Kod Shannona

Część 1

In[6]:=
```
ClearAll["Global`*"]
ShannonAlgorithm[BaseWithCharsAndProbability_] :=
 Module[{X = BaseWithCharsAndProbability, SumOfPreviousProbabilities, SortedX },
SortedX = SortBy[X, Last, Greater];

probability = Table[SortedX[[i, 2]], {i, 1, Length[X]}];

SumOfPreviousProbabilities := {0};
For[i = 1, i < Length[X], i++,
AppendTo[SumOfPreviousProbabilities, Sum[probability[[j]], {j, 1, i}]]];
ShannonLength = Table[ Ceiling[Log[2, 1/probability[[i]]] , {i, 1, Length[SortedX]}];

CodedWords := {};
For[i = 1, i ≤ Length[SumOfPreviousProbabilities], i++,
tmp = SumOfPreviousProbabilities[[i]];
OneCodedWord = {};
For[j = 1, j ≤ ShannonLength[[i]], j++,
If[tmp ≥ 1/2^j, tmp = tmp - (1/2^j);
       AppendTo[OneCodedWord, 1], AppendTo[OneCodedWord, 0]];
];

AppendTo[CodedWords, StringJoin[ToString /@ OneCodedWord]];
];
Base := {};
For[i = 1, i ≤ Length[X], i++,
AppendTo[Base, {SortedX[[i, 1]], CodedWords[[i]]}];
];
Return[Base]
]
```

In[8]:=
```
X = {{x1, 0.2}, {x2, 0.1}, {x3, 0.05}, {x4, 0.05}, {x5, 0.2}, {x6, 0.25}, {x7, 0.15}};
```

```
Y = ShannonAlgorithm[X]
```

Out[9]=
```
{{x6, 00}, {x5, 010}, {x1, 011}, {x7, 101}, {x2, 1100}, {x4, 11100}, {x3, 11110}}
```

Kodowanie

In[12]:=
```
Coding[BaseOfCode_, WordWeWantToCode_] :=
 Module[{Base = BaseOfCode, Word = WordWeWantToCode},
CodedWord := {};
For[i = 1, i ≤ Length[Word], i++,
For[j = 1, j ≤ Length[Base], j++,
If[Word[[i]] == Base[[j, 1]], AppendTo[CodedWord, Base[[j, 2]]];
];
];
];
Return[CodedWord]
]
```

```
Y = ShannonAlgorithm[X]
M = {x4, x7, x2}
Coding[Y, M]
```

Out[13]=
```
{{x6, 00}, {x5, 010}, {x1, 011}, {x7, 101}, {x2, 1100}, {x4, 11100}, {x3, 11110}}
```

Out[14]=
```
{x4, x7, x2}
```

Out[15]=
```
{11100, 101, 1100}
```

Dekodowanie

In[16]:=
```
Decoding[BaseOfCode_, WordWeWantToDecode_] :=
 Module[{Base = BaseOfCode, Word = WordWeWantToDecode},
DecodedWord := {};
For[i = 1, i ≤ Length[Word], i++,
For[j = 1, j ≤ Length[Base], j++,
If[Word[[i]] == Base[[j, 2]], AppendTo[DecodedWord, Base[[j, 1]]];
];
];
];
Return[DecodedWord]
]
Y = ShannonAlgorithm[X]
W = {"010", "00", "011", "11110"}
Decoding[Y, W]
```

Out[17]=
```
{{x6, 00}, {x5, 010}, {x1, 011}, {x7, 101}, {x2, 1100}, {x4, 11100}, {x3, 11110}}
```

Out[18]=
```
{010, 00, 011, 11110}
```

Out[19]=
```
{x5, x6, x1, x3}
```

Tworzenie kodu na bazie hasła

In[27]:=

```
BuildingCodeBase[BaseWord_] := Module[{Word = BaseWord},
DividedWord := CharacterCounts[Word];
char := Keys@DividedWord;
counts := Values@DividedWord;
probability := Normalize[counts, Total];
Base := {};
For[i = 1, i ≤ Length[probability], i++,
AppendTo[Base, {char[[i]], probability[[i]]}];
];
Return[Base]
]
Example = "alamakota"
X1 = BuildingCodeBase[Example]
Y1 = ShannonAlgorithm[X1]
M := Characters[Example]
CodedExample = Coding[Y1, M]
StringJoin[ToString /@ CodedExample]
Decoding[Y1, CodedExample]
```

Out[28]=

alamakota

Out[29]=

$$\left\{\left\{a, \frac{4}{9}\right\}, \left\{t, \frac{1}{9}\right\}, \left\{o, \frac{1}{9}\right\}, \left\{k, \frac{1}{9}\right\}, \left\{m, \frac{1}{9}\right\}, \left\{l, \frac{1}{9}\right\}\right\}$$

Out[30]=

{{a, 00}, {t, 0111}, {o, 1000}, {m, 1010}, {l, 1100}, {k, 1110}}

Out[32]=

{00, 1100, 00, 1010, 00, 1110, 1000, 0111, 00}

Out[33]=

00110000101000111010000111100

Out[34]=

{a, l, a, m, a, k, o, t, a}