events in the Multi-Pendulum Simulation GUI to use the processing modules in order.

6.4.1 State Variables

- `mps_input_init` : init (see Section 8)
- `mps_datastruct_init` : init (see Section 11)
- `mps_lagrang` : calc (see Section 9)
- `mps_hamil` : calc (see Section 10)

6.4.2 Environment Variables

[This section is not necessary for all modules. Its purpose is to capture when the module has external interaction with the environment, such as for a device driver, screen interface, keyboard, file, etc. —SS]

6.4.3 Assumptions

[Try to minimize assumptions and anticipate programmer errors via exceptions, but for practical purposes assumptions are sometimes appropriate. —SS]

6.4.4 Access Routine Semantics

`run_mps(mps_input):`

- transition: The Multi Pendulum Simulation is initialized and the data structure through the modules for calculation (Lagrangian & Hamiltonian). The result is then passed to the plot/simulation/output modules.
- output: None [if appropriate —SS]
- exception: None [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

6.4.5 Local Functions

[As appropriate —SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope. —SS]

7 MIS of Multi-Pendulum Simulation GUI (M3)

[Use labels for cross-referencing —SS]

[You can reference SRS labels, such as R??. —SS]

[It is also possible to use L^AT_EX for hyperlinks to external documents. —SS]

Methods to interact with user to make run Multi-Pendulum Simulation . Serves as interface between the user and the software through the hardware by outputting calculation results and collecting user information (user inputs) for the calculation modules.

7.1 Module

mps_gui

7.2 Uses

mps_datastruct (M7, Section 11)

generic_plot (M8, Section 12), mps_trajplotsim (M9, Section 13)

7.3 Syntax

7.3.1 Exported Constants

None

7.3.2 Exported Access Programs

Name	In	Out	Exceptions
mps_input	int, str	-	-
gui_trajsim	-	GUI object	-
gui_plot	-	GUI object (Poincaré)	-

7.4 Semantics

The Multi-Pendulum Simulation process flow is initialized by user through the GUI. The user triggers the events that start the selected processing step.

7.4.1 State Variables

None

7.4.2 Environment Variables

Plot_TrajSim: GUI object

button_Input: GUI object

button_TrajSim: GUI object

button_Poincaré: GUI object

[This section is not necessary for all modules. Its purpose is to capture when the module has external interaction with the environment, such as for a device driver, screen interface, keyboard, file, etc. —SS]

7.4.3 Assumptions

[Try to minimize assumptions and anticipate programmer errors via exceptions, but for practical purposes assumptions are sometimes appropriate. —SS]

7.4.4 Access Routine Semantics

mps_input():

- transition: Trigger mps_input when button_Input pressed.
- output: [if appropriate —SS]
- exception: WarnOutOfBounds (warn when mps_input are invalid) [if appropriate —SS]

gui_trajsims():

- transition: Trigger gui_trajsims when button_TrajSim pressed.
- output: [if appropriate —SS]
- exception: [if appropriate —SS]

gui_plot():

- transition: Trigger gui_plot when button_Poincaré pressed.
- output: [if appropriate —SS]
- exception: [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

7.4.5 Local Functions

[As appropriate —SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope. —SS]

8 MIS of User Input Module (M4)

[Use labels for cross-referencing —SS]

[You can reference SRS labels, such as R??. —SS]

[It is also possible to use L^AT_EX for hypperlinks to external documents. —SS]

The format and structure of the input data. Loads, verifies and stores the input data into the appropriate data and object structure.

8.1 Module

mps_input

8.2 Uses

mps_gui (M3, Section 7)

mps_datastruct (M7, Section 11)

8.3 Syntax

8.3.1 Exported Constants

None

8.3.2 Exported Access Programs

Name	In	Out	Exceptions
verify_userInput	int, str	-	-
calc_datastruct	int, str	-	-
gui_trajsim	-	GUI object	-
gui_plot	-	GUI object (Poincaré)	-

8.4 Semantics

8.4.1 State Variables

data : object

8.4.2 Environment Variables

Plot_TrajSim: GUI object

[This section is not necessary for all modules. Its purpose is to capture when the module has external interaction with the environment, such as for a device driver, screen interface, keyboard, file, etc. —SS]

8.4.3 Assumptions

[Try to minimize assumptions and anticipate programmer errors via exceptions, but for practical purposes assumptions are sometimes appropriate. —SS]

8.4.4 Access Routine Semantics

verify_userInput():

- transition: [if appropriate —SS]
- output: [if appropriate —SS]
- exception: Check of int or str value out of bounds: $(\exists I : I_{\text{calc}} \notin \mathbb{R}) \ \& \Rightarrow \text{NotReal}$
[if appropriate —SS]

calc_datastruct(mps_input):

- transition: mps_input is the user input that is entered into the GUI. The input is used to initialize the data structure.
- output: [if appropriate —SS]
- exception: [if appropriate —SS]

gui_trajsim(mps_datastruct, mps_input):

- transition: mps_datastruct is a module that takes the mps_input and thus the program gui_trajsim will be prepared for the lagrangian and hamiltonian calculations done by their corresponding modules.
- output: [if appropriate —SS]
- exception: [if appropriate —SS]

gui_plot(mps_datastruct, mps_input):

- transition: mps_datastruct is a module that takes the mps_input and thus the program gui_plot will be prepared for the lagrangian and hamiltonian calculations done by their corresponding modules.
- output: [if appropriate —SS]

- exception: [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

8.4.5 Local Functions

[As appropriate —SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope. —SS]

9 MIS of Lagrangian Module (M5)

[Use labels for cross-referencing —SS]

[You can reference SRS labels, such as R??. —SS]

[It is also possible to use L^AT_EX for hyperlinks to external documents. —SS]

Lagrangian calculation/algorithm. Calculates the variation of Lagrangian for each pendulum in the chain (each element of the array).

9.1 Module

`mps_lagrang`

9.2 Uses

`mps_input` (M4, Section 8)

Processing modules:

`mps_lagrang` (M5, Section 9)

`mps_datastruct` (M7, Section 11)

9.3 Syntax

9.3.1 Exported Constants

None

9.3.2 Exported Access Programs

Name	In	Out	Exceptions
mps_input	int, str	-	-
calc_lagrang	int, str	long, str	-

9.4 Semantics

9.4.1 State Variables

9.4.2 Environment Variables

[This section is not necessary for all modules. Its purpose is to capture when the module has external interaction with the environment, such as for a device driver, screen interface, keyboard, file, etc. —SS]

9.4.3 Assumptions

[Try to minimize assumptions and anticipate programmer errors via exceptions, but for practical purposes assumptions are sometimes appropriate. —SS]

9.4.4 Access Routine Semantics

mps_input():

- transition: mps_input passed to calc_lagrang (which in turn the module utilizes mps_datastruct).
- output: [if appropriate —SS]
- exception: WarnOutOfBounds (warn when mps_input are invalid) [if appropriate —SS]

calc_lagrang(mps_input):

- transition: Utilizing the mps_datastruct the mps_input is calculated and passed to the gui_trajsim and gui_plot [if appropriate —SS]
- output: To gui_trajsim and gui_plot [if appropriate —SS]
- exception: WarnOutOfBounds (warn when mps_input are invalid) [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

9.4.5 Local Functions

[As appropriate —SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope. —SS]

10 MIS of Hamiltonian Module (M6)

[Use labels for cross-referencing —SS]

[You can reference SRS labels, such as R??. —SS]

[It is also possible to use \LaTeX for hyperlinks to external documents. —SS]

Hamiltonian calculation/algorithm. Calculates the variation of Hamiltonian for each pendulum in the chain (each element of the array).

10.1 Module

mps_hamil

10.2 Uses

mps_input (M4, Section 8)

Processing modules:

mps_lagrang (M5, Section 9), mps_hamil (M6, Section 10)

mps_datastruct (M7, Section 11)

10.3 Syntax

10.3.1 Exported Constants

None

10.3.2 Exported Access Programs

Name	In	Out	Exceptions
mps_input	int, str	-	-
calc_lagrang	int, str	long, str	-
calc_hamil	long, str	long, str	-

10.4 Semantics

10.4.1 State Variables

10.4.2 Environment Variables

[This section is not necessary for all modules. Its purpose is to capture when the module has external interaction with the environment, such as for a device driver, screen interface, keyboard, file, etc. —SS]

10.4.3 Assumptions

[Try to minimize assumptions and anticipate programmer errors via exceptions, but for practical purposes assumptions are sometimes appropriate. —SS]

10.4.4 Access Routine Semantics

`mps_input()`:

- transition: `mps_input` passed to `calc_lagrang` (which in turn the module utilizes `mps_datastruct`).
- output: [if appropriate —SS]
- exception: `WarnOutOfBounds` (warn when `mps_input` are invalid) [if appropriate —SS]

`calc_lagrang(mps_input)`:

- transition: Utilizing the `mps_datastruct` the `mps_input` is calculated and passed to the `gui_trajsim` and `gui_plot` [if appropriate —SS]
- output: To `gui_trajsim` and `gui_plot` [if appropriate —SS]
- exception: `WarnOutOfBounds` (warn when `mps_input` are invalid) [if appropriate —SS]

`calc_hamil(mps_input)`:

- transition: Utilizing the `mps_datastruct` the `mps_input` is calculated and passed to the `gui_trajsim` and `gui_plot` [if appropriate —SS]
- output: To `gui_trajsim` and `gui_plot` [if appropriate —SS]
- exception: `WarnOutOfBounds` (warn when `mps_input` are invalid) [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

10.4.5 Local Functions

[As appropriate —SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope. —SS]

11 MIS of Data Structure Module (M7)

[Use labels for cross-referencing —SS]

[You can reference SRS labels, such as R??. —SS]

[It is also possible to use L^AT_EX for hypperlinks to external documents. —SS]

Data format for an image. Provides convenient format to store, read and manipulate all elements (pixel) from an image.

11.1 Module

mps_datastruct

11.2 Uses

mps_gui (M3, Section 7)

mps_input (M4, Section 8)

Processing modules:

mps_lagrang (M5, Section 9), mps_hamil (M6, Section 10)

mps_datastruct (M7, Section 11)

11.3 Syntax

11.3.1 Exported Constants

None

11.3.2 Exported Access Programs

Name	In	Out	Exceptions
calc_lagrang	int, str	long, str	-
calc_hamil	long, str	long, str	-
mps_gui	GUI object	-	-

11.4 Semantics

11.4.1 State Variables

11.4.2 Environment Variables

Plot_TrajSim: GUI object

Plot_Poincaré: GUI object

[This section is not necessary for all modules. Its purpose is to capture when the module has external interaction with the environment, such as for a device driver, screen interface, keyboard, file, etc. —SS]

11.4.3 Assumptions

[Try to minimize assumptions and anticipate programmer errors via exceptions, but for practical purposes assumptions are sometimes appropriate. —SS]

11.4.4 Access Routine Semantics

calc_lagrang(mps_input):

- transition: Utilizing the mps_datastruct the mps_input is calculated and passed to the gui_trajsim and gui_plot [if appropriate —SS]
- output: To gui_trajsim and gui_plot [if appropriate —SS]
- exception: WarnOutOfBounds (warn when mps_input are invalid) [if appropriate —SS]

calc_hamil(mps_input):

- transition: Utilizing the mps_datastruct the mps_input is calculated and passed to the gui_trajsim and gui_plot [if appropriate —SS]
- output: To gui_trajsim and gui_plot [if appropriate —SS]
- exception: WarnOutOfBounds (warn when mps_input are invalid) [if appropriate —SS]

mps_gui(mps_datastruct, gui_trajsim, gui_plot):

- transition: Utilizing the mps_datastruct the mps_input is calculated and passed to the gui_trajsim and gui_plot and thus the program gui_trajsim will be prepared for the lagrangian and hamiltonian calculations done by their corresponding modules.
- output: To gui_trajsim and gui_plot [if appropriate —SS]
- exception: WarnOutOfBounds (warn when mps_input are invalid) [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

11.4.5 Local Functions

[As appropriate —SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope. —SS]

12 MIS of Generic GUI/Plot Module (M8)

[Use labels for cross-referencing —SS]

[You can reference SRS labels, such as R??. —SS]

[It is also possible to use L^AT_EX for hyperlinks to external documents. —SS]

Generic methods to interact with the user. Provides the generic interface methods such as buttons, windows, plotting, entry fields to interact with a user.

12.1 Module

generic_plot

12.2 Uses

Hardware-Hiding (M1)

12.3 Syntax

12.3.1 Exported Constants

None

12.3.2 Exported Access Programs

Name	In	Out	Exceptions
gui_trajsim	GUI object	GUI object	-
gui_plot	GUI object	GUI object	-

12.4 Semantics

12.4.1 State Variables

12.4.2 Environment Variables

Plot_TrajSim: GUI object

Plot_Poincaré: GUI object

[This section is not necessary for all modules. Its purpose is to capture when the module has external interaction with the environment, such as for a device driver, screen interface, keyboard, file, etc. —SS]

12.4.3 Assumptions

[Try to minimize assumptions and anticipate programmer errors via exceptions, but for practical purposes assumptions are sometimes appropriate. —SS]

12.4.4 Access Routine Semantics

gui_trajsim():

- transition: [if appropriate —SS]
- output: To mps_gui(mps_datastruct, gui_trajsim, gui_plot) or the generic_plot module [if appropriate —SS]
- exception: WarnOutOfBounds (warn when gui_trajsim are invalid) [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

12.4.5 Local Functions

[As appropriate —SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope. —SS]

13 MIS of Trajectory Simulation Module (M9)

[Use labels for cross-referencing —SS]

[You can reference SRS labels, such as R??. —SS]

[It is also possible to use \LaTeX for hyperlinks to external documents. —SS]

Algorithm to simulate the plot trajectory of the chain of pendula. Simulates the chain of pendula in space using the Lagrangian and the Hamiltonian.

13.1 Module

mps_trajplotsim

13.2 Uses

mps_gui (M3, Section 7)

mps_input (M4, Section 8)

Processing modules:

mps_lagrang (M5, Section 9), mps_hamil (M6, Section 10)

13.3 Syntax

13.3.1 Exported Constants

None

13.3.2 Exported Access Programs

Name	In	Out	Exceptions
MPS_trajsim	GUI object	GUI object	WarnOutOfBounds

13.4 Semantics

13.4.1 State Variables

data : object

13.4.2 Environment Variables

Plot_TrajSim: GUI object

[This section is not necessary for all modules. Its purpose is to capture when the module has external interaction with the environment, such as for a device driver, screen interface, keyboard, file, etc. —SS]

13.4.3 Assumptions

[Try to minimize assumptions and anticipate programmer errors via exceptions, but for practical purposes assumptions are sometimes appropriate. —SS]

13.4.4 Access Routine Semantics

MPS_trajsim():

- transition:
 1. Read in and verify mps_input.
 2. Calculate Lagrangian module calc_lagrang, iterate over the whole time frame (use data structure).
 3. Calculate Hamiltonian module calc_hamil, iterate over the whole time frame (use data structure).
 4. Return the trajectory plot output as per the output/simulation module specifications.
- output: [if appropriate —SS]
- exception: WarnOutOfBounds (warn when mps_input or calculations of the data structure are invalid) [if appropriate —SS]

[A module without environment variables or state variables is unlikely to have a state transition. In this case a state transition can only occur if the module is changing the state of another module. —SS]

[Modules rarely have both a transition and an output. In most cases you will have one or the other. —SS]

13.4.5 Local Functions

[As appropriate —SS] [These functions are for the purpose of specification. They are not necessarily something that is going to be implemented explicitly. Even if they are implemented, they are not exported; they only have local scope. —SS]

References

[You shouldn't do this manually, especially since you use BibTeX in the next section. The new references can be added to your .bib file and everything will be generated automatically. —SS]

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See bib file that doesn't work for me for full citation.

14 Appendix

[Extra information if required —SS]