

CAS 741: Problem Statement

Dynamical Systems: Multi-Pendulum

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Table 1: Revision History

Date	Developer(s)	Change
September 17, 2018	Karol Serkis	First revision of document
September 14, 2018	Karol Serkis	Problem Idea proposed & discussed with Dr. Spencer Smith

[Why reproduce the contents of the Comments.tex file? It was written separately so that it can easily be included in every document. —SS]

Problem

[Please keep the lines of tex to a fixed width (say 80 characters) so that it is easier to do diffs between commits. Your tex editor should have a facility for doing this. —SS]

A simple gravity pendulum has very easy to system to model and consists of a weight suspended from a pivot and the weight is given enough space to swing freely. To simplify the model we assume no air resistance with a frictionless pivot [1]. The model and calculations for the simple gravity pendulum are well defined and only require simple derivations and differential solvers [2]. [Are you also assuming a small angle? Usually that is an assumption made so that $\sin(\theta)$ is approximately equal to θ . —SS]

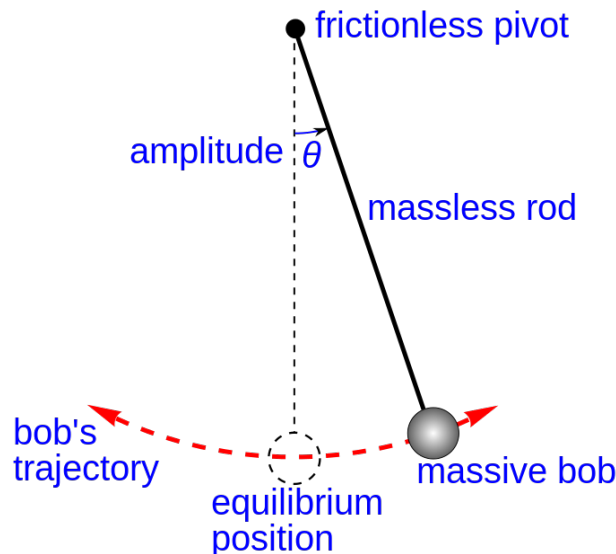


Figure 1: A simple gravity pendulum where the model assumes no friction or air resistance [1]

However, once you attach a pendulum to the bottom of another pendulum in the case of a double pendulum you have a new system that is dynamic and chaotic and requires a set of coupled ordinary differential equation solvers [3]. Once you introduce multiple pendula the system becomes chaotic and interesting to model and simulate.

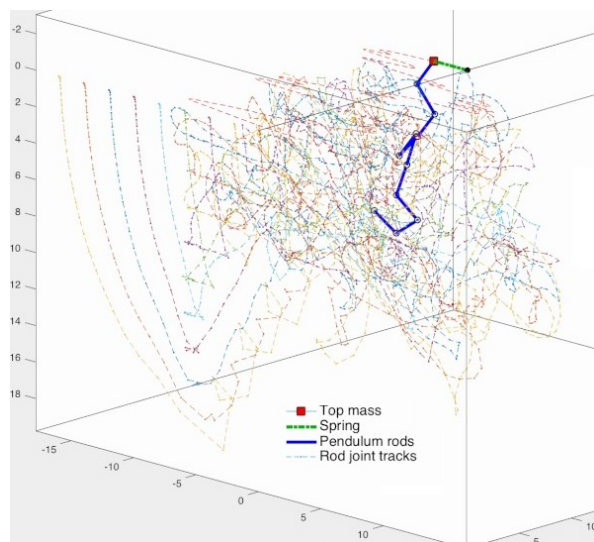


Figure 2: An example of dynamical and chaotic system with Spring-Mass-Multi-Pendulum [5]

Proposed Solution

A proposed software solution will produce a simulation of a multi-pendulum system. Inspiration for this problem came from Dr. Ned Nedialkov's Multi-body Lagrangian Simulations using DAETS (Differential-Algebraic Equations by Taylor Series). DAETS is a C++ package for solving initial value problems for DAE systems [4].

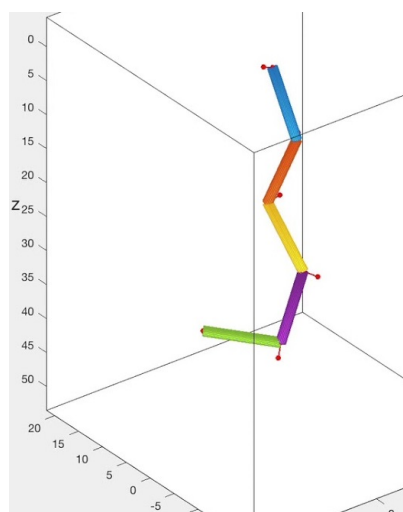


Figure 3: Simulation of Multi-Pendulum system using DAETS [5]

The proposed software is to develop a multi-platform equivalent solution that only focuses on multi-pendulum simulations and tracking the chaotic motion of the system. It will allow users to generate diagrams and plot trajectories over time using two different ODE/DAE initial value problem solvers [4]. If time allows, multiple solvers can be compared for performance and accuracy. [Rather than say “If time allows,” you can just make this part of the original project. If it has to be dropped out, we can “fake” this document later, or simply modify your requirements document. —SS]

Context

Environment

The simulation software will be created with multi-platform support in mind and be compatible with Windows 10, Mac OS, Linux, etc. In order to achieve this, Python and/or MATLAB will be used for development of the software.

Stakeholders

Specific stakeholders include:

- Karol Serkis
- Dr. Spencer Smith
- Dr. Ned Nedialov
- Students of CAS 741
- Individuals studying or working in fields related to physics

References

- [1] Pendulum
<https://en.wikipedia.org/wiki/Pendulum>
- [2] Pendulum (mathematics)
[https://en.wikipedia.org/wiki/Pendulum_\(mathematics\)](https://en.wikipedia.org/wiki/Pendulum_(mathematics))
- [3] Double Pendulum
https://en.wikipedia.org/wiki/Double_pendulum
- [4] Differential-Algebraic Equations by Taylor Series
<http://www.cas.mcmaster.ca/~nedialk/daets/>
- [5] Multi-body Lagrangian Simulations
<https://www.youtube.com/channel/UCCuLch0xOW0yoNE9KOCY1VQ>